

# Physics

Anabratা Biswas

\* TEACHER ⇒ Aayudh Sir

\* By ⇒ PW

\* Class ⇒ 11<sup>th</sup> (NEET)



# NEET

# 2027

#L1

## \* Mathematical tools \*

### # Common Kidnapping

$$\Rightarrow 30 \times 2 + 30 = 30(2+1) = 30(3) = 90$$

$$\Rightarrow 188 \times 9 + 66 \times 3 = 9(188+22) =$$

$$\Rightarrow (10^2 + 70^2) = 10^2 (1^2 + 7^2) = 100(50) = 5000$$

$$\Rightarrow x = R\sqrt{3}$$

$$\Rightarrow \sqrt{x^2 + R^2} = \sqrt{(R\sqrt{3})^2 + R^2} = \sqrt{(R\sqrt{3} \times R\sqrt{3}) + R^2} = \sqrt{R^2 3 + R^2} = \sqrt{4R^2} = 2R \quad \times$$

$$= \sqrt{(R\sqrt{3})^2 + R^2} = \sqrt{R^2 3 + R^2} = \sqrt{CR^2(3+1)} = \sqrt{4R^2} = 2R \quad \checkmark$$

$$x \Rightarrow \sqrt{7R^2} = \sqrt[3]{x^2 + R^3} = \sqrt[3]{7R^3 + R^3} = \sqrt[3]{8R^3} = 2R$$

$$\Rightarrow \sqrt[3]{27000} = \sqrt[3]{27 \times 1000} = 3 \times 10 = 30 \quad \checkmark$$

### # LCM

$$\Rightarrow (60, 40) = 20 (3 \times 2) = 120$$

$$\Rightarrow (144, 60) = 12 (12 \times 5) = 12(60) = 720$$

### # Fractions to Decimals

$$= \frac{1}{2}^{0.5} = \frac{1}{3}^{0.3} = \frac{1}{4}^{0.25}$$

$$\text{So, } \frac{8}{3} = 2 \text{ left so, } 0.6 \quad \{2+0.6\} = 2.\overline{66}$$

$$= \frac{88}{3}^{18.2} = 18 + \frac{1}{3} = 18 + 0.2 = 18.2$$

$$\neq \frac{1}{5} \Rightarrow \text{Numinate } 2 \times 2 = \frac{10.2}{2} \rightarrow \text{Last digit decimal}$$

$$= \frac{33}{5} = 6.6 = \frac{124}{5} = 24.8 = \frac{135}{5} = 27$$

$$\neq \frac{1}{6} = 0.166666\ldots$$

$$= \frac{1}{7} = 0.1421$$

$$= \frac{1}{8} = 0.125$$

$$= \frac{1}{9} = 0.\overline{111} = \frac{2}{9} = 0.\overline{222} = \frac{3}{9} = 0.\overline{333} = \frac{20^2}{9}, 2 = 2.\overline{222} = \frac{100^{11}}{9} = 1 \Rightarrow 11.\overline{111}$$

### # Equivalent Fractions

$$= \frac{1 \times 4}{2 \times 4} = \frac{4}{8}$$

$$= \frac{7}{11} = \frac{11}{121} = \frac{77}{121} \text{ (Same)} = \frac{3}{7} = \frac{2}{63} = \frac{27}{63}$$

## #LCM and Fraction

$$\Rightarrow \frac{1}{2} + \frac{3}{4} = \frac{1}{2} \left( 1 + \frac{3}{2} \right) \rightarrow \text{Use common for fraction}$$

$$\Rightarrow \frac{7}{11} - \frac{2}{121} = \frac{1}{11} \left( 7 - \frac{2}{11} \right) = \frac{1}{11} \left( \frac{75}{11} \right) \Rightarrow \frac{75}{121}$$

{ This work when denominator divides }

#1 田1

$$\Rightarrow \frac{1+15}{8} = \frac{9}{8} \rightarrow \text{Denominator same}$$

$\frac{8}{3} \times \frac{8}{1} \rightarrow$  Denominator same

$$\Rightarrow 1 - \frac{1}{9} = \frac{8}{9}$$

$$\therefore 1 \left( \frac{1}{121} \right) = \frac{119}{121}$$

# Decimals addition, Subtraction Rules (Point se point miso)

$$\Rightarrow 0.2 + 0.3 = \frac{0.2}{0.3} \text{ Ans}$$

$$\Rightarrow 0.20 + 0.03 = \frac{0.20}{+0.03} \\ 0.23$$

$$\Rightarrow 8.27 - 1.99 = \frac{8.27}{1.99} \quad \text{Ans}$$

# Decimal Multiply

$$\Rightarrow \frac{0.02}{1} \times \frac{0.3}{1} = \frac{0.06}{2}$$

$$\Rightarrow 0.2 \times 0.03 = 0.006 \Rightarrow \frac{0.2}{0.3} = \frac{2}{3} = 0.6$$

$$\Rightarrow 0.12 \times 0.\overline{005} = \frac{12}{100}$$

$$\Rightarrow 99.9 \times 0.5$$

$$\frac{999}{10} \times \frac{5}{10} = \frac{4995}{100} = 49.95$$

$$\Rightarrow \frac{6.9}{1.44} = \frac{6.90}{1.44} = \frac{690}{144} \frac{220}{48} = \frac{115}{24}$$

$\Rightarrow$  PUPPY POINT-1

- Common Kidnapping

- LCM = L.C. common factor multiply =  $6, 9 = 3(2, 3) = 18$

$$\bullet \text{Equivalent fraction} = \frac{2}{3} = \frac{16}{24}$$

$$\bullet \text{ Fraction Addition: } \frac{1}{11} - \frac{8}{99} = \frac{1}{11} \left( 1 - \frac{8}{9} \right) = \frac{1}{11} \left( \frac{1}{9} \right) = \frac{1}{99}$$

- Fractional Division & Multiplication Rule:-  $2 \div 2 = 1$  &  $2 \div 5 = \frac{2}{5}$  &  $\frac{3}{5} \times 5 = 3$

- Decimals Addition, Subtraction Rules:- Point se point mila

### Decimals Multiply, Division Rule :-

Point (Gins)

## Shift Karna

+  
 $\frac{x}{10^x}$

#L2

$$\Rightarrow \frac{1}{6} = 0.1666$$

$$\Rightarrow \frac{5}{6} = 0.833 \Rightarrow \frac{1}{7} = 0.142857 \Rightarrow \frac{1}{8} = 0.125$$

$$x^0 = 1$$

$$x^1 = x$$

$$x^2 = x \times x$$

$$x^3 = x \times x \times x$$

$2^0 = 1$	$0.1^0 = 1$
$2^2 = 4$	$0.1^1 = 0.1$
$2^3 = 8$	$0.1^2 = 0.01$
$2^4 = 16$	$0.1^3 = 0.001$
$2^5 = 32$	$0.1^4 = 0.0001$
$2^6 = 64$	

Less not increase

Number increase

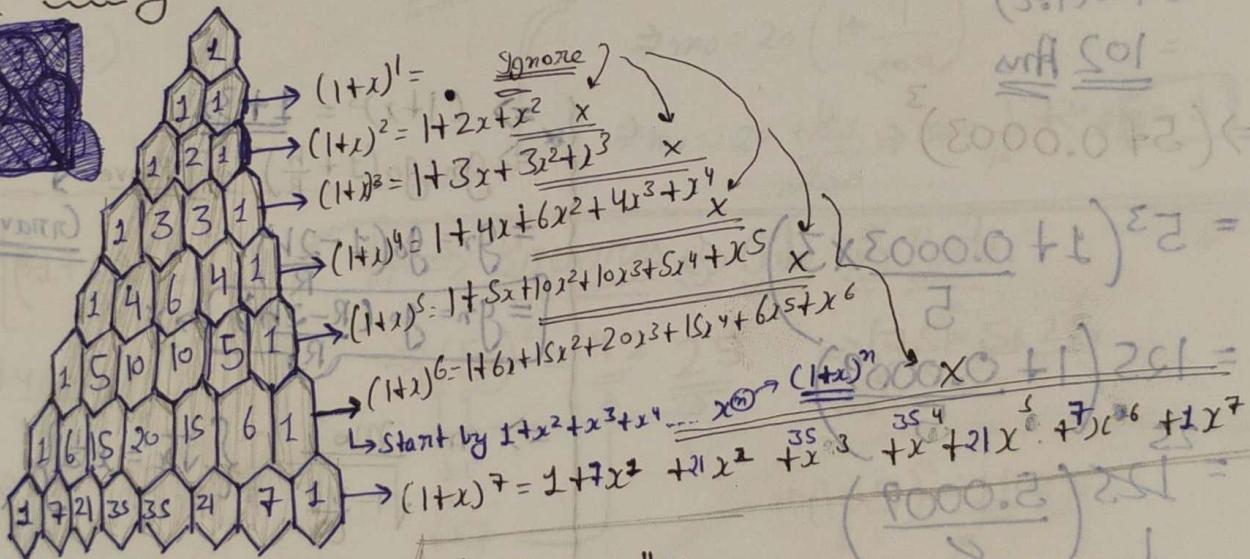
$x > 1$  when  $A = x^4, B = x^6$   
 $\Rightarrow x^n = n \downarrow$  (greater)  
 $x^6 = \underline{\text{High}} \text{ (greater)}$   
 $\Rightarrow x^4 = \underline{\text{High}}$  when  $x < 1$

$$\Rightarrow (1 + 0.001)^{100}$$

$$\begin{aligned} &\Rightarrow 1 + \underbrace{(0.1)}_{\text{small}}^2 + \underbrace{(0.1)}_{\text{very small}}^3 + \underbrace{(0.1)}_{\text{very very small}}^4 \dots \\ &\Rightarrow 1 + 0.1 \\ &\Rightarrow 1.1 \checkmark \end{aligned}$$

[Very Small = Ignore]

# Pascal's Triangle



$$\Rightarrow (1+x)^6 = (1+6x) \quad [x \ll 1]$$

$$\text{So, } (1+x)^n = (1+nx)$$

\* If  $x \ll 1$  then,

- $(1+x)^5 = (1+5x)$
- $(1+x)^{100} = (1+100x)$
- $(1+x)^{-3} = (1-3x)$
- $(1+x)^{-0.5} = (1-0.5x)$

# Binomial Approximation

$\Rightarrow$  if  $x \ll 1$

$$\text{So, } (1+x)^n = (1+nx)$$

$$\therefore \Rightarrow (1+2)^{10} = (1+0.1)^{10} = (1+10 \cdot \frac{1}{10}) = 1+1 = 2$$

$$\therefore \Rightarrow (1+0.05)^5 = (1+(0.05)5) = 1 + \frac{5}{100} \times 8 = 1.25$$

$$\begin{aligned} \therefore (1.0004)^{500} &= (1+0.0004(500)) \\ &= 1 + \frac{4 \times 500}{1000000} \\ &= \frac{6}{5} = 1.2 \end{aligned}$$

$$0.1(1.0) = (1.0 + 0.1)^2 = X$$

$$(1.0 + 2(0.1))^2 = 1$$

$$(1.0 + 0.1 \times 1.0)$$

Common

$$= 1^2 \left( 1 + \frac{0.1}{1.0} \right)^2$$

$$= 1^2 \left( 1 + \frac{0.1}{10} \times 21 \right)$$

$$= 1^2 \left( 1 + \frac{1}{5} \right) = 10 \left( \frac{6}{5} \right) = \frac{600}{5} = 12$$

$$\Rightarrow (10.1)^2$$

$$= (10+0.1)^2$$

= Common

So, Batche koyda

$$= \left( \frac{10+0.1}{10} \right)^2$$

$$= 10^2 \left( 1 + \frac{0.1}{10} \right)^2$$

$$= 10^2 \left( 1 + 2 \frac{0.1}{10} \right)$$

$$= 10^2 (1+0.2)$$

$$= 10^2 (1.2)$$

$$= 100 (1.2)$$

$$= \underline{\underline{102}} \text{ Ans}$$

$$\Rightarrow (5+0.0003)^3$$

$$= 5^3 \left( 1 + \frac{0.0003 \times 3}{5} \right)$$

$$= 125 \left( 1 + \frac{0.0009}{5} \right)$$

$$= 125 \left( \frac{5.0009}{5} \right)$$

$$= 25 \left( \frac{8}{500.09} \right)$$

$$= \frac{500.09}{4}$$

$$= \frac{500.09}{4} + 0.1$$

$$= \underline{\underline{125.09}}$$

$$(0.1 \times 1.0 + 0.1)$$

$$\text{remain}$$

$$\left( \frac{1.0+1}{1} \right)^{0.1} =$$

$$(1.1 \times \frac{100.0}{20} + 1)^{0.1} =$$

$$\star (a+x)^n = a^n \left[ 1 + \frac{nx}{a} \right]$$

$$\star (a+x)^n = (a+nx)$$

$$10^2 \left( 1 + 2 \frac{0.1}{10} \right)$$

$$10^2 \left( 1 + \frac{0.1}{5} \right) \quad \begin{matrix} \text{Double one point} \\ \underline{\underline{0.02}} \end{matrix}$$

$$\Rightarrow (1+x)^3 = 1+3x$$

$$\Rightarrow g_n = g_0 \left( 1 + \frac{h}{R} \right)^{-2}$$

$$= g_0 \left( 1 - \frac{2h}{R} \right)$$

$$= g_0 \left( \frac{R-2h}{R} \right) \rightarrow X$$

$$\Rightarrow m = \frac{m_0}{\sqrt{1-\frac{v^2}{c^2}}} \cdot \left\{ \sqrt{x} = x^{\frac{1}{2}} \right\}$$

$$\approx m = \frac{m_0}{\left( 1 - \frac{v^2}{c^2} \right)^{\frac{1}{2}}} \quad \begin{matrix} (x+t) = (x+t) \\ (x-t) \end{matrix}$$

$$= m = m_0 \left( 1 - \frac{v^2}{c^2} \right)^{-\frac{1}{2}}$$

$$= m = m_0 \left( \frac{1+v^2}{2c^2} \right) \rightarrow X \quad t > x$$

$$t+t = \left( \frac{1}{\sqrt{1-v^2}} + 1 \right) = (1.0+1) = (1.0+1)$$

$$t-t = \frac{1}{\sqrt{1-v^2}} + 1 = (2.0.0+1) = (2.0.0+1)$$

$$200.0 = \frac{1}{\sqrt{1-v^2}} + 1 = \frac{1}{\sqrt{1-0.02}} + 1 = \frac{1}{\sqrt{0.9996}} + 1 = \frac{1}{0.9998} + 1 = 1.0002 + 1 = 2.0002$$

