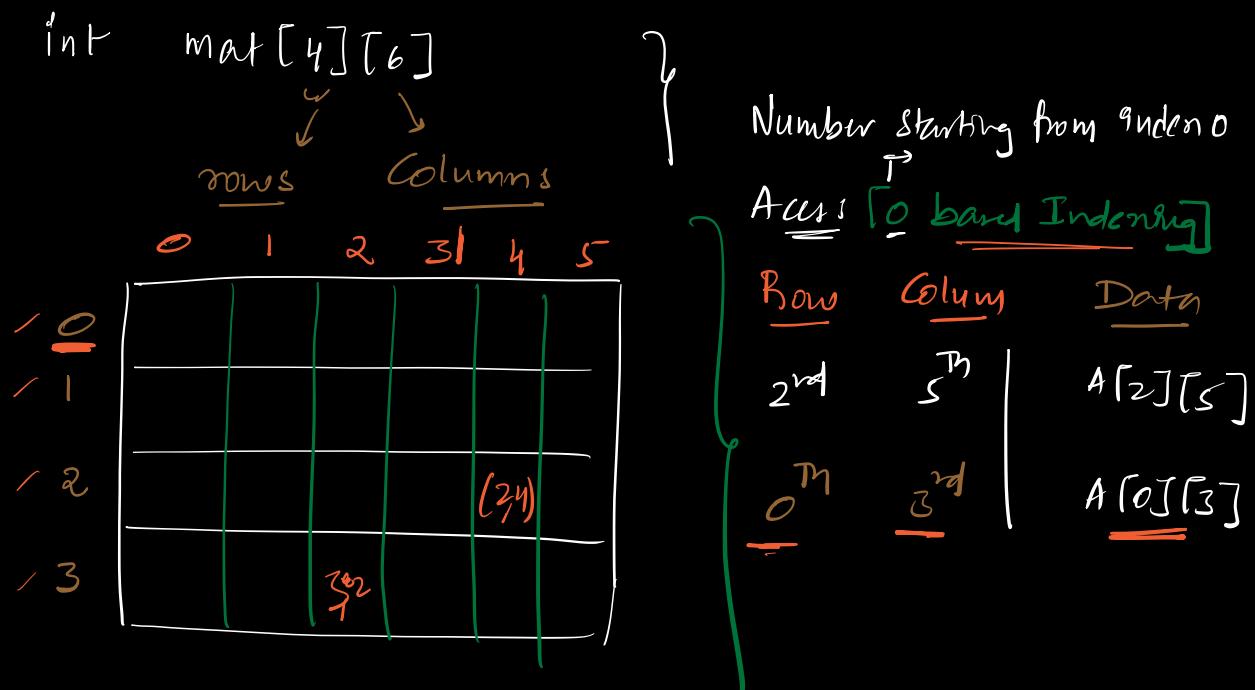


## 2D Matrix

- Arrays ✓
- Prefix Sum ✓
- Carry forward ✓
- Sliding Window ✓
- Contribution Techniques ✓
- Subarrays ✓

## 2D Matrix Basics



Given Mat  $[N][M]$  print all elements  
row by row.

N rows, q M Columns

$[0, N-1]$        $[0, M-1]$

$i = 0; i < N; i++ \{$

$j = 0; j < M; j++ \{$

print mat[i][j]

}

Iterations :  $N M$

Q)  $0 \ 1 \ 2 \ 3 \ 4$  Sum row by row

0	3	-1	2	6	1
1	3	2	1	7	-3
2	6	-3	4	-3	-2
3	10	2	3	-7	3

: 11

: 10

: 2

: 11

// When we iterate on a

particular row: Row number  
Same

// When we iterate on a

particular col: Column number  
Same

Q) Print row wise sum +

a matrix  $[N][M]$

Mat[N][M]

```
i = 0; i < N; i++) {  
    // Get ith row sum  
    S = 0;  
  
    j = 0; j < M; j++) {  
        S = S + mat[i][j];  
    }  
    cout << S // ith row sum  
}
```

```
j = 0; j < M; j++) {  
    // Get jth column sum  
    S = 0;  
  
    i = 0; i < N; i++) {  
        S = S + mat[i][j];  
    }  
    cout << S // jth column sum  
}
```

