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Is everything everywhere? Deterministic and stochastic processes in microbial biogeography

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Declaration

Concept: The concept for this work came from Prof. Thomas Bell and Prof. Ryan Chisholm.

Data: All data for this analysis was collected by myself from the literature as listed in the Supplementary Materials section.

Simulation: All simulation code was written by myself, excluding function 2: coalescence test (simulation scripts) provided by Dr. James Rosindell.

Model: The Classic, Depth and Perimeter models, as well as critical area formulas, were supplied by Prof. Ryan Chisholm.

Analysis: I declare that all analysis was carried out by myself.

Report: I declare that the report was written by myself.

COVID-19

The hypotheses presented in this report were originally investigated using a laboratory-based experiment in Professor Thomas Bell's Microbial Ecology Laboratory, Imperial College London, Silwood Park. Two months into the investigation, laboratory work was ceased due to the COVID-19 pandemic. The following report seeks to test the same hypotheses, using data from the literature.

Abstract

- 1. Microbial communities play an essential role in biogeochemical processes and ecosystem functioning. Despite their importance, relatively little is known about the mechanisms driving spatial scaling within these communities.
- 2. The Theory of Island Biogeography predicts that species richness increases with island area through stochastic colonisation-extinction processes. It has been widely use to describe macroorganism spatial patterns, with little application to microbial communities.
- 3. Despite the popularity of this theory, small islands often show no clear relationship between species richness and area. Chisholm *et al.*, have addressed this by developing a unified theory of species-area relationships that transitions from a niche-structured regime at smaller spatial scales to stochastic mechanisms at larger spatial scales.
- 4. This work modifies the Chisholm model to address microbial communities in a range of habitats. Through model fitting I assess to what extent microorganisms are subject to deterministic or stochastic processes. I also explore how the transition between regimes differs among habitat types and taxonomic groups.
- 5. The models gave good fits to the data. Multiple regression analysis showed significant evidence that taxonomic group explained variance in the critical area of transition between regimes. Less motile groups exhibited higher critical areas supporting my hypothesis. Habitat type was non-significant in predicting critical area.
- 6. A proportion of the datasets exhibited a biphasic species-area relationship. Broadly the critical area hypotheses of lower transition areas for more motile taxa was supported by the data. These results can assist in predicting the spatial scaling of microbial diversity, with application to climate change modelling.

Keywords: species-area relationships, taxa-area relationships, microbial biogeography, small-island effect, niche structure, colonisation-extinction balance, island biogeography

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Introduction

The species—area relationship (SAR) is one of the oldest fundamental ecological laws (Gooriah and Chase, 2019). Positive SARs, where number of species increases with sampling area, has been observed for a broad range of faunal (Ricklefs and Lovette, 1999) (Lomolino, 1982) (Eadie et al., 1986) and floral groups (Zacharias and Brandes, 1990) (Price and Wagner, 2011). The ubiquitous nature of positive SARs has been used to inform conservation practises in natural (Haila, 2002) (Samson, 1980) and urban environments (Davis and Glick, 1978). Whilst a large number of studies have examined macroorganism SARs, little is known about the spatial scaling of microbial biodiversity.

Understanding the factors that regulate microbial community structure is important as they play a vital role in biogeochemical cycling and ecosystem functioning (Griffiths et al., 2011). Little is known about below-ground regulators of biodiversity as few terrestrial environments present insular habitats for microbial community dynamics to be easily studied. Microorganisms also play a metabolically active role in polar regions previously believed to be abiotic (Stibal et al., 2020). Rapid climate change is leading to exposure of soils dominant in high-latitude carbon (Bradley et al., 2017). Understanding the mechanisms that drive microbial colonisation of polar environments can help produce accurate climate models (Malard and Pearce, 2018).

Debate around the applicability of SARs to microbial systems stems from the assumption that they are limited only by niche filtering, as articulated by Bass-Becking: 'Everything is everywhere, but, the environment selects' (Baas-Becking, 1934). This classic tenet of microbiology assumes that the abundance, short generation times and small size of microorganisms gives them an almost cosmopolitan distribution (Green and Bohannan, 2006). High abundances increase the probability of transport between environments via an accidental vector. Small size increases the likelihood of passive transport via air or water, (Green and

Bohannan, 2006). Uninhibited dispersal may also be facilitated by dormancy as a biogeographic response (Locey, 2010).

One of the most commonly used tools in biogeography is the power-law model:

$$S = cA^z (1.1)$$

Where S is species richness as a function of area (A), c is a constant specific to that taxa/habitat and the z exponent is the slope of the line associating area and species richness (Darcy et al., 2018). z typically falls in the range of 0.1 to 0.3 for continuous habitats and 0.25 to 0.35 for insular habitats (Green and Bohannan, 2006). Microbial z values are typically well below those seen in macro-organisms (z < 0.1), supporting the idea of cosmopolitan distribution (Green and Bohannan, 2006).

One of the limitations for microbial biogeography has been in quantifying taxa, given that many cannot be accurately identified using morphological techniques (Green and Bohannan, 2006). Microbial biogeography is usually concerned with taxa-area relationships (TARs), rather than SARs as microbial diversity is quantified in operational taxonomic groups (OTUs). With recent advances in molecular approaches such as single-celled sequencing, the genomes of previously uncultivated bacterial taxa are filling in the microbial phylogenetic tree (Lasken and McLean, 2014). Limited data on temporal and spatial microbial distributions has led to a lack of detailed distribution maps, inhibiting taxa richness estimations and artificially lowering z values (Green and Bohannan, 2006).

The mechanisms driving island SARs have been of particular interest to ecologists since the 1800s (MacDonald et al., 2018). Islands are important paradigms for fragmented habitats and larger geographic regions (Simberloff, 1974). Their insular nature allows for ecological patterns to be investigated in a simplified and relatively closed system.

MacArthur and Wilson's Theory of Island Biogeography (MacArthur, 1967) is one of the most widely accepted island SAR theories, explaining the maintenance of biodiversity on islands through stochastic processes of colonisation and extinction. The rates of these processes are determined by island area and isolation. Islands that are nearer to source

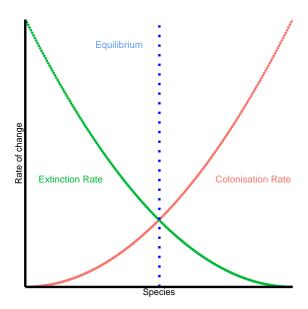


Figure 1.1: Colonisation-Extinction Dynamic Equilibrium

populations will experience a higher rate of immigration. This in turn can produce a rescue effect leading to decreased extinction risk (Brown and Kodric-Brown, 1977). Larger islands receive more immigrants as species actively target larger habitats with more resources, or will be more likely to immigrate randomly due to island size. A larger population is also less susceptible to inbreeding depressions and random extinction (MacDonald et al., 2018). This results in higher species richness at the point of balance between immigration and extinction rates (i.e. the colonisation-extinction dynamic equilibrium, Figure 1.1) for larger, less isolated islands.

It has been suggested the significance of area has been overplayed, to the exclusion of interspecific relationships, biotic and abiotic factors (Abbott, 1974). Empirical evidence indicates smaller islands do not always follow the positive SAR pattern (Triantis et al., 2006) (Sfenthourakis and Triantis, 2009). MacArthur and Wilson noted that archipelagos showed unusual SARs, with smaller island species-richness varying independently of size (MacArthur, 1967). This exception to MacArthur and Wilson's ecological law has been dubbed the small-island effect (SIE).

Several hypotheses have been offered to explain the SIE. The 'subsidised island biogeography' hypothesis suggests that smaller islands have a greater edge to interior ratio, thus receive a greater amount of nutrients per unit area (Barrett et al., 2003) (Anderson and Wait, 2001). Secondly, extinction rates on islands may operate independently of area due to environmental instability and high temporal turnover (MacArthur, 1967). Thirdly, the

'habitat hypothesis' suggests that diversity is limited on smaller islands, compared to larger islands (Triantis et al., 2008). However, the environmental instability and habitat hypotheses contradict empirical data that indicate small islands have unusually high numbers of species. The Habitat–Diversity Hypothesis addresses the SIE by stating that as observation area increases we encounter a greater range of habitats (Connor and McCoy, 1979). Species richness should increase with habitat diversity, which varies independently of area (MacDonald et al., 2018).

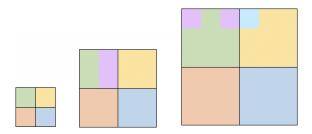


Figure 1.2: A graphical representation of a simulation (using the Classic Model, see Methods) of three islands of varying size, with the same number of niches (K=4) and low immigration rate (m=0.03). Each of the three main squares represents an island. Each smaller square represents an individual niche. Each unique colour patch within a niche represents a unique species. The smallest island has one individual per niche, the medium size island has four individuals per niche and the largest island has nine individuals per niche. Species richness on the smallest island is $\bf 4$, on the medium island is $\bf 5$ and the large island is $\bf 6$

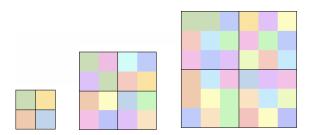


Figure 1.3: A graphical representation of a simulation (using the Classic Model, see Methods) of three islands of varying size, with the same number of niches (K=4) and **high** immigration rate (m=0.9). Each of the three main squares represents an island. Each smaller square represents an individual niche. Each unique colour patch within a niche represents a unique species. The smallest island has one individual per niche, the medium size island has four individuals per niche and the largest island has nine individuals per niche. Species richness on the smallest island is 4, on the medium island is 15 and the large island is 33

Chisholm et al., (2016) explain both deterministic and stochastic SARs in a unified theory. They posit this pattern is due to transition from a niche-structured regime on smaller islands, to colonisation-extinction regime on larger islands. The niche-structured regime is characteristic of deterministic theories like the Habitat-Diversity Hypothesis, where habitat structure and intra- and interspecific interactions determine species richness (Chase and Myers, 2011). The colonisation-extinction regime is characteristic of stochastic mechanisms such as the Theory of Island Biogeography and ecological neutral theory, where richness is dictated by random colonisation and extinction events, as well as ecological drift (Hubbell, 2001). Chisholm et al., hypothesise that species richness on all islands is maintained by these two mechanisms, where niche diversity increases slowly with area and immigration rate increases quickly. Smaller islands are constrained by niche-structured regimes, until a critical area threshold where species richness is constrained by immigration. Figures 1.2 and 1.3 show the effect of immigration rate and area on species richness, where each 'island' is made of four niches and the different coloured patches inside each niche represent a species unique to that niche. Small islands where each niche supports a small number of individuals will be constrained by those niches and species richness will not vary considerably with immigration rate. Larger island species richness varies considerably with immigration rate as they are less constrained by the number of niches and diversity is dictated by immigration and extinction. Chisholm et al., developed a parsimonious mechanistic model to test their hypotheses, and applied it to 100 archipelago datasets. Their results supported the prediction that critical area will be lower for species with higher motility and less isolated habitats.

Previous research indicates that microbial TARs may be controlled by either deterministic or stochastic processes (Stegen et al., 2012). Phylogenetic analysis of subsurface microbial communities showed related taxa utilised similar habitats, illustrating that environmental filtering determined community composition (Stegen et al., 2012). Niche filtering has a greater influence in spatially and temporally diverse environments and varies with community functionality (Stegen et al., 2012) (Caruso et al., 2011).

Whilst both stochastic and deterministic processes affect microbial communities, few studies discuss the transition of mechanisms across a spatial scale. An investigation of phytoplankton TARs in water bodies indicated that for the smallest spatial scales, niche structure determine OTU richness, before transitioning to an immigration dominated regime (Várbíró et al., 2017). The SIE has also been seen in benthic diatoms where stochastic variation in OTU richness is a function of small habitat instability (Bolgovics et al., 2016).