#L3

$$x = (100000)^{\frac{1}{5}}$$

$$\Rightarrow (100000+1)^{\frac{1}{5}}$$

$$= 100000^{\frac{1}{5}} \left( 1 + \frac{1}{5} \times \frac{1}{100000} \right)$$

$$= 10^5 \times \frac{1}{5} \left( 1 + \frac{1}{500000} \right)$$

$$= 10 \left( 1 + \frac{1}{5 \times 10^5} \right) \left[ \frac{1}{5 \times 10^4} \right] \text{Very small}$$

$$= 10 \left( 1 + \frac{0.2}{105} \right) = 10 \left( 1 + \frac{0.2}{100000} \right)$$

$$= 10 \left( 1 + 0.2 \times 10^{-5} \right)$$

$$= 10 \left( 1 + 0.000002 \right)$$

$$= 10(1.000002)$$

$$= 10.000002$$

$$\Rightarrow \sqrt{y} = (y)^{\frac{1}{2}}$$

$$\Rightarrow \sqrt{0.98} = (0.98)^{\frac{1}{2}} = (1 - 0.02)^{\frac{1}{2}} = 1 - \frac{0.02}{2} = \frac{1 - \frac{2}{100}}{\sqrt{1 - \frac{2}{100}}} = \frac{99}{100} = 0.99$$

$$\Rightarrow m = \frac{m^o}{\sqrt{1 - \frac{v^2}{c^2}}} \Rightarrow m = m^o \left( \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \right)$$

$$\Rightarrow \frac{m^o}{(1 - \frac{v^2}{c^2})} \Rightarrow m^o \left( \frac{1 - \frac{v^2}{c^2}}{1 - \frac{v^2}{c^2}} \right)^{-\frac{1}{2}} \Rightarrow m^o = \frac{1 + \frac{v^2}{c^2}}{2c^2}$$

$$\Rightarrow m^o = 20 \left( \frac{1 + \frac{v^2}{c^2}}{2 \times \frac{1}{2} \times 10^8 \times \frac{1}{2} \times 10^8} \right)$$

$$\Rightarrow m^o = 20 \left( 1 + \frac{1}{200} \right)$$

$$\Rightarrow m^o = 20 + \frac{1}{200} \Rightarrow m^o = \frac{1}{10} + 20 \Rightarrow 20.1$$

$$\Rightarrow E = K \left[ \left( 1 + \frac{\Delta \theta}{\theta_0} \right)^4 - 1 \right]$$

$$= K \left[ \left( 1 + \frac{4\Delta \theta}{\theta_0} - 1 \right) \right]$$

$$= K \left[ \frac{4\Delta \theta}{\theta_0} \right]$$

# Squares &amp; Cube &amp; Roots.

$$\Rightarrow (65)^2 = \frac{42}{6} \frac{25}{7} \Rightarrow (75)^2 = \frac{56}{7} \frac{25}{8}$$

$$\Rightarrow (105)^2 = \frac{11025}{10} \frac{11}{11}$$

$$\Rightarrow (97)^2 = \frac{94}{10} \frac{99}{9} \quad \left. \begin{array}{l} \text{Square} \\ 99-90 \text{ or } 101-109 \end{array} \right\}$$

$$\bullet 100-3-3 \quad \left. \begin{array}{l} \text{Square} \\ 90-81 \end{array} \right\}$$

$$\left. \begin{array}{l} \text{Valid for } 90 \text{ to } 110 \\ q.c. \end{array} \right\}$$

$$\Rightarrow \sqrt{0.98} = \sqrt{\frac{98}{100}} = \frac{0.98}{10} = 0.98 \text{ Ans}$$

$$\begin{aligned} (42)^2 &= \frac{17}{5} \frac{64}{8} \\ \Rightarrow 50-B &= \frac{17}{5} \frac{64}{8} \\ \Rightarrow 2S-B &= \frac{17}{5} \frac{64}{8} \end{aligned}$$

$$\left. \begin{array}{l} \frac{6}{365} \pm q = \frac{6}{5} \pm \frac{6}{8} \\ \frac{6}{365} \end{array} \right\}$$

## # Square root

$$\Rightarrow ( )^{\frac{1}{2}} = \sqrt{ }$$

$$\bullet \sqrt{125} = \sqrt{5 \times 5 \times 5} = \underline{\underline{5\sqrt{5}}}$$

$$\bullet \sqrt{1} = 1$$

$$\cdot \sqrt{2} = 1.414$$

$$\sqrt{3} = 1.732$$

$$\sqrt{5} = 2.236$$

$$\therefore \sqrt{18} = 3.16 \approx \pi$$

$$\cdot (\pi)^2 = 1$$

100 - 1

Learn

#Cube

$$\left( \frac{1}{4} \right)^{\frac{1}{3}} = \sqrt[3]{\frac{1}{4}}$$

$$3\sqrt{250} = \sqrt[3]{2 \times 5 \times 5 \times 5}$$

$$= \underline{\underline{5}} \sqrt[3]{2}$$

# Surds  $\rightarrow$  powers (Grandal!)

$$\Rightarrow x^{\frac{5}{6}} = \left(x^5\right)^{\frac{1}{6}} = \sqrt[6]{x \times x \times x \times x} = \underbrace{\left(x^6\right)^{\frac{1}{6}}}_{\text{cancel } x^6} = \left(\sqrt[6]{x}\right)^5$$

$$Ex \frac{8^{\frac{2}{3}}}{8^{\frac{1}{3}}} = (8^2)^{\frac{1}{3}} =$$

\* Puppy point - 3

$$\bullet \text{Binomial approximation} = (1+x)^n = (1+nx)$$

$$(a \pm x)^n = a^n \left(1 \pm \frac{nx}{a}\right) \quad \star$$

$$\begin{aligned} \bullet \text{ Square Root} &= \bullet \sqrt{2} = 1.414 \\ &\quad - \sqrt{3} = 2.236 \end{aligned} \quad \left| \quad \begin{aligned} \bullet \sqrt{3} &= 1.732 \\ \sqrt{10} &\approx \pi = 3.1 \end{aligned} \right.$$

$$\bullet \text{Cube Root} = \bullet \sqrt[3]{8} = \sqrt[3]{2 \times 2 \times 2} = 2$$

$$\text{***} \rightarrow 3\sqrt{p^3 \pm e} = p \pm \frac{e}{3p^2}$$

\* PUPPY \*

$$*\underline{\text{PUPPY}} \Rightarrow \sqrt{29} = \sqrt{25+4}$$

$$= 5 + \frac{4^2}{2 \times 5} = 5 + \frac{2}{5} = 5 + 0.4 \approx 5.4$$

$$\Rightarrow \sqrt{23} = \sqrt{25-2}$$

$$= 5 - \frac{2}{2 \times 5} = 5 - \frac{1}{5} = \frac{24}{5} = \underline{\underline{4.8}}$$

$$\Rightarrow \text{close} = \boxed{n} \pm \frac{\boxed{z}}{2n} \rightarrow \text{what add "+" or subtract "-"}$$

$$\Rightarrow \sqrt{12} = \sqrt{4 \times 3} = 2\sqrt{3} = 2 \times 1.732$$

$$= \underline{\underline{3.464}} \text{ Am}$$

$$\Rightarrow \sqrt[3]{127} = \boxed{125 + 2}$$

$\Rightarrow \sqrt{1 - x^2}$

## #L4

# Logarithms (Log)

$$\Rightarrow \text{Power}^0 = 1$$

$$\Rightarrow \text{Power}^1 = \underline{\text{Same}}$$

$$\Rightarrow \underline{2^3}^4 \quad (\text{super script})$$

$$\Rightarrow \underline{2^3}^4 \quad (\text{subscript})$$

$$\Rightarrow \log_b a = \log \text{of a base } b$$

$\Rightarrow$  Mathematical Function:

$$\cdot \log_2 512 = 9$$

$$\text{So, } 2^9 = 512$$

$$x = 9$$

$$\text{So, } \log_2 512 = 9$$

$\Rightarrow$  Base ki power me Kya  
Ki 512 aa jaye o.

$$\begin{aligned} &\Rightarrow \log 1 = 0 \\ &\Rightarrow \log 2 = 0.3 \\ &\Rightarrow \log 3 = 0.48 \\ &\Rightarrow \log 4 = 0.6 \\ &\Rightarrow \log 5 = 0.7 \\ &\Rightarrow \log 6 = 0.78 \\ &\Rightarrow \log 7 = 0.84 \\ &\Rightarrow \log 8 = 0.9 \\ &\Rightarrow \log 9 = 0.96 \\ &\Rightarrow \log 10 = 1 \end{aligned}$$

$$\begin{aligned} 2^0 &= 1 \\ 2^1 &= 2 \\ 2^2 &= 4 \\ 2^3 &= 8 \\ 2^4 &= 16 \\ 2^5 &= 32 \\ 2^6 &= 64 \\ 2^7 &= 128 \\ 2^8 &= 256 \\ 2^9 &= 512 \\ 2^{10} &= 1024 \end{aligned}$$

$$\begin{aligned} 2^4 &= 16 \\ 3^4 &= 81 \\ 4^4 &= 256 \\ 5^4 &= 625 \end{aligned}$$

$$\left\{ \begin{array}{l} 1000 = 10^3 \\ \hline \end{array} \right.$$

$$\Rightarrow \log_{10} 1 = 0 \quad 1^0 = 1 \Rightarrow \underline{1^0 = 1}$$

$$\Rightarrow \log_2 x = 1 \quad x^0 = x \Rightarrow x^1 = x$$

$$\Rightarrow \text{if no base So, it} = 10$$

$$\cdot \log 5 = \underline{\log_{10} 5}$$

## # Rule 1

$$\star \Rightarrow [\log(ab) = \log a + \log b]$$

$$\log 4 = \log(2 \times 2) = \log 2 + \log 2 = 0.3 + 0.3 = \boxed{0.6}$$

$$\star \Rightarrow [\log\left(\frac{a}{b}\right) = \log a - \log b]$$

$$\log\left(\frac{1}{4}\right) = \log 1 - \log 4 \rightarrow \star = 0 - 0.6 = \boxed{-0.6} \Rightarrow \log\left(\frac{1}{a}\right) = -\log a$$

## # Decimal log

$$\Rightarrow \log(2.5) = \log\left(\frac{25}{10}\right) = \log\left(\frac{5}{2}\right) = \log 5 - \log 2 = 0.7 - 0.3 = 0.4$$

$$\star \Rightarrow \log a^x = x \log a$$

$$\text{Ex. } \log 1024 = \log 2^{10} = 10 \log 2$$

$$= 10(0.3) = \boxed{3}$$

$$\Rightarrow \log(5 \times 10^7) = \log 5 + \log 10^7$$

$$= 0.7 + 7$$

$$= \boxed{7.7}$$

## # Denominator

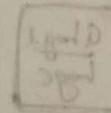
$$\Rightarrow \log_3 7 = \frac{\log 7}{\log 3} = \frac{0.84}{0.48} = \frac{84}{48} = \frac{7}{4} = \boxed{\frac{7}{4}}$$

[No a-b work]

$$\Rightarrow \log(1.25 \times 10^{-5}) = \log \frac{5}{4} + \log 10^{-5} = 0.1 - 5$$

$$= \boxed{-4.9}$$

Not in Syllabus



$$\log D = \frac{1}{4} \log 10 = \frac{1}{4} \times 1 = \frac{1}{4}$$

## # Puppy point 4

- $\Rightarrow 2 \text{ Power, } \log(1-10)$
  - $\Rightarrow \log(ab) = \log a + \log b$
  - $\Rightarrow \log\left(\frac{a}{b}\right) = \log a - \log b$
  - $\Rightarrow \log\left(\frac{1}{a}\right) = -\log a$
  - $\Rightarrow \log a^x = x \log a$
  - $\Rightarrow \log_{10} x = x$
  - $\Rightarrow \log_b a = \frac{\log a}{\log b}$  [No Substitution]
- Except 10

