

$y = [y_{\text{ср. exp.}}] - \text{МПК}$

	$x_1 = R_1, \Omega$	$x_2 = C_1, \text{нФ}$	$x_3 = R_2, \Omega$
x_i^0	100	680	500
x_i^{\min}	70	600	450
x_i^{\max}	130	760	550
z_i	30	80	50

N°	R_1	C_1	R_2	y_{i1}	y_{i2}	y_{i3}	\bar{y}_i	$S^2(y_i)$	$S^2(y)$	$S^2(b_i)$	\hat{y}_i
1	-	-	-	3,3	3,5	4,5	3,77	0,41	0,20	0,008	4,41
2	+	-	-	3,4	3,9	3,9	3,73	0,08			4,21
3	-	+	-	3,2	2,5	2,8	2,83	0,12			2,89
4	+	+	-	2,8	2,5	3,0	2,77	0,06			2,69
5	-	-	+	4,4	5,2	5,8	5,13	0,49			5,55
6	+	-	+	4,0	4,4	4,5	4,30	0,07			4,51
7	-	+	+	2,8	3,4	3,8	3,33	0,25			4,03
8	+	+	+	3,4	3,8	3,0	3,40	0,16			2,99

1) $b_0 = (4,5 + 3,9 + 2,8 + 3,0 + 5,8 + 4,5 + 3,8 + 3,0) / 8 = 3,91$
 $b_1 = (-4,5 + 3,9 - 2,8 + 3,0 - 5,8 + 4,5 - 3,8 + 3,0) / 8 = -0,31$
 $b_2 = (-4,5 - 3,9 + 2,8 + 3,0 - 5,8 - 4,5 + 3,8 + 3,0) / 8 = -0,76$
 $b_{12} = 0,16$; $b_3 = 0,36$; $b_{13} = -0,21$; $b_{23} = -0,11$
 $b_{123} = -0,04 \rightarrow y = 3,91 - 0,31x_1 - 0,76x_2 + 0,16x_1x_2 +$
 $+ 0,36x_3 - 0,21x_1x_3 - 0,11x_2x_3 - 0,04x_1x_2x_3$

2) $t = 2,13$ при $\alpha = 0,95$ и $f = 8(3-1) = 16$ $|b_i| > 2,13\sqrt{0,008} = 0,19$
 $y = 3,91 - 0,31x_1 - 0,76x_2 + 0,36x_3 - 0,21x_1x_3$

3) $S_{\text{ог}}^2 = \frac{3}{8-5} \sum_{i=1}^N (y_{i3} - \hat{y}_i)^2$

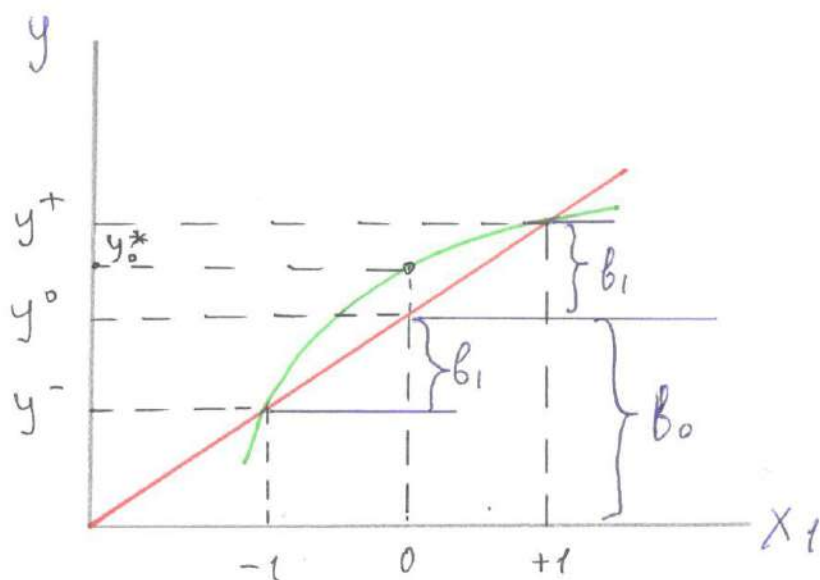
$y_{13} = 4,5$ $\hat{y}_1 = 3,91 - 0,31(-1) - 0,76(-1) + 0,36(-1) -$
 $\hat{y}_1 = 4,41 - 0,21(-1)(-1) = 3,91 + 0,31 + 0,76 - 0,36 - 0,21$

