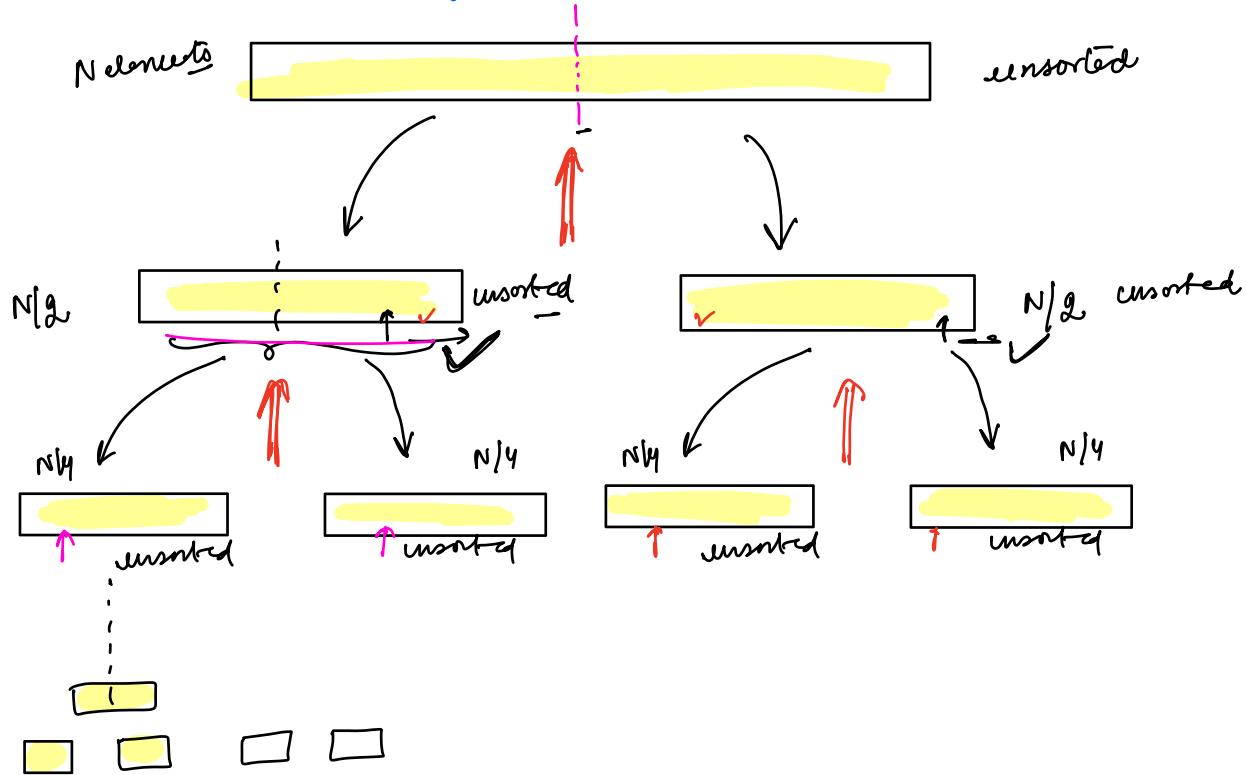