\* Prime number  $\Rightarrow \log 17$  So,  $\log 16 = 1.20$  ] 1-23  
 $\log 18 = 1.26$

$$\Rightarrow \log \sqrt{27} \Rightarrow \log(27)^{\frac{1}{2}}$$

$$\Rightarrow \log 3^{3 \times \frac{1}{2}}$$

$$\Rightarrow \frac{3}{2} \log 3$$

$$\Rightarrow \frac{3}{2} \times 0.48 \Rightarrow 0.72$$

## # h → 5

$$\Rightarrow \log_3 2 \log_2 3$$

$$\Rightarrow \frac{\log 2}{\log 3} \times \frac{\log 3}{\log 2} = 1$$

$$\Rightarrow \frac{0.31}{0.48} \times \frac{1.61}{1}$$

$$\Rightarrow 1$$

$$\Rightarrow \log 2 \log 3$$

$$\Rightarrow 0.3 \times 0.48$$

$$\Rightarrow 0.144$$

$$\Rightarrow \log 3^2 \log 2^3$$

$$\Rightarrow 2 \log 3 \times \log 2$$

$$\Rightarrow 2(0.48) \times 3(0.3)$$

$$\Rightarrow 0.96 \times 0.9$$

$$\Rightarrow 0.864$$

$$\Rightarrow \log \frac{2}{3} \log \left(\frac{3}{2}\right)$$

$$\Rightarrow 0.18 \times 0.18$$

$$\Rightarrow 0.0324$$

## # Antilog

$$\Rightarrow \log x = 0.3 \quad \text{Find } x = 2$$

$$\Rightarrow \log x = 0.7 \quad \text{Find } x = 5$$

$$\Rightarrow \log_3 x = 4 \quad \text{Find } x = 3^4 = x \Rightarrow 81$$

$$\Rightarrow \log_c x = y$$

$$c^y = x$$

## # Puppy point 5

$$\Rightarrow \log_{10} x = y$$

$$\Rightarrow \log_c a = \frac{\log a}{\log c}$$

$$\Rightarrow \log_c x = y \Rightarrow c^y = x$$

$$\Rightarrow \ln x = \log_{10} x = 2.303$$

$$\Rightarrow \log_c x^a = a \log_c x = \frac{a \log x}{\log c}$$

## # Rule 4

$$\Rightarrow e = 2.72$$

Base = e } Natural log

\* Eq. = Natural log of 2

$$\Rightarrow \log_{10} 2 \text{ or } \ln 2$$

$$\ln = 2.303$$

$$\therefore \ln 10 = 2.303 \log_{10} 2 = 2.303$$

$$\Rightarrow \log_2 25^3 \Rightarrow 3 \log_2 25$$

$$\Rightarrow \frac{3 \log 25}{\log 2}$$

$$\left[ \text{draw} \right] \Rightarrow 3 \left( \frac{1.4}{0.3} \right)$$

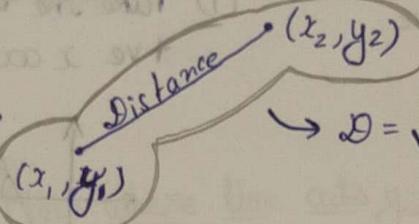
$$\Rightarrow 14$$

#L6

$$\Rightarrow \log_e X = \frac{\log X}{\log e} = \frac{\log x}{\log 2.72} = \frac{\log x}{0.303} = 2.303 \quad \boxed{m}$$

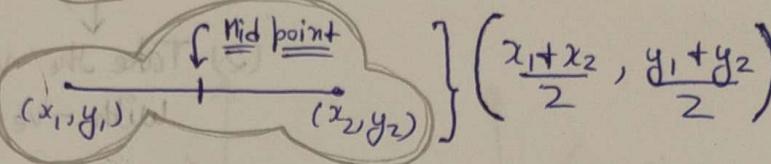
#Graphs

\* Distance formula

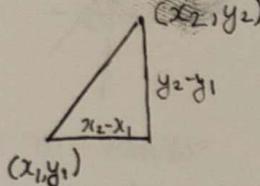


$$D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

\* Midpoint formula



$$\left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

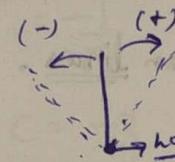


$$\Rightarrow H = \sqrt{p^2 + b^2}$$

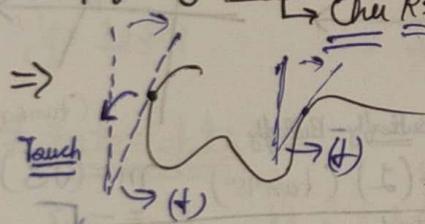
$$\Rightarrow D = \sqrt{(y_2 - y_1)^2 + (x_2 - x_1)^2}$$

# Slope (Dhalaoon) (m)

$$\Rightarrow \frac{-}{-} m=0 \quad | \quad m=\infty$$



↳ Slope find by tangent



Chu kii mere graph, ek point tangent tune mare!

\* Magnitude =  $|m|$  + and -

↳ Eg Magnitude of -10 is  $\frac{10}{-10}$ .

$$\Rightarrow \tan 30^\circ = \frac{1}{\sqrt{3}}$$

$$\Rightarrow \tan 45^\circ = 1$$

$$\Rightarrow \tan 60^\circ = \sqrt{3}$$

$$\Rightarrow \tan 37^\circ = \frac{3}{4}$$

$$\Rightarrow \tan 53^\circ = \frac{4}{3}$$

$$\Rightarrow \text{Slope} :- \tan \theta = \frac{y_2 - y_1}{x_2 - x_1} = \frac{y^2 - y_1}{x^2 - x_1}$$

$$\Rightarrow \text{Left angle} = -\theta$$

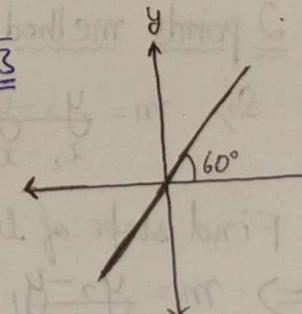


$$\begin{aligned} &\Rightarrow 180^\circ - 120^\circ \\ &= 60^\circ \quad \{ \text{from left} \} \\ &= -(\tan 60^\circ) \\ &= -\sqrt{3} \end{aligned}$$

$$\Rightarrow \text{Slope} = \tan 60^\circ = \sqrt{3}$$

$$\Rightarrow \text{Slope} = \sqrt{3}$$

$\Rightarrow (+) \Rightarrow \text{Angle} \uparrow \text{Slope} \uparrow$   
 $\Rightarrow (-) \Rightarrow \text{Angle} \uparrow \text{Slope} \downarrow$

# Puppy point #6  $D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ 

$$\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}$$

$$m=0$$

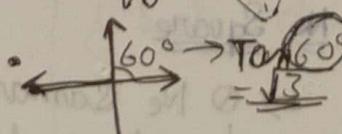
• Slope tangent that touch one point.

$$\Rightarrow \text{Slope} = \frac{y_2 - y_1}{x_2 - x_1}, \quad \left[ \tan \theta = \frac{\sin \theta}{\cos \theta} \right]$$

$$\cdot \tan 37^\circ = \frac{3}{4}$$

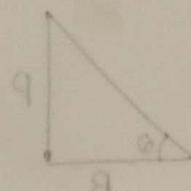
$$\begin{aligned} &\Rightarrow 180^\circ - x \\ &\Rightarrow 0 \end{aligned}$$

• Butterfly



$$m = \infty$$

↳ tan 60° But Negative (-).



#L7

$$\# \underline{y = mx + c}$$

$\Rightarrow$  Equation of straight line

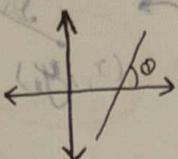
$$y = mx + c$$

$\downarrow$

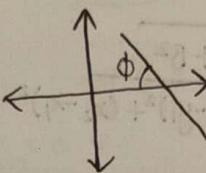
$m$  is slope

$$\left( \frac{\sin \phi}{\cos \phi}, \frac{\cos \phi}{\sin \phi} \right)$$

(1) Take the tan of angle made by line with +ve x axis. ( $m = \tan \phi$ )

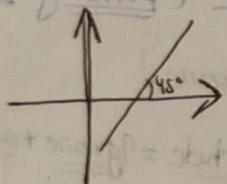


(2) Take the -ve of tan of angle made by line with -ve x axis. ( $m = -\tan \phi$ )

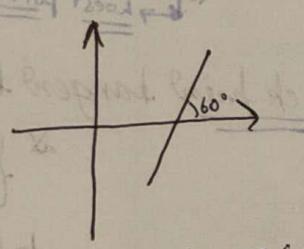


Q Find  $m$  (slope) for the given lines.

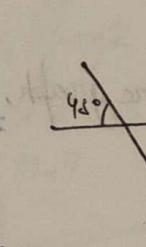
(bottom portion) will go to trigonometry



$$m = 1 (\tan 45^\circ)$$

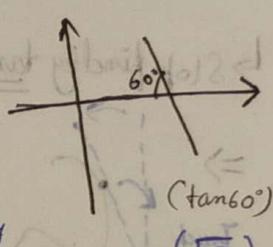


$$m = \sqrt{3} (\tan 60^\circ)$$



$$m = -(1) (\tan 45^\circ)$$

Butterfly - Butterfly



$$m = (\sqrt{3}) -$$

$$= -\sqrt{3}$$

③ 2 points method  $(x_2, y_2)$  and  $(x_1, y_1)$

$$\therefore m = \frac{y_2 - y_1}{x_2 - x_1}$$

Q. Find slope of line passing through  $(1, 2)$  &  $(5, 8)$

$$\Rightarrow m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{8 - 2}{5 - 1} = \frac{3}{2}$$

Q. Find slope of line passing through  $(0, 7)$  &  $(20, 67)$

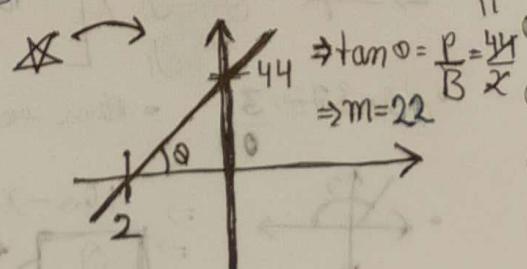
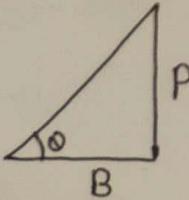
$$m = \frac{36}{20} = 3$$

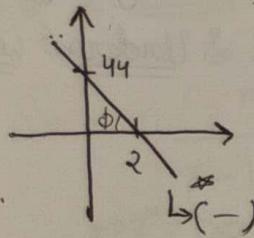
$\hookrightarrow$  No Square

$$m = \frac{36}{20} \Rightarrow m = \frac{9}{5}$$

$\Rightarrow$  Re Same P.

$\hookrightarrow$  Uske saat joint B.  $\Rightarrow$





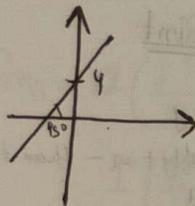
$$= \tan \theta = \frac{2}{2} X$$

So,  $\tan \theta = \frac{4}{2}$

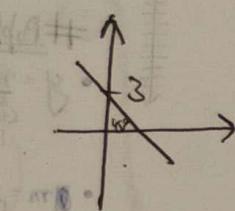
$$= \underline{\underline{-2}} \text{ Ans}$$

$$\Rightarrow y = mx + c$$

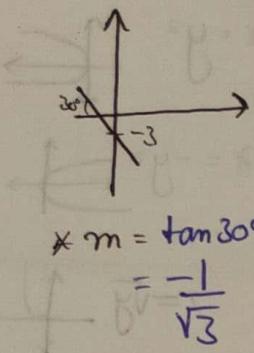
y-intercept: Place where line cuts y-axis



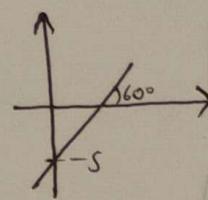
$$* m = \tan 45^\circ \\ = 1$$



$$* m = \tan 45^\circ \\ = -1$$



$$* m = \tan 30^\circ \\ = \frac{1}{\sqrt{3}}$$



$$* m = \tan 60^\circ \\ = \sqrt{3}$$

$$* c = 4$$

$$* c = 3$$

$$* c = -3$$

$$* c = -5$$

$$\Rightarrow y = mx + c$$

$$\Rightarrow y = 1x + 4$$

$$\Rightarrow y = mx + c \Rightarrow y = mx + c$$

$$\Rightarrow y = -1x + 3 \Rightarrow y = -\frac{x}{\sqrt{3}} - 3$$

$$\Rightarrow y = mx + c$$

$$\Rightarrow \sqrt{3}x - 5$$

# Intercepts:

y-intercept  $\rightarrow$  Jaha y axis ko katesa...

x-intercept  $\rightarrow$  Jaha x axis ko katesa...

$$\Rightarrow y = mx + c$$

$$* \boxed{y \text{ intercept} = c}$$

$$\Rightarrow x \rightarrow \boxed{y = 0}$$

$$\bullet y = mx + c \\ 0 = mx + c$$

$$m = -\frac{c}{x}$$

$$\boxed{x \text{ intercept} = -\frac{c}{m}}$$

$$2. 2y = 3x - 6 \quad (\text{find } x \text{ and } y)$$

$$y = \frac{3x - 6}{2}$$

\* (for straight line)

$$y = \frac{-6}{2} \quad y = -3$$

$$x = \frac{-6}{3} = \frac{6}{2} = 3$$

$y = -3$
$x = 2$

Puppy

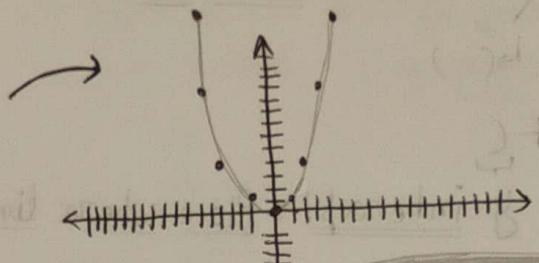
$$\begin{cases} x \text{ So, } y = 0 \Rightarrow x = 2 \\ y \text{ So, } x = 0 \Rightarrow y = -3 \end{cases}$$

# Parabola: Graph with equations like  $y = x^2$ ,  $y = -x^2$ ,  $x = y^2$ ,  $x = -y^2$ ,  $y = \sqrt{x}$   
 $x = \sqrt{y} \Rightarrow$  (Quadratic & Under root value eq)

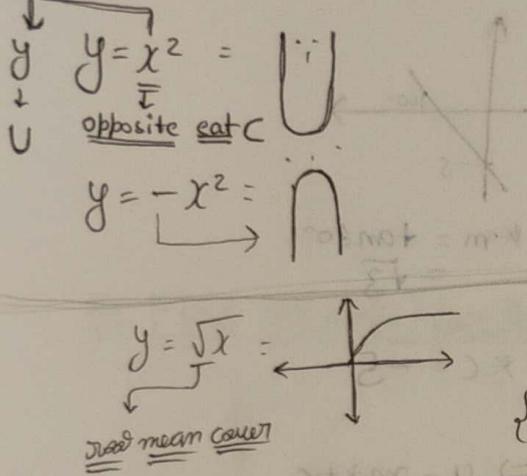
• Draw  $y = x^2$

$x$	0	1	2	3	4	-1
$y$	0	1	4	9	16	1

...



