

- Movie ticket line
- job queues
- printer

operations by queue :-

front
rear

- $O(1)$
- Enqueue(x) \longrightarrow insert at an end (rear)
 - Dequeue() \longrightarrow delete from an end (front)
 - front()
 - Empty()

Implementation

• Arrays

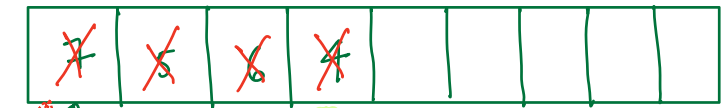
7 5 6 4 dequeue front()

```
void enqueue(x)
{
    if (r == n-1) { overflow }
    else { r++;
           arr[r] = x; }
}
```

```
void dequeue()
{
    if (isempty()) { no elem }
    else f++;
}
```

```
int front()
{
    if (isEmpty())
        return arr[f+1];
}
```

$f = -1$
 $r = -1$
 denote \rightarrow element which was deleted
 $f+1$ to r

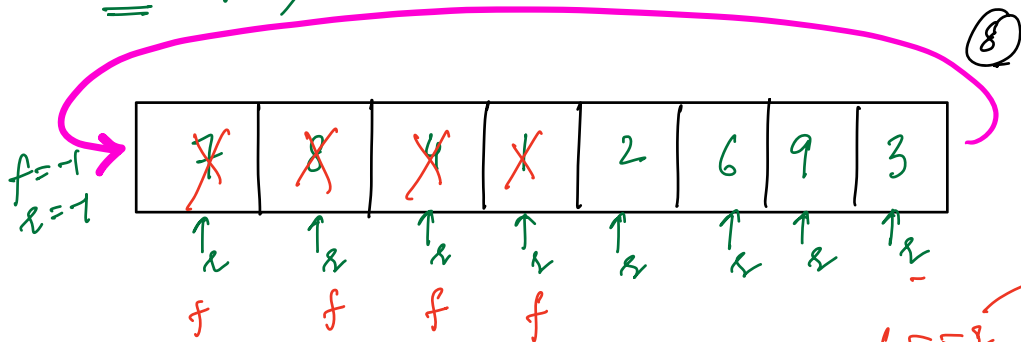


last element which was deleted

```
bool isEmpty()
{
```

```
    if (f == r)
        return true;
    return false;
}
```

}



circular Queue

linked list

size = 0;
 ↓
 total ele
 currently in
 queue

```
void enqueue( int x)
{
    if( size == N) { overflow; }
    else { x = (x+1) % N;
           arr[x] = x;
           size++;
        }
}
```

```
void dequeue( )
{
    if( size == 0) { // empty }
    else
    {
        f = (f+1) % N;
        size--;
    }
}
```

```
int front()
{
    if( size == 0) { empty }
    else
    {
        return
        arr[(f+1) % N];
    }
}
```

```
bool isEmpty( )
{
    if( size == 0) return true;
    else return false;
}
```

• DL

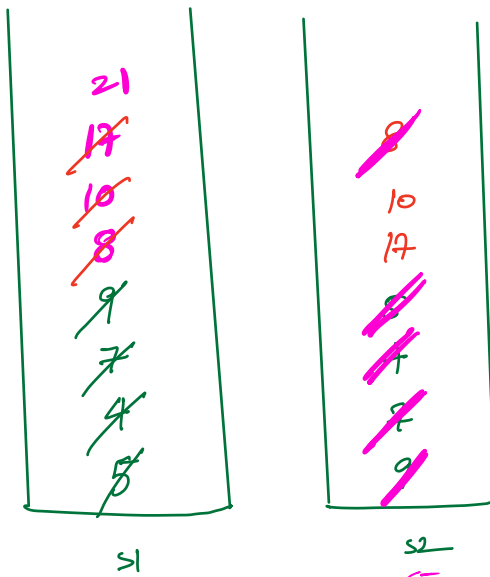
enqueue head, tail
 ↓
 insert at tail

dequeue
 ↓
 delete from head
head = head.next;

```
front()
{
    head.data;
}
```

- Implement queues using stack (s).

5 4 7 9 ↓ 8 10 ↓ ↓ 17 ↓ ↓ 21



We can't implement
a queue using
a single stack.