## Arithmetic operation on Matrices

### Add

mat<sub>1</sub> [3][3]

(3)	-1	6
5	(2)	6
10	11	(12)

mat<sub>2</sub> [3][2]

-1	6
2	(1)
4	5

Note: To Add or  
to Subtract 2  
Matrix both their  
dimensions should  
be same

Note: While +, - , f 2 matrices If we take  
i, j from mat<sub>1</sub>, Even from mat<sub>2</sub> we need to take i, j

Mat<sub>1</sub> [N][M], Mat<sub>2</sub> [N][M], Mat<sub>3</sub> [N][M]

Q Add Mat<sub>1</sub> q Mat<sub>2</sub> q same q Mat<sub>3</sub>

Dimensional check for  
a matrix is

$$\left\{ \begin{array}{l} i=0; i < N; i++ \\ j=0; j < M; j++ \end{array} \right\}$$

$$\left\{ \begin{array}{l} \text{Mat}_1[N_1][M_1] \\ \text{Mat}_2[N_2][M_2] \end{array} \right\}$$

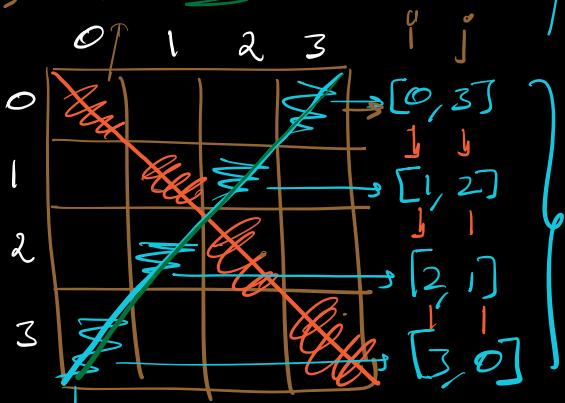
Imp

$$\left| \begin{array}{l} N_1 = N_2 \\ M_1 = M_2 \end{array} \right.$$

For add / Subtraction

$$\text{Mat}_3[i][j] = \text{Mat}_1[i][j] + \text{Mat}_2[i][j]$$

$\rightarrow$   $N \times N$  Square



Diagonal R-L

Observations :

- A)  $i$  is increasing  $\downarrow$   
 $j$  is decreasing  $\downarrow$
- B)  $i+j = N-1$   $\downarrow$   $\downarrow$
- C)  $(i, j)$  start  $\rightarrow [0, N-1]$
- D)  $(i, j)$  end  $\rightarrow [N-1, 0]$