## # Quadratic equation



$$x = y^2$$

$$x = -y^2$$

$$r = \sqrt{y}$$

{ Root never negative }

### # Puppy point

- $y = mx + c$  slope  $\rightarrow$   $y$  Butterfly + or - than tan  $\theta$
- $m = \frac{y_2 - y_1}{x_2 - x_1}$
- for  $x$  and  $y$   $\{x = 0\}, \{y = 0\}$
- Parabola  $\rightarrow$  opposite and corner  $\rightarrow$  real  $\rightarrow$  cover only

## # L8 $\Rightarrow$ G.P [Geometric Progression]

$\Rightarrow 1, 5, 25, 125, 625 \dots$  G.P [Geometric Progression]

$\Rightarrow 1, 10, 11, 100, 101 \dots$  (only 1's & 0's)

$$\left\{ \begin{array}{l} \Rightarrow a = \text{first term} \\ \Rightarrow r = \text{common ratio} \end{array} \right.$$

$$\Rightarrow 1, \frac{1}{2}, \frac{1}{4}, \frac{1}{8} \dots$$

$$\left[ \begin{array}{l} a = 1 \\ r = \frac{1}{2} \end{array} \right]$$

$$\Rightarrow 1, -\frac{1}{2}, \frac{1}{4}, -\frac{1}{8} \dots$$

$$\left[ \begin{array}{l} a = 1 \\ r = -\frac{1}{2} \end{array} \right]$$

$$\Rightarrow \frac{GM}{r^2}, \frac{GM}{4r^2}, \frac{GM}{16r^2} \dots$$

$$a = \frac{GM}{r^2} \quad r = \frac{1}{4}$$

$\Rightarrow$  General formate of G.P.

$$\Rightarrow a, ar, ar^2, ar^3, ar^4 \dots$$

$$\left\{ \frac{ar^{n-1}}{r} \right\}$$

$$\Sigma = B$$

$$\Sigma = x$$

$$\Sigma = \frac{B}{x}$$

$\Rightarrow S_n$  of  $n^{\text{th}}$  terms  $\Rightarrow a + ar + ar^2 + ar^3 \dots$

$$\Rightarrow S_n = a \frac{(r^n - 1)}{r - 1} = a \frac{(1 - r^n)}{(1 - r)}$$

$$* \underline{a}^\infty = \begin{cases} \rightarrow r = \infty [a > 1] \\ \rightarrow \frac{1}{r} = 0 [a < 1] \\ \rightarrow [a = 1] = \text{Not Define} \end{cases} \quad a = r (\text{common difference})$$

Q. Find value of  $\Rightarrow 1 + 2 + 4 + 8 + 16 + 32 + 64 + 128 = ?$

$$\underline{a=1} \quad \underline{r=2}$$

$$S_{n_8} = a \left( \frac{r^n - 1}{r - 1} \right)$$

$$= 1 \left( \frac{2^8 - 1}{2 - 1} \right)$$

$$= 1 \left( \frac{256 - 1}{1} \right)$$

$$\Rightarrow \underline{\underline{255}}$$

$\Rightarrow 1 + 3 + 9 + 27 + 81 + \dots 10 \text{ terms} =$

$$\underline{a=1} \quad \underline{r=3}$$

$$S_{n_{10}} = 1 \left( \frac{3^n - 1}{3 - 1} \right)$$

$$ar^9 \Rightarrow 1 \times 3^9$$

$$\underline{10^{\text{th}}} \Rightarrow \underline{\underline{3^9}}$$

$$\Rightarrow \underline{\underline{19,683}}$$

$$= 1 \left( \frac{59049 - 1}{2} \right)$$

$$= \frac{59048}{2} = \underline{\underline{29524}}$$

$\Rightarrow 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} \dots 10 \text{ terms}$

$$\underline{a=1} \quad \underline{r=\frac{1}{2}} = 0$$

$$S_{n_{10}} = 1 \left( \frac{1}{2} - 1 \right) \times \Rightarrow a \left( \frac{1 - r^n}{1 - r} \right) \rightarrow \frac{r < 1}{(1 - r)^{n+1}} \times \frac{1}{2}$$

$$\Rightarrow 1 \left( \frac{1 - \left(\frac{1}{2}\right)^{10}}{\frac{1}{2} - 1} \right) \Rightarrow 1 \left( \frac{1 - \frac{1}{1024}}{\frac{1}{2}} \right)$$

$$= \frac{1023}{1024} \times \frac{2}{1} = \underline{\underline{\frac{1023}{512}}}$$

$\Rightarrow 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} \dots \infty$

$$\bullet a = 1 \quad \bullet r = \frac{1}{2} \quad \bullet n^{\text{th}} = \infty$$

$$\Rightarrow 1 \left( \frac{1 - \left(\frac{1}{2}\right)^{\infty}}{1 - \frac{1}{2}} \right) \Rightarrow 1 \left( \frac{1 - 0}{\frac{1}{2}} \right) \Rightarrow \frac{1}{\frac{1}{2}} \Rightarrow \underline{\underline{2}}$$

$$So, (1 - r)^{\infty} So, = \left( \frac{1 - r}{1 - r} \right) \text{ Formula}$$

## #L9 G.P Then A.P (Arithmetic Progression)

$$\Rightarrow 2, 5, 8, 11, 14, \dots$$

$$a, d = a^2 - a^1$$

$\downarrow$   $d = 3$  → Common difference

First term

$$\Rightarrow a, a+d, a+2d, \dots \left\{ \begin{array}{l} a + (n-1)d = a_n = l \xrightarrow{\text{Last term}} \\ \frac{H}{9} \leftarrow 3000 \\ \frac{H}{8} \leftarrow 300 \\ \frac{H}{7} \leftarrow 100 \\ \frac{H}{6} \leftarrow 50 \\ \frac{H}{5} \leftarrow 20 \\ \frac{H}{4} \leftarrow 10 \\ \frac{H}{3} \leftarrow 5 \\ \frac{H}{2} \leftarrow 2 \\ \frac{H}{1} \leftarrow 1 \end{array} \right. \right\}$$

$$\sum n = a_1 + a_2 + a_3 + a_4 + \dots = a + a+d + a+2d$$

$$= (a+a+a+\dots+n) + (d+2d+3d+\dots+(n-1)d)$$

$$= n a + d [1+2+\dots+(n-1)] \quad \text{--- (i)}$$

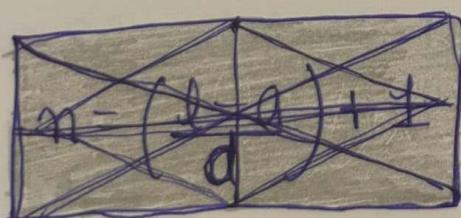
$$\text{So, we know that } \Rightarrow 1+2+3+\dots+(n-1)+n = n \frac{(n+1)}{2}$$

$$1+2+3+\dots+(n-1) = n \frac{(n+1)}{2} - n = \frac{n^2 - n}{2}$$

From eq(i) and (ii)

$$\Rightarrow \left[ \sum n = \frac{n}{2} \{ 2a + (n-1)d \} \right]$$

$$\left[ \sum n = \frac{n}{2} \{ a + l \} \right]$$



$$\Rightarrow \sum n = \frac{n}{2} \{ 2a + (n-1)d \}$$

$$= \frac{n}{2} \{ 2 + (n-1)d \}$$

$$= \frac{n}{2} \{ 2 + (n-1)n \}$$

$$= \frac{n(n+1)}{2}$$

$$\left[ \Rightarrow \text{Sum of number } n \cdot 1+2+3+4+\dots+n = n \frac{(n+1)}{2} \right]$$

$$\left[ \Rightarrow \text{Sum of } n \text{ odd numbers} \cdot 1+3+5+\dots+n = n^2 \right]$$

$$1+3=4=2^2$$

$$1+3+5=9=3^2$$

$$\text{So, } 1+3+5+\dots+n = (n)^2$$

$$\sqrt{B+5x} = N, x=4, B=9$$

$$SV = \frac{B}{H} = \frac{9}{4} = 2.25$$

$$SV = \frac{Bx}{H} = \frac{9 \times 4}{4} = 6$$

$$SV = \frac{(Bx)}{H} = \frac{9 \times 4}{4} = 6$$

# # Neet Level Maths

$\Rightarrow$  Trigonometry

$$\Rightarrow \sin \Rightarrow \frac{P}{H}$$

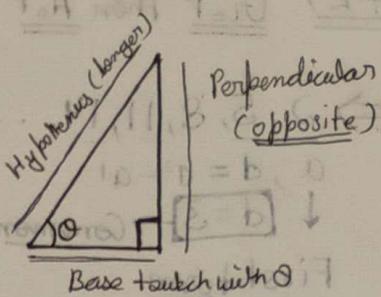
$$\cos = \frac{H}{P}$$

$$\Rightarrow \cos \Rightarrow \frac{B}{H}$$

$$\sec = \frac{H}{B}$$

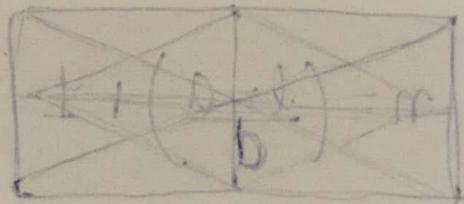
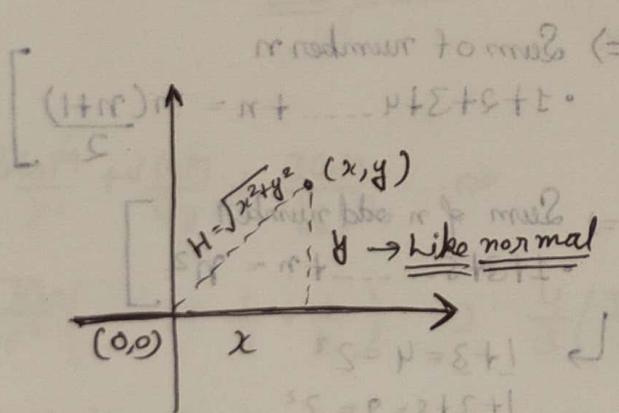
$$\Rightarrow \tan \Rightarrow \frac{P}{B}$$

$$\cot = \frac{B}{P}$$



(ii)

	0°	30°	45°	60°	90°	120°	135°	150°	180°	37°	53°
sin	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1						
cos	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0						
tan	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	N.D.						



## # Trigo in 4 quadrants

$$\Rightarrow p=y, B=x, H=\sqrt{x^2+y^2}$$

$$\bullet \sin = \frac{P}{H} = \frac{y}{H}^+ = +ve$$

$$\bullet \cos = \frac{B}{H} = \frac{x}{H}^+ = +ve$$

$$\bullet \tan = \frac{P}{B} = \frac{y}{x}^+ = +ve$$

II

$$\bullet \sin = \frac{P}{H} = \frac{y}{H}^+ = +ve$$

$$\bullet \cos = \frac{B}{H} = \frac{x}{H}^- = -ve$$

$$\bullet \tan = \frac{P}{B} = \frac{y}{x}^- = -ve$$

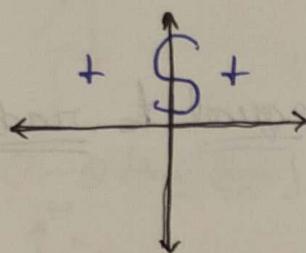
III

- $\sin \theta = \frac{y}{h} = \frac{y}{h} = + = +ve$
- $\cos \theta = \frac{x}{h} = \frac{x}{h} = + = -ve$
- $\tan \theta = \frac{y}{x} = \frac{y}{x} = + = +ve$

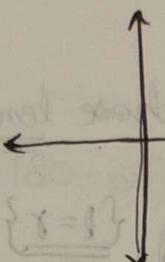
IV

- $\sin \theta = \frac{y}{h} = \frac{y}{h} = - = -ve$
- $\cos \theta = \frac{x}{h} = \frac{x}{h} = + = +ve$
- $\tan \theta = \frac{y}{x} = \frac{y}{x} = + = -ve$