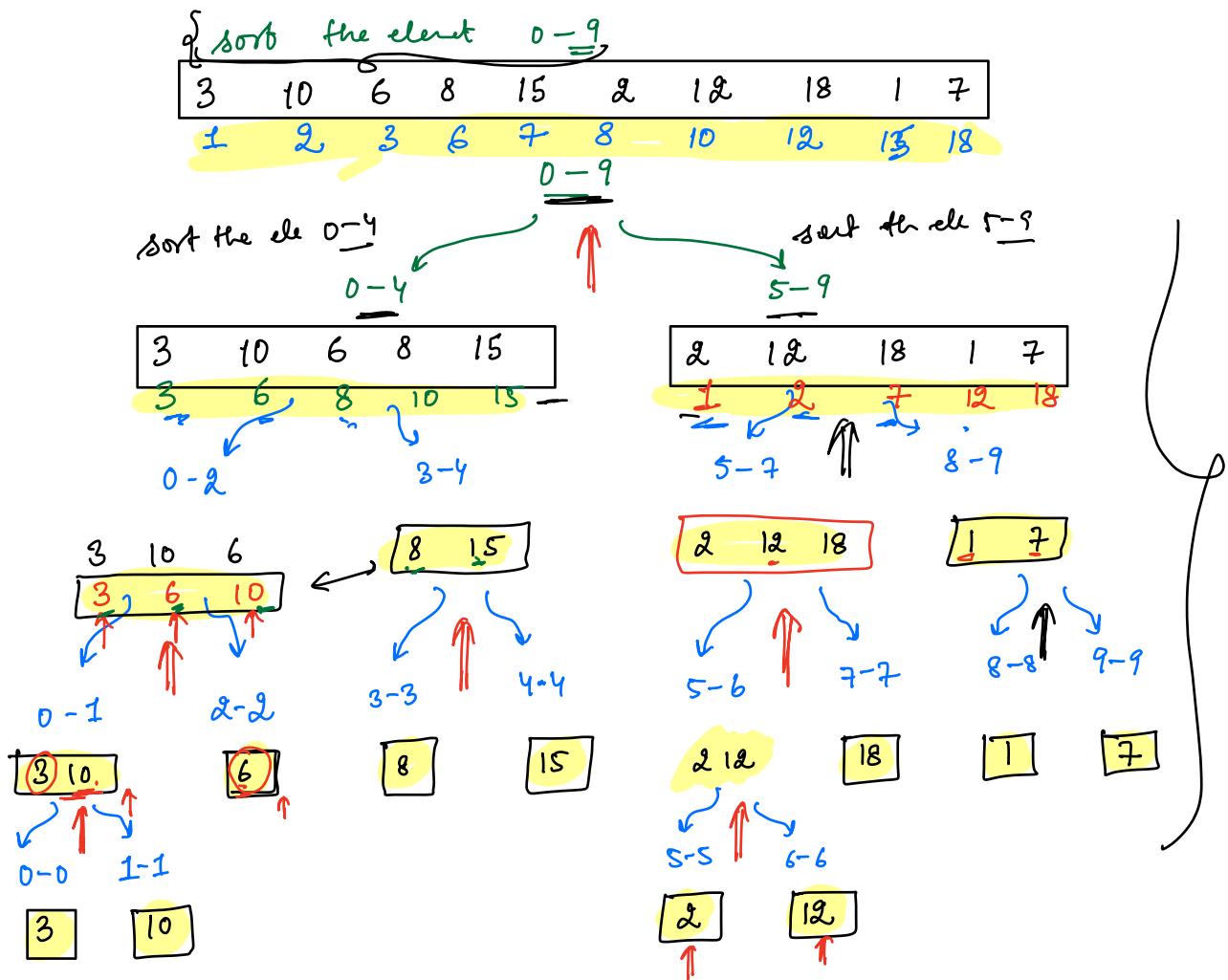


