

sort a given array ↴

min heap  
 $\xrightarrow{O(N)}$

extract Min()

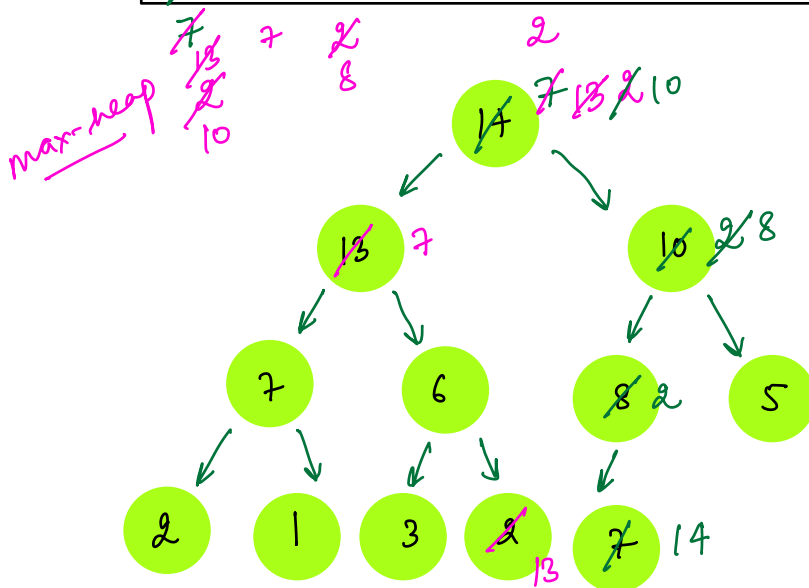
$\Downarrow$   $N \log N$

put the min in the new array

S.C:  $O(N)$

max value should come at  
 the last

0	1	2	3	4	5	6	7	8	9	10	11
14	13	10	7	6	8	5	2	1	3	2	7



extract Max()

size--

extract

T.C:  $\approx N \log N$   
 S.C:  $O(1)$

Not stable

HeapSort

array  $\xrightarrow{\text{build}}$  maxheap  $\longrightarrow$  sorted array

# Find  $K^{\text{th}}$  largest element in an array

8 5 1 2 4 9 7  $K=3^{\text{rd}}$

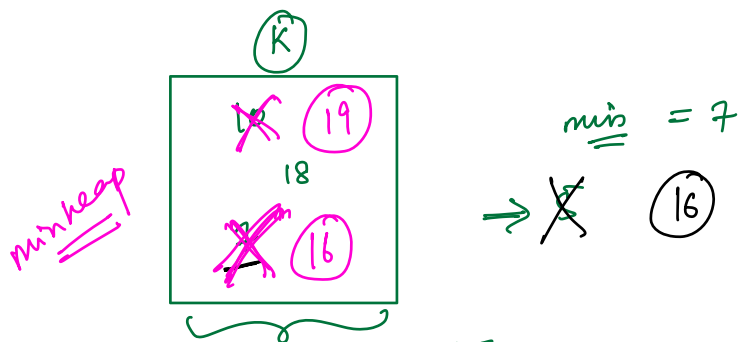
Heaps  $\Rightarrow$  max heap  $\Rightarrow$  extract max  
3 times ( $K$  times)

Q  $K^{\text{th}}$  largest element & (0-i) windows  
 $i \geq K-1$

[ 10 18 7 5 16 19 3 ]  $K=3$   
7 7 10 16 16

B.F  $\Rightarrow$  19 18 16 10 7 5 3 T.C:  $O(n^2)$   $\frac{K \log K}{K^2}$   
     $\uparrow \uparrow$   $\uparrow$

10 1 9 5 8  
 $\downarrow$   
min  $5^{\text{th}}$  largest



ans = min of min-heap

$K^{th}$  smallest  $\rightarrow$  max-heap

# Nearly sorted array, sort the array  
 $\Downarrow$   
 every element is at most  $K$  position away from its sorted position

0	1	2	3	4	5	6
6	5	3	2	8	10	9

qin  $\leftarrow K=3$

sorted	2	3	5	6	8	9	10
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B-F 1) sort the data  $n \log n$

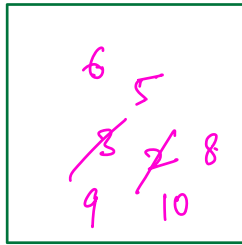
minimum element will def in first  $K+1$  elements

