# **Appendix 3- Part III**

Now let's take a look at the interaction between all of the costs (A,B,C) per state. We generate linear models with different data sets to gain multiple insights. Notice that error is being considered and added to the total cost, as seen in the data sets provided.

## Appendix 3.1 Model 1

With the weights per factor A  $\rightarrow$  0.70, B  $\rightarrow$  0.15,C  $\rightarrow$  0.15

See dataset used below:

Table 1: M1\_Data

State_ID	A	В	С	Error	Total_Cost
AL	1594.53	104.43	588.84	-74.99	1145.17
AK	2259.97	122.89	393.78	-47.32	1612.16
ΑZ	954.37	111.20	431.73	39.06	788.55
AR	931.80	141.87	249.40	45.79	756.74
CA	857.33	153.38	484.82	31.99	727.85
CO	1453.55	138.10	358.18	-106.83	985.10
CT	1246.11	185.92	483.35	-49.96	922.71
DE	1780.28	189.15	421.86	90.52	1428.36
FL	1492.55	140.77	464.32	10.09	1145.64
GA	1465.55	116.38	490.41	-154.11	962.79
HI	910.70	217.17	376.87	-152.38	574.21
ID	1211.35	48.62	350.52	435.93	1343.74
IL	1057.05	118.42	502.71	111.71	944.82
IN	2016.91	95.60	554.17	333.95	1843.26
IA	1285.52	82.58	427.60	43.52	1019.91
KS	1591.34	132.12	253.67	-119.60	1052.20
KY	1535.39	48.95	358.66	246.42	1382.33
LA	1712.72	57.20	452.73	-39.53	1235.87
ME	1594.78	107.60	345.89	214.93	1399.30
MD	701.06	63.82	522.92	-151.95	426.80
MA	1029.61	145.55	325.05	279.57	1070.89
MI	2538.05	75.50	415.19	134.32	1984.55
MN	1677.14	187.37	206.34	-177.23	1055.82
MS	1122.35	110.09	350.56	102.90	957.64
MO	1032.29	119.12	452.46	-129.18	679.16
MT	1620.01	97.69	290.73	-157.86	1034.41
NE	258.94	186.39	337.28	-128.88	130.93
NV	733.30	87.25	411.85	-109.82	478.36
NH	699.78	72.22	590.32	185.31	774.54
NJ	1172.15	99.46	583.98	38.91	961.93
NM	521.42	80.62	429.80	218.22	659.78
NY	556.41	165.97	366.54	-69.08	400.29
NC	517.26	68.15	445.26	-9.63	429.46
ND	438.47	186.50	151.41	-43.78	313.84
OH	331.12	183.50	291.83	104.01	407.10
OK	434.05	201.28	240.21	-129.09	240.97
OR	479.14	154.61	476.62	-96.87	333.22
PA	667.03	135.05	369.33	32.55	575.13

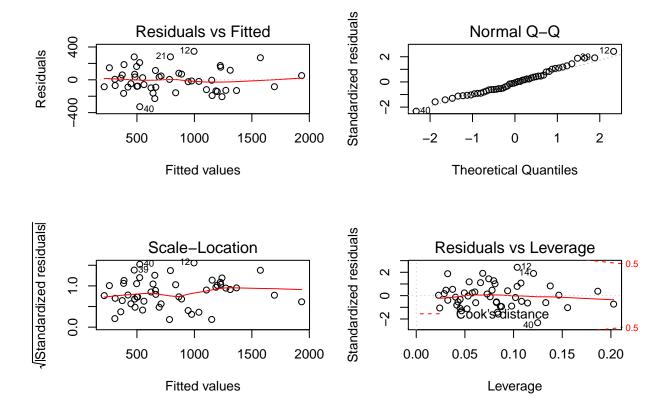
State_ID	A	В	С	Error	Total_Cost
RI	516.67	130.18	528.25	294.88	755.32
SC	566.61	59.24	320.34	-256.93	196.64
SD	568.88	113.20	305.38	56.94	517.94
TN	482.11	74.65	464.36	129.79	548.12
TX	700.27	143.84	338.94	-60.33	502.27
UT	621.44	103.06	281.04	240.98	733.61
VT	550.91	115.41	465.21	-52.33	420.40
VA	438.32	144.00	258.52	12.27	379.47
WA	395.00	109.87	420.48	-137.17	218.88
WV	487.61	204.44	376.18	3.43	431.85
WI	664.26	120.95	708.42	-64.96	524.43
WY	469.10	183.22	444.36	150.42	572.93