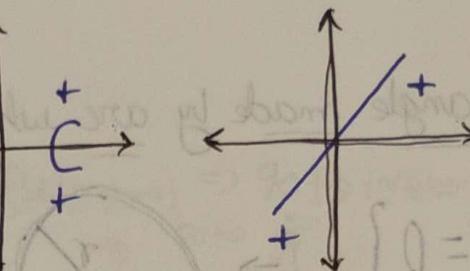
sin



cos



tan



\*

$$\Rightarrow \sin \theta = \frac{y}{\sqrt{x^2+y^2}} = \frac{y}{h}$$

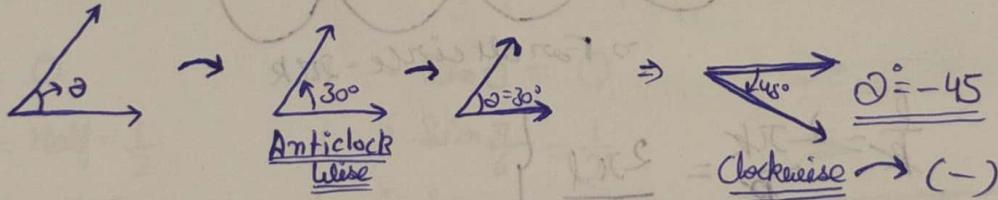
$$\Rightarrow \cos \theta = \frac{x}{\sqrt{x^2+y^2}} = \frac{x}{h}$$

$$\Rightarrow \tan \theta = \frac{y}{x} = \frac{y}{x}$$

or

A	S	T	C	=
opp (all)	Sub (sin)	tan (tan)	chalc (cos)	=

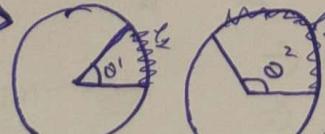
# L 10 Angle :-



# Bye - Bye Degree :-

$\Rightarrow$  S.I unit of Angle = Radian

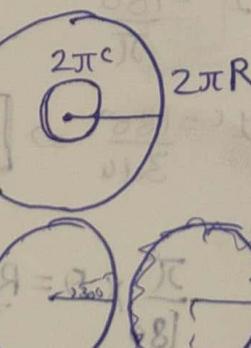
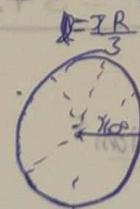
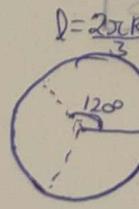
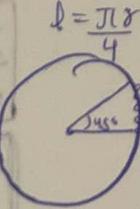
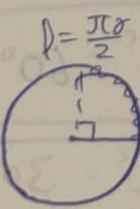
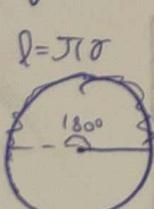
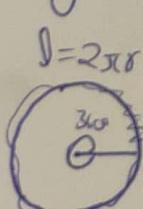
$\Rightarrow \{ \text{Angle} \propto \text{Length of Arc} \}$



$$\Rightarrow \theta^2 > \theta' \\ \Rightarrow l^2 > l'$$

# Circumference of a circle  $\{2\pi r\}$

Angle of full circle is  $2\pi$  radians  $\Rightarrow 2\pi^c$



$$\Rightarrow [\theta^c = \frac{l}{R}]$$

$$\theta^c = \frac{\pi R}{6}$$

$$\theta^c = \frac{3}{4} \cdot 2\pi R = \frac{3}{2} \pi R$$

\* For Radian, Radius  $R$  to make

$$\Rightarrow 360^\circ = 2\pi R = 2\pi^c$$

$$\Rightarrow 180^\circ = \frac{\pi R}{2} = \frac{\pi^c}{2}$$

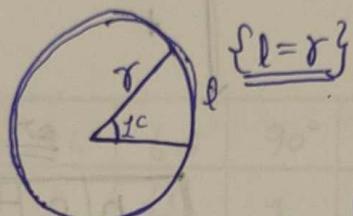
$$\Rightarrow 270^\circ = \frac{3\pi R}{4} = \frac{3\pi^c}{4}$$

$$\Rightarrow \left\{ \begin{array}{l} \frac{2\pi R}{x \rightarrow 90 \text{ Se divide}} \\ \boxed{\text{Excess} = 360^\circ} \end{array} \right.$$

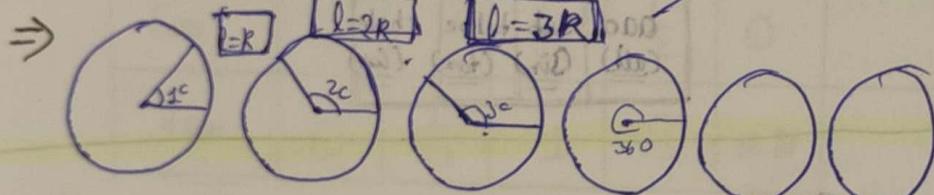
## # 1 Radian

$\Rightarrow 1^\circ$  is the angle made by arc whose length is equal to radius.

$$* 1^\circ = \{R = l\}$$



$$\{R = l\} = 0^\circ$$



For all circle  $= 2\pi R$

$$\left\{ 2 = \frac{l}{R} = \frac{2\pi R}{R} = \frac{2\pi l}{R} \right\}$$

$$\Rightarrow 360 = 2\pi^c$$

$$\Rightarrow 2\pi^c = 360$$

$$\Rightarrow \underline{\underline{\pi^c = 180^\circ}}$$

$$\Rightarrow \underline{\underline{\pi^c = 180^\circ}}$$

$$\Rightarrow 1^\circ = \frac{180^\circ}{\pi}$$

$$\Rightarrow 1^\circ = \frac{180^\circ}{3.14} \Rightarrow \boxed{1^\circ = 57.3^\circ}$$

$$\left[ \frac{\pi}{180} \times D = \underline{\underline{\text{Radian}}} \right]$$

$$\boxed{\pi^c = 180^\circ}$$

$$\boxed{\frac{\pi^c}{2} = 90^\circ}$$

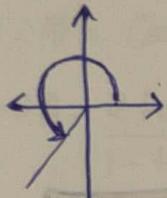
$$\boxed{\frac{\pi^c}{4} = 45^\circ}$$

$$\boxed{\frac{\pi^c}{3} = 60^\circ}$$

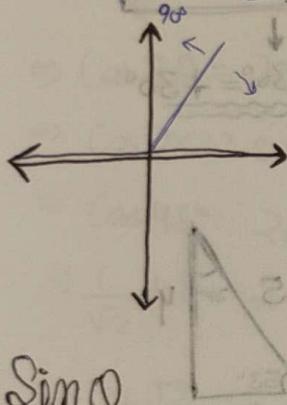
$$\boxed{\frac{\pi^c}{6} = 30^\circ}$$

## # Quadrants

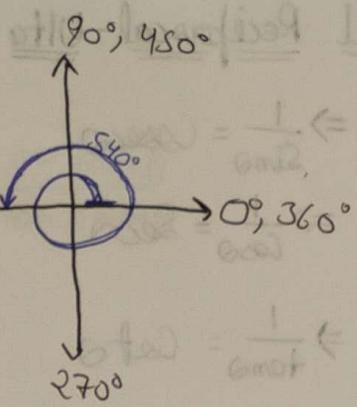
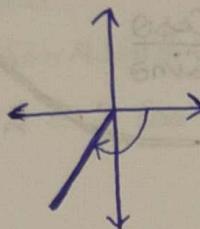
$$\theta = 247^\circ \\ = 180^\circ + 67^\circ$$



$$\Rightarrow 90^\circ - \theta \{ 90^\circ \text{ se chotta} \}$$

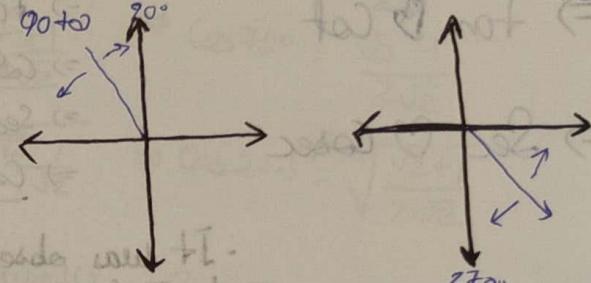
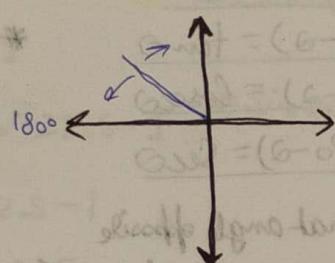


$$\theta = -120^\circ$$



$$= 180^\circ - \theta \{ 180^\circ \text{ se chotta} \}$$

$$\Rightarrow 180^\circ - \theta \{ 180^\circ \text{ se chotta} \} \Rightarrow 90^\circ + \theta \{ 90^\circ \text{ se barao} \} \Rightarrow 270^\circ + \theta \{ 270^\circ \text{ se barao} \}$$



## # Sin θ

- $\sin 0^\circ = 0$
- $\sin 30^\circ = \text{Half} = \frac{1}{2}$
- $\sin 45^\circ = \text{Half } \sqrt{2} = \frac{1}{\sqrt{2}}$
- $\sin 60^\circ = \text{Half } \sqrt{3} = \frac{\sqrt{3}}{2}$
- $\sin 90^\circ = 1$

- $\sin 0^\circ = 0$
- $\sin \frac{\pi}{6} = \frac{1}{2}$
- $\sin \frac{\pi}{4} = \frac{1}{\sqrt{2}}$
- $\sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$
- $\sin \frac{\pi}{2} = 1$

→ For positive or negative see ASTC

$$\Rightarrow 90^\circ \& 270^\circ \Rightarrow \underline{\text{opposite}} \quad \underline{\sin \rightarrow \cos}$$

$$\Rightarrow 180^\circ \& 360^\circ \Rightarrow \underline{\text{Same}} \quad \underline{\sin \rightarrow \sin}$$

• form a table So, Same

$$\Rightarrow \sin(60^\circ + 45^\circ) = ?$$

$$\Rightarrow \sin(90^\circ + 45^\circ) = ?$$

$$\Rightarrow \sin(90^\circ + 45^\circ) = +\cos 45^\circ$$

$$= \sin 45^\circ = \left[ \frac{1}{\sqrt{2}} \right]$$

$$(\frac{1}{2})(\frac{1}{\sqrt{2}}) - (\frac{\sqrt{3}}{2})\frac{1}{\sqrt{2}} = (\cos 45^\circ)(\sin 45^\circ) - (\sin 45^\circ)(\cos 45^\circ)$$

$$\boxed{\frac{1-\sqrt{3}}{2\sqrt{2}}} = \frac{1}{2\sqrt{2}} - \frac{\sqrt{3}}{2\sqrt{2}}$$

## # LII Reciprocal - Ultra

$$\Rightarrow \frac{1}{\sin \theta} = \operatorname{cosec} \theta$$

$$\Rightarrow \frac{1}{\cos \theta} = \sec \theta$$

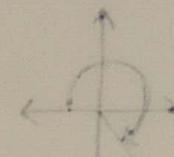
$$\Rightarrow \frac{1}{\tan \theta} = \cot \theta$$

$$\Rightarrow \tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\Rightarrow \cot \theta = \frac{\cos \theta}{\sin \theta}$$

$$\Rightarrow -\theta \Rightarrow$$

$$\Rightarrow \theta = -\theta^\circ$$



## # Complimentary angle

$$\Rightarrow \sin \theta \propto \cos$$

$$\Rightarrow \tan \theta \propto \cot$$

$$\Rightarrow \sec \theta \propto \cosec$$

$$\Rightarrow \sin(90 - \theta) = \cos \theta$$

$$\Rightarrow \cos(90 - \theta) = \sin \theta$$

$$\Rightarrow \tan(90 - \theta) = \cot \theta$$

$$\Rightarrow \cot(90 - \theta) = \tan \theta$$

$$\Rightarrow \sec(90 - \theta) = \cosec \theta$$

$$\Rightarrow \cosec(90 - \theta) = \sec \theta$$

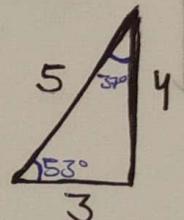
$$\boxed{\cos = +} \quad \boxed{\sec = +}$$

$$*\underline{\cos 30^\circ = +30^\circ}$$

- It was observe that angle opposite to 3 is  $37^\circ$  and angle opposite to 4 is  $53^\circ$ .