$S_{\text{ог}}^2 = 0,324$ $F_p = \frac{0,324}{0,2} = 1,62$

$F_{kp} = 3,2$ при $\alpha = 0,95$ $f_{kp} = 8-3=5$ и $f_y = 8(3-1) = 16$

$1,62 < 3,2 \rightarrow \text{ММ согласована}$

Рис. 22



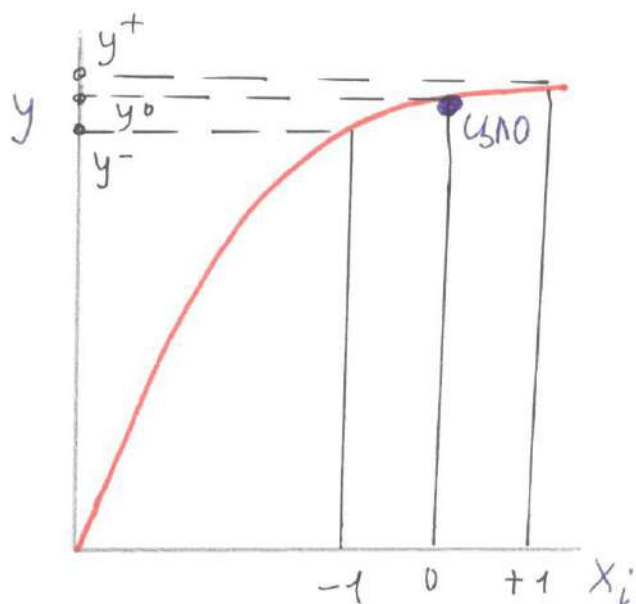
$$y = b_0 + b_1 x_i \quad (22)$$

$$\left. \begin{aligned} b_0 &= y^0 \\ b_0 &= y_0^* \end{aligned} \right\}$$

$$|y_0 - b_0| < S_{on}^2 \quad (23)$$

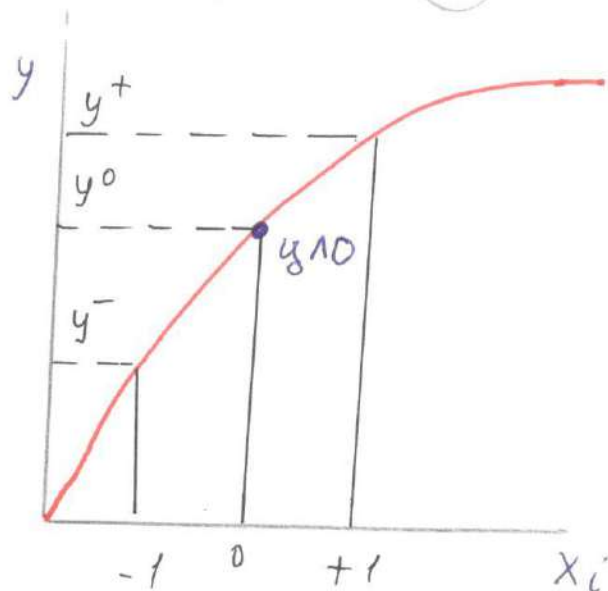
$$S_{on}^2 = \frac{S^2(y)}{m} \quad (24)$$

