

Step 1. Resample a *points* path into n evenly spaced points. We use $n=64$. For gestures serving as templates, Steps 1-3 should be carried out once on the raw input points. For candidates, Steps 1-4 should be used just after the candidate is articulated.

RESAMPLE(*points*, n)

```

1   $I \leftarrow \text{PATH-LENGTH}(\text{points}) / (n - 1)$ 
2   $D \leftarrow 0$ 
3   $\text{newPoints} \leftarrow \text{points}_0$ 
4  foreach point  $p_i$  for  $i \geq 1$  in points do
5     $d \leftarrow \text{DISTANCE}(p_{i-1}, p_i)$ 
6    if  $(D + d) \geq I$  then
7       $q_x \leftarrow p_{i-1}_x + ((I - D) / d) \times (p_i_x - p_{i-1}_x)$ 
8       $q_y \leftarrow p_{i-1}_y + ((I - D) / d) \times (p_i_y - p_{i-1}_y)$ 
9      APPEND(newPoints,  $q$ )
10     INSERT(points,  $i$ ,  $q$ ) //  $q$  will be the next  $p_i$ 
11      $D \leftarrow 0$ 
12   else  $D \leftarrow D + d$ 
13 return newPoints
```

PATH-LENGTH(*A*)

```

1   $d \leftarrow 0$ 
2  for  $i$  from 1 to  $|A|$  step 1 do
3     $d \leftarrow d + \text{DISTANCE}(A_{i-1}, A_i)$ 
4  return  $d$ 
```

Step 2. Find and save the indicative angle ω from the *points*' centroid to first point. Then rotate by $-\omega$ to set this angle to 0° .

INDICATIVE-ANGLE(*points*)

```

1   $c \leftarrow \text{CENTROID}(\text{points})$  // computes  $(\bar{x}, \bar{y})$ 
2  return  $\text{ATAN}(c_y - \text{points}_0_y, c_x - \text{points}_0_x)$  // for  $-\pi \leq \omega \leq \pi$ 
```

ROTATE-BY(*points*, ω)

```

1   $c \leftarrow \text{CENTROID}(\text{points})$ 
2  foreach point  $p$  in points do
3     $q_x \leftarrow (p_x - c_x) \cos \omega - (p_y - c_y) \sin \omega + c_x$ 
4     $q_y \leftarrow (p_x - c_x) \sin \omega + (p_y - c_y) \cos \omega + c_y$ 
5    APPEND(newPoints,  $q$ )
6  return newPoints
```

Step 3. Scale *points* so that the resulting bounding box will be of size^2 size. We use $\text{size}=250$. Then translate *points* to the origin $k=(0,0)$. BOUNDING-BOX returns a rectangle defined by $(\min_x, \min_y), (\max_x, \max_y)$.

SCALE-TO(*points*, *size*)

```

1   $B \leftarrow \text{BOUNDING-BOX}(\text{points})$ 
2  foreach point  $p$  in points do
7     $q_x \leftarrow p_x \times \text{size} / B_{\text{width}}$ 
8     $q_y \leftarrow p_y \times \text{size} / B_{\text{height}}$ 
9    APPEND(newPoints,  $q$ )
10 return newPoints
```

TRANSLATE-TO(*points*, k)

```

1   $c \leftarrow \text{CENTROID}(\text{points})$ 
2  foreach point  $p$  in points do
3     $q_x \leftarrow p_x + k_x - c_x$ 
4     $q_y \leftarrow p_y + k_y - c_y$ 
5    APPEND(newPoints,  $q$ )
6  return newPoints
```

Step 4. Match *points* against a set of *templates*. The *size* variable on line 7 of RECOGNIZE refers to the *size* passed to SCALE-TO in Step 3. The symbol ϕ equals $\frac{1}{2}(-1 + \sqrt{5})$. We use $\theta = \pm 45^\circ$ and $\theta_\Delta = 2^\circ$ on line 3 of RECOGNIZE. Due to using RESAMPLE, we can assume that A and B in PATH-DISTANCE contain the same number of points, i.e., $|A|=|B|$.

RECOGNIZE(*points*, *templates*)

```

1   $b \leftarrow +\infty$ 
2  foreach template  $T$  in templates do
3     $d \leftarrow \text{DISTANCE-AT-BEST-ANGLE}(\text{points}, T, -\theta, +\theta, \theta_\Delta)$ 
4    if  $d < b$  then
5       $b \leftarrow d$ 
6       $T' \leftarrow T$ 
7     $\text{score} \leftarrow 1 - b / 0.5\sqrt{(\text{size}^2 + \text{size}^2)}$ 
8  return  $\langle T', \text{score} \rangle$ 
```

DISTANCE-AT-BEST-ANGLE(*points*, $T, \theta_a, \theta_b, \theta_\Delta$)

```

1   $x_1 \leftarrow \phi\theta_a + (1 - \phi)\theta_b$ 
2   $f_1 \leftarrow \text{DISTANCE-AT-ANGLE}(\text{points}, T, x_1)$ 
3   $x_2 \leftarrow (1 - \phi)\theta_a + \phi\theta_b$ 
4   $f_2 \leftarrow \text{DISTANCE-AT-ANGLE}(\text{points}, T, x_2)$ 
5  while  $|\theta_b - \theta_a| > \theta_\Delta$  do
6    if  $f_1 < f_2$  then
7       $\theta_b \leftarrow x_2$ 
8       $x_2 \leftarrow x_1$ 
9       $f_2 \leftarrow f_1$ 
10      $x_1 \leftarrow \phi\theta_a + (1 - \phi)\theta_b$ 
11      $f_1 \leftarrow \text{DISTANCE-AT-ANGLE}(\text{points}, T, x_1)$ 
12   else
13      $\theta_a \leftarrow x_1$ 
14      $x_1 \leftarrow x_2$ 
15      $f_1 \leftarrow f_2$ 
16      $x_2 \leftarrow (1 - \phi)\theta_a + \phi\theta_b$ 
17      $f_2 \leftarrow \text{DISTANCE-AT-ANGLE}(\text{points}, T, x_2)$ 
18 return  $\text{MIN}(f_1, f_2)$ 
```

DISTANCE-AT-ANGLE(*points*, T, θ)

```

1  newPoints  $\leftarrow \text{ROTATE-BY}(\text{points}, \theta)$ 
2   $d \leftarrow \text{PATH-DISTANCE}(\text{newPoints}, T_{\text{points}})$ 
3  return  $d$ 
```

PATH-DISTANCE(A, B)

```

1   $d \leftarrow 0$ 
2  for  $i$  from 0 to  $|A|$  step 1 do
3     $d \leftarrow d + \text{DISTANCE}(A_i, B_i)$ 
4  return  $d / |A|$ 
```

¹ This pseudocode is modified slightly from that which appears in the original ACM UIST 2007 publication by Wobbrock, Wilson and Li to be parallel to the more recent \$N multistroke recognizer. This algorithm's logic remains unchanged.