Aquatic habitats are some of the most studied in microbial biogeography due to the avail-

ability of insular water bodies and their range of spatial scales. An investigation into bacterial diversity in aquatic tree holes found a z value comparable to macro-organisms (z = 0.26) (Bell et al., 2005). Antarctic cryoconite holes have also exhibited positive TARs on glaciers where dispersal is limitated (Darcy et al., 2018). Positive TARs have been reported for habitats as diverse as lakes (Battes et al., 2019), membrane bioreactors (Van Der Gast et al., 2006) (Van Der Gast et al., 2005) and vertebrate bodies (Godon et al., 2016).

Previous investigations into ectomycorrhizal fungi communities within 'tree island' root systems showed that total OTU richness increased significantly with size, although distance effects vary (Glassman et al., 2017) (Peay et al., 2007). Bacterial and fungal diversity has been positively correlated with area but via different mechanisms (Li et al., 2020). Country and continent-scale patterns of pathogen diversity have also been shown to be a function of area and isolation (Jean et al., 2016) (Cashdan, 2014). In both terrestrial and aquatic systems microbial communities exhibit significant TARs. The varying mechanisms underlying these TARs warrant further investigation.

In this project I apply three modified versions of the model presented by Chisholm et al.,:

- · Classic Model: Where per capita immigration rate is proportional to area (e.g. in the case of aerial and directed dispersal species immigrating into a two-dimensional habitat)
- · **Perimeter Model**: Where per capita immigration is proportional to perimeter (e.g. in the case of water or soil dispersed species immigrating into a two-dimensional habitat)
- · **Depth Model**: Where per capita immigration rate is proportional to depth (e.g. in the case of species dispersing into a volume via a surface portal (three-dimensional habitat))

These models are applied to bacterial, archaeal and micro-eukaryote insular spatial data with the aim of testing whether there is a biphasic microbial TAR, as well as investigating the impact of habitat type and taxonomic group on critical area of transition between the deterministic and stochastic regimes.

Methods

I developed a simulation model with three variants, based on the model presented by Chisholm et al., (2016). The variants consist of the Classic Model, and two modifications (Depth Model and Perimeter Model) for use in microbial TARs. I verified the simulation data by comparison to analytic results from the simplified equation presented by Chisholm et al., (2016) (2.2). The model fitting procedure was validated by fitting the model to simulation data with known parameters. The model fitting procedure was then applied to empirical data from the literature.

2.1 The Model

The model describes a metacommunity and an island community. The metacommunity represents a source population from which propagules can immigrate to an island. Both communities are made up of K non-overlapping niches. We assume that area is measured in number of individuals present ($\rho=1$). Neutral theory assumes that an individual's probability of birth and death do not depend on its species or density. In my model, each niche follows two suppositions of ecological neutral theory: niches operate under a zero-sum assumption (where community size is constant) and each species within the niche is considered ecologically equivalent (with the same probability of producing a propagule or dying). The metacommunity is generated by a modified coalescence algorithm (Rosindell et al., 2008) (see Supplementary Materials, Figure 7.1). A separate metacommunity is generated for each of K niches and each niche consists of 10 000 individuals (J). The metacommunity is assumed to be constant over timescales relevant to the island communities.

Each island niche is initiated with one unique species. At each timestep I process one randomly selected niche of every island. One individual in that niche dies and leaves a gap for another individual of a species suitable to occupy that niche. With probability m (the per capita immigration rate), the dead individual is replaced with a randomly chosen propagule from the metacommunity. Species may only immigrate from the same niche in the metacommunity, to the corresponding niche in the island community. With probability 1 - m, the dead individual is replaced with a local propagule from the same niche. The species richness for each island is stored every 5000 timesteps.

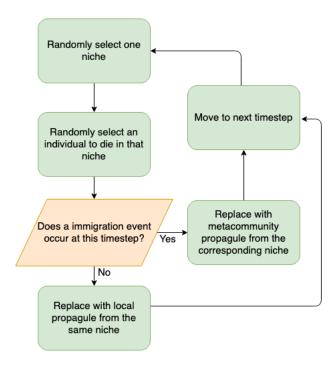


Figure 2.1: Flowchart of simulation design

The probability of an immigration event occurring at each birth/death event (m) is calculated with three variations, the Classic Model, the Depth Model and Perimeter Model (Figure 2.2). m_{θ} is the immigration constant parameter from which m is calculated. The Classic Model is the original model presented by Chisholm $et\ al\ (2016)$ and is most appropriate for species utilising aerial or directed dispersal, where immigration rate is directly proportional to area. The Depth Model simulates immigration into a three-dimensional space where species inhabit depth as well as area. For the Depth Model, each island simulation is given a depth of 1 unit. The Perimeter Model calculates m as proportional to perimeter, for species that immigrate across land or water and whose likelihood of encountering a habitat is based on its perimeter.

I ran 200 simulations 100 times for each of the three models (Classic, Depth and Perimeter) using the High Performance Computing (HPC) service at Imperial College London.

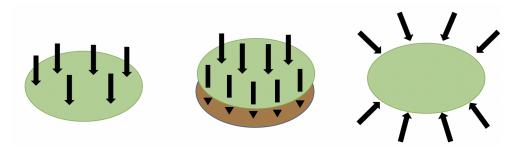


Figure 2.2: Classic $(m=m_0)$, Depth $(m=m_0/depth)$, Perimeter $(m=m_0/\sqrt{area})$

The 200 simulations consisted of 20 island areas differing in powers of 2 multiplied by 10 unique parameter combinations (Table 2.1). m_0 values for the Perimeter Model simulation were higher than those for the Classic and Depth Models, to allow the simulation to reach equilibrium within 24 hours. Parameter values are not indicative of real-world speciation or immigration rates and are arbitrary values to facilitated running the simulation to equilibrium within 24 hours. I plotted a timeseries for each simulation to ensure equilibrium has been reached, before calculating the mean species richness for each set of simulation parameters.

Table 2.1: Simulation parameters where the same range of parameters is applied to each of the Classic, Depth and Perimeter Model simulations. Higher m_0 values were given to the Perimeter Model simulation to allow it to reach equilibrium within 24 hours. Simulations with larger areas and low immigration rates (m) take longer to reach equilibrium and for the Perimeter Model simulation $m=m_0/\sqrt{area}$ thus immigration rates were considerably lower than for the Classic and Depth Models

| Parameter | Values |
|---|---------------------------------|
| speciation rate (nu) | 0.00001 - 0.0001 |
| immigration constant (m_0) | 0.01 - 0.1 (0.09-0.1 Perimeter) |
| number of niches (K) | 5 - 50 |
| simulation areas (i.e. number of individuals) | 5 - 20,000 |

2.1.1 Validation and Model Fitting Procedure

The results of the model were found analytically by applying the simplified mathematical model presented by Chisholm *et al.*, (2.2-2.5). Analytic and simulation results were compared to ensure the model had been simulated successfully. In these analytical solutions the species richness (S) is given by:

$$S = \theta\{\psi(\frac{\theta}{K} + \gamma(\psi(\gamma + J) - \psi(\gamma))) - \psi(\frac{\theta}{K})\}$$
 (2.1)

Where ψ is the digamma function, J is the number of individuals per niche, K is the number of niches and θ is the fundamental biodiversity number calculated as

$$nu*(J*K-1)/(1-nu)$$

$$\gamma = (J-1)m/(1-m)$$
 (2.2)

and

$$m = m_0$$
 or $m = m_0/D$ or $m = m_0/\sqrt{A}$ (2.3)

Where m_{θ} is the immigration constant used to calculate per capita immigration rate m, D = depth, A = area and

$$J = A \rho/K$$
 or $J = A \rho D/K$ (2.4)

Where $J = A \rho/K$ is used for the two-dimensional models (Classic and Perimeter) and $J = A \rho D/K$ is used for the three-dimensional model (Depth). For all simulations ρ is given as 1 as area (A) is measured in units corresponding to number of individuals.

The mathematical model was fit to the simulation data using non-linear least squares (NLLS) fitting in R (version 3.6.1 (2019-07-05)). The model fitting procedure uses the minpack.lm package. This package provides a Levenberg-Marquardt NLLS fitting function (nlsLM) that uses a more robust algorithm than it's base-R counterpart.

The three fitted parameters of the model are K, m_{θ} and θ . To aid the fitting procedure values of K were looped through from 1 to maximum species richness and from this \hat{m}_{θ} and $\hat{\theta}$ starting values were calculated, where A_{med} is median surface area of habitats, $S_{A_{\text{max}}}$ is species richness in the largest habitat and $W_{-1}(x)$ is the lower branch of the Lambert W function. The best-fit values were stored for the K and corresponding m_{θ} and θ that gave the highest \mathbb{R}^2 score. They were calculated as follows:

$$\hat{m}_0 = \frac{-K}{\rho \ A_{med} \ W_{-1} \ (-K \ \rho \ A_{med})} \tag{2.5}$$

$$\hat{\theta} = \frac{S_{A_{max}} \,\hat{\gamma} \, log \, \hat{m}_0}{S_{A_{max}} - \hat{\gamma} \, log \, \hat{m}_0 \, W_{-1} (exp(S_{A_{max}} / \hat{\gamma} \, log \hat{m}_0 \, S_{A_{max}}) / (\hat{\gamma} \, log \, \hat{m}_0))}$$
(2.6)

Where $\hat{\gamma}$ is calculated as:

$$\hat{\gamma} = \frac{(\rho A_{max}) - 1)\hat{m_0}}{1 - \hat{m_0}} \tag{2.7}$$

Using NLLS to fit the three models to their corresponding simulations I was able to validate the fitting procedure by recapturing the known parameters $(K, m_0 \text{ and } \theta)$.

2.1.2 Critical Area

The critical area of transition from niche-structured regime to extinction-colonisation equilibrium regime (A_{crit}) where the TAR starts to increase to a steeper gradient can be calculated as:

Classic Model

$$A_{\text{crit}} = \frac{\theta(1 - m_0)(exp(K/\theta) - 1)}{m_0 \ \rho \ log(1/m)}$$
 (2.8)

Depth Model

$$A_{\text{crit}} = \frac{1}{\rho D} \left[\frac{\theta(exp^{\frac{K}{\theta}} - 1)(D - m_0)}{m_0 \log(\frac{m_0}{D})} + 1 \right]$$
 (2.9)

Perimeter Model

$$x = \frac{\theta(exp^{\frac{K}{\theta}} - 1)}{m_0 \rho} \quad \text{and} \quad A_{\text{crit}} = \left\{ \frac{x}{W_0(x/m_0)} \right\}^2$$
 (2.10)

For each model fitting, A_{crit} is estimated from the best-fit parameters of K, θ and m_{θ} . For higher values of K and lower values of K and K are validated by visual inspection of fits to the simulation data.

With parameter estimations obtained from the NLLS fitting of the three models to empirical datasets, A_{crit} was estimated. For habitats with varying area and depth values A_{crit} was calculated for each depth value, the mean taken then multiplied by the mean depth of the dataset to give a mean critical volume (V_{crit}) and plotted with habitat volume (depth x area) and species richness. The mean A_{crit} from these fittings is used in the statistical analysis for comparison with homogenous depth habitats. By finding A_{crit} for empirical datasets, I was able to test the theory that regime shift would occur at lower areas for less isolated habitats and for more motile taxa.

2.2 Data Collection and Analysis

Table 2.2: Summary of datasets collected from the literature

| Taxa | Habitat | Count |
|------------------------|------------------------|-------|
| algae | lacustrine | 10 |
| algae | riverine | 3 |
| archaea | lacustrine | 1 |
| bacteria | lacustrine | 9 |
| bacteria | machine | 4 |
| bacteria | terrestrial | 4 |
| fungi | lacustrine | 4 |
| fungi | plant | 5 |
| fungi | terrestrial | 4 |
| pathogen | terrestrial | 4 |
| protozoa | lacustrine | 7 |
| protozoa | riverine | 1 |
| protozoa | terrestrial | 1 |

I compiled 57 datasets from 29 studies on microbial TARs (Table 2.2) (see Supplementary Materials, Table 7.1). They include a range of taxonomic groups and habitat types. Before model fitting, datasets without positive correlation between area and OTU richness were excluded. Datasets with a positive correlation were imported into each of the three NLLS fitting scripts (Classic, Depth, Perimeter). ρ was estimated separately from the other three parameters. Estimations were taken from the original study or proxy papers (see Supplementary Material, Table 7.2). I also fitted each dataset with the simple power-law model

(Introduction, Equation 1.1) and the model fit is compared to each of the Classic, Depth and Perimeter models using Akaike Information Criterion (AIC) score to determine if, by incorporating θ , K, m_{θ} and ρ parameters, our models are better fits to the data.