Pue. 23

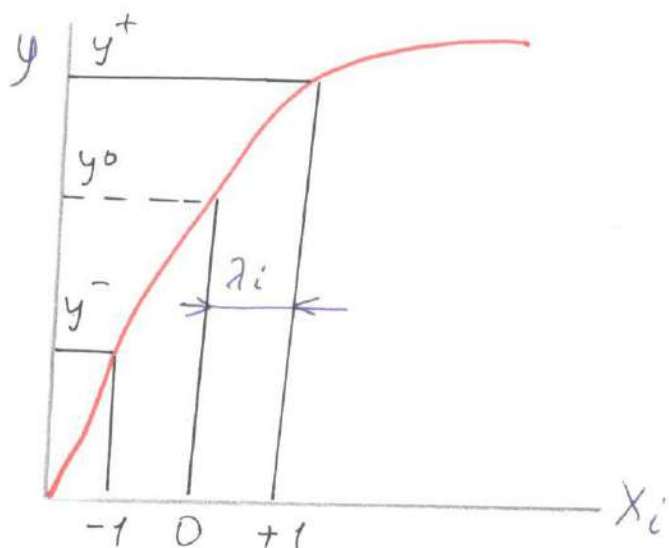
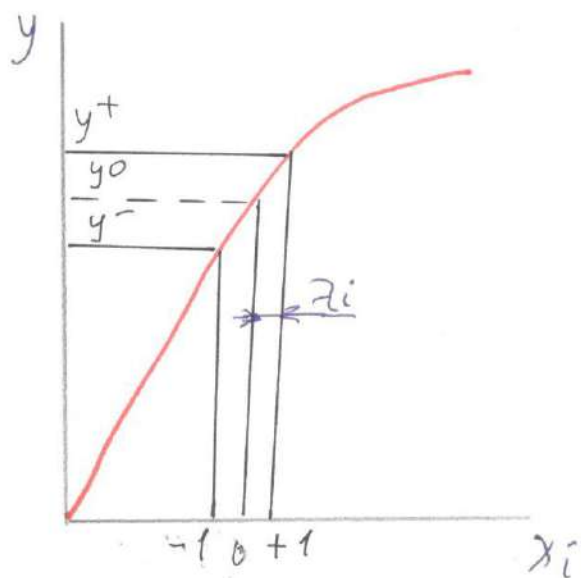


$$b_0 = \beta_0 + \sum \beta_{ii} \quad (25)$$

$$A = |y_0^* - b_0| \quad (26)$$



Pue. 24



Pue. 25

$$B_i = 2b_i \quad (27)$$

$$y = b_0 + b_1 x_1 - b_2 x_2 \quad (28)$$

$$y = b_0 + b_1 x_1 - b_2 x_2 + b_{12} x_1 x_2 \quad (29)$$

Модель

Линейная

N°	X ₁	X ₂	y = 10 + 2x ₁ + 3x ₂
1	-	-	10 - 2 - 3 = 5
2	+	-	10 + 2 - 3 = 9
3	-	+	10 - 2 + 3 = 11
4	+	+	10 + 2 + 3 = 15

$$B_1 = 9 - 5 = 4$$

$$B_1 = 15 - 11 = 4$$

$$B_2 = 11 - 5 = 6$$

$$B_2 = 15 - 9 = 6$$

$$B_1^- = 2$$

$$B_1^+ = 6$$

$$B_2^- = 4$$

$$B_2^+ = 8$$

$$\left. \begin{array}{l} B_1^- = 2 \\ B_1^+ = 6 \\ B_2^- = 4 \\ B_2^+ = 8 \end{array} \right\} \quad (30)$$

$$\left. \begin{array}{l} B_1^- = B_1 - B_{12} = 2(b_1 - b_{12}) \\ B_1^+ = B_1 + B_{12} = 2(b_1 + b_{12}) \\ B_2^- = B_2 - B_{12} = 2(b_2 - b_{12}) \\ B_2^+ = B_2 + B_{12} = 2(b_2 + b_{12}) \end{array} \right\} \quad (31)$$