1) Build min-heap for first  $K$  elements

2)  $\log_2 K$   $O(K)$  extract next

$K + (N-K) * \log K$

size =  $k+1$

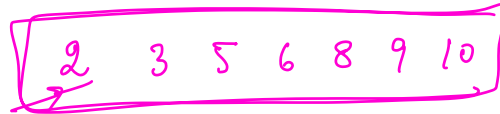


← put first  $k+1$  elements into heap

$T.C$   $O(k)$

$(n-k) \log k$

extract min()



#

infinite stream of integers, Find median of the recent set of elements

9 8 7 3 6 4 1 ----

as: 9 8 8 7 7 6 6 ----

median

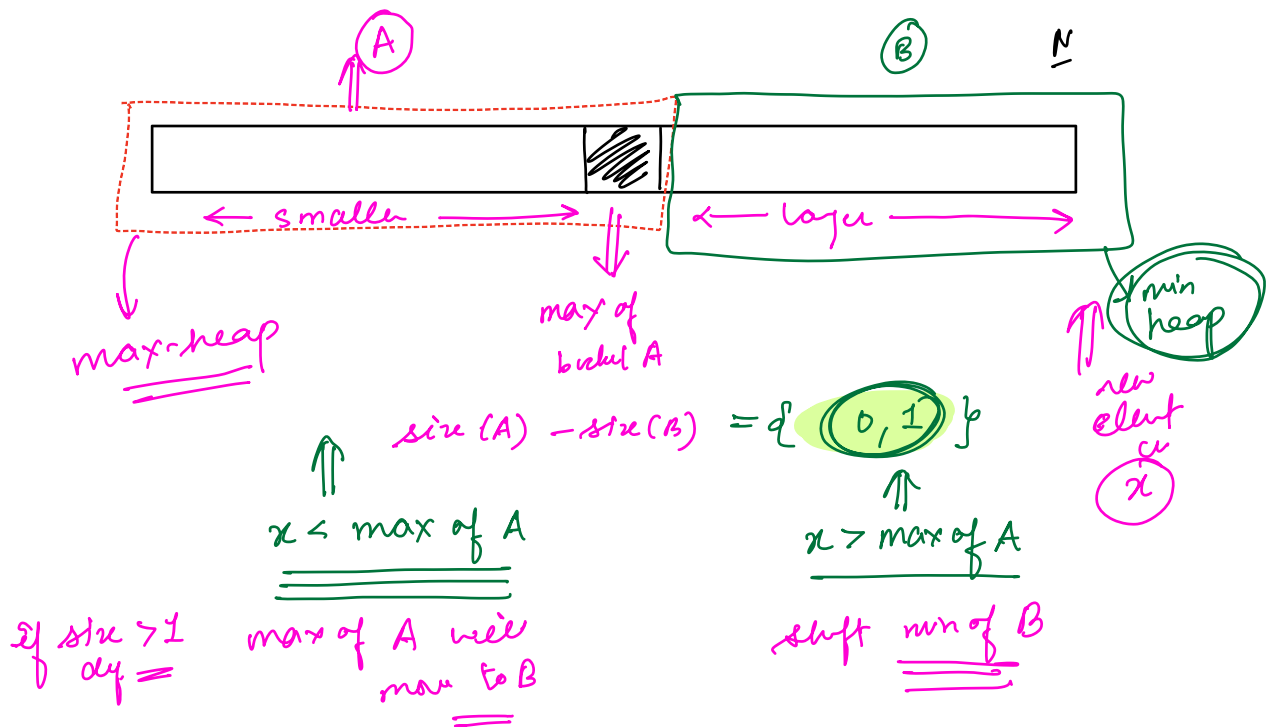
1 2 3 odd

1 3 5 6 even

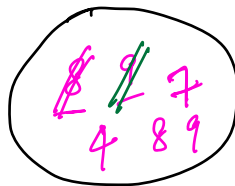
$$K = \left( \frac{N+1}{2} \right)$$

B.F:-

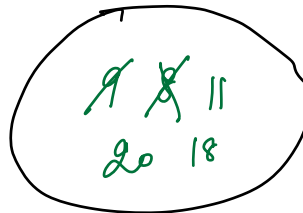
- sort again & again
- insertion sort -  $O(n^2)$



9 8 7 4 11 20



max heap



min heap

9 8 8 7 8

7 8 9

(2)

if (  $x < \text{max of maxheap}$  )

insert  $x$  in maxheap

if (  $\text{size}(\text{max}) - \text{size}(\text{min}) > 1$  )

{ extract max() & insert it  
in min heap() }

}

else  
{

insert  $x$  in minheap

if (  $\text{size}(\text{min}) > \text{size}(\text{max})$  )

{ extract min() & insert  
into maxheap() }

}

}

ans: insert ( get max() from maxheap );

priority que & heaps

Doubt 15

Merge  $k$  sorted arrays