2.3 Statistical Analysis

For empirical datasets where adjusted R^2 was between 0 and 1 and at least one of the three models was a reasonable fit, I found the mean R^2 and adjusted R^2 as well as the standard deviation and range. For datasets that were equally well fit to two or more of the models I found the mean A_{crit} and parameter estimations (θ, m_0, K) for each of those fittings and used these in the analysis. The median, standard deviation and range of the fitted parameters was found and correlation tests carried out. Differences between mean A_{crit} across habitat types and taxonomic groups was found. Multiple regression analysis of log A_{crit} was carried out with habitat type and taxonomic group as categorical explanatory variables.

Results

3.1 Simulation

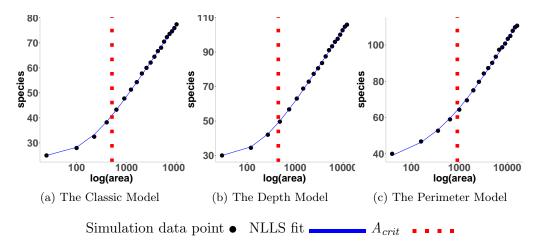


Figure 3.1: NLLS fitting of simulation data. A) The Classic Model with true parameters θ =13, m_0 =0.05, K=25 and estimated parameters θ =13, m_0 =0.05, K=25. B) The Depth Model with true parameters θ =18, m_0 =0.06, K=30 and estimated parameters θ =19, m_0 =0.05, K=30. C) The Perimeters Model with true parameters θ =32, m_0 =0.7, K=40 and estimated parameters θ =35, m_0 =0.6, K=39.

My results verified that the simulation and analytic formula are in agreement as expected. The three A_{crit} formulas for each of the three model variations give reasonable estimations.

3.1.1 Classic Model

The Classic Model fitted the simulated data well. Estimated parameters were slightly higher than the true parameters for θ and slightly lower for m_{θ} and K. There was a significant difference between the true and estimated parameters for θ (p=0.0009, 9 df) and m_{θ} (p=0.0002, 9 df). There was no significant difference in parameters for K (p=0.08, 9 df). As K parameters showed no significant difference, and there was only a small difference between m_{θ} and θ parameters, the model fitting process is considered validated and fit for

applying to empirical datasets.

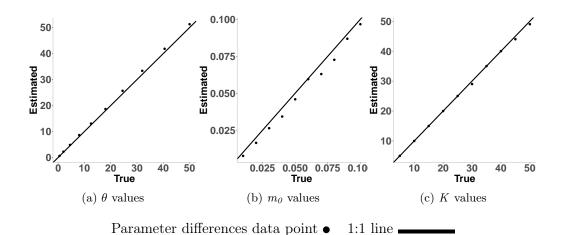


Figure 3.2: The true parameters values of θ (A), m_{θ} (B) and K (C) were simulated and the results fitted using the Classic Model analytical NLLS fitting procedure to get the parameters back. True and estimated values for the three fitted parameters are plotted above. Fittings of the Classic Model to simulated data returned mean $R^2 = 0.99$, adjusted $R^2 = 0.99$.

Table 3.1: Comparison between true and estimated mean parameters across 200 Classic Model simulations clustered into 10 groups where parameter values (θ, m_0, K) were the same for each simulation group with varying areas.

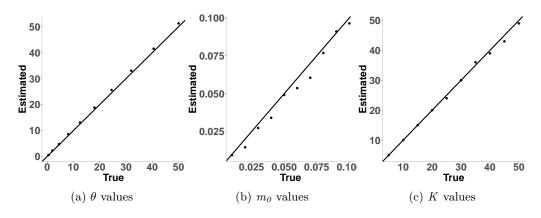
| Parameter | True | Estimated | Difference |
|-----------|--------|-----------|------------|
| theta | 19.251 | 20.008 | 0.756 |
| m0 | 0.055 | 0.051 | -0.004 |
| K | 27.500 | 27.200 | -0.300 |

3.1.2 Depth Model

The Depth Model fitted the simulated data well. Estimated values of θ were higher, K and m_{θ} values were lower than the true parameters (Table 3.2). There was a significant difference between the true and estimated values for θ (p=0.0005, 9 df) and m_{θ} (p=0.005, 9 df), but there was no significant difference for K (p=0.168, 9 df). As K showed no significant difference, and the difference in estimated θ and m_{θ} values were low, the model fitting process is considered validated and fit for applying to empirical datasets.

3.1.3 Perimeter Model

The Perimeter Model fitted the simulated data well. Estimated parameters for θ were slightly higher than true parameters, whilst m_0 and K were slightly lower than the true



Parameter differences data point • 1:1 line _____

Figure 3.3: The true parameters values of θ (A), m_{θ} (B) and K (C) were simulated and the results fitted using the Depth Model analytical NLLS fitting procedure to get the parameters back. True and estimated values for the three fitted parameters are plotted above. Fittings of the Depth Model to simulated data returned mean $R^2 = 0.99$, adjusted $R^2 = 0.99$.

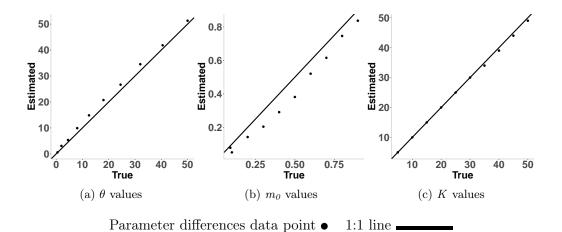


Figure 3.4: The true parameters values of θ (A), m_{θ} (B) and K (C) were simulated and the results fitted using the Perimeter Model analytical NLLS fitting procedure to get the parameters back. True and estimated values for the three fitted parameters are plotted above. Fittings of the Perimeter Model to simulated data returned mean $R^2 = 0.99$, adjusted $R^2 = 0.99$.

Table 3.2: Comparison between true and estimated mean parameters across 200 Depth Model simulations clustered into 10 groups where parameter values (θ, m_0, K) were the same for each simulation group with varying areas.

| Parameter | True | Estimated | Difference |
|-----------|--------|-----------|------------|
| theta | 19.251 | 19.965 | 0.713 |
| m0 | 0.055 | 0.051 | -0.004 |
| K | 27.500 | 27.100 | -0.400 |

Table 3.3: Comparison between true and estimated mean parameters across 200 Perimeter Model simulations clustered into 10 groups where parameter values (θ, m_0, K) were the same for each simulation group with varying areas.

| Parameter | True | Estimated | Difference |
|-----------|--------|-----------|------------|
| theta | 19.251 | 20.885 | 1.634 |
| m0 | 0.459 | 0.387 | -0.072 |
| K | 27.500 | 27.100 | -0.400 |

parameters (Table 3.3). There was significant difference between the true and estimated values for θ (p=0.0002, 9 df), m_0 (p=5x10⁵, 9 df) and K (p=0.04, 9df). Despite the significant difference between the estimated and true values, the differences are small and the model fitting process is considered validated and fit for applying to empirical datasets.

3.2 Model Fitting

3.2.1 Non-Linear Least Squares Fitting

50 of the 57 datasets exhibited a positive TAR and were used for the NLLS fitting. Of the 50 datasets 26 failed to achieve adjusted R² scores of between 0 and 1. These datasets were excluded from further analysis (see Supplementary Materials, Figure 7.2).

Table 3.4: The mean R^2 and adjusted R^2 results for each model (Classic, Depth, Perimeter) after being successfully fitted to 24 empirical datasets.

| Model | R^2 | $AdjR^2$ |
|-----------|-------|----------|
| Classic | 0.492 | 0.409 |
| Depth | 0.493 | 0.410 |
| Perimeter | 0.486 | 0.401 |

All three models had similar mean R² and adjusted R² scores and fit the data moderately well (Table 3.4). The Classic Model was best-fit for 1 dataset, Depth and Perimeter were

best for 2 each and the rest of the datasets were either best described by both Classic and Depth or all of the models (Table 3.5).

Table 3.5: The best-fit models (Classic, Depth, Perimeter) by highest adjusted R^2 value for each empirical dataset (note some datasets had equal adjusted R^2 values for two or more models).

| Models | BestFit |
|-----------------------|---------|
| Classic | 1 |
| Depth | 2 |
| Perimeter | 2 |
| Classic and Depth | 10 |
| Classic and Perimeter | 0 |
| Depth and Perimeter | 0 |
| All | 9 |

The best model fits had mean $R^2 = 0.49$ and mean adjusted $R^2 = 0.41$ with standard deviation 0.28 and range 0.01 - 0.96. The median value of θ was 8, with a range of 0.28 – 159709. The median value of m_{θ} was 2.17 x10⁻⁹ with a range of 4.97 x 10⁻¹⁶ – 0.56. The median value for K was 7, with range 1 – 424. There was no correlation between the best fitted-values of the four parameters (Table 3.6).

Table 3.6: p-values of correlations between the four model parameters (θ, m_0, K, ρ) that show no correlation

| Parameter | K | Theta | m_0 | rho |
|----------------------|-------|-------|-------|-------|
| K | NA | 0.472 | 0.369 | 0.518 |
| Theta | 0.472 | NA | 0.110 | 0.200 |
| m0 | 0.369 | 0.110 | NA | 0.140 |
| rho | 0.518 | 0.200 | 0.140 | NA |

The power-law model had the same number of successful fittings as the Classic, Depth and Perimeter models. After removing failed fits the mean z value was 0.16. The power-law model performed more poorly than the other three models (R^2 =0.47, adjusted R^2 =0.38) (see Supplementary Materials, Table 7.3). AIC scores indicated that the power-law model was not a more parsimonious model than the Classic, Depth or Perimeter models relative to model fit for any of the datasets (see Supplementary Materials, Table 7.4). The Classic and Depth models were significantly better than the power-law model for 9 datasets each. The Perimeter model was a better fit than the power-law model for 5 datasets.

3.3 Critical Area

Of the five habitat types (terrestrial, riverine, lacustrine, plant and machine) and six taxonomic groups (algae, archaea, bacteria, fungi, pathogens and protozoa), the riverine habitat and archaea group did not have any successful fittings and are excluded from the following analysis.

The log A_{crit} data were not normally distributed with non-homogenous variances. Despite the violation of normality I have proceeded with the multiple regression analysis, although interpretation of results will take this into consideration.

Initial multiple regression revealed that the model was a poor fit to the data (R^2 =0.39, adjusted R^2 =0.05, p=0.374) and neither categorical variable was significant in predicting log A_{crit} (habitat type p=0.1759, taxonomic group p=0.6402). A plot of the model indicated that there was an outlying data point. After removing the outlying data point the model was significant in describing the data (R^2 =0.62, adjusted R^2 =0.44, p=0.02). Taxonomic group became weakly significant in predicting log A_{crit} (p=0.0187), habitat type did not (p=0.097). After removing habitat type as a variable the model was a similar fit to the data but more significant (R^2 =0.55, adjusted R^2 =0.45, p=0.004).

Multiple regression including taxonomic group upheld the prediction that A_{crit} would occur at lower areas for more motile OTUs as bacteria show the lowest $\log A_{crit}$ estimate and host-dependent pathogens show the highest (Table 3.7).

There was a large variation in mean log A_{crit} between habitats and taxonomic groups. Terrestrial habitats showed the highest mean log A_{crit} (27.33), whilst machine habitats showed the lowest (4.66) (Figure 3.6). Pathogens exhibited the largest mean log A_{crit} for taxonomic groups (55.15), with bacteria having the lowest (4.06) (Figure 3.6).