$$B_i^\mp = 2(b_i \mp b_{ij}) \quad (32)$$

$$y = 10 + 2x_1 + 3x_2 + x_1x_2$$

1

$$B_1^- = 2(2-1) = 2$$

$$B_1^+ = 2(2+1) = 6$$

$$B_2^- = 2(3-1) = 4$$

$$B_2^+ = 2(3+1) = 8$$

$$y = 10 - 2x_1 - 3x_2 + x_1x_2$$

3

$$B_1^- = 2(-2-1) = -6$$

$$B_1^+ = 2(-2+1) = -2$$

$$B_2^- = 2(-3-1) = -8$$

$$B_2^+ = 2(-3+1) = -4$$

$$y = 10 + 2x_1 + 3x_2 - x_1x_2$$

2

$$B_1^- = 2(2+1) = 6$$

$$B_1^+ = 2(2-1) = 2$$

$$B_2^- = 2(3+1) = 8$$

$$B_2^+ = 2(3-1) = 4$$

$$y = 10 - 2x_1 - 3x_2 - x_1x_2$$

4

$$B_1^- = 2(-2+1) = -2$$

$$B_1^+ = 2(-2-1) = -6$$

$$B_2^- = 2(-3+1) = -4$$

$$B_2^+ = 2(-3-1) = -8$$

$$y = 10 - 2x_1 + 3x_2 + x_1x_2$$

5

$$B_1^- = 2(-2-1) = -6$$

$$B_1^+ = 2(-2+1) = -2$$

$$B_2^- = 2(3-1) = 4$$

$$B_2^+ = 2(3+1) = 8$$

$$y = 10 - 2x_1 + 3x_2 - x_1x_2$$

6

$$B_1^- = 2(-2+1) = -2$$

$$B_1^+ = 2(-2-1) = -6$$

$$B_2^- = 2(3+1) = 8$$

$$B_2^+ = 2(3-1) = 4$$

$$y = 10 - 2x_1 + x_1x_2$$

7

$$B_1^- = 2(-2-1) = -6$$

$$B_1^+ = 2(-2+1) = -2$$

$$B_2^- = 2(0-1) = -2$$

$$B_2^+ = 2(0+1) = 2$$

$$y = 10 + 2x_1 + x_1x_2$$

8

$$B_1^- = 2(+2-1) = 2$$

$$B_1^+ = 2(+2+1) = 6$$

$$B_2^- = 2(0-1) = -2$$

$$B_2^+ = 2(0+1) = 2$$

$$y = 10 + 2x_1 - x_1x_2$$

9

$$B_1^- = 2(2+1) = 6$$

$$B_1^+ = 2(2-1) = 2$$

$$B_2^- = 2(0+1) = 2$$

$$B_2^+ = 2(0-1) = -2$$

$$y = 10 - 2x_1 - x_1x_2$$

10

$$B_1^- = 2(-2+1) = -2$$

$$B_1^+ = 2(-2-1) = -6$$

$$B_2^- = 2(0+1) = 2$$

$$B_2^+ = 2(0-1) = -2$$

$$y = 10 + x_1x_2$$

11

$$B_1^- = 2(0-1) = -2$$

$$B_1^+ = 2(0+1) = 2$$

$$B_2^- = 2(0-1) = -2$$

$$B_2^+ = 2(0+1) = 2$$

$$y = 10 - x_1x_2$$

12

$$B_1^- = 2(0+1) = 2$$

$$B_1^+ = 2(0-1) = -2$$

$$B_2^- = 2(0+1) = 2$$

$$B_2^+ = 2(0-1) = -2$$

$$1. \quad \bar{X}_{i \min} \dots \bar{X}_{i \max}$$

$$2. \quad \bar{X}_i^0 = \frac{1}{2} (\bar{X}_{\max} - \bar{X}_{i \min})$$

$$\bar{\lambda}_i = \bar{X}_i^0 - \bar{X}_{i \min} = \bar{X}_{i \max} - \bar{X}_i^0$$

$$X_i' = \frac{\bar{X}_i - \bar{X}_i^0}{\bar{\lambda}_i}$$

3.