sort an array from $0 \rightarrow n-1$





Merge sort

```
void sort mergesort ( int arr[], int l, int r)
```

{ // sort your arr from l-1
 if (l == r) return;

$$\text{int mid} = \underline{l} + (\underline{r}-\underline{l})/2$$

xmergesort(arr, l, mid); T(N/2)

xmergesort(arr, mid+1, r); T(N/2)

merge(arr, l, mid+1, r);

$$\begin{aligned} & 5-9 \\ & 5/2 = \frac{9}{2} \end{aligned}$$

$$\begin{aligned} & 9-5/2 \\ & 4/2 = \underline{\underline{2}} \end{aligned}$$

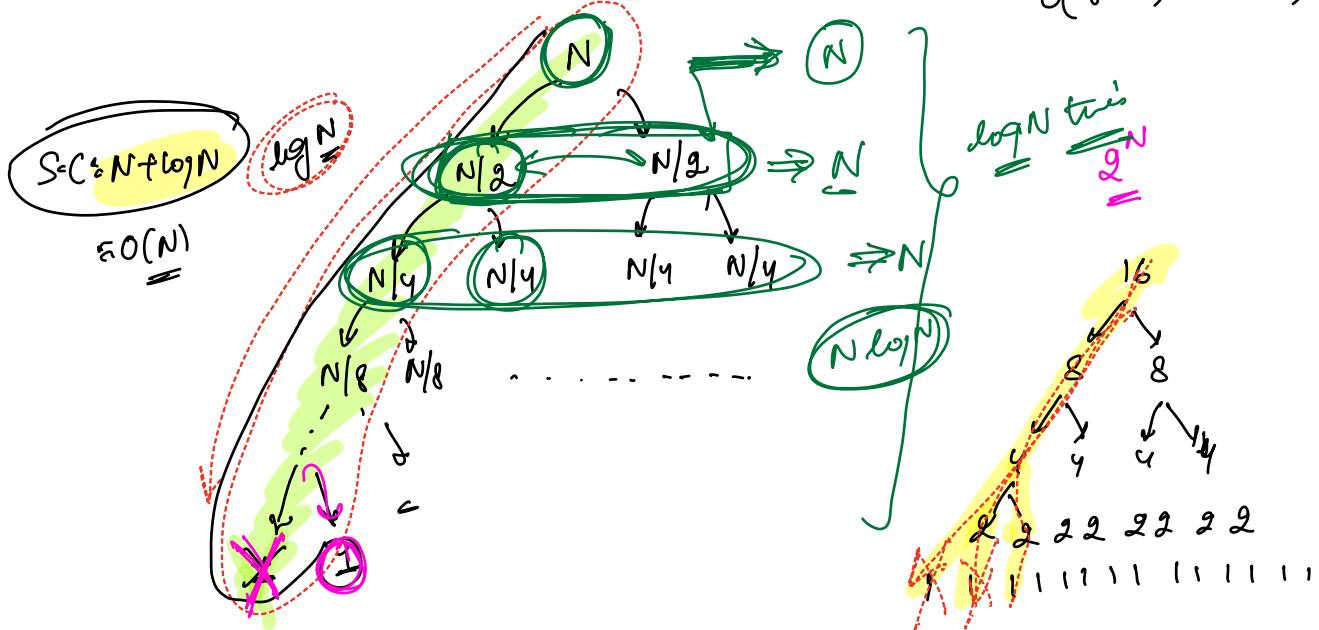
l
r

$$\begin{aligned} & l, y, r \\ & l-y-1 \\ & y-r \end{aligned}$$

$$T(N) = T(N/2) + T(N/2) + N$$

$\frac{T(N)}{=}$

$O(N+1) \approx O(N)$

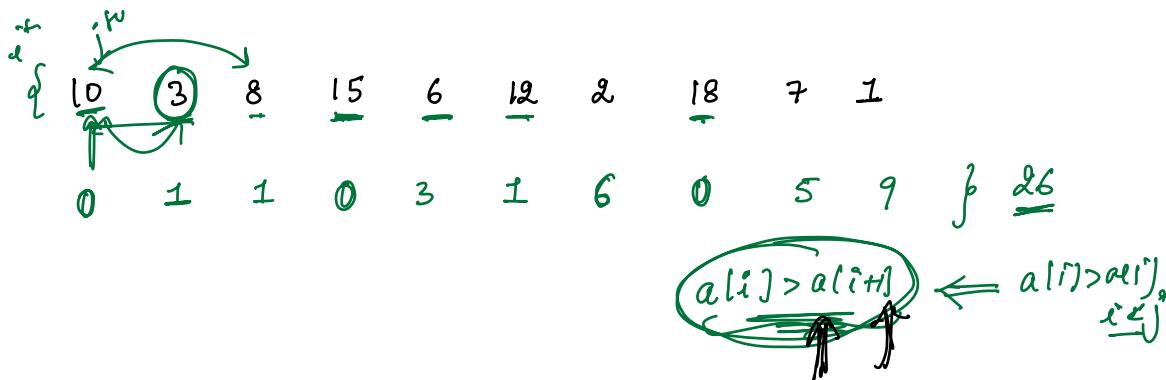


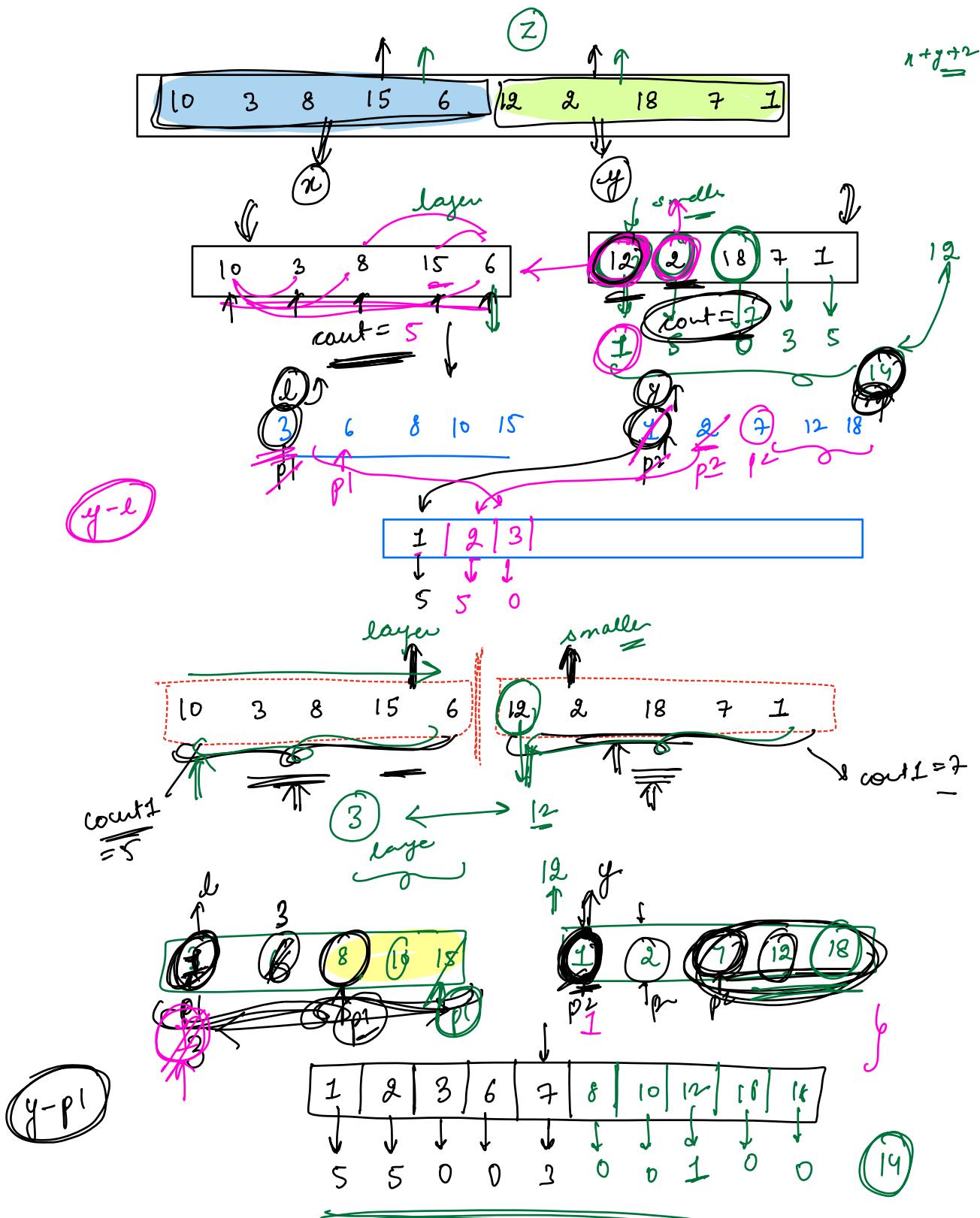
Q array of N integers, find total count of pairs (i, j)