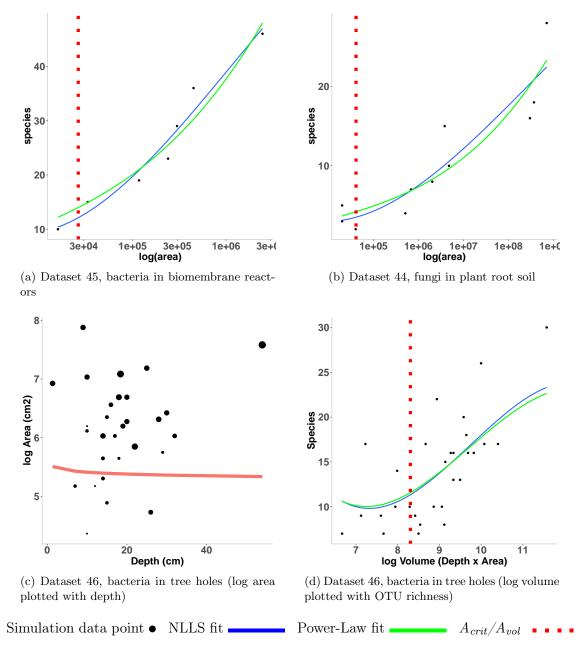


Figure 3.5: A) Best-fit Classic Model for dataset 45, bacteria in biomembrane reactors. Red line indicates A_{crit} , blue line indicates NLLS fit and green line indicates power-law fit (NLLS fit: R^2 =0.96, adjusted R^2 =0.88, θ =9, m_0 =4.97 x 10^{-16} , K=7, power-law fit: R^2 =0.94, adjusted R^2 =0.82, z=0.27, z=0.88). B) Best-fit Perimeter Model for dataset 44, fungi in plant soil (NLLS fit: R^2 =0.85, adjusted R^2 =0.77, θ =5, m_0 =6.15 x 10^{-11} , K=2, power-law fit: R^2 =0.87, adjusted R^2 =0.78, z=0.18, z=0.64). C) Best-fit Depth Model for dataset 46, bacteria in freshwater treeholes. The size of the black circles represents increasing OTU richness at that corresponding depth (x-axis) and log area (y axis) (R^2 =49, adjusted R^2 =0.40, θ =8, m_0 =3.75 x 10^{-9} , K=6, power-law fit: R^2 =0.46, adjusted R^2 =0.38, z=0.33, z=1.74). Where the red line passes through depth and area space is where A_{crit} occurs. D) Dataset 46 plotted as log Volume by OTU richness to illustrate the model fit and log critical volume (A_{vol})

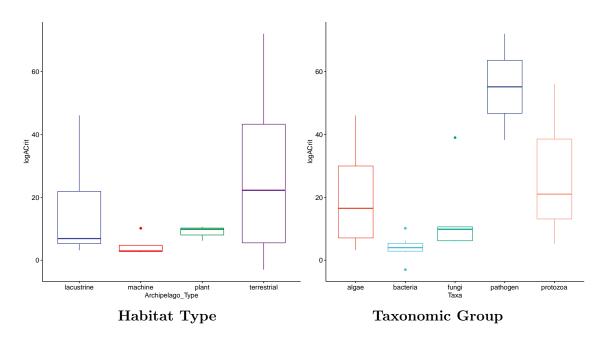


Figure 3.6: $\log A_{crit}$ by habitat type and taxonomic group after removing anomalous result

Table 3.7: Table showing the results of multiple regression analysis of estimated effect of taxonomic group only on log A_{crit}

| Variable | Estimate | 95% CI | p-value |
|-------------------|----------|-----------------|---------|
| intercept (algae) | 20.56 | [5.07, 36.07] | 0.0121 |
| taxonomic group | | | 0.004 |
| bacteria | -16.500 | [-35.12, 2.12] | 0.0791 |
| fungi | -6.222 | [-27.01, 14.56] | 0.5373 |
| pathogens | 34.587 | [7.75, 61.42] | 0.0144 |
| protozoa | 6.879 | [-16.79, 30.55] | 0.5491 |

Discussion

I have presented three variations of the Chisholm model (Chisholm et al., 2016) that take into account varying habitats and immigration routes and have successfully fit all three to microbial TAR data. The relatively equal success of the three model variations (Classic, Depth, Perimeter) suggests that immigration route is not a significant factor in defining microbial TARs (see Supplementary Materials, Table 7.5). Microorgansims can cross oceanic, glacial and global barriers through a variety of dispersal mechanisms (Rosselli et al., 2015) (Darcy et al., 2018) (Kleinteich et al., 2017). Microbial OTUs utilise a variety of immigration routes when entering a new environment. No significant accuracy was lost in assessing three-dimensional habitats using the two-dimensional models (Classic, Perimeter), suggesting habitat depth did not affect OTU richness as strongly as area, where area acts as immigration portal into the three-dimensional habitat. Algae and bacteria have shown negative correlations between OTU richness and depth (Battes et al., 2019) (Turner et al., 2017). Nutrient-poor, low-energy environments may accompany increasing habitat depth. The immigration portal may be characterised by a nutrient-rich, high-energy stratification that is a more potent predictor of OTU richness than depth.

The phenomenological power-law model did not perform significantly better than the mechanistic Classic, Depth and Perimeter models, according to the AIC measure of parsimony, relative to model fit (see Supplementary Materials, Table 7.4). This indicates that the model parameters $(\theta, m_{\theta}, K, \rho)$ were useful in describing TARs, supporting the hypothesis that OTU richness is influenced by the parameters, rather than being a constant power of area. The mean slope of positive TARs across these datasets was comparable to macroorganisms (z=0.16) and higher than those previously reported for microbial taxa (Rosenzweig et al., 1995) (Green et al., 2004) (see Supplementary Materials, Table 7.3). These observations show habitat area has a relatively strong influence on OTU richness.

Successfully fitted datasets exhibit both the classic MacArthur and Wilson (MacArthur, 1967) biogeographic pattern and the SIE. The results demonstrate that some microbial communities are constrained by niche-structured regimes at smaller areas where immigration is low, before transitioning to colonisation-extinction balance regimes at larger areas where immigration is high. This lends support to the theory that microbial species are not ubiquitous and unlimited in dispersal, that they can be limited by habitat heterogeneity, resource availability and dispersal barriers, but this is not a ubiquitous pattern with over 50% of the datasets failing to be fit by the model.

Many datasets with positive TARs could not be successfully fit with the power-law, Classic, Depth or Perimeter models (see Supplementary Materials, Figure 7.2). Despite positive z values, confidence intervals included zero and were not statistically significant. Stochastic variation between data points inhibited identification of significant TARs (see Supplementary Materials, Figure 7.2 a & b). The majority of failed fits were aquatic habitats and may be due to uncertainty in the spatial sample regime of a heterogenous habitat. In order to elucidate these patterns it might be useful to take a stratified approach. Some failed fits had too few data points in comparison to the number of model parameters, producing low adjusted \mathbb{R}^2 values (see Supplementary Materials, Figure 7.2 b). Microbial TARs may also be undetected due to the disparity between sample and community sizes meaning rare taxa are missed (Woodcock et al., 2006).

This project is, to the best of my knowledge, the first attempt to apply a biphasic mechanistic TAR model to microbial data. The model demonstrates that when niche diversity increases slowly or remains constant and immigration increases quickly with area, a biphasic TAR is produced. At an A_{crit} specific to that habitat and taxonomic group, the TAR will transition from deterministic to a stochastic mechanisms. I hypothesised that A_{crit} would be lower where immigration is higher (i.e. for more motile OTUs and less isolated habitats). My analysis indicated that taxonomic group was significant in predicting A_{crit} , while habitat type was not. Taxonomic group is significant in predicting A_{crit} as taxa are constrained (or liberated) by their life stages (activity and dormancy) and dispersal methods. According to this data isolated habitats present no significant dispersal barriers to microorganisms as a whole, although their relative accessibility varies between taxonomic groups. Overall, after removing the outlying datapoint and removing habitat type as an explanatory variable, the model accounts for nearly half of the variation in log A_{crit} using

broad taxonomic groups.

My analysis indicated that pathogenic OTUs had overwhelmingly higher A_{crit} values (mean 9.43 x 10^{30} cm²), suggesting they are more constrained by resource availability and dispersal barriers. This may be due to their dependence on host species, although this will be directly related to the motility and sociability of their hosts. The two datasets used in this study quantify human pathogen richness on 'true' islands (Jean et al., 2016). Human pathogen OTU richness is negatively correlated with disease control efforts (Dunn et al., 2010). I suggest that global mitigation strategies such as behavioural change, medicine and vaccination mean pathogens face considerable dispersal barriers that limit immigration and constrain them to niche-structured spatial regimes over larger areas (Nicolaides et al., 2020).

Bacterial OTUs exhibited the lowest mean A_{crit} value (3.02 x 10^3 cm²). The small size of bacteria allows them to dispersal more freely than size-limited macroorganisms (Martiny et al., 2006). They may also overcome dispersal limitation through dormancy and enormous population sizes (Locey, 2010) (Fenchel and Finlay, 2004). Bacteria have a variety of ecological traits that allow them to move freely and access isolated habitats, thus they transition to stochastic TAR mechanisms at lower areas.

Fungi also showed low A_{crit} values (mean 1.72 x 10^{16} cm²). Mycorrhizal fungi that share beneficial associations with plant roots, have large spores that immigration slowly through soil (Bueno and Moora, 2019), however, the close proximity of potential host plants might mitigate low fungal motility. For other fungal groups, long distance spore dispersal is facilitated by meteorological, biotic and anthropogenic vectors (Golan and Pringle, 2017). Fungal sporulation allows taxa to overcome local and regional barriers, thus contributing to the low A_{crit} values seen in these datasets.

Algae (mean $2.56 \times 10^{19} \text{ cm}^2$) and protozoa (mean $7.43 \times 10^{23} \text{ cm}^2$) exhibited similar broad, midrange A_{crit} values which may be due issues of sampling in spatially heterogenous aquatic environments. Issues of taxonomic classification, particularly for protists, may contribute to varying estimations of diversity (Foissner, 2006). Whilst it seems algae and protists transition from deterministic to stochastic mechanisms in the midrange of areas, further investigation is needed to discern a true pattern within the wide range of A_{crit}

values estimated. The multiple regression model coefficients (Table 3.7) broadly confirm the overall taxonomic results.

As the multiple regression analysis showed that habitat type was non-significant in predicting A_{crit} I cannot assess the relative isolation of habitats or how they may affect A_{crit} . The non-significance of habitat type, despite marked differences in the mean A_{crit} is due to the large, overlapping estimate ranges. It is interesting however to look at mean A_{crit} values for each habitat, as a sign post towards what may be found with a more comprehensive dataset. Terrestrial habitats show the highest mean A_{crit} values (2.36 x 10^{30} cm²). This may be due to immigration via an accidental vector being limited to aerial species that can reach land islands. Passive immigration to land islands relies on stochastic success which may limit dispersal, although fungal and bacteria OTU richness on land islands has been shown be unaffected by isolation (Li et al., 2020).

Lacustrine habitats exhibited low mean A_{crit} values (1.28 x 10^{19} cm²) suggesting immigration to these habitats is high. Aquatic taxa utilise a variety of dispersal mechanisms between habitats, including dispersal via insects and waterfowl (Stewart and Schlichting Jr, 1966). It may be easier for microbial OTUs to colonise inland lacustrine environments where animal activity increases the probability of vector transport. There may be higher rates of passive transport to lacustrine environments due to the interconnectivity of rivers and streams that empty into watershed areas, filling lakes and ponds.

Plant habitats also have low mean A_{crit} values (2.01 x 10^4 cm²). For many symbiotic plant-microbe species relationships, plant seeds are already inoculated with associated microbial taxa on dispersal (Ho et al., 2017). Thus dispersal barriers between plant and microbes are removed, contributing to low A_{crit} values. Many plant communities are comprised of the same species in close proximity, providing ready access to source populations and increasing immigration.