μ_i^0	X_1	X_2	...	X_n	y_i
1	-	-		-	y_1
2	+	-		-	y_2
\vdots	\vdots	\vdots	...	\vdots	\vdots
N	+	+		+	y_N

$$4. \quad Y = b_0 + b_1 X_1 + b_2 X_2 + b_{12} X_1 X_2 + \dots + b_{12\dots n} X_1 X_2 \dots X_n$$

$$5. \quad b_0 = \frac{1}{N} \sum_{i=1}^N y_i$$

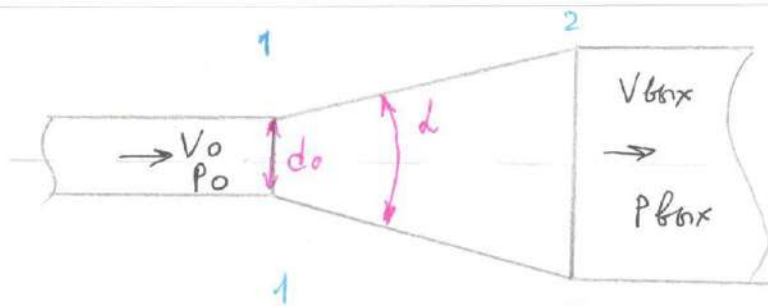
$$b_1 = \frac{1}{N} [-y_1 + y_2 - y_3 + \dots + y_N]$$

$$\vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots$$

$$6. \quad B_1^- = ? \quad B_1^+ = ? \quad B_2^- = ? \quad B_2^+ = ?$$

$$B_1^- = ? \quad B_1^+ = ? \quad B_3^- = ? \quad B_3^+ = ?$$

$$\vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots$$



$$\begin{array}{c} 1-1 \\ S_1 \\ V_0 \\ p_0 \\ E_1 \end{array}$$

$$\begin{array}{c} 2-2 \\ S_2 \\ V_{btx} \\ p_{btx} \\ E_2 \end{array}$$

$$E_1 = E_2 = p_0 + \rho \frac{V_0^2}{2} = p_{btx} + \rho \frac{V_{btx}^2}{2} + \Delta p_r \quad (33)$$

$$\Delta p_r = \xi \rho \frac{V_0^2}{2} \quad (34) \quad \xi = \varphi(d, m, Re) \quad (35)$$

$$m = \frac{S_1}{S_2} ; Re = \frac{V_0 d_0}{\mu} \quad (36)$$

Re · 10 ⁵	d, mm				
	4	6	8	10	12
0,5	0,135	0,121	m=0,5 0,112	0,107	0,109
1,0	0,106	0,090	0,083	0,080	0,088
2,0	0,082	0,070	0,068	0,062	0,062

Re · 10 ⁵	d, mm				
	4	6	8	10	12
0,5	0,197	0,165	m=0,25 0,151	0,157	0,174
1,0	0,154	0,126	0,119	0,120	0,131
2,0	0,120	0,101	0,096	0,096	0,107

$$d = 6 \dots 10^0$$

$$m = 0,25 \dots 0,50$$

$$Re = 0,5 \cdot 10^5 \dots 1,0 \cdot 10^5$$

N°	x ₁ = d	x ₂ = m	x ₃ = Re	y = ξ
1	-	-	-	0,165
2	+	-	-	0,157
3	-	+	-	0,121
4	+	+	-	0,107
5	-	-	+	0,126
6	+	-	+	0,120
7	-	+	+	0,090
8	+	+	+	0,080

$$\begin{aligned} \bar{x}_1^0 &= (6+10)/2 = 8^0 \\ \bar{x}_2^0 &= (0,25+0,5)/2 = 0,375 \\ \bar{x}_3^0 &= (0,5+1)/2 = 0,75 \cdot 10^5 \\ \bar{\lambda}_1 &= 2^0 \quad \bar{\lambda}_2 = 0,125 \\ \bar{\lambda}_3 &= 0,125 \cdot 10^5 \end{aligned}$$

$$\begin{aligned} d &= \frac{\bar{d} - 8}{2} = x_1 & m &= \frac{\bar{m} - 0,375}{0,125} = x_2 & Re &= \frac{\bar{Re} - 0,75}{0,25} = x_3 \\ b_0 &= 0,121 & b_2 &= -0,021 & b_3 &= -0,017 & b_{23} &= 0,002 \\ b_1 &= -0,005 & b_{12} &= -0,001 & b_{13} &= 0,001 & b_{123} &= 0 \end{aligned}$$

$$\xi = 0,121 - 0,005 d - 0,021 m - 0,001 d m - 0,017 Re + 0,001 d Re + 0,002 m Re \quad (37)$$