Diagonal  
R-L

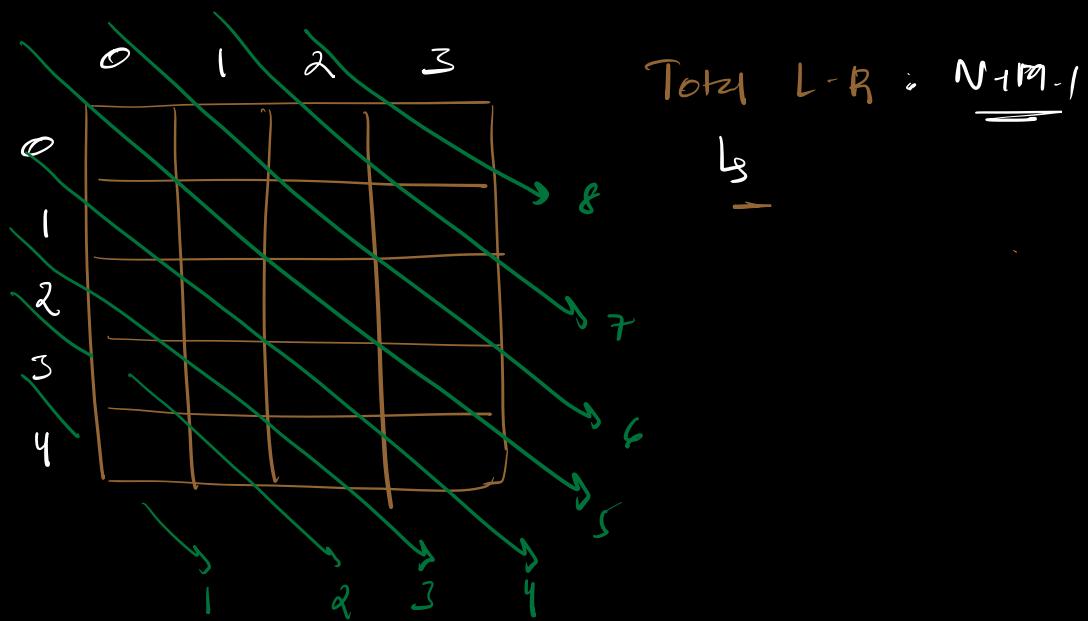
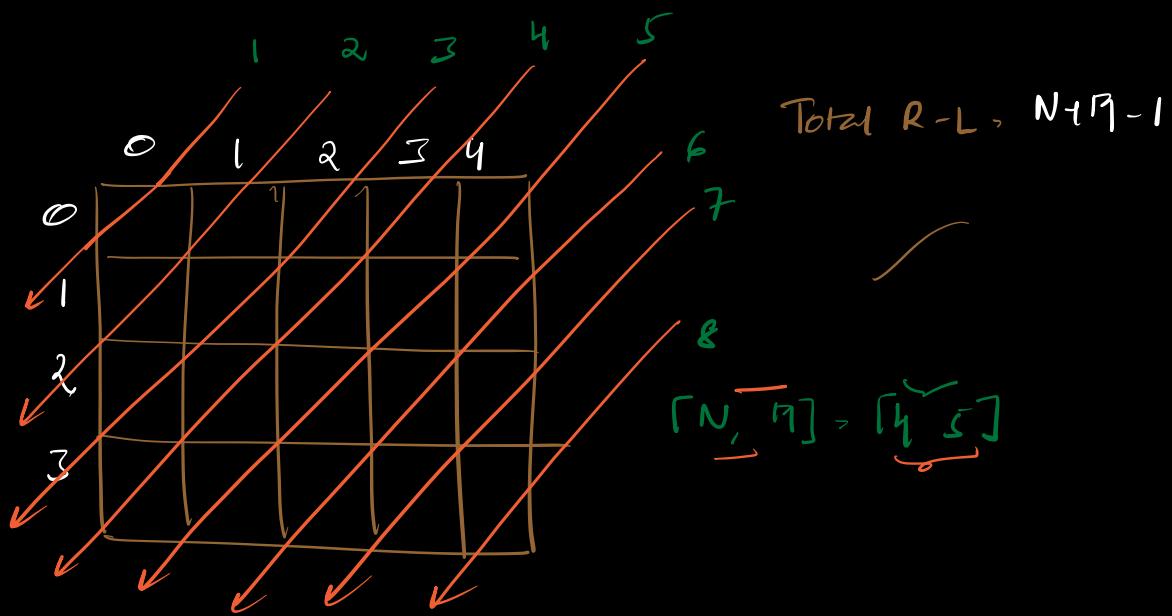
$$\begin{cases} i=0; i < N; i+1 \\ j=N-1-i \end{cases}$$