Four of the six best-fit datasets were for bacteria in machine habitats (Van Der Gast et al., 2006) (Van Der Gast et al., 2005). It may be the strong TAR is a function of isolation, relative to natural habitats. When constrained by immigration more prominent and easily quantifiable TAR patterns arise. The model fitting process supports this by estimating extremely low immigration rates for machine habitats. Despite this, machine habitats had the lowest mean A_{crit} (6.56 x 10³ cm²). A_{crit} is not only affected by immigration as in my

primary hypothesis, but can also be affected K, ρ and θ . In the fitted model the low A_{crit} for machine habitats in spite of their isolation is caused by the low K values of homogenous, man-made environments, a characteristic of these unusual habitats that warrants further investigation.

The reason for the lack of successful fittings for riverine habitats is due to the low number of data points that forced low adjusted R² scores, despite initial good fits (see Table 7.1, Supplementary Material). Only one dataset included archaeal TARs and no significant relationship between area and OTU richness was found. This is likely due to the importance of environmental filtering for extremophile OTUs in soda lakes (Lanzén et al., 2013). It is interesting to note other datasets removed from the fitting process due to a lack of positive TARs. These included, fungi in the Antarctic cryoconite holes of two glaciers where extreme biomass influx negated observable TARs (Darcy et al., 2018). Inappropriate diversity metrics and spatial scaling may have led to undetectable root-symbiotic fungi TARs (Davison et al., 2018). Fungi OTU richness did not increase with area on submerged leaves due to a lack of energy increase with corresponding area as expressed by the species-energy theory (Feinstein and Blackwood, 2012) (Wright, 1983). TARs may not have arisen in protozoan communities due to a failure to reach equilibrium (dataset 55) (Henebry and Cairns Jr, 1980). It is clear that the factors affecting microbial TARs are diverse and each habitat/taxa pairing may require unique assessment.

The anomalous result removed from analysis concerned pathogenic bacterial OTU richness on 'true' geographic islands (Jean et al., 2016). The model was a poor fit to the data ($R^2=0.23$, adjusted $R^2=0.18$) and it's likely the error associated with estimating density for pathogenic bacteria over such large geographic scales lead to poor estimations of the remaining parameters and excessive A_{crit} .

Whilst the data indicate that habitat type is non-significant in predicting A_{crit} , the large range in A_{crit} values suggests there many be too few data points to discern a significant pattern. I also encountered challenges when trying to compare studies that used a variety of quantification techniques. Microbial OTUs inhabit three-dimensional habitats and whilst steps have been taken to account for this there is more work to be done to incorporating this fully. In an extension of this model I would consider each stratification of a habitat separately, to account for spatial heterogeneity. Volume has been shown to be more

accurate in quantifying microbial TARs (Van Der Gast et al., 2006). It would be useful to further modify the model to explicitly incorporate volume and V_{crit} across datasets, as nearly all of them concern habitats within a volume even though often only area data is available. Here I have used area with a depth metric (Depth Model) which suggests the habitat maintains the same area for the full depth, whereas natural habitats rarely take this shape and this reduces the accuracy of my results.

Another issue I encountered was ρ estimations as direct counts are rarely given for microbial OTUs. Estimations were made in various ways, using gene sequence numbers or proxy papers. It would be beneficial to develop more robust methods for estimating ρ as data from proxy papers introduces error. A broad scale experiment to quantify microbial TARs in a laboratory, where data specific to the needs of these models could be collected would provide a more vigorous assessment of the models applicability to microbial TARs.

When validating my fitting procedures there was small but significant error between true and estimated parameters. Parameter ranges of speciation rate, m_0 and K were not inferred from microbial ecological theory, but were selected for ease of computation. A more thorough exploration of the parameter space, with ecologically relevant parameter ranges, to further validate the fitting procedure and the areas of parameter space where there may be errors in fitting would be desirable in further work.

There remains to be a thorough synthesis between biogeography and microbial ecology. Here I have gone some way to evaluate the influence of immigration on microbial TARs, however more work is needed to examine dispersal barriers. Dormancy is a widespread microbial response that may allow OTUs to overcome dispersal barriers and increase immigration to new habitats. However, it is a slow, passive process that will not necessarily lead the individual to a viable habitat (Locey, 2010). To fully elucidate the interplay of microbial ecology and biogeographic patterns, work is needed to incorporate dormancy as a biogeographic response.

An implication of this work is that if we can identify the niches within a habitat and the taxonomic groups that tend to occupy those niches, we may be able to better predict OTU richness at a range of spatial scales. This presents a complex challenge that requires the integration of environmental variables and habitat stratification. If these challenges could

be overcome, it would be a useful tool in predicting colonisation of new habitats such as soil exposed by glacier retreat, helping us model the biogeochemical processes of colonisation.

This study has demonstrated that microbial communities in isolated 'island' habitats can be subject to niche-structured regimes, before a critical area of transition to colonisation—extinction regimes. I have shown that taxonomic group is significant in predicting critical area, but habitat type is not. The overwhelming number, complexity and importance of microbial life illustrates the need to understand their biogeographic patterns. I hope that my study will lead to further research into deterministic and stochastic mechanisms in microbial biogeography, as well as the importance of taxonomic group on the relative influence of these processes. The synthesis of microbial ecology and biogeography will be of increasing interest as climate change alters habitats, extending microbial ranges and leading to climate feedback loops. Microbial biogeography is an essential area of study in our global challenge to predict and mitigate the impacts of climate change. Everything is not everywhere, and everything is changing.

Data and Code Availability

All data and code are available at GitHub: amysolman/CMEECourseWork/Project.

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Bibliography

- Abbott, I. (1974). Numbers of plant, insect and land bird species on nineteen remote islands in the southern hemisphere. *Biological Journal of the Linnean Society*, 6(2):143–152.
- Anderson, W. and Wait, D. (2001). Subsidized island biogeography hypothesis: another new twist on an old theory. *Ecology Letters*, 4(4):289–291.
- Antón, J., Rosselló-Mora, R., Rodríguez-Valera, F., and Amann, R. (2000). Extremely halophilic bacteria in crystallizer ponds from solar salterns. Applied and environmental microbiology, 66(7):3052–3057.
- Baas-Becking, L. G. M. (1934). Geobiologie; of inleiding tot de milieukunde. WP Van Stockum & Zoon NV.
- Barberán, A. and Casamayor, E. O. (2011). Euxinic freshwater hypolimnia promote bacterial endemicity in continental areas. *Microbial Ecology*, 61(2):465–472.
- Barrett, K., Wait, D., and Anderson, W. (2003). Small island biogeography in the gulf of california: lizards, the subsidized island biogeography hypothesis, and the small island effect. *Journal of Biogeography*, 30(10):1575–1581.
- Battes, K. P., Cimpean, M., Momeu, L., ŞUTEU, A. M., Pauliuc, G., Stermin, A. N., and David, A. (2019). Species-area relationships for aquatic biota in several shallow lakes from the fizes valley (transylvania, romania). *North-Western Journal of Zoology*, 15(2).
- Bell, T., Ager, D., Song, J.-I., Newman, J. A., Thompson, I. P., Lilley, A. K., and Van der Gast, C. J. (2005). Larger islands house more bacterial taxa. *Science*, 308(5730):1884–1884.
- Bolgovics, Á., Ács, É., Várbíró, G., Görgényi, J., and Borics, G. (2016). Species area relationship (sar) for benthic diatoms: a study on aquatic islands. *Hydrobiologia*, 764(1):91–102.

- Bradley, J. A., Anesio, A. M., and Arndt, S. (2017). Microbial and biogeochemical dynamics in glacier forefields are sensitive to century-scale climate and anthropogenic change. Frontiers in Earth Science, 5:26.
- Brown, J. H. and Kodric-Brown, A. (1977). Turnover rates in insular biogeography: effect of immigration on extinction. *Ecology*, 58(2):445–449.
- Bueno, C. G. and Moora, M. (2019). How do arbuscular mycorrhizal fungi travel? New Phytologist, 222(2):645–647.
- Cameron, K. A., Hodson, A. J., and Osborn, A. M. (2012). Structure and diversity of bacterial, eukaryotic and archaeal communities in glacial cryoconite holes from the arctic and the antarctic. FEMS microbiology ecology, 82(2):254–267.
- Caruso, T., Chan, Y., Lacap, D. C., Lau, M. C. Y., McKay, C. P., and Pointing, S. B. (2011). Stochastic and deterministic processes interact in the assembly of desert microbial communities on a global scale. *The ISME Journal*, 5(9):1406–1413.
- Cashdan, E. (2014). Biogeography of human infectious diseases: A global historical analysis. *PLoS One*, 9(10):e106752.
- Chase, J. M. and Myers, J. A. (2011). Disentangling the importance of ecological niches from stochastic processes across scales. *Philosophical transactions of the Royal Society B: Biological sciences*, 366(1576):2351–2363.
- Chisholm, R. A., Fung, T., Chimalakonda, D., and O'Dwyer, J. P. (2016). Maintenance of biodiversity on islands. *Proceedings of the Royal Society B: Biological Sciences*, 283(1829):20160102.
- Cole, J. J., Pace, M. L., Caraco, N. F., and Steinhart, G. S. (1993). Bacterial biomass and cell size distributions in lakes: more and larger cells in anoxic waters. *Limnology and Oceanography*, 38(8):1627–1632.
- Connor, E. F. and McCoy, E. D. (1979). The statistics and biology of the species-area relationship. *The American naturalist*, 113(6):791–833.
- Darcy, J. L., Gendron, E., Sommers, P., Porazinska, D. L., and Schmidt, S. K. (2018).
 Island biogeography of cryoconite hole bacteria in antarctica's taylor valley and around the world. Frontiers in Ecology and Evolution, 6:180.

- Davis, A. M. and Glick, T. F. (1978). Urban ecosystems and island biogeography. *Environmental Conservation*, 5(4):299–304.
- Davison, J., Moora, M., Öpik, M., Ainsaar, L., Ducousso, M., Hiiesalu, I., Jairus, T., Johnson, N., Jourand, P., Kalamees, R., et al. (2018). Microbial island biogeography: isolation shapes the life history characteristics but not diversity of root-symbiotic fungal communities. *The ISME journal*, 12(9):2211–2224.
- Delgado-Baquerizo, M., Eldridge, D. J., Hamonts, K., Reich, P. B., and Singh, B. K. (2018). Experimentally testing the species-habitat size relationship on soil bacteria: A proof of concept. Soil Biology and Biochemistry, 123:200–206.
- Dunn, R. R., Davies, T. J., Harris, N. C., and Gavin, M. C. (2010). Global drivers of human pathogen richness and prevalence. Proceedings of the Royal Society B: Biological Sciences, 277(1694):2587–2595.
- Eadie, J. M., Hurly, T. A., Montgomerie, R. D., and Teather, K. L. (1986). Lakes and rivers as islands: species-area relationships in the fish faunas of ontario. *Environmental Biology of Fishes*, 15(2):81–89.
- Elloumi, J., Carrias, J.-F., Ayadi, H., Sime-Ngando, T., Boukhris, M., and Bouaïn, A. (2006). Composition and distribution of planktonic ciliates from ponds of different salinity in the solar saltwork of sfax, tunisia. *Estuarine, Coastal and Shelf Science*, 67(1-2):21–29.
- Feinstein, L. M. and Blackwood, C. B. (2012). Taxa–area relationship and neutral dynamics influence the diversity of fungal communities on senesced tree leaves. *Environmental Microbiology*, 14(6):1488–1499.
- Fenchel, T. and Finlay, B. J. (2004). The ubiquity of small species: patterns of local and global diversity. *Bioscience*, 54(8):777–784.
- Foissner, W. (2006). Biogeography and dispersal of micro-organisms: a review emphasizing protists. *Acta protozoologica*, 45(2):111–136.
- Glassman, S. I., Lubetkin, K. C., Chung, J. A., and Bruns, T. D. (2017). The theory of island biogeography applies to ectomycorrhizal fungi in subalpine tree "islands" at a fine scale. *Ecosphere*, 8(2):e01677.
- Godon, J.-J., Arulazhagan, P., Steyer, J.-P., and Hamelin, J. (2016). Vertebrate bacterial gut diversity: size also matters. *BMC ecology*, 16(1):12.