$$\left\{ \begin{array}{l} 3 \text{ opposite} = 37^\circ \\ 4 \text{ opposite} = 53^\circ \end{array} \right.$$

$$\left\{ \begin{array}{l} 4 \text{ opposite} = 53^\circ \end{array} \right.$$



$$\Rightarrow \sin 37^\circ = \frac{3}{5}$$

$$\Rightarrow \cos 37^\circ = \frac{4}{5}$$

$$\Rightarrow \tan 37^\circ = \frac{3}{4}$$

$$\Rightarrow \sin 53^\circ = \frac{4}{5}$$

$$\Rightarrow \cos 53^\circ = \frac{3}{5}$$

$$\Rightarrow \tan 53^\circ = \frac{4}{3}$$

$$\Rightarrow \sin^2 \theta + \cos^2 \theta = 1$$

$$\Rightarrow \sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\Rightarrow \cot^2 \theta - \cosec^2 \theta = 1$$

$$\Rightarrow \sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\Rightarrow \sec^2 \theta - \tan^2 \theta = 1$$

$$\Rightarrow \sin 2A = 2 \sin A \cos A$$

$$\therefore \sin 75^\circ = \sin(45^\circ + 30^\circ) = \sin 45^\circ \cos 30^\circ + \cos 45^\circ \sin 30^\circ$$

$$= \frac{1}{\sqrt{2}} \left( \frac{\sqrt{3}}{2} \right) - \left( \frac{1}{\sqrt{2}} \right) \left( \frac{1}{2} \right)$$

$$= \frac{\sqrt{3}}{2\sqrt{2}} - \frac{1}{2\sqrt{2}} \Rightarrow \boxed{\frac{\sqrt{3}-1}{2\sqrt{2}}}$$

$$\Rightarrow \cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\Rightarrow \tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B} \quad \Rightarrow \tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$\Rightarrow \cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\Rightarrow \cos(2A) = \cos^2 A - \sin^2 A = 2 \cos^2 A - 1 = 1 - 2 \sin^2 A$$

$$\Rightarrow \tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$

2.  $\cos 22.5^\circ$

$$\Rightarrow \sin 15^\circ = \frac{\sqrt{3}-1}{2\sqrt{2}} \Rightarrow \cos 15^\circ = \left[ \frac{\sqrt{3}+1}{2\sqrt{2}} \right]$$

$$\Rightarrow \cos 2A = 2 \cos^2 A - 1$$

$$\Rightarrow \sin 75^\circ = \frac{\sqrt{3}+1}{2\sqrt{2}} \Rightarrow \cos 75^\circ = \frac{\sqrt{3}-1}{2\sqrt{2}}$$

$$\Rightarrow \cos 45^\circ = 2 \cos^2 22.5^\circ - 1$$

$$\Rightarrow \sin 22.5^\circ = \frac{\sqrt{2}-1}{2\sqrt{2}} \Rightarrow \cos 22.5^\circ = \frac{\sqrt{2}+1}{2\sqrt{2}}$$

$$\Rightarrow \frac{1}{\sqrt{2}} + 1 = 2 \cos^2 22.5^\circ$$

$$\Rightarrow \tan 15^\circ = 2 - \sqrt{3}$$

$$\Rightarrow \frac{1+\sqrt{2}}{\sqrt{2}} = 2 \cos^2 22.5^\circ$$

$$\Rightarrow \tan 75^\circ = 2 + \sqrt{3}$$

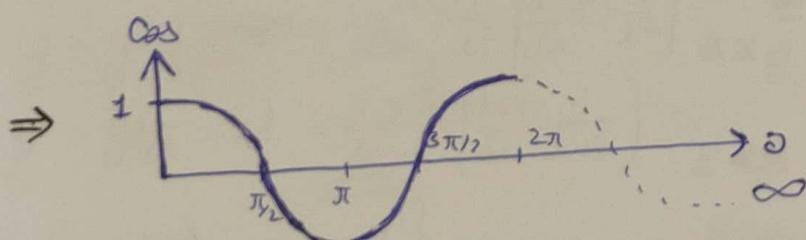
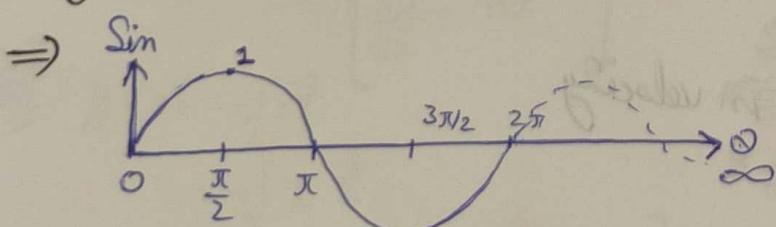
$$\left\{ \Rightarrow \frac{1+\sqrt{2}}{2\sqrt{2}} = \underline{\cos^2 22.5^\circ} \right.$$

$$\Rightarrow \tan 22.5^\circ = \sqrt{2} - 1$$

#L12  $\Rightarrow$  (A+B) Identities  $\Rightarrow$   $\sin 15^\circ$   $= \sin(45^\circ - 30^\circ) = \sin 45^\circ \cos 30^\circ - \cos 45^\circ \sin 30^\circ$

$$= \frac{1}{\sqrt{2}} \left( \frac{\sqrt{3}}{2} \right) - \left( \frac{1}{\sqrt{2}} \right) \left( \frac{1}{2} \right)$$

# Graph  $\Rightarrow$  Small Angle



## # Small Angle Approximation

$\Rightarrow$  This is valid only for very small angles.

$\theta$  is very small:-

$$\textcircled{1} \quad \lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

$$\textcircled{2} \quad \cos \theta = 1 \quad \text{In Radian}$$

$$\Rightarrow \left[ \frac{\pi}{180} \times 1^\circ \right] \rightarrow \text{if in Degree change into Radian.}$$

# L13 Calculus :- Change =  $\Delta = \text{Final} - \text{Initial}$

$$\% v = 10 \text{ m/s} \rightarrow v = 5 \text{ m/s} \quad \Rightarrow \Delta v = 5 - 10 = -5 \text{ m/s}$$

$\Delta$  Difference = (Bada - Chala)

$$\% v = 10 \text{ m/s} \rightarrow v = 5 \text{ m/s} \quad \{ \text{Difference in } v = 10 - 5 = 5 \text{ m/s} \}$$

$$\% \text{ Increase by 5 times} \quad \begin{array}{|c|c|} \hline & \text{Increase to} \\ \hline v & v = 10 \text{ Increase to 5 times} \\ \hline v & v = 10 \times 5 = 50 \text{ m/s} \\ \hline \end{array}$$

$\Delta$  [  $\Rightarrow d \rightarrow$  bahan chala so change ]

$\Delta x \rightarrow$  change in displacement.

$dx \rightarrow$  bahan chala so change in displacement

$\Delta v \rightarrow$  change in velocity

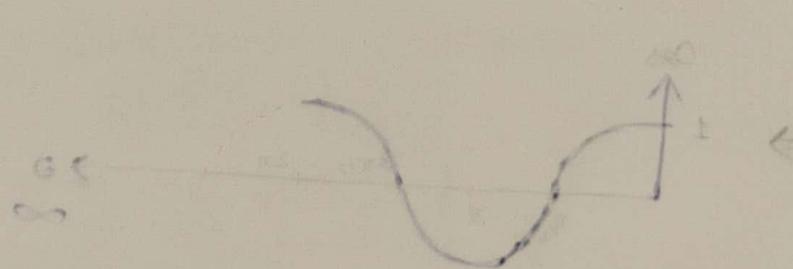
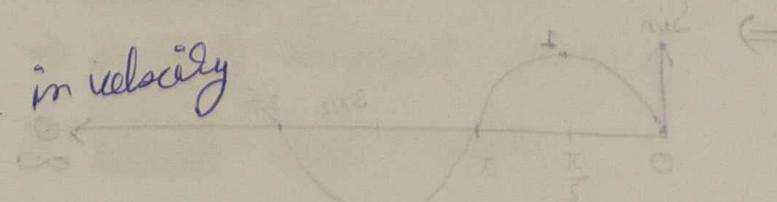
$dv \rightarrow$  bahan chala so change in velocity

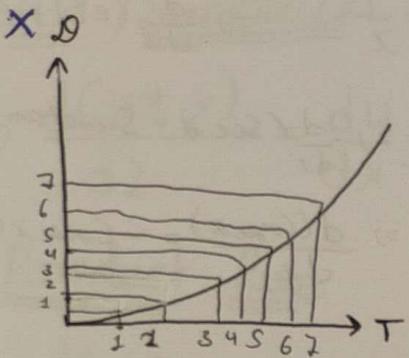
$\Delta \omega \rightarrow$  change in angle

$\Delta t \rightarrow$

$\Delta t \rightarrow$  change in time

$\Delta t \rightarrow$





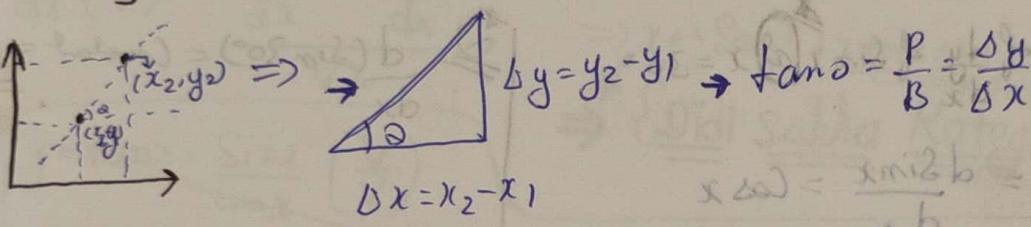
$$u = \text{Speed} = \frac{\Delta D}{\Delta T} = \frac{\Delta x}{\Delta t}$$

$$\Rightarrow \Delta t = 3 \text{ sec} = x = 3$$

$$\Rightarrow \Delta t = 6 \text{ sec} = x = 6$$

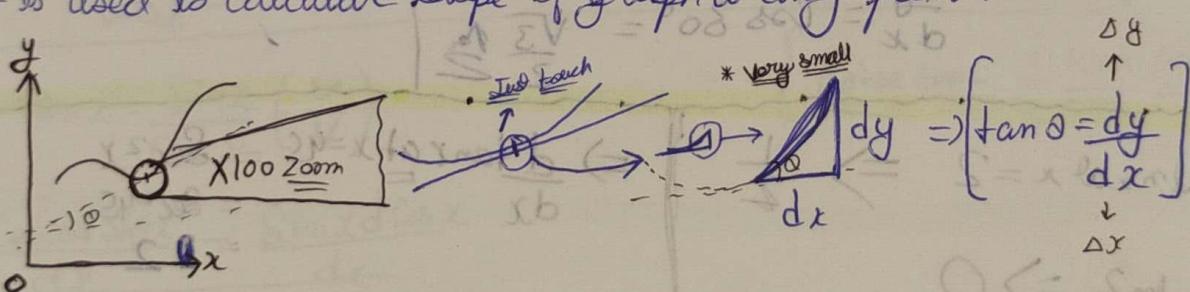
Distance (B/w) =  $\frac{6-3}{6-3} = 1$  Speed

$$\Rightarrow \tan \theta = \frac{P}{B}$$



### Differentiation

⇒ It is used to calculate slope of graph at any point.



### # Formula

$$\textcircled{1} \quad y = x^n$$

⇒ Differentiation of  $y = x^n$

$$\Rightarrow \left[ \frac{dy}{dx} = nx^{n-1} \right]$$

$$\textcircled{2} \quad y = x^{-\frac{1}{2}} = -\frac{1}{2}x^{\frac{-3}{2}}$$

$$= -\frac{1}{2}x^{-\frac{3}{2}}$$

$$\textcircled{3} \quad y = x^{10} = \frac{dy}{dx} = 10x^9$$

$$\textcircled{4} \quad y = x^{123} = \frac{dy}{dx} = 123x^{122}$$

$$\textcircled{5} \quad y = x^3 = \frac{dy}{dx} = 3x^2$$

$$\textcircled{6} \quad y = x^2 = \frac{dy}{dx} = 2x$$

$$\textcircled{7} \quad y = \frac{1}{x} = x^{-1} = -x^{-2} = -\frac{1}{x^2} \quad \left[ \frac{d(\frac{1}{x})}{dx} = \frac{-1}{x^2} \right] \quad \textcircled{8} \quad y = x = \frac{1}{x} = \frac{1}{x^2}$$

$$\textcircled{9} \quad y = \sqrt{x} = x^{\frac{1}{2}} = \frac{1}{2}x^{-\frac{1}{2}} = \left[ \frac{d(\sqrt{x})}{dx} = \frac{1}{2\sqrt{x}} \right] \quad \textcircled{10} \quad y = 5x^3 = 5x^2 = 15x^2$$

$$\left\{ \frac{d(y)}{dx} = nx^{n-1} \right\}$$

$$\textcircled{11} \quad y = x^{-s} = -sx^{-s-1} = -sx^{-6}$$

$$\textcircled{12} \quad y = x^{\frac{1}{2}} = \frac{1}{2}x^{-\frac{1}{2}} = \frac{1}{2}x^{-\frac{1}{2}}$$

$$\begin{aligned} \Rightarrow \frac{d(\text{constant})}{dx} &= \text{constant} \quad x=0 = 0 & \Rightarrow \frac{d}{dx} (\ln x) = \frac{1}{x} & \Rightarrow \frac{d}{dx} (e^x) = e^x \\ \Rightarrow \frac{d(\sin x)}{dx} &= \cos x & \Rightarrow \frac{d(\tan x)}{dx} = \sec^2 x & \Rightarrow \frac{d}{dx} (\sec x) = \sec x \tan x \\ \Rightarrow \frac{d(\cos x)}{dx} &= -\sin x & \Rightarrow \frac{d}{dx} (\cot x) = -\operatorname{cosec}^2 x & \Rightarrow \frac{d(\operatorname{cosec} x)}{dx} = -\operatorname{cosec} x \cot x \end{aligned}$$

$$\begin{aligned} \therefore y &= \sin x + \cos x \\ \Rightarrow \cos x - \sin x & \end{aligned}$$

Q2 :- Find value of  $\frac{dy}{dx}$  of  $\sin x$  at  $x = 30^\circ$

$$\Rightarrow \frac{dy}{dx} = \frac{d \sin x}{dx} = \cos x$$

$x = 30^\circ$  (given)

$$\frac{dy}{dx} = \cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$\frac{d(\sin 30^\circ)}{dx} = \text{constant} = 0$$

$$\Rightarrow \frac{d}{dx} \ln x \text{ at } x=2 \Rightarrow \frac{1}{2}$$

$$\Rightarrow \frac{d}{dx} \ln 2 \Rightarrow 0$$

$$\Rightarrow \frac{de^x}{dx} \text{ at } x=3 \Rightarrow e^3$$

$$\Rightarrow \frac{de^3}{dx} \Rightarrow 0$$

$$\Rightarrow \frac{d(4^4)}{dx} \Rightarrow 0$$

$$\Rightarrow \frac{d(x^4)}{dx} \Rightarrow \text{at } x=4 = 4 \cdot 3 = 4(4)^3 = 4 \times 64 = \underline{\underline{256}}$$

$$\Rightarrow \frac{d \tan x}{dx} \text{ at } x=45^\circ = \sec^2 x = \sec^2 45^\circ = 2$$

$$\Rightarrow \frac{d \tan 45^\circ}{dx} = 0$$

[at  $\frac{1}{2}$  bad me]