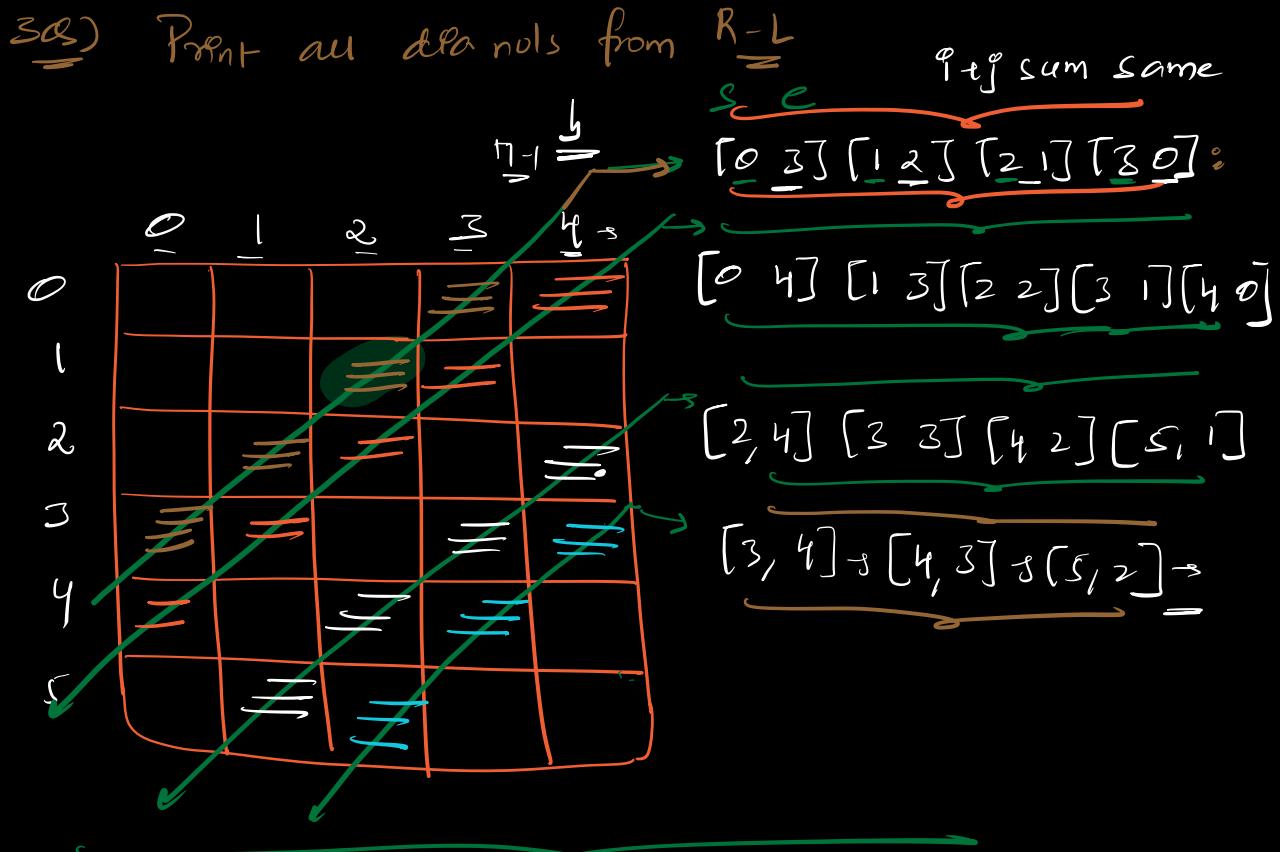
Print  $\underline{\text{mat}[i][j]}$

$$i=0; i < N; i+1 \}$$

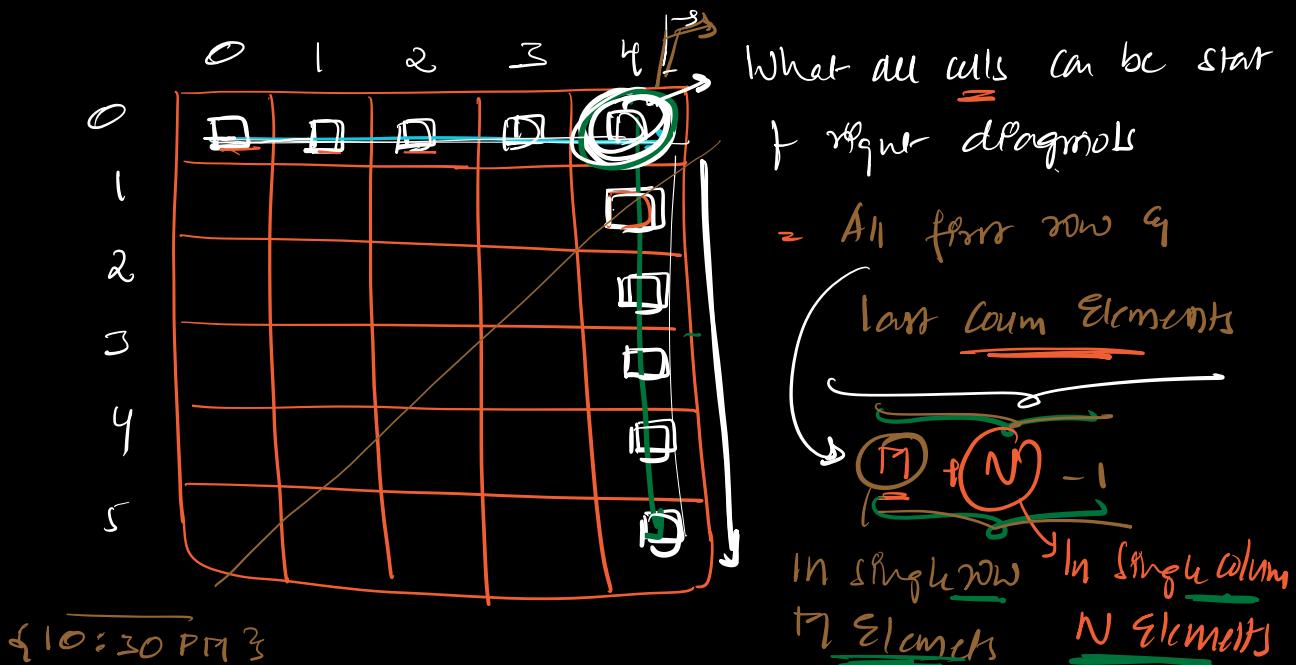
$i$   $j$   
 $\dot{}$  Point  $\underline{\text{mat}[i][j]}$