- Golan, J. J. and Pringle, A. (2017). Long-distance dispersal of fungi. The Fungal Kingdom, pages 309–333.
- Gooriah, L. D. and Chase, J. M. (2019). Sampling effects drive the species area relationship in lake zooplankton. *Oikos*, 129(1):124–132.
- Green, J. and Bohannan, B. J. (2006). Spatial scaling of microbial biodiversity. *Trends in ecology & evolution (Amsterdam)*, 21(9):501–507.
- Green, J. L., Holmes, A. J., Westoby, M., Oliver, I., Briscoe, D., Dangerfield, M., Gillings, M., and Beattie, A. J. (2004). Spatial scaling of microbial eukaryote diversity. *Nature*, 432(7018):747–750.
- Griffiths, R. I., Thomson, B. C., James, P., Bell, T., Bailey, M., and Whiteley, A. S. (2011). The bacterial biogeography of british soils. *Environmental microbiology*, 13(6):1642–1654.
- Grossmann, L., Jensen, M., Pandey, R., Jost, S., Bass, D., Psenner, R., and Boenigk, J. (2016). Molecular investigation of protistan diversity along an elevation transect of alpine lakes. *Aquatic Microbial Ecology*, 78.
- Haila, Y. (2002). A conceptual genealogy of fragmentation research: from island biogeography to landscape ecology. *Ecological applications*, 12(2):321–334.
- Henebry, M. S. and Cairns Jr, J. (1980). The effect of island size, distance and epicenter maturity on colonization in freshwater protozoan communities. American Midland Naturalist, pages 80–92.
- Ho, Y.-N., Mathew, D. C., and Huang, C.-C. (2017). Plant-microbe ecology: interactions of plants and symbiotic microbial communities. *Plant Ecology-Traditional Approaches*To Recent Trends, pages 93–119.
- Hubbell, S. P. (2001). The unified neutral theory of biodiversity and biogeography (MPB-32). Princeton University Press.
- Humayoun, S. B., Bano, N., and Hollibaugh, J. T. (2003). Depth distribution of microbial diversity in mono lake, a meromictic soda lake in california. Applied and environmental microbiology, 69(2):1030–1042.
- Jean, K., Burnside, W. R., Carlson, L., Smith, K., and Guégan, J.-F. (2016). An equilibrium theory signature in the island biogeography of human parasites and pathogens. Global Ecology and Biogeography, 25(1):107–116.

- Karatayev, A. Y., Burlakova, L. E., and Dodson, S. I. (2005). Community analysis of belarusian lakes: relationship of species diversity to morphology, hydrology and land use. *Journal of Plankton Research*, 27(10):1045–1053.
- Kavazos, C. (2016). Small-scale biogeographic patterns of benthic bacterial and ciliate communities in the saline ponds of lake macleod, north-western australia.
- Kleinteich, J., Hildebrand, F., Bahram, M., Voigt, A. Y., Wood, S. A., Jungblut, A. D., Küpper, F. C., Quesada, A., Camacho, A., Pearce, D. A., et al. (2017). Pole-to-pole connections: similarities between arctic and antarctic microbiomes and their vulnerability to environmental change. Frontiers in Ecology and Evolution, 5:137.
- Kulkarni, S., Dhakar, K., and Joshi, A. (2019). Alkaliphiles: diversity and bioprospection. In *Microbial Diversity in the Genomic Era*, pages 239–263. Elsevier.
- Lanzén, A., Simachew, A., Gessesse, A., Chmolowska, D., Jonassen, I., and Øvreås, L. (2013). Surprising prokaryotic and eukaryotic diversity, community structure and biogeography of ethiopian soda lakes. *PloS one*, 8(8):e72577.
- Lasken, R. S. and McLean, J. S. (2014). Recent advances in genomic dna sequencing of microbial species from single cells. *Nature Reviews Genetics*, 15(9):577–584.
- Lepère, C., Domaizon, I., Taïb, N., Mangot, J.-F., Bronner, G., Boucher, D., and Debroas,
 D. (2013). Geographic distance and ecosystem size determine the distribution of
 smallest protists in lacustrine ecosystems. FEMS Microbiology Ecology, 85(1):85–94.
- Li, S.-p., Wang, P., Chen, Y., Wilson, M. C., Yang, X., Ma, C., Lu, J., Chen, X.-y., Wu, J., Shu, W.-s., et al. (2020). Island biogeography of soil bacteria and fungi: similar patterns, but different mechanisms. *The ISME Journal*, pages 1–11.
- Locey, K. J. (2010). Synthesizing traditional biogeography with microbial ecology: the importance of dormancy: Synthesizing traditional biogeography with microbial ecology.

 Journal of biogeography, pages no-no.
- Lomolino, M. V. (1982). Species-area and species-distance relationships of terrestrial mammals in the thousand island region. *Oecologia*, 54(1):72–75.
- MacArthur, R. H. (1967). The theory of island biogeography. Monographs in population biology; 1. Princetown University Press, Princetown.

- MacDonald, Z. G., Anderson, I. D., Acorn, J. H., and Nielsen, S. E. (2018). The theory of island biogeography, the sample-area effect, and the habitat diversity hypothesis: complementarity in a naturally fragmented landscape of lake islands. *Journal of Biogeography*, 45(12):2730–2743.
- Malard, L. A. and Pearce, D. A. (2018). Microbial diversity and biogeography in arctic soils. *Environmental microbiology reports*, 10(6):611–625.
- Martiny, J. B. H., Bohannan, B. J., Brown, J. H., Colwell, R. K., Fuhrman, J. A., Green, J. L., Horner-Devine, M. C., Kane, M., Krumins, J. A., Kuske, C. R., et al. (2006). Microbial biogeography: putting microorganisms on the map. Nature Reviews Microbiology, 4(2):102–112.
- McCormick, P., Pratt, J., Jenkins, D., and Cairns Jr, J. (1988). A comparison of protozoan, algal, and metazoan colonization of artificial substrates of differing size. Transactions of the American Microscopical Society, pages 259–268.
- Nicolaides, C., Avraam, D., Cueto-Felgueroso, L., González, M. C., and Juanes, R. (2020).
 Hand-hygiene mitigation strategies against global disease spreading through the air transportation network. Risk Analysis, 40(4):723–740.
- Olive, M., Gan, C., Carratalà, A., and Kohn, T. (2020). Control of waterborne human viruses by indigenous bacteria and protists is influenced by temperature, virus type, and microbial species. *Applied and Environmental Microbiology*, 86(3).
- Orrock, J. L., Allan, B. F., Drost, C. A., Rohani, A. E. P., and Bronstein, E. J. L. (2011). Biogeographic and ecological regulation of disease: Prevalence of sin nombre virus in island mice is related to island area, precipitation, and predator richness. *The American naturalist*, 177(5):691–697.
- Pasztaleniec, A. and Poniewozik, M. (2010). Phytoplankton based assessment of the ecological status of four shallow lakes (eastern poland) according to water framework directive—a comparison of approaches. Limnologica-Ecology and Management of Inland Waters, 40(3):251–259.
- Patrick, R. (1967). The effect of invasion rate, species pool, and size of area on the structure of the diatom community. *Proceedings of the National Academy of Sciences of the United States of America*, 58(4):1335.

- Peay, K. G., Bruns, T. D., Kennedy, P. G., Bergemann, S. E., and Garbelotto, M. (2007).
 A strong species—area relationship for eukaryotic soil microbes: island size matters for ectomycorrhizal fungi. *Ecology letters*, 10(6):470–480.
- Pepper, I. (2019). Biotic characteristics of the environment. In *Environmental and Pollution Science*, pages 61–87. Elsevier.
- Prevost-Boure, N. C., Christen, R., Dequiedt, S., Mougel, C., Lelievre, M., Jolivet, C., Shahbazkia, H. R., Guillou, L., Arrouays, D., and Ranjard, L. (2011). Validation and application of a pcr primer set to quantify fungal communities in the soil environment by real-time quantitative pcr. *PloS one*, 6(9):e24166.
- Price, J. P. and Wagner, W. L. (2011). A phylogenetic basis for species—area relationships among three pacific island floras. *American Journal of Botany*, 98(3):449–459.
- Reche, I., Pulido-Villena, E., Morales-Baquero, R., and Casamayor, E. O. (2005). Does ecosystem size determine aquatic bacterial richness? *Ecology*, 86(7):1715–1722.
- Rengefors, K., Laybourn-Parry, J., Logares, R., Marshall, W. A., and Hansen, G. (2008).

 Marine-derived dinoflagellates in antarctic saline lakes: Community composition and annual dynamics 1*[link]. *Journal of phycology*, 44(3):592–604.
- Rengefors, K., LOGARES, R., and LAYBOURN-PARRY, J. (2012). Polar lakes may act as ecological islands to aquatic protists. *Molecular ecology*, 21(13):3200–3209.
- Ricklefs, R. E. and Lovette, I. J. (1999). The roles of island area per se and habitat diversity in the species—area relationships of four lesser antillean faunal groups. *Journal of Animal Ecology*, 68(6):1142–1160.
- Rivett, D. W. and Bell, T. (2018). Abundance determines the functional role of bacterial phylotypes in complex communities. *Nature microbiology*, 3(7):767–772.
- Rosenzweig, M. L. et al. (1995). Species diversity in space and time. Cambridge University Press.
- Rosindell, J., Wong, Y., and Etienne, R. S. (2008). A coalescence approach to spatial neutral ecology. *Ecological Informatics*, 3(3):259–271.
- Rosselli, R., Fiamma, M., Deligios, M., Pintus, G., Pellizzaro, G., Canu, A., Duce, P., Squartini, A., Muresu, R., and Cappuccinelli, P. (2015). Microbial immigration across the mediterranean via airborne dust. *Scientific reports*, 5:16306.

- Samson, F. B. (1980). Island biogeography and the conservation of prairie birds. In *Proceedings of the North American Prairie Conference*, volume 7, pages 293–305.
- Sfenthourakis, S. and Triantis, K. A. (2009). Habitat diversity, ecological requirements of species and the small island effect. *Diversity and Distributions*, 15(1):131–140.
- Simberloff, D. S. (1974). Equilibrium theory of island biogeography and ecology. *Annual review of Ecology and Systematics*, 5(1):161–182.
- Stegen, J. C., Lin, X., Konopka, A. E., and Fredrickson, J. K. (2012). Stochastic and deterministic assembly processes in subsurface microbial communities. The ISME Journal, 6(9):1653–1664.
- Stewart, K. and Schlichting Jr, H. (1966). Dispersal of algae and protozoa by selected aquatic insects. *The Journal of Ecology*, pages 551–562.
- Stibal, M., Bradley, J. A., Edwards, A., Hotaling, S., Zawierucha, K., Rosvold, J., Lutz, S., Cameron, K. A., Mikucki, J. A., Kohler, T. J., et al. (2020). Glacial ecosystems are essential to understanding biodiversity responses to glacier retreat. *Nature Ecology & Evolution*, 4(5):686–687.
- Stomp, M., Huisman, J., Mittelbach, G. G., Litchman, E., and Klausmeier, C. A. (2011). Large-scale biodiversity patterns in freshwater phytoplankton. *Ecology (Durham)*, 92(11):2096–2107.
- Triantis, K., Vardinoyannis, K., Tsolaki, E., Botsaris, I., Lika, K., and Mylonas, M. (2006).