We are now able to identify a linear model from the above data that depends on variables A,B and C with the results displayed as follows.

```
par(mfrow=c(2,2))
M1<-lm(Total_Cost ~ A+B+C, data = M1_Data)
summary(M1)
```

```
##
## Call:
## lm(formula = Total_Cost ~ A + B + C, data = M1_Data)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
                    -9.56
   -327.99 -96.02
                            77.43 346.92
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 104.20753
                        133.38293
                                      0.781
                                               0.439
                                              <2e-16 ***
## A
                            0.04038
                                    17.616
                 0.71137
## B
                -0.73504
                            0.52447
                                     -1.401
                                               0.168
## C
                 0.19008
                            0.20780
                                     0.915
                                               0.365
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 151.1 on 46 degrees of freedom
## Multiple R-squared: 0.8833, Adjusted R-squared: 0.8756
                 116 on 3 and 46 DF, p-value: < 2.2e-16
## F-statistic:
```

plot(M1)



The results of the linear model M1 provide evidence that variable A displays a linear relationship with total cost, with a significance level of 0.05. Furthermore, the Adjusted R-squared provides insight on how well the model fits with the data collected. As displayed in the graphs above, the errors and different metrics confirm to be unbiased and follow Gaussian assumptions. The Residuals vs Fitted display errors with a 0 mean and the Normal Q-Q displays the model following Gaussian assumptions which allow us to apply hypothesis tests like *t*-tests.

### Appendix 3.2 Model 2

With the weights per factor A -> 0.95,B -> 0.025, C -> 0.025

See dataset used below:

## The following objects are masked from M1\_Data:

##

## A, B, C, Error, State\_ID, Total\_Cost

Table 2: M2 Data

State_ID	A	В	С	Error	Total_Cost
AL	1594.53	104.43	588.84	-74.99	1457.14
AK	2259.97	122.89	393.78	-47.32	2112.57
ΑZ	954.37	111.20	431.73	39.06	959.28
AR	931.80	141.87	249.40	45.79	940.78
CA	857.33	153.38	484.82	31.99	862.41
CO	1453.55	138.10	358.18	-106.83	1286.45

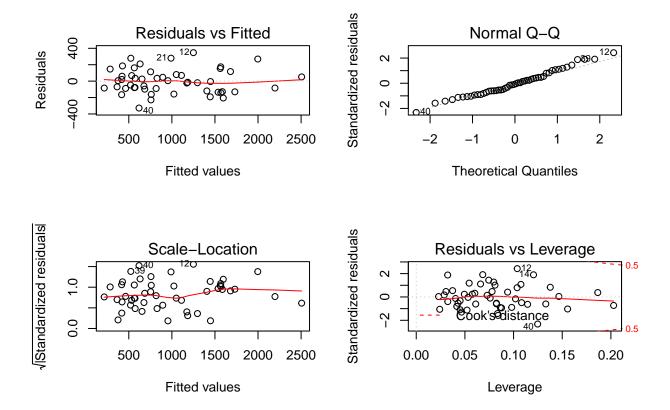
State_ID	A	В	С	Error	Total_Cost
CT	1246.11	185.92	483.35	-49.96	1150.58
DE	1780.28	189.15	421.86	90.52	1797.06
FL	1492.55	140.77	464.32	10.09	1443.14
GA	1465.55	116.38	490.41	-154.11	1253.33
HI	910.70	217.17	376.87	-152.38	727.63
ID	1211.35	48.62	350.52	435.93	1596.69
IL	1057.05	118.42	502.71	111.71	1131.44
IN	2016.91	95.60	554.17	333.95	2266.26
IA	1285.52	82.58	427.60	43.52	1277.52
KS	1591.34	132.12	253.67	-119.60	1401.82
KY	1535.39	48.95	358.66	246.42	1715.23
LA	1712.72	57.20	452.73	-39.53	1600.31
ME	1594.78	107.60	345.89	214.93	1741.31
MD	701.06	63.82	522.92	-151.95	528.72
MA	1029.61	145.55	325.05	279.57	1269.47
MI	2538.05	75.50	415.19	134.32	2557.73
MN	1677.14	187.37	206.34	-177.23	1425.89
MS	1122.35	110.09	350.56	102.90	1180.65
MO	1032.29	119.12	452.46	-129.18	865.78
MT	1620.01	97.69	290.73	-157.86	1390.86
NE	258.94	186.39	337.28	-128.88	130.21
NV	733.30	87.25	411.85	-109.82	599.29
NH	699.78	72.22	590.32	185.31	866.67
NJ	1172.15	99.46	583.98	38.91	1169.54
NM	521.42	80.62	429.80	218.22	726.33
NY	556.41	165.97	366.54	-69.08	472.83
NC	517.26	68.15	445.26	-9.63	494.60
ND	438.47	186.50	151.41	-43.78	381.21
ОН	331.12	183.50	291.83	104.01	430.46
OK	434.05	201.28	240.21	-129.09	294.30
OR	479.14	154.61	476.62	-96.87	374.10
PA	667.03	135.05	369.33	32.55	678.84
RI	516.67	130.18	528.25	294.88	802.18
SC	566.61	59.24	320.34	-256.93	290.84
SD	568.88	113.20	305.38	56.94	607.84
TN	482.11	74.65	464.36	129.79	601.27
TX	700.27	143.84	338.94	-60.33	616.99
UT	621.44	103.06	281.04	240.98	840.96
VT	550.91	115.41	465.21	-52.33	485.55
VA	438.32	144.00	258.52	12.27	438.74
WA	395.00	109.87	420.48	-137.17	251.34
WV	487.61	204.44	376.18	3.43	481.17
WI	664.26	120.95	708.42	-64.96	586.82
WY	469.10	183.22	444.36	150.42	611.76