$O(1)$ \nearrow

```

void enqueue(int x)
{
    s1.push(x);
}

int front()  $\rightarrow O(1)$  amortized
{
    if (s2.empty())
    {
        while (!s1.empty())
        {
            s2.push(s1.top());
            s1.pop();
        }
        if (!s2.empty())
            return s2.top();
    }
}

```

amortized
 $O(n)$

```

void dequeue()  $\rightarrow O(1)$  amortized
{
    if (s2.empty())
    {
        while (!s1.empty())
        {
            s2.push(s1.top());
            s1.pop();
        }
        if (!s2.empty())
            s2.pop();
    }
}

```

Q

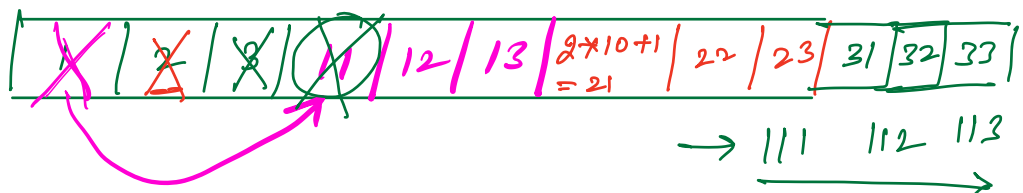
N^{th} number \rightarrow 1, 2, or 3

1	31
2	32
3	33
11	111
12	112
13	113
21	
22	
23	

N^{th}

B.F:-

Start from 1 ----, check if it's valid
increase count



Q

N^{th} perfect number

- ↳ even length
- palindrome
- 122

11
22

1111

1221

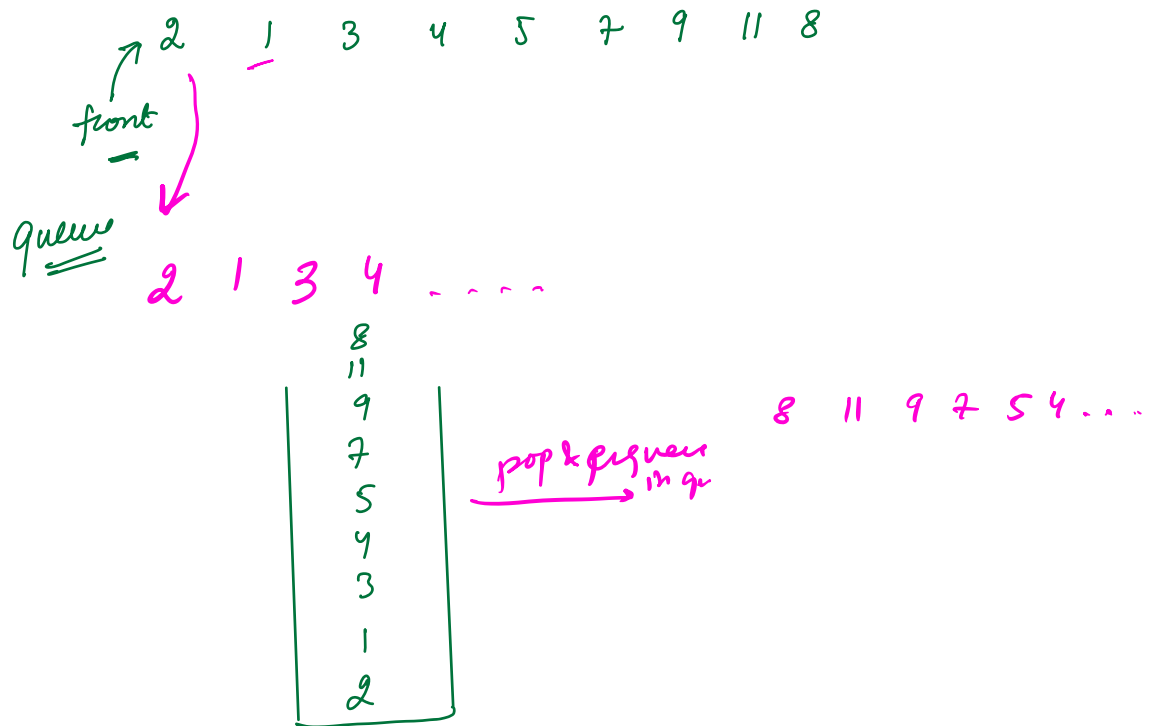
2112

2222

111111

aa'
↓
reverse

Reverse a queue



Hw1 # stack using queues
#2 deque
double ended