## # Add / Subtract

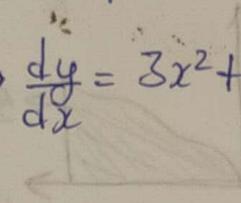
$$\Rightarrow \frac{d(u \pm v)}{dx} = \frac{du}{dx} \pm \frac{dv}{dx}$$

$$y = x^3 + x^7$$

$$\Rightarrow \frac{dy}{dx} = 3x^2 + 7x^6$$

$$y = x^4 - x^2$$

$$\Rightarrow \frac{dy}{dx} = 4x^3 - 2x$$



## # Product Rule

$$\Rightarrow \frac{d(uv)}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$y = x \sin x$$

$$\Rightarrow \frac{dy}{dx} = \frac{x d \sin x}{dx} + \frac{\sin x dx}{dx} \Rightarrow x \cos x + \sin x$$

## # Division Rule

$$\Rightarrow \frac{d(u/v)}{dx} = \frac{vu'}{v^2} - \frac{uv'}{v^2}$$

$$y = \tan x = x e^x \tan \text{one by one}$$

$$\Rightarrow x e^x \frac{dtan x}{dx} + x \tan x \frac{dex}{dx} + e^x \tan x \frac{dx}{dx}$$

$$\Rightarrow x e^x \sec^2 + x \tan x e^x + e^x \tan x$$

\* No any change  
no change

\* Didi Sakka Kategori

$$\rightarrow y = \tan x = \frac{\sin x}{\cos x} \left( \frac{v}{u} \right)$$

$$\frac{\sin x d \cos x}{\cos^2 x} - \frac{\cos x d \sin x}{\cos^2 x}$$

$$\frac{\sin - \sin x}{\cos x + \cos x}$$

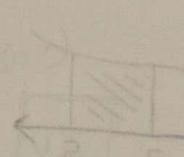
$$\Rightarrow y = \tan x = \frac{\sin x}{\cos x} \left( \frac{v}{u} \right)$$

{ Ratse same & Kahil/kate! }

$$= \frac{\cos x d \sin x}{\cos^2 x} - \frac{\sin x d \cos x}{\cos^2 x}$$

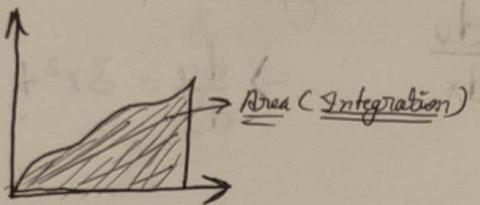
$$= \frac{\cos x (\cos x) - \sin x (-\sin x)}{\cos^2 x}$$

$$\Rightarrow \frac{\cos^2 x + \sin^2 x}{\cos^2 x} = \frac{1}{\cos^2 x} = \underline{\underline{\sec^2 x}}$$



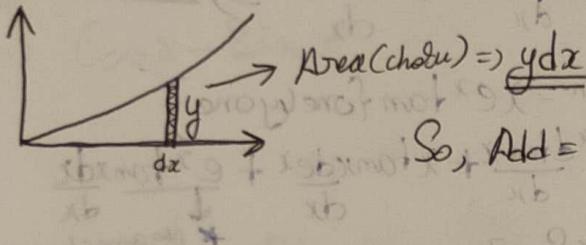
$$s = p$$

# Integration  $\Rightarrow$  It is used to calculate Area under the curve.

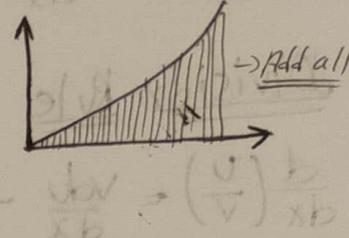


$\Rightarrow$  Formula  $\rightarrow$  opposite of differentiation.

$\Rightarrow$  Integration  $\Rightarrow \int =$  Add like ~~like~~ because of Net effect of triangle we use this sign.



$$\text{So, Add total} = \left[ \underline{ydx} \right]$$



$$\Rightarrow \left[ \int x^n dx = \frac{x^{n+1}}{n+1} \right]$$

$$\Rightarrow \int e^x dx = e^x$$

$$\Rightarrow \int \sec^2 dx = \tan x$$

$$\Rightarrow \int dx = x$$

$$\Rightarrow \int \frac{1}{x} dx = \ln x$$

$$\Rightarrow \int \csc x \cot x dx = -\csc x$$

$$\Rightarrow \int \frac{1}{x^2} dx = -\frac{1}{x}$$

$$\Rightarrow \int \cos x dx = \sin x$$

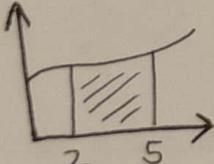
$$\Rightarrow \int \sec x \tan x dx = \sec x$$

$$\Rightarrow \int \frac{1}{\sqrt{x}} dx = 2\sqrt{x}$$

$$\Rightarrow \int \sin x dx = -\cos x$$

$$\Rightarrow \int \csc x \cot x dx = -\csc x$$

# L15



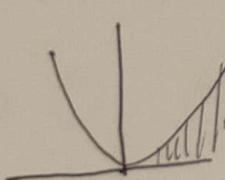
$$\Rightarrow \int_2^5 f(x) dx \rightarrow \text{upper (Big)} = \text{Area under} \\ \rightarrow \text{lower small}$$

$$\Rightarrow \int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\left[ \int x^1 dx = \frac{x^2}{2} + C \right] \text{Bd} \left[ \int x^{-1} dx = \frac{\ln x}{x} \right]$$

# Infinite Integration.  $\rightarrow$  kisi limit nahi hain

$$y = x^2$$



$$\Rightarrow \text{Area} = \int y dx = \int x^2 dx = \frac{x^3}{3} + C$$

$$\Rightarrow \text{The Area between } 1-9 \int_{\underline{1}}^{\underline{9}} x^{1-9} dx = \left[ \frac{x^0}{0} \right] \rightarrow \text{find} \\ \text{Same} \quad \frac{dy}{dx} = x^{1-9}$$

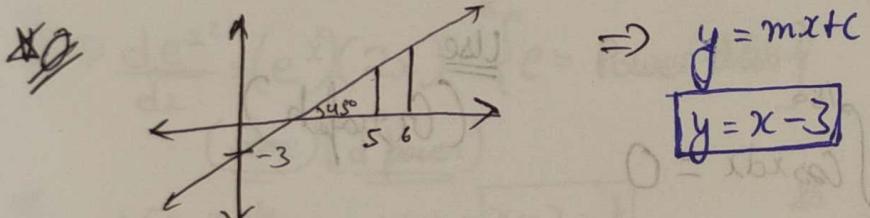
Thusly all Formula of integration are opposite to differentiation.

# Definite Integration (Limits are given)  $\rightarrow \int_a^b f(x) dx$  (No C used)

$$\text{Q. } \int_1^5 x^2 dx = \left[ \frac{x^3}{3} \right]_1^5 = \frac{5^3}{3} - \frac{1^3}{3} \Rightarrow \frac{125-1}{3} = \frac{124}{3} \quad * \left\{ \frac{2}{\sqrt{2}} = \sqrt{2} \right\}$$

$$\text{Q. } \int_{-3}^{10} 7 dx = 7[x]_{-3}^{10} = 7(10-(-3)) = 7 \times 7 = 49$$

$$\text{Q. } \int_0^3 8x^3 dx = 8[x^4]_0^3 = 8[3^4 - 0^4] = 162$$



$$\Rightarrow \int_0^6 [x^2 - 3x] dx \Rightarrow \left[ \frac{x^3}{3} - \frac{3x^2}{2} \right]_0^6 = \left[ \frac{6^3}{3} - \frac{3 \cdot 6^2}{2} \right] = 2.5$$

$$\text{Q. } \int_{30^\circ}^{90^\circ} \sin x dx = \left[ -\cos x \right]_{30^\circ}^{90^\circ} = (-\cos 90^\circ) - (-\cos 30^\circ) = 0 - (-\sqrt{3}/2) = \frac{\sqrt{3}}{2}$$

$$\text{Q. } \int_0^{\frac{\pi}{2}} \cos x dx = [\sin x]_0^{\frac{\pi}{2}} = \sin 90^\circ = 1$$

$$\text{Q. } \int \frac{1}{x} dx = \ln x + C$$

$$\text{Q. } \int_4^8 \frac{1}{x} dx = \left[ \ln x \right]_4^8 = \ln 8 - \ln 4 = 0.6 - 0.48 = 0.12 \quad \times \quad \ln \left( \frac{8}{4} \right) = 0.693$$

(b)  $\int \frac{1}{x} dx = \ln x + C$

$$\int \frac{1}{x+3} dx = \ln(x+3) + C$$

$$\int_1^{ss} \frac{1}{x+s} dx = \left[ \ln(x+s) \right]_1^{ss} \Rightarrow \ln(60) - \ln(6) = \ln\left(\frac{60}{6}\right) = \ln 10 = 2.303$$

$\Rightarrow \sin 760^\circ \rightarrow$  Pass well Se 90 (Multiply) and Subtract

$$\begin{array}{c} -72^\circ \\ \boxed{\sin 46^\circ} \end{array}$$

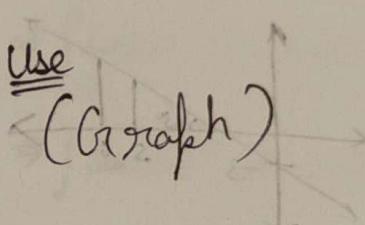
$$\int_0^{90} \sin x dx = 1$$

$$\int_0^{72^\circ} \sin x dx =$$

$$\Rightarrow \frac{x}{90^\circ} = \int_0^1 \sin x dx \quad \text{Use (Graph)}$$

$$x(b-x) = xb - x^2$$

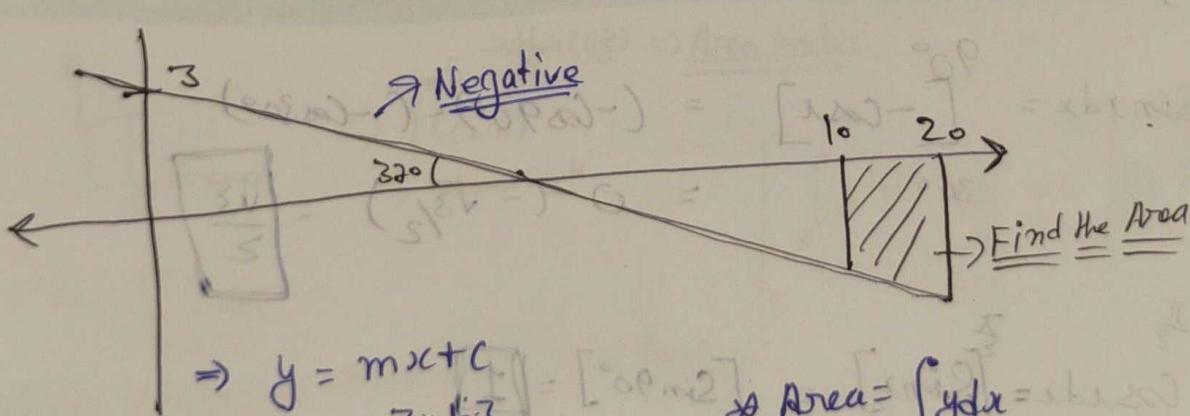
$$x+b-x = b$$



$$\int_0^{90} \cos x dx = 1$$

$$\int_0^{180^\circ} \cos x dx = 0$$

$$\Rightarrow \int_0^1 \cos x dx = 0$$



$$\Rightarrow y = mx + c$$

$$\Rightarrow m = -\frac{3}{4}x + 3$$

$$\Rightarrow \text{Area} = \int y dx$$

$$\Rightarrow \int_{1.0}^{2.0} \left( -\frac{3}{4}x + 3 \right) dx$$

$$\Rightarrow -\frac{3}{8}x^2 + 3x \Big|_{1.0}^{2.0}$$

$$\Rightarrow \left( -\frac{3}{8} \times 2^2 + 6 \right) - \left( -\frac{3}{8} \times 1^2 + 3 \right)$$

$$\Rightarrow -9.0 - (-7.8)$$

$$\Rightarrow -82.5 \text{ (Area negative)} \checkmark$$

$$\Rightarrow \frac{d \sin y}{dy} = \cos y \quad \checkmark$$

$$\Rightarrow \frac{d \sin x}{dx} = X \star \text{But} \Rightarrow \frac{d \sin x}{dx} = \cos x \cdot \frac{dx}{dx} \quad \left\{ \begin{array}{l} \text{Multiply Extra term} \\ \hline \end{array} \right\}$$

#L16

Ultraulta

$$\Delta P_{prove} : - \frac{d(\sin \theta)}{d\theta} \times \frac{d\theta}{dx} \Rightarrow \frac{d(\sin \theta)}{d\theta} \cdot \frac{d\theta}{dx} \Rightarrow \left\{ \frac{d(\sin \theta)}{dx} = \cos \theta \cdot \frac{d\theta}{dx} \right\}$$

$$\stackrel{?}{=} \frac{d(x^2 + 2x - 3)}{dy} \times \frac{dx}{dy} \Rightarrow \frac{d(x^2 + 2x - 3)}{dx} \times \frac{1}{\frac{dy}{dx}}$$

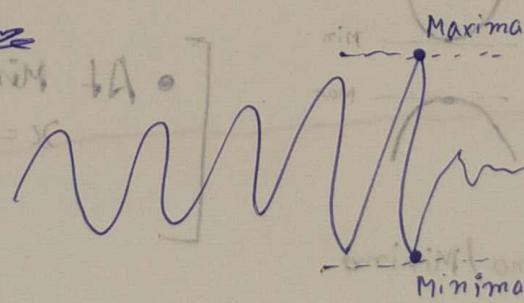
$$\stackrel{?}{=} \frac{d(\sin x^n)}{dx} = \left( \frac{d \sin}{dx} \right) (x^n) \quad \left\{ \begin{array}{l} \text{Motibby} \\ \hline \end{array} \right\} \Rightarrow \left\{ \begin{array}{l} \frac{\partial}{\partial} \frac{\sin \ln (x^2 + 4x + 9)}{3} \\ \downarrow \\ (\text{Break so, whole}) \end{array} \right\}$$