We are now able to identify a linear model from the above data that depends on variables A,B and C with the results displayed as follows.

```
par(mfrow=c(2,2))
M2<-lm(Total_Cost ~ A+B+C, data = M2_Data)
summary(M2)</pre>
```

```
##
##
  Call:
##
   lm(formula = Total_Cost ~ A + B + C, data = M2_Data)
##
##
   Residuals:
                                 3Q
##
       Min
                 1Q
                    Median
                                         Max
            -96.02
                      -9.56
                              77.43
                                      346.92
##
   -327.99
##
##
   Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
##
   (Intercept) 104.20947
                           133.38346
                                        0.781
                                                 0.439
                  0.96137
                             0.04038
                                       23.806
                                                <2e-16
##
##
  В
                 -0.86004
                             0.52447
                                       -1.640
                                                 0.108
  C
                                        0.313
##
                  0.06508
                             0.20780
                                                 0.756
##
                            0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 151.1 on 46 degrees of freedom
## Multiple R-squared: 0.9314, Adjusted R-squared:
## F-statistic: 208.1 on 3 and 46 DF, p-value: < 2.2e-16
```

#### plot(M2)



The results of the linear model M2 provide evidence that variable A displays a linear relationship with total cost, with a significance level of 0.05. The p values associated with each variable can be compared with those in resulting in M1. Furthermore, the Adjusted R-squared provides insight on how well the model fits with the data collected, as seen the M2

linear model has a higher value than the one in M1. As displayed in the graphs above, the errors and different metrics confirm to be unbiased and follow Gaussian assumptions. The Residuals vs Fitted display errors with a 0 mean and the Normal Q-Q displays the model following Gaussian assumptions which allow us to apply hypothesis tests like *t*-tests.

## Appendix 3.3 Model 3

This model uses model M1 as base and violates the Gaussian distribution of error. When generating the data we added a variance following a uniform distribution.

See dataset used below:

```
## The following objects are masked from M2_Data:
##
## A, B, C, Error, State_ID, Total_Cost
## The following objects are masked from M1_Data:
##
## A, B, C, Error, State_ID, Total_Cost
```

Table 3: M3\_Data

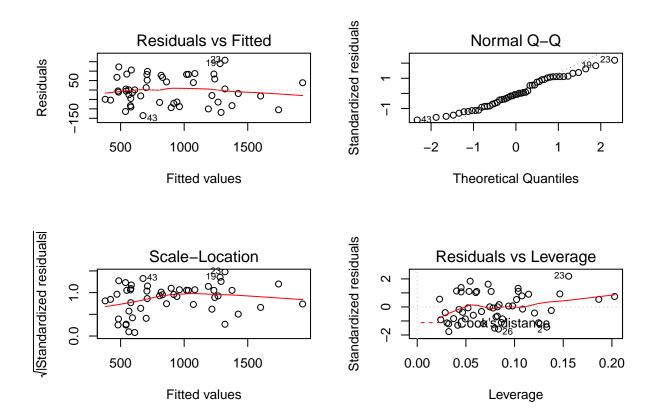
State_ID	A	В	С	Error	Total_Cost
AL	1594.53	104.43	588.84	106	1326.16
AK	2259.97	122.89	393.78	-22	1637.48
AZ	954.37	111.20	431.73	155	904.50
AR	931.80	141.87	249.40	186	896.95
CA	857.33	153.38	484.82	45	740.86
CO	1453.55	138.10	358.18	-2	1089.93
CT	1246.11	185.92	483.35	139	1111.67
DE	1780.28	189.15	421.86	69	1406.85
FL	1492.55	140.77	464.32	183	1318.55
GA	1465.55	116.38	490.41	72	1188.90
HI	910.70	217.17	376.87	170	896.60
ID	1211.35	48.62	350.52	194	1101.82
IL	1057.05	118.42	502.71	46	879.10
IN	2016.91	95.60	554.17	60	1569.30
IA	1285.52	82.58	427.60	195	1171.39
KS	1591.34	132.12	253.67	31	1202.81
KY	1535.39	48.95	358.66	163	1298.91
LA	1712.72	57.20	452.73	18	1293.39
ME	1594.78	107.60	345.89	238	1422.37
MD	701.06	63.82	522.92	135	713.75
MA	1029.61	145.55	325.05	13	804.32
MI	2538.05	75.50	415.19	120	1970.24
MN	1677.14	187.37	206.34	246	1479.05
MS	1122.35	110.09	350.56	20	874.74
MO	1032.29	119.12	452.46	39	847.34
MT	1620.01	97.69	290.73	-21	1171.27
NE	258.94	186.39	337.28	70	329.81
NV	733.30	87.25	411.85	201	789.18
NH	699.78	72.22	590.32	221	810.23
NJ	1172.15	99.46	583.98	193	1116.02