Diagonal L-R





In every right to left diagonal,  $9_{ij}$  is same.



// All right diagonal start

a)  $\theta^T \underline{\underline{w}} \rightarrow$  printing of  $\theta^M$  rows  
 $j = \underline{\underline{\theta / j \times M / j + 1}}$ ,

$(s, e) = [\underline{\underline{0}}, j]$  // start point of diagonal  
while ( $s < N$  &  $e = 0$ )  
print( $\text{mat}[\underline{s}][\underline{e}]$ ) ↗  
 $s++$ ,  $e--$        $w =$  column  
print("ln")  
↓  
e  
e--  
w  
=

$s = \underline{\underline{\text{row number}}}$  is continuously

increasing man's value we can

have is  $N-1$

$e = \underline{\underline{\text{column number}}}$ , is continuously

decreasing, min e value we can

have is 0

b)  $M-1$  columns       $\rightarrow$  We need to start from 1?  
 Because we already  
 considered  $[0, M-1]$

$$i = \underbrace{0}_{\text{start}} \times N + \underbrace{i}_{\text{index}} \{$$

$$(s, e) = \underbrace{[i, M-1]}$$

while ( $s \leq N$  &  $e >= 0$ )  
 print( $\text{mat}[s][e])$   
 $s += 1, e--$   
 print( $"\ln"$ )

Given a Square Matrix

→ Find Transpose of a matrix ?

3	-2	1	6
4	3	2	1
7	2	9	3
2	1	6	8

3	4	7	2
-2	3	2	1
1	2	9	6
6	1	3	8

Transpose

3	-2	1	6
3	3	6	9
2	1	7	8

3 × 4

3	3	2
-2	3	1
1	6	7

4 × 3

0<sup>th</sup> row → After transpose 0<sup>th</sup> column  
1<sup>st</sup> row → 1<sup>st</sup> column  
2<sup>nd</sup> row → 2<sup>nd</sup> column

Note: In a rectangular matrix, after transpose dimensions will change

Ex:

$\text{mat}[5][5]$ :

	0	1	2	3	4
0	-1	3	2	6	-2
1	4	1	3	5	8
2	-3	2	-6	5	
3	7	3	2	9	-8
4	4	-3	2	4	3

Transpon

	0	1	2	3	4
0	-1	4	-3	7	4
1	3	1	2	3	-3
2	2	3	-6	2	2
3	6	5	1	9	4
4	-2	8	5	-8	3

An Elent  $\text{mat}[i][j]$

After Transpon

at  $i=3, j=0$  at  $\text{mat}[j][i]$

Pseudo code :