(Same) (d power)

$$\stackrel{?}{=} \frac{d(x-2)^{10}}{dx} \quad \begin{array}{l} \text{Hint} \Rightarrow x-2=t \\ \Rightarrow \frac{df}{dx} = 10t^9 \cdot \frac{dt}{dx} \end{array} \Rightarrow \left\{ \begin{array}{l} \text{Slope} = \frac{dy}{dx} = \text{tan} = \text{inclination} \end{array} \right\}$$

$$\Rightarrow \underline{10(x-2)^9}$$

# Maxima & Minima  
Hill point & Valley point



$\Rightarrow$  Slope at Maxima & Minima = 0

$\Rightarrow$  Just after Maxima - slope is Negative = ↘  
 $\Rightarrow$  Just after Minima - slope is positive = ↗

$\Rightarrow$  Trigo function  $\Rightarrow \sin - \left\{ \begin{array}{l} \text{Max} = 1 \\ \text{Min} = -1 \end{array} \right.$

$\Rightarrow \cos - \left\{ \begin{array}{l} \text{Max} = 1 \\ \text{Min} = -1 \end{array} \right.$

$\Rightarrow \tan x \cot x \rightarrow \text{Max} \rightarrow \infty$   
 $\rightarrow \text{Min} \rightarrow -\infty$

$\Rightarrow \sec x, \csc x \rightarrow \text{anything but never } \underline{\text{between}} \quad (-1 \text{ } \& \text{ } 1) \rightarrow \underline{\text{B/W X}}$

$$\Rightarrow \text{Maximum value of } y = 7 \sin x + 10 \quad \left\{ \begin{array}{l} \text{Max} \rightarrow \sin x \rightarrow 1 \\ \Rightarrow 7(1) + 10 = 17 \end{array} \right.$$

$$\Rightarrow \text{Maximum value of } y = \frac{1}{10 \sin^2 x + 2} \quad \left\{ \begin{array}{l} y \uparrow = \frac{1}{x \downarrow} \\ \text{(Minimizes use } \frac{1}{x}) \end{array} \right.$$

$y =$  (So we use Maxima)

but  $x^2 \Rightarrow 1$   
(So, we use min = 0)

$$\left[ \begin{array}{l} y_{\max} = \frac{1}{x_{\min}} \\ y_{\min} = \frac{1}{x_{\max}} \end{array} \right]$$

$$\Rightarrow y = \frac{1}{2}$$

$$\Rightarrow a \sin \theta \pm b \cos \theta$$

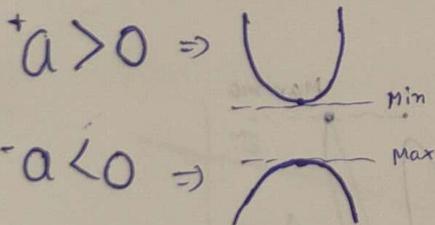
$$\left\{ \begin{array}{l} \text{Max} \leq \sqrt{a^2 + b^2} \\ \text{Min} = -\sqrt{a^2 + b^2} \end{array} \right.$$

$$\Rightarrow y_{\min} = \frac{(a \sin \theta + b \cos \theta)_{\min}}{(a \sin \theta + b \cos \theta)_{\max}}$$

$$\Rightarrow \frac{1}{\sqrt{a^2 + b^2}}$$

$\Rightarrow$  Quadratic Equation  $y \Rightarrow ax^2 + bx + c = 0$

$$x = \frac{-b \pm \sqrt{D}}{2a}$$



$$\left[ \begin{array}{l} \bullet \text{ At Minima / Maxima} \\ x = \frac{-b}{2a} \quad y = \frac{-D}{4a} \end{array} \right]$$

2. Find Maxima / Minima.

$$\Rightarrow y = x^2 + 10x + 3$$

+a > 0  $\Rightarrow$  U  $\Rightarrow$  Minima

$$\Rightarrow \text{Minima} = y = \frac{-D}{4a} = \frac{b^2 - 4ac}{4a} = \frac{(10)^2 - 4 \times 1 \times 3}{4 \times 1} = \frac{100 - 12}{4} = \frac{88}{4}$$

$$\Rightarrow \text{Minima} = \frac{22}{4}$$

$$\Rightarrow -\frac{100 + 12}{4} = -\frac{112}{4} = -28$$

$$\Rightarrow \text{Maxima} = \frac{-b}{2a} = \frac{-10}{2} = -5$$

$$\Rightarrow y = -x^2 + 10x + 3$$

$$\Rightarrow a < 0 \Rightarrow \text{Maxima} = \frac{-D}{4a} = \boxed{11}$$

$\Rightarrow 0 = x \rightarrow$  Maxima

$$x = -\frac{b}{2a} = \frac{-10}{2} = -5$$

Prove:- We know  $\Rightarrow \text{Slope} = 0$   $\left[ \frac{dy}{dx} = 0 \right]$  (Not Important)

$$y = ax^2 + bx + c \quad \text{---(i)}$$

$$\frac{dy}{dx} = 2ax + b = 0$$

$$= 2ax + b = 0$$

$$= 2ax = -b$$

$$= \boxed{x = \frac{-b}{2a}} \quad \text{---(ii)}$$

$\rightarrow$  Put value of  $x$  in eq

$$\Rightarrow y = ax^2 + bx + c$$

$$\Rightarrow y = a\left(\frac{-b}{2a}\right)^2 + b\left(\frac{-b}{2a}\right) + c$$

$$\Rightarrow \frac{ab^2}{4a^2} - \frac{b^2}{2a} + c$$

$$\Rightarrow \frac{b^2 - 2b^2 + 4ac}{4a}$$

$$\Rightarrow \frac{-b^2 + 4ac}{4a}$$

$$y_{m/m} \Rightarrow - \frac{(b^2 - 4ac)}{4a}$$

$$\boxed{y_{m/m} = -\frac{b}{4a}}$$

## # Double Differentiation (2 Bndx)

$$\Rightarrow y = x^3 + 4x^2 + 3x + 7$$

$$y' = \frac{dy}{dx} = 3x^2 + 8x + 3$$

$$y'' = \frac{d^2y}{dx^2} = \underline{\underline{6x + 8}}$$

$$\frac{d}{dx} \left( \frac{dy}{dx} \right)$$

$$\exists. \quad y = \ln x$$

$$y' = \frac{dy}{dx} = \frac{1}{x}$$

$$y'' = \frac{d^2y}{dx^2} = -\frac{1}{x^2}$$

#L1

# \* Mathematical tools \*

# Common Kidnapping

$$\Rightarrow 30 \times 2 + 30 = 30(2+1) = 30(3) = 90$$

$$\Rightarrow 188 \times 9 + 66 \times 3 = 9(188+22) =$$

$$\Rightarrow (10^2 + 70^2) = 10^2 (1 + 7^2) \xrightarrow{\text{out common}} = 100(50) = 5000$$

$$\Rightarrow X = R\sqrt{3} \quad \checkmark$$

$$\Rightarrow \sqrt{(X^2 + R^2)} = \sqrt{(R\sqrt{3})^2 + R^2} = \sqrt{(R\sqrt{3} \times R\sqrt{3}) + R^2} = \sqrt{R^2 3 + R^2} = \sqrt{4R^2} = 2R \quad \checkmark$$

$$= \sqrt{(R\sqrt{3})^2 + R^2} = \sqrt{R^2 3 + R^2} = \sqrt{(R^2)(3+1)} = \sqrt{4R^2} = 2R \quad \checkmark$$

$$X \Rightarrow \sqrt{7R^2} = \sqrt[3]{(X^2 + R^2)} = \sqrt[3]{7R^3 + R^3} = \sqrt[3]{8R^3} = 2R \quad \checkmark$$

$$\Rightarrow 3\sqrt{27000} = 3\sqrt{27 \times 1000} = 3 \times 10 = 30 \quad \checkmark$$

# LCM

$$\Rightarrow (60, 40) = 20(3 \times 2) = 120$$

$$\Rightarrow (144, 60) = 12(12 \times 5) = 12(60) = 720$$

# Fractions to Decimals

$$= \frac{1}{2} \stackrel{0.5}{=} \frac{1}{3} \stackrel{0.3}{=} \frac{1}{4} \stackrel{0.25}{=}$$

$$\text{So, } \frac{8}{3} = 2 \text{ (left) So, } 0.6 \quad \{ 2 + 0.6 \} = 2.66$$

$$= \frac{55}{2} \stackrel{18.2}{=} 18 + \frac{1}{3} = 18 + 0.2 = 18.2$$

$$\neq \frac{1}{5} = \frac{1}{2} \times 2 \stackrel{0.2}{=} \frac{1}{2} \xrightarrow{\text{Last digit decimal}} \frac{1}{2} \times \frac{5}{1} = 2.5$$

$$= \frac{33}{5} = 6.6 \quad = \frac{124}{5} \stackrel{24.8}{=} \frac{135}{5} = 27$$

$$\neq \frac{1}{6} = 0.166666\ldots$$

$$= \frac{1}{7} = 0.1421$$

$$= \frac{1}{8} = 0.125$$

$$= \frac{1}{9} = 0.\overline{111} \quad = \frac{2}{9} = 0.\overline{222} \quad = \frac{3}{9} = 0.\overline{333} = \frac{20^2}{9}, 2 = 2.\overline{222} = \frac{100^{11}}{9} = 1 \Rightarrow 11.\overline{333}$$

# Equivalent Fractions

$$= \frac{1}{2} \xrightarrow{x4} \frac{4}{8}$$

$$= \frac{7}{11} \xrightarrow{x11} \frac{77}{121} \text{ (Same)} \quad = \frac{3}{7} \xrightarrow{x7} \frac{21}{49} = \frac{27}{63}$$

## # LCM and Fraction

$$\Rightarrow \frac{1}{2} + \frac{3}{4} = \frac{1}{2}(1 + \frac{3}{2}) \rightarrow \text{Use common denominator}$$

$$\Rightarrow \frac{7}{11} - \frac{2}{121} = \frac{1}{11}(7 - \frac{2}{11}) \\ = \frac{1}{11}(\frac{75}{11}) \Rightarrow \frac{75}{121}$$

{ This work when denominator divides }

$$0^2 = (2)(5) = (1+3)0^2 = 0^2 + 2^2 \\ = (25+28)0^2 = 250^2 + 2^2 \times 3^2$$

## # 1

$$\Rightarrow 1 + \frac{1}{8} = \frac{9}{8}$$

→ Denominator same

$$\Rightarrow 1 - \frac{1}{9} = \frac{8}{9}$$

$$\Rightarrow 1 \oplus \frac{2}{121} = \frac{119}{121}$$

$$\left. \begin{array}{l} \# \frac{a}{b} \text{ of } - (\text{opposite}) \\ = \frac{2}{1} \text{ or } 2 \text{ divide } \frac{3}{5} \\ \frac{3}{5} \Rightarrow 2 \times \frac{5}{3} \end{array} \right\}$$

## # Decimals addition, Subtraction Rules (Point se point mila)

$$\Rightarrow 0.2 + 0.3 = \underline{\underline{0.2}} \quad \Rightarrow 0.20 + 0.03 = \underline{\underline{0.23}}$$

$$\Rightarrow 0.27 - 1.99 = \underline{\underline{8.27}} - \underline{\underline{1.99}} = \underline{\underline{6.28}}$$

## # Decimal Multiply

$$\Rightarrow 0.2 \times 0.3 = \underline{\underline{0.06}}$$

$$\Rightarrow 0.2 \times 0.03 = \underline{\underline{0.006}} \Rightarrow \frac{0.2}{0.03} = \frac{2}{3} = 0.\bar{6}$$

$$\Rightarrow 0.12 \times 0.005 = \frac{12}{100} \times \frac{5}{1000} = \frac{60}{10000} = 0.0006 \Rightarrow \frac{0.3}{0.04} = \frac{3}{4} = \frac{30}{40} X$$

$$\Rightarrow 99.9 \times 0.5$$

$$\frac{999}{10} \times \frac{5}{10} = \frac{4995}{100} = 49.95$$

$$\Rightarrow \frac{6.9}{1.44} = \frac{6.90}{1.44} = \frac{690}{144} = \frac{115}{24} \quad \downarrow \text{add}$$

## => PUPPY POINT-1

$$\bullet \text{Common Kidnapping} \quad 4+8 = 4(1+2) = 4 \times 3 = 12$$

$$\bullet \text{LCM} = \text{Le common kar multiply} = 6, 9 = 3(2, 3) = 18$$

$$\bullet \text{Equivalent fraction} = \frac{2}{3} = \frac{2 \times 4}{3 \times 4} = \frac{8}{12}$$

$$\bullet \text{Fraction Addition} = \frac{1}{11} - \frac{8}{99} = \frac{1}{11}(1 - \frac{8}{9}) = \frac{1}{11}(\frac{1}{9}) = \frac{1}{99}$$

$$\bullet \text{Fraction Division & Multiplication Rule} = 2 \div \frac{2}{5} \quad \& \quad 2 \div \frac{3}{5} \rightarrow 2 \times \frac{5}{2} \quad \& \quad 2 \times \frac{5}{3}$$

$$\bullet \text{Decimals Addition, Subtraction Rules} = \text{Point se point mila}$$

$$\bullet \text{Decimals Multiply, Division Rule} :-$$

Point (line)

Shift Karo

$$+ \frac{x}{10^x}$$