 Re-approaching the small island effect. *Journal of Biogeography*, 33(5):914–923.
- Triantis, K. A., Mylonas, M., and Whittaker, R. J. (2008). Evolutionary species—area curves as revealed by single-island endemics: insights for the inter-provincial species—area relationship. *Ecography*, 31(3):401–407.
- Turner, S., Mikutta, R., Meyer-Stüve, S., Guggenberger, G., Schaarschmidt, F., Lazar, C. S., Dohrmann, R., and Schippers, A. (2017). Microbial community dynamics in soil depth profiles over 120,000 years of ecosystem development. Frontiers in microbiology, 8:874.
- Van Der Gast, C. J., Jefferson, B., Reid, E., Robinson, T., Bailey, M. J., Judd, S. J., and Thompson, I. P. (2006). Bacterial diversity is determined by volume in membrane bioreactors. *Environmental microbiology*, 8(6):1048–1055.

- Van Der Gast, C. J., Lilley, A. K., Ager, D., and Thompson, I. P. (2005). Island size and bacterial diversity in an archipelago of engineering machines. *Environmental microbiology*, 7(8):1220–1226.
- Várbíró, G., Görgényi, J., Tóthmérész, B., Padisák, J., Hajnal, É., and Borics, G. (2017). Functional redundancy modifies species—area relationship for freshwater phytoplankton. *Ecology and evolution*, 7(23):9905–9913.
- Wildman, H. (1987). Fungal colonization of resources in soil—an island biogeographical approach. Transactions of the British Mycological Society, 88(3):291–297.
- Woodcock, S., Curtis, T. P., Head, I. M., Lunn, M., and Sloan, W. T. (2006). Taxa–area relationships for microbes: the unsampled and the unseen. *Ecology letters*, 9(7):805–812.
- Wright, D. H. (1983). Species-energy theory: an extension of species-area theory. *Oikos*, pages 496–506.
- Wurzbacher, C. M., Bärlocher, F., and Grossart, H.-P. (2010). Fungi in lake ecosystems. Aquatic Microbial Ecology, 59(2):125–149.
- Zacharias, D. and Brandes, D. (1990). Species area-relationships and frequency—floristical data analysis of 44 isolated woods in northwestern germany. *Vegetatio*, 88(1):21–29.

Supplementary Material

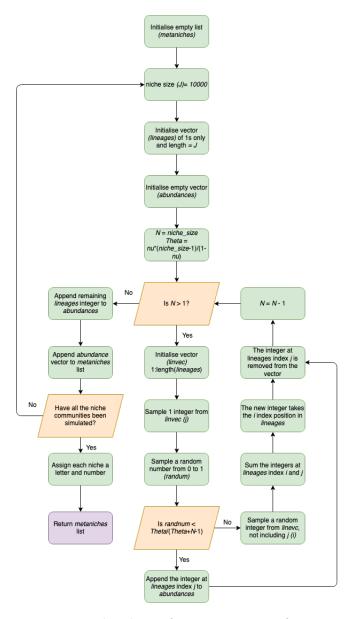


Figure 7.1: Flowchart of metacommunity function

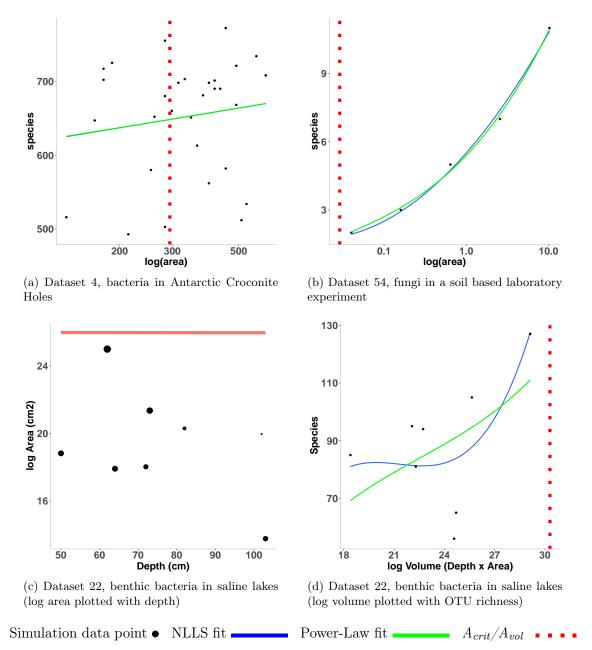


Figure 7.2: Selection of plots of datasets that failed to be fit using either of the three model variants (Classic, Depth, Perimeter) or the power-law model, where the blue line is the model fit, the green line is the power-law model fit and the red dotted line is the A_{crit} estimation. A) Dataset 4, bacteria in cryoconite holes with the Classic Model (NLLS fit: R₂=0.02, adjusted R₂=-0.13, θ =29, m_{θ} =0.208, K=354, A_{crit} =294 cm², power-law fit: R₂=0.02, adjusted R₂=-0.14, z=0.04, z=5.03). B) Fungi in soil based laboratory experiment plotted with the Perimeter Model (R₂=0.099, adjusted R₂=Inf, θ =6, m_{θ} =6.24 x 10⁻⁶, K=1, A_{crit} =2.89 x 10⁻² cm², power-law fit: R₂=0.99, adjusted R₂=-Inf, z=0.30, z=5.41). C) Benthic bacteria in saline lakes plotted with the Depth Model (R₂=0.51, adjusted R₂=-0.15, θ =14, m_{θ} =1.98 x 10⁻¹⁶, z=1.89 x 10¹¹ cm², power-law fit: R₂=0.24, adjusted R₂=-0.77, z=0.04, z=39)

Table 7.1: Summary of Datasets

| Study and Dataset ID | Author and Year | Habitat | Taxa |
|----------------------------|----------------------------------|-------------|---------------------------|
| Study 1, Datasets 1 & 2 | (Li et al., 2020) | Terrestrial | Bacteria & Fungi |
| Study 2, Dataset 3 | (Battes et al., 2019) | Lacustrine | Algae |
| Study 3, Datasets 4-15 | (Darcy et al., 2018) | Lacustrine | Bac, Alg, Fungi & |
| | | | Proto |
| Study 4, Datasets 16 & 17 | (Delgado-Baquerizo et al., 2018) | Terrestrial | Bacteria |
| Study 5, Dataset 18 | (Davison et al., 2018) | Terrestrial | Fungi |
| Study 6, Datasets 19 & 20 | (Glassman et al., 2017) | Plant | Fungi |
| Study 7, Dataset 21 | (Várbíró et al., 2017) | Lacustrine | Algae |
| Study 8, Datasets 22 & 23 | (Kavazos, 2016) | Lacustrine | Bac & Proto |
| Study 9, Dataset 24 | (Bolgovics et al., 2016) | Lacustrine | Algae |
| Study 10, Datasets 25-27 | (Grossmann et al., 2016) | Lacustrine | Alg, Proto & Fun |
| Study 11, Datasets 28-32 | (Jean et al., 2016) | Terrestrial | Bac, Path, Fun & Proto |
| Study 12, Dataset 33 | (Cashdan, 2014) | Terrestrial | Pathogens |
| Study 13, Dataset 34 | (Lepère et al., 2013) | Lacustrine | Protozoa |
| Study 14, Datasets 35 & 36 | (Lanzén et al., 2013) | Lacustrine | Bacteria & Archaea |
| Study 15, Dataset 37 | (Rengefors et al., 2012) | Lacustrine | Algae |
| Study 16, Datasets 38-39 | (Feinstein and Blackwood, 2012) | Plant | Fungi |
| Study 17, Dataset 40 | (Stomp et al., 2011) | Lacustrine | Algae |
| Study 18, Dataset 41 | (Orrock et al., 2011) | Terrestrial | Pathogens |
| Study 19, Datasets 42 & 43 | (Barberán and Casamayor, 2011) | Lacustrine | Bacteria |
| Study 20, Dataset 44 | (Peay et al., 2007) | Plant | Fungi |
| Study 21, Dataset 45 | (Van Der Gast et al., 2006) | Machine | Bacteria |
| Study 22, Dataset 46 | (Bell et al., 2005) | Lacustrine | Bacteria |
| Study 23, Dataset 47 | (Reche et al., 2005) | Lacustrine | Bacteria |
| Study 24, Datasets 48-50 | (Van Der Gast et al., 2005) | Machine | Bacteria |
| Study 25, Dataset 51 | (Karatayev et al., 2005) | Lacustrine | Algae |
| Study 26, Datasets 52 & 53 | (McCormick et al., 1988) | Riverine | Protozoa and Algae |
| Study 27, Dataset 54 | (Wildman, 1987) | Terrestrial | |
| Study 28, Dataset 55 | (Henebry and Cairns Jr, 1980) | Lacustrine | |
| Study 29, Datasets 56 & 57 | (Patrick, 1967) | Riverine | Algae |

Table 7.2: Rho Estimation Methods (S & D ID = Study & Dataset ID)

| Study/Data | Taxa | Habitat | $\rho \ (\mathrm{cm^3})$ | Method |
|---------------|-----------------------|------------|--------------------------|------------------------------------|
| S1, D1 | Bacteria | Soil | $1.48 \text{x} 10^{12}$ | Gene seq num from paper |
| S1, D2 | Fungi | Soil | $7.41 \text{x} 10^3$ | Gene seq num from paper |
| S2, D3 | Algae | Freshwater | $3.56 \text{x} 10^3$ | Proxy (Pasztaleniec and |
| | | | | Poniewozik, 2010) |
| S3, D4-6 | Bacteria | Cryo Holes | 4.50×10^4 | Proxy (Cameron et al., 2012) |
| S3, D7-9 | Algae | Cryo Holes | 1 | Gene seq num from paper |
| S3, D10-12 | Fungi | Cryo Holes | 1 | Gene seq num from paper |
| S3, D13-15 | Protozoa | Cryo Holes | 1 | Gene seq num from paper |
| S4, D16 | Bacteria | Soil | 3.50×10^{12} | Gene seq num from paper |
| S4, D17 | Bacteria | Soil | 1.48×10^{13} | Gene seq num from paper |
| S5, D18 | Fungi | Soil | 1 | 1 as area includes entire island |
| S6, D19 & 20 | Fungi | Soil | 2.98×10^3 | Gene seq num from paper |
| S7, D21 | Algae | Freshwater | 3.56×10^3 | Same proxy as D3 |
| S8, D22 | Bacteria | Sal Water | 3.00×10^6 | Proxy (Antón et al., 2000) |
| S8, D23 | Protozoa | Sal Water | 1.84×10^2 | Proxy (Elloumi et al., 2006) |
| S9, D24 | Algae | Freshwater | 3.56×10^3 | Same proxy as D3 |
| S10, D25 | Algae | Freshwater | 3.56×10^3 | Same proxy as D3 |
| S10, D26 | Protozoa | Freshwater | 1.92×10^3 | Proxy (Olive et al., 2020) |
| S10, D27 | Fungi | Freshwater | 1 | Proxy (Wurzbacher et al., 2010) |
| S11, D28-32 | Bac, Pat, Fun, Pro | Hosts | 1 | 1 as area includes entire island |
| S12, D33 | Pathogens | Hosts | 1 | 1 as area includes entire island |
| S13, D34 | Protozoa | Freshwater | $5.72 \text{x} 10^3$ | Nanoflag count taken from pa- |
| | | | | per |
| S14, D35 | Archaea | Sal Water | $1.00 \text{x} 10^7$ | Book (Kulkarni et al., 2019) |
| S14, D36 | Bacteria | Sal Water | $6.00 \text{x} 10^6$ | Proxy (Humayoun et al., 2003) |
| S15, D37 | Algae | Sal Water | $4.85 \text{x} 10^3$ | Proxy (Rengefors et al., 2008) |
| S16, D38-39 | Fungi | Plant | 10 | No proxy found so 10 est |
| S17, D40 | Algae | Freshwater | $3.56 \text{x} 10^3$ | Same proxy as D3 |
| S18, D41 | Pathogens | Hosts | 1 | 1 as area includes entire island |
| S19, D42 & 43 | Bacteria | Freshwater | 1.16×10^7 | Proxy (Cole et al., 1993) |
| S20, D44 | Fungi | Soil | 6.90×10^6 | Proxy (Prevost-Boure et al., 2011) |
| S21, D45 | Bacteria | Machine | $2.29 \text{x} 10^{10}$ | Cell abund taken from paper |
| S22, D46 | Bacteria | Tree Holes | $4.90 \text{x} 10^5$ | Proxy (Rivett and Bell, 2018) |
| S23, D47 | Bacteria | Freshwater | $1.16 \text{x} 10^7$ | Same proxy as D43 |
| S24, D48-50 | Bacteria | Machine | $2.29 \text{x} 10^{10}$ | Same proxy as D46 |
| S25, D51 | Algae | Freshwater | $3.56 \text{x} 10^3$ | Same proxy as D3 |
| S26, D52 | Protozoa | River | $5.72 \text{x} 10^3$ | Same proxy as D34 |
| S26, D53 | Algae | River | $3.56 \text{x} 10^3$ | Same proxy as D3 |
| S27, D54 | Fungi | Soil | $1.00 \text{x} 10^5$ | Book (Pepper, 2019) |
| S28, D55 | Protozoa | Freshwater | $5.72 \text{x} 10^3$ | Same proxy as D34 |
| S29, D56 & 57 | Algae | River | 3.56×10^3 | Same proxy as D3 |