State_ID	A	В	C	Error	Total_Cost
NM	521.42	80.62	429.80	99	540.56
NY	556.41	165.97	366.54	221	690.36
NC	517.26	68.15	445.26	126	565.09
ND	438.47	186.50	151.41	181	538.62
OH	331.12	183.50	291.83	64	367.08
OK	434.05	201.28	240.21	102	472.06
OR	479.14	154.61	476.62	203	633.08
PA	667.03	135.05	369.33	84	626.58
RI	516.67	130.18	528.25	30	490.43
SC	566.61	59.24	320.34	41	494.56
SD	568.88	113.20	305.38	74	535.00
TN	482.11	74.65	464.36	120	538.33
TX	700.27	143.84	338.94	-22	540.61
UT	621.44	103.06	281.04	119	611.62
VT	550.91	115.41	465.21	107	579.73
VA	438.32	144.00	258.52	241	608.20
WA	395.00	109.87	420.48	119	475.05
WV	487.61	204.44	376.18	118	546.42
WI	664.26	120.95	708.42	172	761.39
WY	469.10	183.22	444.36	2	424.51

We are now able to identify a linear model from the above data that depends on variables A,B and C with the results displayed as follows.

```
par(mfrow=c(2,2))
M3<-lm(Total_Cost ~ A+B+C, data = M3_Data)
summary(M3)</pre>
```

```
##
## Call:
## lm(formula = Total_Cost ~ A + B + C, data = M3_Data)
##
## Residuals:
       Min
##
                 1Q
                     Median
                                   3Q
                                           Max
## -135.736 -64.054
                     -5.291
                               67.101 158.025
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                          69.27845
## (Intercept) 138.28601
                                    1.996
                                             0.0519 .
## A
                0.67879
                           0.02097 32.362
                                             <2e-16 ***
## B
                0.06144
                           0.27241
                                     0.226
                                             0.8226
## C
                0.15899
                           0.10793
                                     1.473
                                             0.1475
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 78.49 on 46 degrees of freedom
## Multiple R-squared: 0.9604, Adjusted R-squared: 0.9578
## F-statistic: 371.6 on 3 and 46 DF, p-value: < 2.2e-16
```



As displayed in the graphs above, the errors and different metrics do not confirm to be unbiased and do not follow Gaussian assumptions. The Residuals vs Fitted display errors with a mean not equal to 0 and the Normal Q-Q displays the model not following Gaussian assumptions which does not allow us to apply hypothesis tests like *t*-tests. That being said we are still able to retrieve a linear model even without strong assumptions being held.

#### Appendix 3.4 Model 4

Violating linear model with different weights of each cost given to different groups of states.

See dataset used below:

```
## The following objects are masked from M3_Data:
##
## A, B, C, Error, State_ID, Total_Cost

## The following objects are masked from M2_Data:
##
## A, B, C, Error, State_ID, Total_Cost

## The following objects are masked from M1_Data:
##
## A, B, C, Error, State_ID, Total_Cost
```