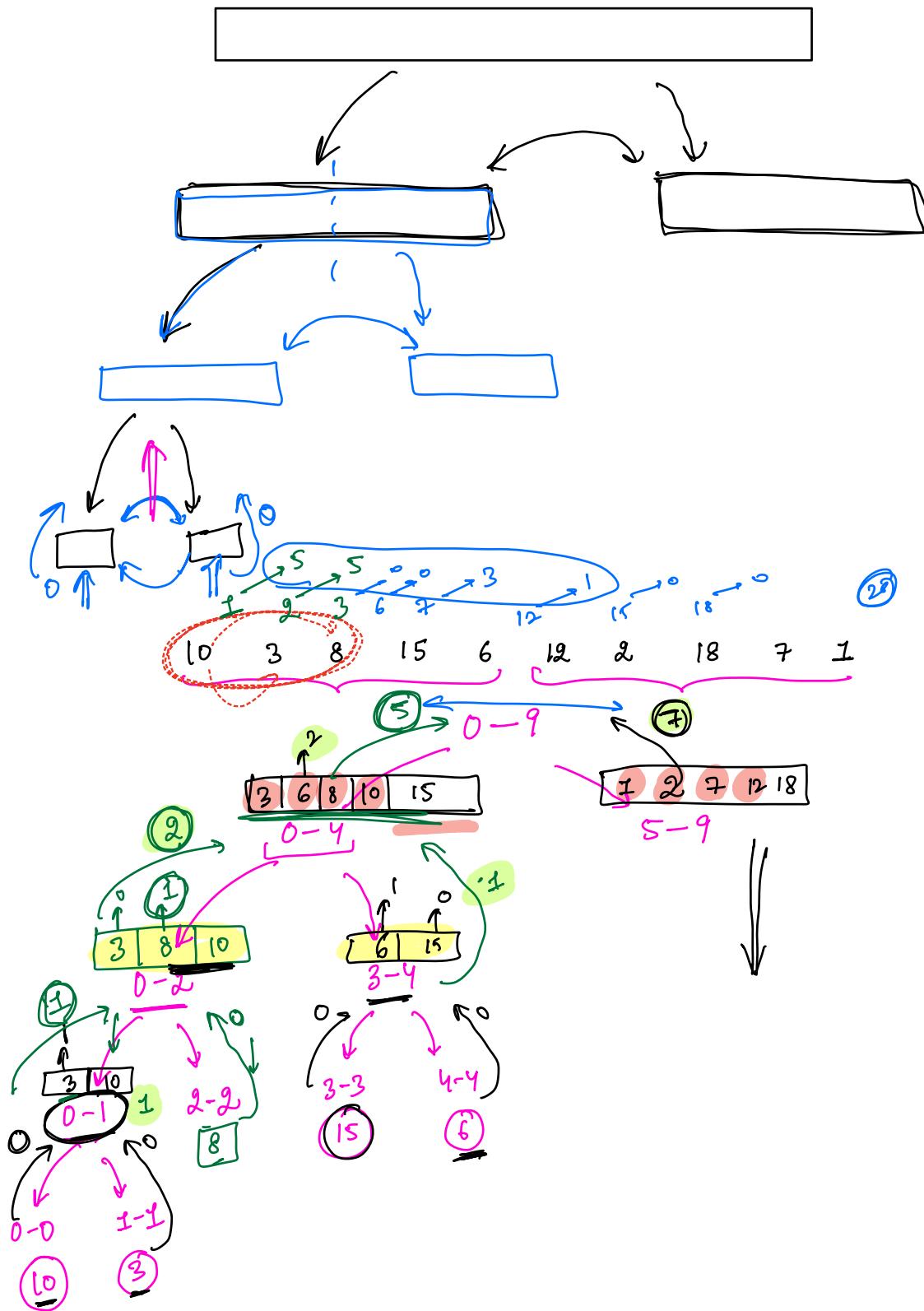
$i < j$ & $a[i] > a[j]$ \rightarrow inversion pair
large value - smaller index

0	1	2	3	4	5	6	7	8	9
10	3	8	15	6	12	2	18	7	1

$\frac{3}{1} \frac{9}{15} \frac{1}{1}$







```

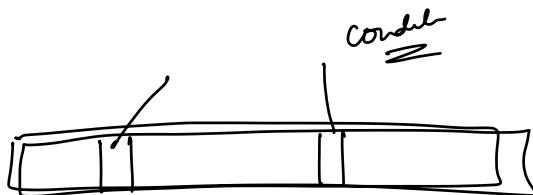
int inversion( int arr[], int l, int r)
{
    if (l == r) return 0;
    int mid = (l+r)/2;
    int x = inversion( arr, l, mid );
    int y = inversion( arr, mid+1, r );
    int z = merge( arr, l, mid+1, r );
    return x+y+z;
}

```

$$\left\{ \begin{array}{l} T.C \in O(N) \\ S.C \in O(n \log n) \end{array} \right.$$

divide & conquer

y



int merge(int arr[], int l, int m, int r)

{

 int p1 = l;
 p2 = m;
 p3 = 0; int count = 0;
 int temp[r-l+1];

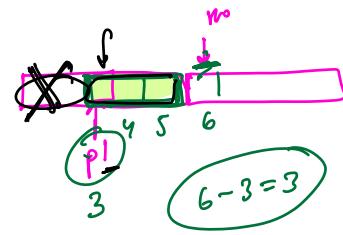
 while (p1 < m && p2 <= r)

{

 if (arr[p1] <= arr[p2])
 temp[p3++] = arr[p1++];
 else
 temp[p3++] = arr[p2++];
 count += m - p1;