$i = 0; i < N; i++ \{$

$j = 0; j < N; j++ \{$

$// Swap \underline{\text{mat}[i][j]} \& \underline{\text{mat}[j][i]}$  \*

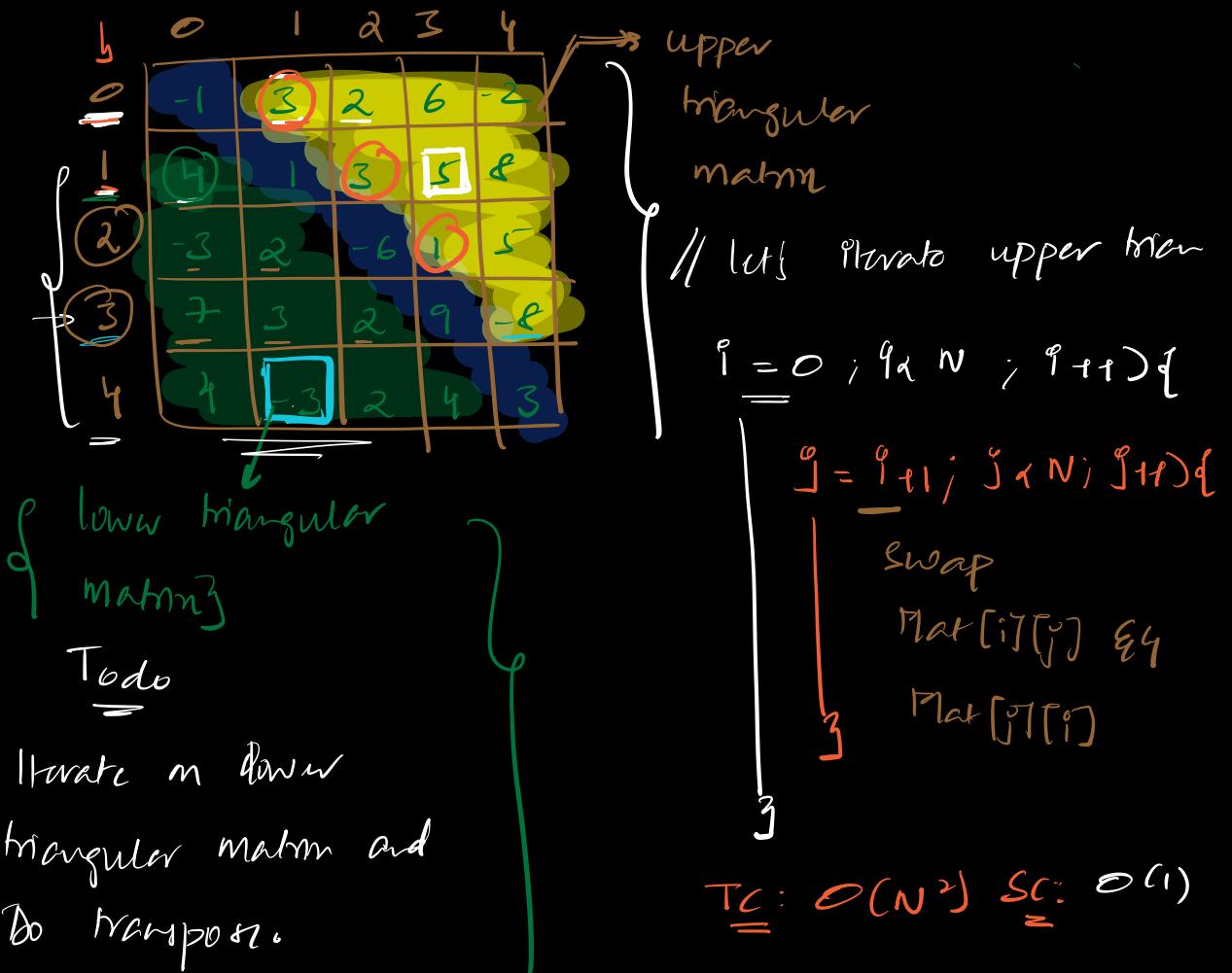
$i=0, j=3 :$

Swap  $\text{mat}[0][3] \& \text{mat}[3][0]$

$i=3, j=0 :$

Swap  $\text{mat}[3][0] \& \text{mat}[0][3]$

wrong because



$i = 1, i \leq N, i+1 \{$   
 $j = 0, j \leq i, j+1 \{$   
 Swap  
 $\text{Mat}[i][j] \Leftarrow$   
 $\text{Mat}[j][i]$

→ Given a Square Matrix rotate  $90^\circ$ , Clockwise

The diagram illustrates two methods for rotating a  $5 \times 5$  matrix  $M$   $90^\circ$  clockwise.