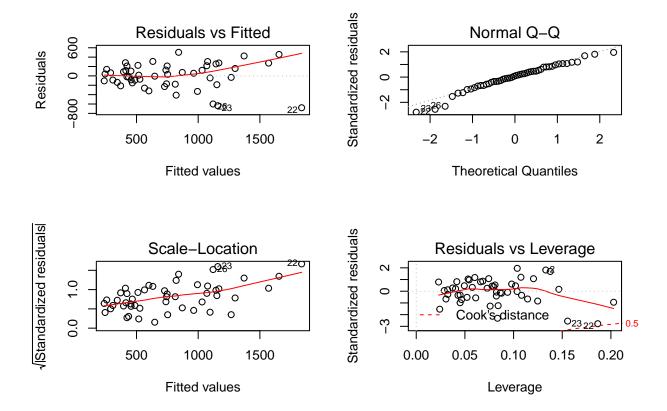
Table 4: M4\_Data

AL 1594.53 104.43 588.84 -74.99 1457.15 0.95 0.025 AK 2259.97 122.89 393.78 -47.32 2112.57 0.95 0.025 AZ 954.37 111.20 431.73 39.06 959.28 0.95 0.025 AR 931.80 141.87 249.40 45.79 940.78 0.95 0.025 CA 857.33 153.38 484.82 31.99 862.41 0.95 0.025 CO 1453.55 138.10 358.18 -106.83 1286.45 0.95 0.025 CT 1246.11 185.92 483.35 -49.96 1150.58 0.95 0.025 DE 1780.28 189.15 421.86 90.52 1797.06 0.95 0.025 FL 1492.55 140.77 464.32 10.09 1443.14 0.95 0.025 GA 1465.55 116.38 490.41 -154.11 962.79 0.70 0.150 HI 910.70 217.17 376.87 -152.38 574.22 0.70 0.150 IL 1057.05 118.42 502.71 111.71 944.81 0.70 0.150 IL 1057.05 118.42 502.71 111.71 944.81 0.70 0.150 IN 2016.91 95.60 554.17 333.95 1843.25 0.70 0.150 KS 1591.34 132.12 253.67 -119.60 1052.21 0.70 0.150 KS 1591.34 132.12 253.67 -119.60 1052.21 0.70 0.150 KS 1594.78 107.60 345.89 214.93 1399.30 0.70 0.150 MA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 MA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 52.92 0.34 0.330 MN 521.42 80.62 429.80 218.22 633.16 0.60 0.200 NY 556.41 165.97 366.54 -69.08 371.27 0.60 0.200 NY 556.41 165.97 366.54 -69.08 371.27 0.60	0.025 0.025 0.025
AK 2259.97 122.89 393.78 -47.32 2112.57 0.95 0.025 AZ 954.37 111.20 431.73 39.06 959.28 0.95 0.025 AR 931.80 141.87 249.40 45.79 940.78 0.95 0.025 CA 857.33 153.38 484.82 31.99 862.41 0.95 0.025 CO 1453.55 138.10 358.18 -106.83 1286.45 0.95 0.025 CT 1246.11 185.92 483.35 -49.96 1150.58 0.95 0.025 DE 1780.28 189.15 421.86 90.52 1797.06 0.95 0.025 FL 1492.55 140.77 464.32 10.09 1443.14 0.95 0.025 GA 1465.55 116.38 490.41 -154.11 962.79 0.70 0.150 HI 910.70 217.17 376.87 -152.38 574.22 0.70 0.150 IL 1057.05 118.42 502.71 111.71 944.81 0.70 0.150 IN 2016.91 95.60 554.17 333.95 1843.25 0.70 0.150 IA 1285.52 82.58 427.60 43.52 1019.91 0.70 0.150 KS 1591.34 132.12 253.67 -119.60 1052.21 0.70 0.150 KY 1535.39 48.95 358.66 246.42 1382.33 0.70 0.150 ME 1594.78 107.60 345.89 214.93 1399.30 0.70 0.150 MA 1029.61 145.55 325.05 415.19 39.30 0.70 0.150 MM 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MM 1679.8 72.22 590.32 185.31 641.87 0.34 0.330 NM 1679.8 72.22 590.32 185.31 641.87 0.34 0.330 NM 521.42 80.62 429.80 218.22 633.16 0.60 0.200 NM 551.42 80.62 429.80 218.22 633.16 0.60 0.200 NM 551.42 80.62 429.80 218.22 633.16 0.60 0.200 NM 556.41 165.97 366.54 -69.08 371.27 0.60 0.200 NM 538.47 186.50 151.41 -43.78 286.88 0.60 0.200	
AZ 954.37 111.20 431.73 39.06 959.28 0.95 0.025 AR 931.80 141.87 249.40 45.79 940.78 0.95 0.025 CA 857.33 153.38 484.82 31.99 862.41 0.95 0.025 CO 1453.55 138.10 358.18 -106.83 1286.45 0.95 0.025 CT 1246.11 185.92 483.35 -49.96 1150.58 0.95 0.025 DE 1780.28 189.15 421.86 90.52 1797.06 0.95 0.025 FL 1492.55 140.77 464.32 10.09 1443.14 0.95 0.025 GA 1465.55 116.38 490.41 -154.11 962.79 0.70 0.150 HI 910.70 217.17 376.87 -152.38 574.22 0.70 0.150 ID 1211.35 48.62 350.52 435.93 1343.75 0.70 0.150 IL 1057.05 118.42 502.71 111.71 944.81 0.70 0.150 IN 2016.91 95.60 554.17 333.95 1843.25 0.70 0.150 IA 1285.52 82.58 427.60 43.52 1019.91 0.70 0.150 KS 1591.34 132.12 253.67 -119.60 1052.21 0.70 0.150 KY 1535.39 48.95 358.66 246.42 1382.33 0.70 0.150 KAY 1535.39 48.95 358.66 246.42 1382.33 0.70 0.150 MB 1594.78 107.60 345.89 214.93 1399.30 0.70 0.330 MA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 MA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MN 1677.15 188.25 110.09 350.56 102.90 636.51 0.34 0.330 MN 1677.15 188.25 110.09 350.56 102.90 636.51 0.34 0.330 MN 1677.15 188.35 110.99 350.56 102.90 636.51 0.34 0.330 MN 1677.15 188.35 110.99 350.56 102.90 636.51 0.34 0.330 MN 1677.14 187.37 206.34 -178.88 131.97 0.34 0.330 NN 733.30 87.25 411.85 -109.82 304.21 0.34 0.330 NN 733.30 87.25 411.85 -109.82 304.21 0.34 0.330 NN 521.42 80.62 429.80 218.22 633.16 0.60 0.200 NN 556.41 165.97 366.54 -69.08 371.27 0.60 0.200 ND 438.47	