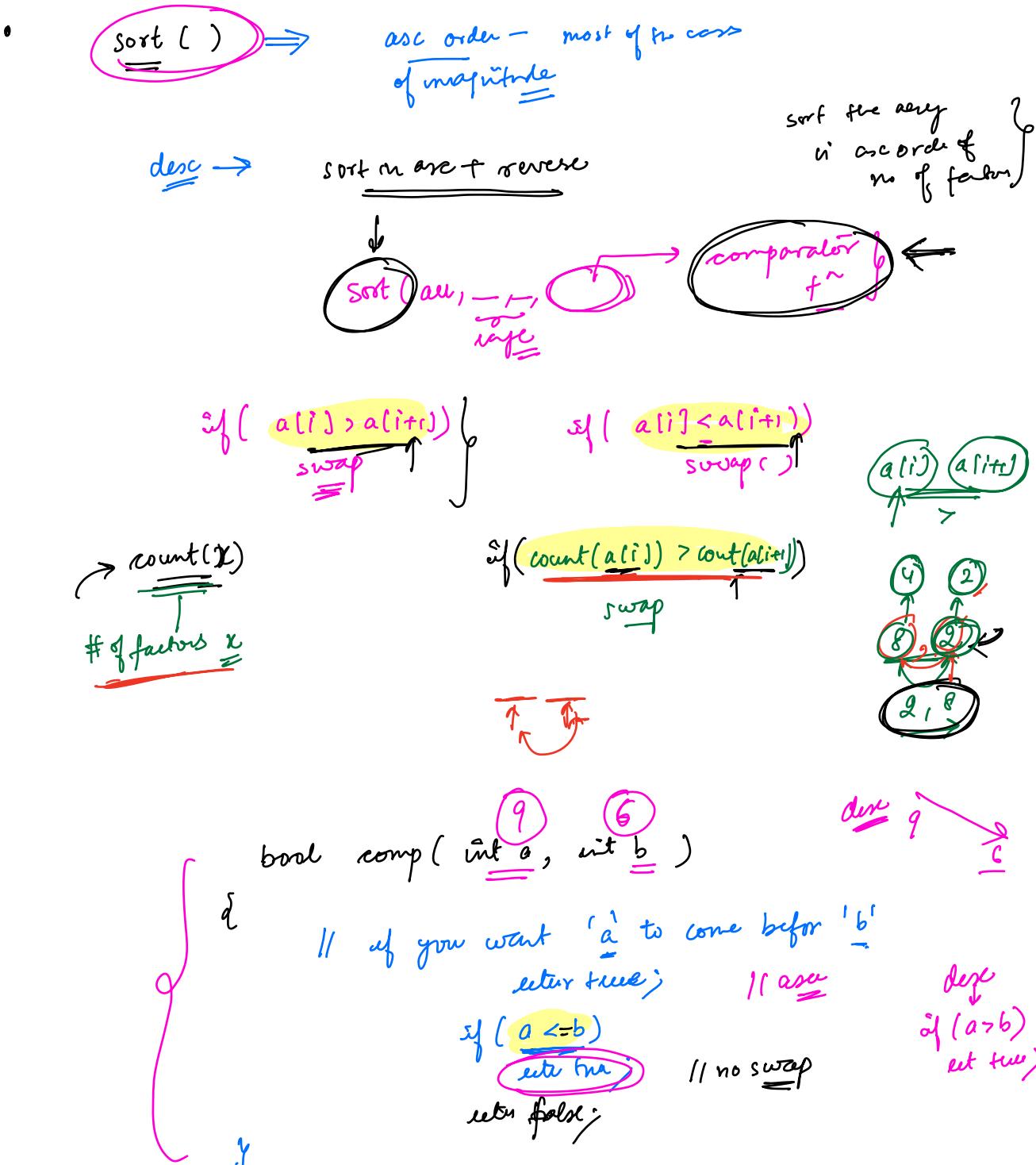
}

 while () { }
 while () { }



 for (i=0; i< r-l+1; i++)
 {
 arr[l+i] = temp[i];
 }
 return count;

}



```

bool comp( int a, int b )
{
    if ( count(a) <= count(b) )
        return true;
    return false;
}

```

array → sort acc to asc order of count of factors,
 if two numbers have equal no of factors,
 sort acc to magnitude of den

```

comp( a, b )
{
    int x = count(a);
    int y = count(b);
    if ( x < y )
        return true;
    else if ( x == y && a < b )
        return true;
    else
        return false;
}