**Method 1:**  $M \xrightarrow{\text{Transpose}} M^T \xrightarrow{\text{Row reverse}} \text{Result}$

**Method 2:**  $M \xrightarrow{\text{Column reverse}} M^R \xrightarrow{\text{Transpose}} \text{Result}$

**Matrix  $M$ :**

$$\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ \hline 0 & -3 & 2 & 1 & 6 & 4 \\ 1 & 2 & 3 & -1 & 6 & 2 \\ 2 & 3 & 9 & 8 & -1 & 2 \\ 3 & 3 & -2 & 4 & 6 & 1 \\ 4 & 9 & -3 & 1 & 2 & -1 \end{matrix}$$

**Result (Method 1):**

$$\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ \hline 0 & 9 & 3 & 3 & 2 & -3 \\ 1 & -3 & -2 & 1 & 3 & 2 \\ 2 & 1 & 1 & 8 & -1 & 1 \\ 3 & 2 & 6 & -1 & 6 & 6 \\ 4 & -9 & 1 & 2 & 2 & 1 \end{matrix}$$

**Result (Method 2):**

$$\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ \hline 0 & 9 & 3 & 3 & 2 & -3 \\ 1 & -3 & -2 & 1 & 3 & 2 \\ 2 & 1 & 1 & 8 & -1 & 1 \\ 3 & 2 & 6 & -1 & 6 & 6 \\ 4 & -9 & 1 & 2 & 2 & 1 \end{matrix}$$

To Rotate  $90^\circ$  Clockwise

- ① Transpose :  $\rightarrow$
- ② Reverse every row  $\left\{ \right\}$

$$TC: O(N^2)$$

$$SC: O(1)$$

Given a Matrix  $\underline{\underline{[N][M]}}$ , Print The boundary  
Clockwise

$\underline{\underline{\text{Mat}[4][5]}}$

0	1	2	3	4
0	(-1)	3	-2	4
1	2	4	-3	2
2	3	-2	4	-1
3	1	3	1	2

- 1)  $\underline{\underline{\text{Row}(L-R)}}$
- 2)  $\underline{\underline{\text{1}^{\text{th}} \text{ column}(T-D)}}$
- 3)  $\underline{\underline{\text{N}-1^{\text{th}} \text{ row}(R-L)}}$
- 4)  $\underline{\underline{\text{0}^{\text{th}} \text{ column}(D-T)}}$

$\underline{\underline{\text{Mat}[N][M]}}$

{ Notes: Take Care of corner  
Elements }

4 Steps:

$\underline{\underline{\text{Row}}}:$   $i = 0; j < M-1; j+1 \{ \Rightarrow \}$  }  $\rightarrow \underline{\underline{M-1}}$   
 $\quad \quad \quad | \quad \quad \quad \text{Print}(\text{mat}[i][j]) \quad \quad \quad \}$

// After above loop  $j = \underline{\underline{M-1}}$

$\underline{\underline{\text{M-1 col}}}:$   $i = 0; i < N-1; i+1 \{ \quad \quad \quad \}$  }  $\underline{\underline{N-1}}$   
 $\quad \quad \quad | \quad \quad \quad \text{Print}(\text{mat}[i][j]) \quad \quad \quad \}$