Table 7.3: Results of successful Power-Law Model fitting to the 24 positive TAR datasets with $\rm R^2$, adjusted $\rm R^2$, z values (model exponent), c values (model constant) (S & D ID = Study & Dataset ID)

| S & D ID | Author & Year | \mathbb{R}^2 | $rac{	ext{Adj}}{	ext{R}^2}$ | z | c |
|----------|----------------------------------|----------------|------------------------------|------|---------|
| S1, D1 | (Li et al., 2020) | 0.56 | 0.49 | 0.09 | 1294.63 |
| S1, D2 | (Li et al., 2020) | 0.60 | 0.53 | 0.10 | 332.03 |
| S3, D6 | (Darcy et al., 2018) | 0.23 | 0.10 | 0.32 | 70.02 |
| S3, D11 | (Darcy et al., 2018) | 0.27 | 0.15 | 0.42 | 4.68 |
| S4, D16 | (Delgado-Baquerizo et al., 2018) | 0.82 | 0.75 | 0.11 | 340.96 |
| S4, D17 | (Delgado-Baquerizo et al., 2018) | 0.70 | 0.54 | 0.08 | 451.61 |
| S6, D19 | (Glassman et al., 2017) | 0.23 | 0.02 | 0.27 | 0.48 |
| S6, D20 | (Glassman et al., 2017) | 0.32 | 0.13 | 0.16 | 1.93 |
| S7, D21 | (Várbíró et al., 2017) | 0.02 | 0.0001 | 0.01 | 23.10 |
| S9, D24 | (Bolgovics et al., 2016) | 0.62 | 0.48 | 0.05 | 32.25 |
| S10, D25 | (Grossmann et al., 2016) | 0.38 | 0.28 | 0.06 | 48.28 |
| S10, D26 | (Grossmann et al., 2016) | 0.29 | 0.17 | 0.14 | 0.29 |
| S11, D28 | (Jean et al., 2016) | 0.23 | 0.18 | 0.01 | 39.29 |
| S11, D29 | (Jean et al., 2016) | 0.34 | 0.30 | 0.02 | 19.31 |
| S11, D30 | (Jean et al., 2016) | 0.24 | 0.19 | 0.02 | 4.27 |
| S11, D31 | (Jean et al., 2016) | 0.35 | 0.31 | 0.03 | 4.60 |
| S11, D32 | (Jean et al., 2016) | 0.33 | 0.29 | 0.05 | 4.26 |
| S20, D44 | (Peay et al., 2007) | 0.87 | 0.78 | 0.18 | 0.64 |
| S21, D45 | (Van Der Gast et al., 2006) | 0.94 | 0.82 | 0.27 | 0.88 |
| S22, D46 | (Bell et al., 2005) | 0.46 | 0.38 | 0.33 | 1.74 |
| S24, D48 | (Van Der Gast et al., 2005) | 0.73 | 0.63 | 0.36 | 1.25 |
| S24, D49 | (Van Der Gast et al., 2005) | 0.84 | 0.76 | 0.32 | 1.80 |
| S24, D50 | (Van Der Gast et al., 2005) | 0.80 | 0.73 | 0.36 | 1.34 |
| S25, D51 | (Karatayev et al., 2005) | 0.10 | 0.09 | 0.11 | 19.00 |

Table 7.4: Results of Power-Law Model AIC score - Classic, Depth and Perimeter AIC scores. There must be a difference of at least 2 to be statistically significant (positive results favour the Classic, Depth and Perimeter Models, negative results favour the Power-Law Model) (S & D ID = Study & Dataset ID)

| S & D ID | Author & Year | Classi | c Depth | Perimeter |
|----------|----------------------------------|--------|---------|-----------|
| S1, D1 | (Li et al., 2020) | 7.25 | 7.25 | 6.91 |
| S1, D2 | (Li et al., 2020) | 10.37 | 10.18 | 9.49 |
| S3, D6 | (Darcy et al., 2018) | 0.23 | 0.23 | 0.08 |
| S3, D11 | (Darcy et al., 2018) | 0.005 | 0.02 | 0.02 |
| S4, D16 | (Delgado-Baquerizo et al., 2018) | 0.005 | 0.005 | 0.005 |
| S4, D17 | (Delgado-Baquerizo et al., 2018) | 0.002 | 0.002 | 0.002 |
| S6, D19 | (Glassman et al., 2017) | 0.03 | 0.03 | 0.01 |
| S6, D20 | (Glassman et al., 2017) | 0.72 | 0.72 | 0.52 |
| S7, D21 | (Várbíró et al., 2017) | 1.20 | 1.22 | 1.03 |
| S9, D24 | (Bolgovics et al., 2016) | 2.64 | 2.62 | 3.33 |
| S10, D25 | (Grossmann et al., 2016) | 0.91 | 1.03 | 0.92 |
| S10, D26 | (Grossmann et al., 2016) | 0.05 | 0.11 | 0.04 |
| S11, D28 | (Jean et al., 2016) | 0.49 | 0.49 | -0.61 |
| S11, D29 | (Jean et al., 2016) | 0.33 | 0.34 | 0.11 |
| S11, D30 | (Jean et al., 2016) | 2.77 | 2.78 | 3.16 |
| S11, D31 | (Jean et al., 2016) | 0.76 | 0.75 | -0.05 |
| S11, D32 | (Jean et al., 2016) | 2.22 | 2.21 | 0.75 |
| S20, D44 | (Peay et al., 2007) | -0.05 | -0.05 | -0.27 |
| S21, D45 | (Van Der Gast et al., 2006) | 2.67 | 2.67 | 2.25 |
| S22, D46 | (Bell et al., 2005) | 0.45 | 1.34 | 0.17 |
| S24, D48 | (Van Der Gast et al., 2005) | 2.84 | 2.87 | 0.47 |
| S24, D49 | (Van Der Gast et al., 2005) | 4.28 | 4.33 | 1.80 |
| S24, D50 | (Van Der Gast et al., 2005) | 3.38 | 3.42 | 0.59 |
| S25, D51 | (Karatayev et al., 2005) | 0.23 | -1.18 | 0.17 |

Table 7.5: Best-fit results of the Classic, Depth and Perimeter Model fittings, with best-fit parameters (θ, m_{θ}, K) , A_{crit} and best-fit model (S & D ID = Study & Dataset ID)

| S & D ID | \mathbb{R}^2 | Adj R ² | θ | m_{θ} | K | A_{crit} | Best-fit Model |
|----------|----------------|-----------------------|------------------------|---------------------------------|-----|---------------------------|-------------------|
| S1, D1 | 0.65 | 0.60 | $1.73 \text{x} 10^3$ | $3.67 \mathrm{x} 10^{-5}$ | 1 | $5.00 \mathrm{x} 10^{-2}$ | All |
| S1, D2 | 0.72 | 0.67 | $3.56 \text{x} 10^2$ | $1.80 \text{x} 10^{-8}$ | 1 | $4.21 \text{x} 10^2$ | Classic |
| | | | | | | | & Depth |
| S3, D6 | 0.23 | 0.11 | $1.60 \mathrm{x} 10^5$ | $2.43x10^{-5}$ | 204 | $1.98 \text{x} 10^2$ | All |
| S3, D11 | 0.27 | 0.15 | $5.89 \text{x} 10^4$ | $5.64 \text{x} 10^{\text{-}1}$ | 25 | $1.92 \text{x} 10^2$ | All |
| S4, D16 | 0.82 | 0.75 | $1.42 \text{x} 10^2$ | $1.53 \text{x} 10^{\text{-}12}$ | 315 | 5.52x10 | All |
| S4, D17 | 0.70 | 0.54 | 1.08×10^2 | $5.12x10^{-13}$ | 424 | $5.02 \text{x} 10^2$ | All |
| S6, D19 | 0.23 | 0.02 | 13 | 5.88×10^{-7} | 4 | 1.91×10^4 | All |
| S6, D20 | 0.34 | 0.17 | 2 | $5.09 \text{x} 10^{-8}$ | 1 | 4.91×10^2 | Classic |
| | | | | | | | & Depth |
| S7, D21 | 0.02 | 0.01 | 1 | $1.39 \text{x} 10^{-4}$ | 21 | $1.03 \text{x} 10^{20}$ | Classic |
| | | | | | | | & Depth |
| S9, D24 | 0.69 | 0.58 | 16 | $2.79 \text{x} 10^{-8}$ | 60 | $4.83 \text{x} 10^{10}$ | Perimeter |
| S10, D25 | 0.41 | 0.31 | 10 | $1.19 \text{x} 10^{-6}$ | 2 | 2.38x10 | Depth |
| S10, D26 | 0.29 | 0.18 | 1 | $2.86 \text{x} 10^{-13}$ | 3 | $1.33 \text{x} 10^9$ | Classic |
| | | | | | | | & Depth |
| S11, D28 | 0.23 | 0.18 | 1 | $1.70 \text{x} 10^{-12}$ | 51 | $1.07 \text{x} 10^{48}$ | Classic |
| | | | | | | | & Depth |
| S11, D29 | 0.34 | 0.30 | 1 | 3.75×10^{-6} | 28 | 1.89×10^{31} | All |
| S11, D30 | 0.28 | 0.23 | $2.43x10^3$ | $5.87 \text{x} 10^{-10}$ | | $8.52 \text{x} 10^{16}$ | Perimeter |
| S11, D31 | 0.36 | 0.32 | 1 | 3.31×10^{-13} | | $2.23 \text{x} 10^{24}$ | Classic |
| S11, D32 | 0.35 | 0.31 | 3 | $1.44 \text{x} 10^{-15}$ | 17 | $4.24 \text{x} 10^{16}$ | Classic |
| | | | | | | | & Depth |
| S20, D44 | 0.85 | 0.77 | 5 | $6.15 \text{x} 10^{-11}$ | | $4.08 \text{x} 10^4$ | All |
| S21, D45 | 0.96 | 0.88 | 9 | $4.97 \text{x} 10^{-16}$ | 7 | $2.62 \text{x} 10^4$ | Classic |
| | | | | | | | & Depth |
| S22, D46 | 0.49 | 0.40 | 8 | $3.75 \text{x} 10^{-9}$ | 6 | $2.19 \text{x} 10^2$ | Depth |
| S24, D48 | 0.78 | 0.69 | 7 | 7.97x10 ⁻¹⁴ | 1 | 1.95x10 | Classic |
| | | | | | | | & Depth |
| S24, D49 | 0.89 | 0.83 | 6 | $1.15 \text{x} 10^{-13}$ | 1 | 1.38x10 | Classic |
| | | | | | | | & Depth |
| S24, D50 | 0.84 | 0.78 | 7 | $8.74 \text{x} 10^{-14}$ | 1 | 1.78x10 | Classic |
| | | | | | | | & Depth |
| S25, D51 | 0.10 | 0.09 | 12 | $3.25 \text{x} 10^{-5}$ | 28 | $4.46 \text{x} 10^3$ | All |