AR 931.80 141.87 249.40 45.79 940.78 0.95 0.025 CA 857.33 153.38 484.82 31.99 862.41 0.95 0.025 CO 1453.55 138.10 358.18 -106.83 1286.45 0.95 0.025 CT 1246.11 185.92 483.35 -49.96 1150.58 0.95 0.025 DE 1780.28 189.15 421.86 90.52 1797.06 0.95 0.025 FL 1492.55 140.77 464.32 10.09 1443.14 0.95 0.025 GA 1465.55 116.38 490.41 -154.11 962.79 0.70 0.150 HI 910.70 217.17 376.87 -152.38 574.22 0.70 0.150 ID 1211.35 48.62 350.52 435.93 1343.75 0.70 0.150 III 1057.05 118.42 502.71 111.71 944.81 0.70 0.150 IIN 2016.91 95.60 554.17 333.95 1843.25 0.70 0.150 IA 1285.52 82.58 427.60 43.52 1019.91 0.70 0.150 KS 1591.34 132.12 253.67 -119.60 1052.21 0.70 0.150 KY 1535.39 48.95 358.66 246.42 1382.33 0.70 0.150 KY 1535.39 48.95 358.66 246.42 1382.33 0.70 0.150 ME 1594.78 107.60 345.89 214.93 1399.30 0.70 0.150 MB 1594.78 107.60 345.89 214.93 1399.30 0.70 0.150 MA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 MA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MN 1677.15 99.46 583.98 38.91 662.98 0.34 0.330 NV 733.30 87.25 411.85 -109.82 304.21 0.34 0.330 NV 733.30 87.25 411.85 -109.82 304.21 0.34 0.330 NM 521.42 80.62 429.80 218.22 633.16 0.60 0.200 NC 517.26 68.15 445.26 -9.63 403.41 0.60 0.200 NC 517.26 68.15 445.26 -9.63 403.41 0.60 0.200 ND 438.47 186.50 151.41 -43.78 286.88 0.60 0.200	0.043
CA         857.33         153.38         484.82         31.99         862.41         0.95         0.025           CO         1453.55         138.10         358.18         -106.83         1286.45         0.95         0.025           CT         1246.11         185.92         483.35         -49.96         1150.58         0.95         0.025           DE         1780.28         189.15         421.86         90.52         1797.06         0.95         0.025           FL         1492.55         140.77         464.32         10.09         1443.14         0.95         0.025           GA         1465.55         116.38         490.41         -154.11         962.79         0.70         0.150           HI         910.70         217.17         376.87         -152.38         574.22         0.70         0.150           ID         1211.35         48.62         350.52         435.93         1343.75         0.70         0.150           IL         1057.05         118.42         502.71         111.71         944.81         0.70         0.150           IA         1285.52         82.58         427.60         43.52         1019.91         0.70         0.150	0.025
CO         1453.55         138.10         358.18         -106.83         1286.45         0.95         0.025           CT         1246.11         185.92         483.35         -49.96         1150.58         0.95         0.025           DE         1780.28         189.15         421.86         90.52         1797.06         0.95         0.025           FL         1492.55         140.77         464.32         10.09         1443.14         0.95         0.025           GA         1465.55         116.38         490.41         -154.11         962.79         0.70         0.150           HI         910.70         217.17         376.87         -152.38         574.22         0.70         0.150           ID         1211.35         48.62         350.52         435.93         1343.75         0.70         0.150           IL         1057.05         118.42         502.71         111.71         944.81         0.70         0.150           IN         2016.91         95.60         554.17         333.95         1843.25         0.70         0.150           KS         1591.34         132.12         253.67         -119.60         1052.21         0.70         0.150 <td>0.025</td>	0.025
CT         1246.11         185.92         483.35         -49.96         1150.58         0.95         0.025           DE         1780.28         189.15         421.86         90.52         1797.06         0.95         0.025           FL         1492.55         140.77         464.32         10.09         1443.14         0.95         0.025           GA         1465.55         116.38         490.41         -154.11         962.79         0.70         0.150           HI         910.70         217.17         376.87         -152.38         574.22         0.70         0.150           ID         1211.35         48.62         350.52         435.93         1343.75         0.70         0.150           IL         1057.05         118.42         502.71         111.71         944.81         0.70         0.150           IN         2016.91         95.60         554.17         333.95         1843.25         0.70         0.150           IA         1285.52         82.58         427.60         43.52         1019.91         0.70         0.150           KS         1591.34         132.12         253.67         -119.60         1052.21         0.70         0.150	0.025