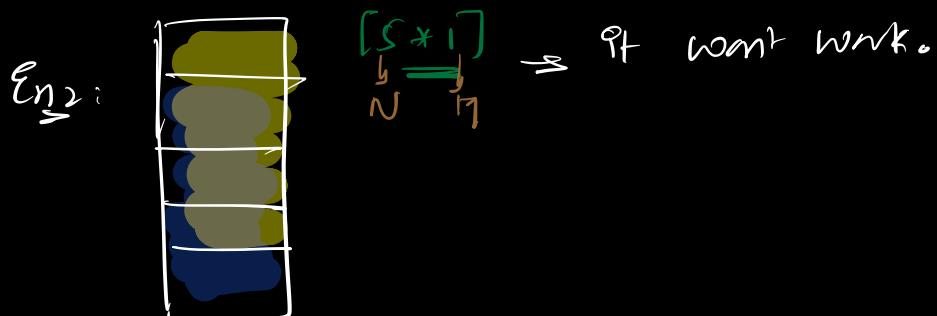
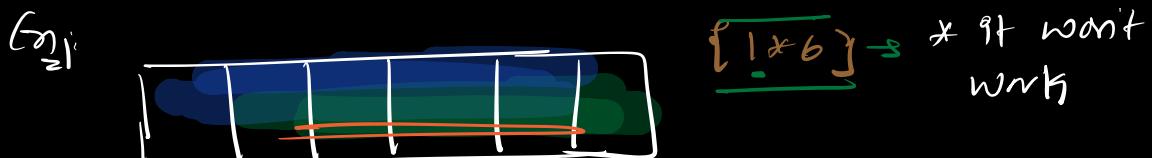
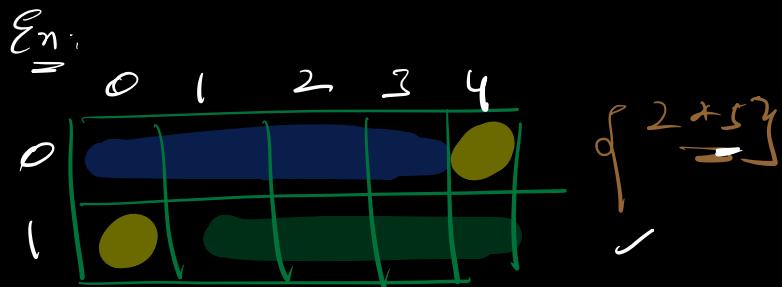
// After above loop  $i = N-1$

$\text{N-1 now}$   
 $(R-L)$

$j = N-1; j > 0; j-- \{$   
 $\quad \quad \quad \text{print}(mat[i][j]) \}$   
 $\}$   
 $// After above loop  $j=0$$

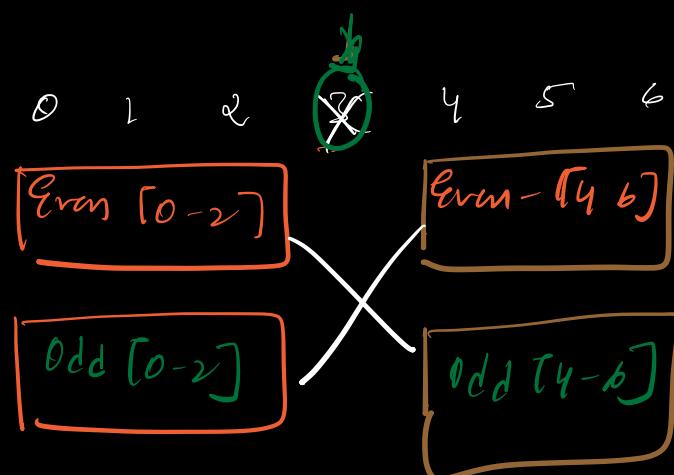
$0 \text{ col}$   
 $(B-T)$

$i = N-1; i > 0; i-- \{$   
 $\quad \quad \quad \text{print}(mat[i][j]) \}$   
 $\}$   
 $// After above loop  $i=0, j=0$$



Note: If it's a single row or column, & it want work. (Don't enter data directly)

Doubts:



$$\left\{ \begin{array}{l} \text{PFF}[i] = \text{Sum of all even index from } [0-i] \\ \text{PFO}[i] = \text{Sum of all odd index from } [0-i] \end{array} \right. \quad \left\{ \begin{array}{l} \text{arr}[6]: \begin{array}{|c|c|c|c|c|c|c|} \hline 0 & 1 & 2 & 3 & 4 & 5 \\ \hline 3 & -1 & 2 & 6 & 2 & 1 \\ \hline \end{array} \\ \text{PFE}: \begin{array}{|c|c|c|c|c|c|c|} \hline 3 & 5 & 5 & 3 & 7 \\ \hline \end{array} \\ \text{PFO}: \begin{array}{|c|c|c|c|c|c|c|} \hline 0 & -1 & -1 & 5 & 5 & 6 \\ \hline \end{array} \end{array} \right.$$

$$\sum_{q=0}^{N-1} \left\{ \text{SumF}[0-q-1] + \text{SumO}[q+1, N-1] = \right. \\ \left. \text{SumF}[q+1, N-1] + \text{SumO}[0, q-1] \right\}$$

XOR Prefix Value

$$Pf[i] = Pf[i-1] \oplus ar[i]$$

→ If update in array

↓  
array bit // bit  
↓

