

You might find the environments `\bmatrix` and `\pmatrix` useful for the following exercises.

$$\rho_\theta = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \quad (21)$$

$$\left[\begin{array}{c|ccc} 1 & 0 & \cdots & 0 \\ \hline 0 & * & \cdots & * \\ \vdots & \vdots & \ddots & \vdots \\ 0 & * & \cdots & * \end{array} \right] = \begin{array}{|c|ccc|} \hline 1 & 0 & \cdots & 0 \\ \hline 0 & * & \cdots & * \\ \vdots & \vdots & \ddots & \vdots \\ 0 & * & \cdots & * \\ \hline \end{array} \quad (22)$$

Note the locations of the bounds on the summation in the following exercise.

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N p_i (x_i - \bar{x})^2} = \sqrt{\frac{\sum_{i=1}^N p_i (x_i - \bar{x})^2}{N}} \quad (23)$$