DE         1780.28         189.15         421.86         90.52         1797.06         0.95         0.025           FL         1492.55         140.77         464.32         10.09         1443.14         0.95         0.025           GA         1465.55         116.38         490.41         -154.11         962.79         0.70         0.150           HI         910.70         217.17         376.87         -152.38         574.22         0.70         0.150           ID         1211.35         48.62         350.52         435.93         1343.75         0.70         0.150           IL         1057.05         118.42         502.71         111.71         944.81         0.70         0.150           IN         2016.91         95.60         554.17         333.95         1843.25         0.70         0.150           IA         1285.52         82.58         427.60         43.52         1019.91         0.70         0.150           KS         1591.34         132.12         253.67         -119.60         1052.21         0.70         0.150           KY         1535.39         48.95         358.66         246.42         1382.33         0.70         0.150	0.025
FL 1492.55 140.77 464.32 10.09 1443.14 0.95 0.025 GA 1465.55 116.38 490.41 -154.11 962.79 0.70 0.150 HI 910.70 217.17 376.87 -152.38 574.22 0.70 0.150 ID 1211.35 48.62 350.52 435.93 1343.75 0.70 0.150 IL 1057.05 118.42 502.71 111.71 944.81 0.70 0.150 IN 2016.91 95.60 554.17 333.95 1843.25 0.70 0.150 KS 1591.34 132.12 253.67 -119.60 1052.21 0.70 0.150 KY 1535.39 48.95 358.66 246.42 1382.33 0.70 0.150 ME 1594.78 107.60 345.89 214.93 1399.30 0.70 0.150 MD 701.06 63.82 522.92 -151.95 280.03 0.34 0.330 MA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MN 1620.35 110.09 350.56 102.90 636.51 0.34 0.330 MN 1620.01 97.69 290.73 -157.86 521.12 0.34 0.330 MT 1620.01 97.69 290.73 -157.86 521.12 0.34 0.330 NN 733.30 87.25 411.85 -109.82 304.21 0.34 0.330 NN 521.42 80.62 429.80 218.22 633.16 0.60 0.200 NN 556.41 165.97 366.54 -69.08 371.27 0.60 0.200 NN 556.41 165.97 366.54 -69.08 371.27 0.60 0.200 NN 556.41 165.97 366.54 -69.08 371.27 0.60 0.200 ND 438.47 186.50 151.41 -43.78 286.88 0.60 0.200	0.025
GA         1465.55         116.38         490.41         -154.11         962.79         0.70         0.150           HI         910.70         217.17         376.87         -152.38         574.22         0.70         0.150           ID         1211.35         48.62         350.52         435.93         1343.75         0.70         0.150           IL         1057.05         118.42         502.71         111.71         944.81         0.70         0.150           IN         2016.91         95.60         554.17         333.95         1843.25         0.70         0.150           IA         1285.52         82.58         427.60         43.52         1019.91         0.70         0.150           KS         1591.34         132.12         253.67         -119.60         1052.21         0.70         0.150           KY         1535.39         48.95         358.66         246.42         1382.33         0.70         0.150           KY         1535.39         48.95         214.93         1399.30         0.70         0.150           ME         1594.78         107.60         345.89         214.93         1399.30         0.70         0.150	0.025