```

$a = 7 \quad b = 5$

$x < y$

~~return true;~~

~~return false;~~

\boxed{a} \boxed{b}

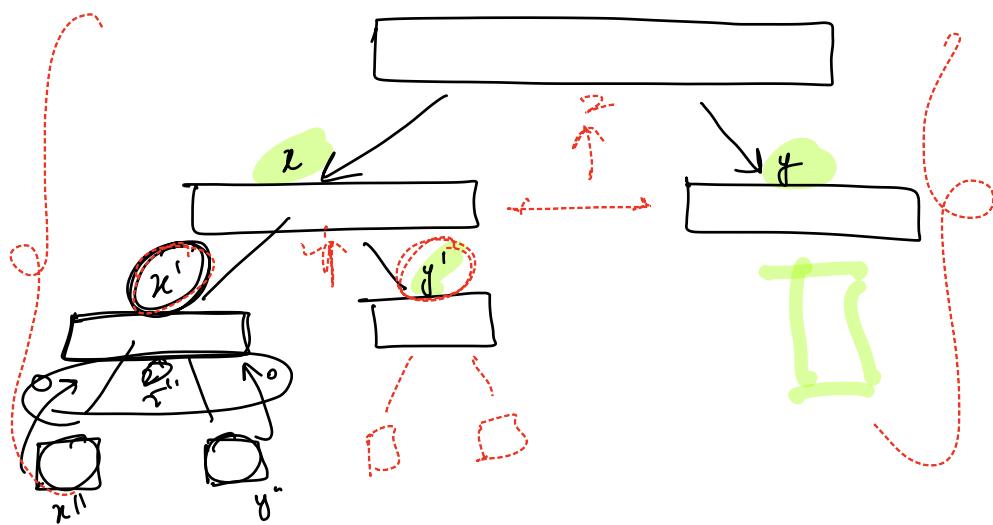
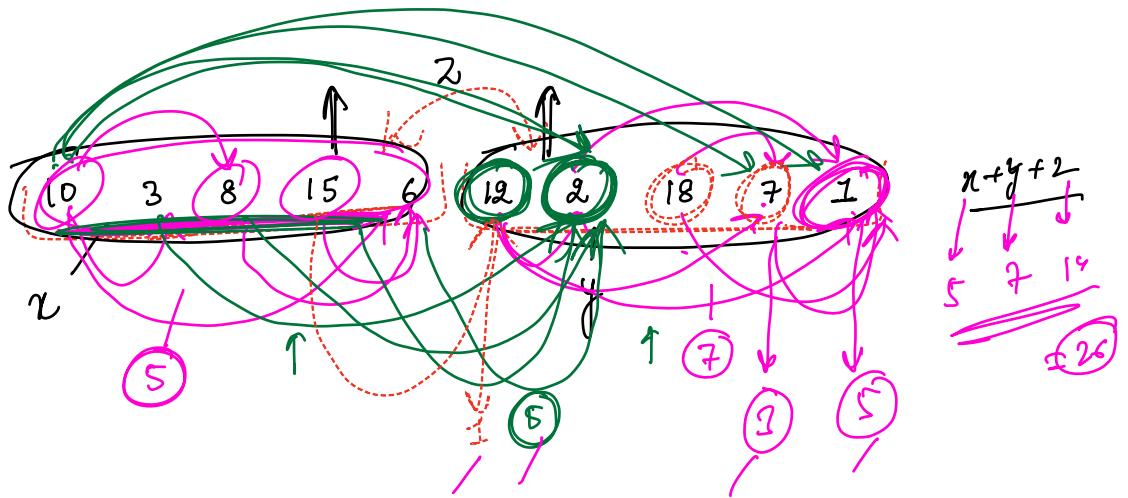
comp(\boxed{a} , \boxed{b})

\boxed{a}

\boxed{b}

B points from origin
Layout NO.

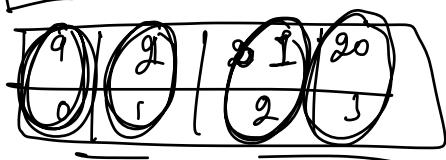
↑ ↑



$$9 \left\{ \begin{array}{cccc} 0 & 1 & 2 & 3 \\ \textcircled{9} & \textcircled{2} & \textcircled{1} & \textcircled{20} \end{array} \right. \underline{1 \ 2 \ 9 \ 20}$$

0 1 2 3
2 1 0 3

metres < pairs



$\text{comp}(\text{pair} \xrightarrow{a}, \text{para} \hookleftarrow)$