HI 910.70 217.17 376.87 -152.38 574.22 0.70 0.150 ID 1211.35 48.62 350.52 435.93 1343.75 0.70 0.150 IIL 1057.05 118.42 502.71 111.71 944.81 0.70 0.150 IN 2016.91 95.60 554.17 333.95 1843.25 0.70 0.150 IA 1285.52 82.58 427.60 43.52 1019.91 0.70 0.150 KS 1591.34 132.12 253.67 -119.60 1052.21 0.70 0.150 KY 1535.39 48.95 358.66 246.42 1382.33 0.70 0.150 LA 1712.72 57.20 452.73 -39.53 1235.86 0.70 0.150 ME 1594.78 107.60 345.89 214.93 1399.30 0.70 0.150 MD 701.06 63.82 522.92 -151.95 280.03 0.34 0.330 MA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MS 1122.35 110.09 350.56 102.90 636.51 0.34 0.330 MT 1620.01 97.69 290.73 -157.86 521.12 0.34 0.330 NT 1620.01 97.69 290.73 -157.86 521.12 0.34 0.330 NT 1620.01 97.69 290.73 -157.86 521.12 0.34 0.330 NT 699.78 72.22 590.32 185.31 641.87 0.34 0.330 NT 172.15 99.46 583.98 38.91 662.98 0.34 0.330 NM 521.42 80.62 429.80 218.22 633.16 0.60 0.200 NT 517.26 68.15 445.26 -9.63 403.41 0.60 0.200 ND 438.47 186.50 151.41 -43.78 286.88 0.60 0.200 ND 438.47 186.50 151.41 -43.78 286.88 0.60 0.200	0.150
ID	0.150
IL 1057.05 118.42 502.71 111.71 944.81 0.70 0.150 IN 2016.91 95.60 554.17 333.95 1843.25 0.70 0.150 IA 1285.52 82.58 427.60 43.52 1019.91 0.70 0.150 KS 1591.34 132.12 253.67 -119.60 1052.21 0.70 0.150 KY 1535.39 48.95 358.66 246.42 1382.33 0.70 0.150 IA 1712.72 57.20 452.73 -39.53 1235.86 0.70 0.150 IA 1594.78 107.60 345.89 214.93 1399.30 0.70 0.150 IA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 IA 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 IA 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 IA 1122.35 110.09 350.56 102.90 636.51 0.34 0.330 IA 0.330 IA 1620.01 97.69 290.73 -157.86 521.12 0.34 0.330 IA 0.330 IA 1620.01 97.69 290.73 -157.86 521.12 0.34 0.330 IA 0.3	0.150
IN 2016.91 95.60 554.17 333.95 1843.25 0.70 0.150 IA 1285.52 82.58 427.60 43.52 1019.91 0.70 0.150 KS 1591.34 132.12 253.67 -119.60 1052.21 0.70 0.150 KY 1535.39 48.95 358.66 246.42 1382.33 0.70 0.150 LA 1712.72 57.20 452.73 -39.53 1235.86 0.70 0.150 ME 1594.78 107.60 345.89 214.93 1399.30 0.70 0.150 MD 701.06 63.82 522.92 -151.95 280.03 0.34 0.330 MA 1029.61 145.55 325.05 279.57 784.94 0.34 0.330 MI 2538.05 75.50 415.19 134.32 1159.18 0.34 0.330 MN 1677.14 187.37 206.34 -177.23 522.92 0.34 0.330 MS 1122.35 110.09 350.56 102.90 636.51 0.34 0.330 MO 1032.29 119.12 452.46 -129.18 410.42 0.34 0.330 MT 1620.01 97.69 290.73 -157.86 521.12 0.34 0.330 NF 258.94 186.39 337.28 -128.88 131.97 0.34 0.330 NF 258.94 186.39 337.28 -128.88 131.97 0.34 0.330 NF 699.78 72.22 590.32 185.31 641.87 0.34 0.330 NH 699.78 72.22 590.32 185.31 641.87 0.34 0.330 NM 521.42 80.62 429.80 218.22 633.16 0.60 0.200 NY 556.41 165.97 366.54 -69.08 371.27 0.60 0.200 NC 517.26 68.15 445.26 -9.63 403.41 0.60 0.200 ND 438.47 186.50 151.41 -43.78 286.88 0.60 0.200	0.150
IA         1285.52         82.58         427.60         43.52         1019.91         0.70         0.150           KS         1591.34         132.12         253.67         -119.60         1052.21         0.70         0.150           KY         1535.39         48.95         358.66         246.42         1382.33         0.70         0.150           LA         1712.72         57.20         452.73         -39.53         1235.86         0.70         0.150           ME         1594.78         107.60         345.89         214.93         1399.30         0.70         0.150           MD         701.06         63.82         522.92         -151.95         280.03         0.34         0.330           MA         1029.61         145.55         325.05         279.57         784.94         0.34         0.330           MI         2538.05         75.50         415.19         134.32         1159.18         0.34         0.330           MN         1677.14         187.37         206.34         -177.23         522.92         0.34         0.330           MS         1122.35         110.09         350.56         102.90         636.51         0.34         0.330	0.150
KS         1591.34         132.12         253.67         -119.60         1052.21         0.70         0.150           KY         1535.39         48.95         358.66         246.42         1382.33         0.70         0.150           LA         1712.72         57.20         452.73         -39.53         1235.86         0.70         0.150           ME         1594.78         107.60         345.89         214.93         1399.30         0.70         0.150           MD         701.06         63.82         522.92         -151.95         280.03         0.34         0.330           MA         1029.61         145.55         325.05         279.57         784.94         0.34         0.330           MI         2538.05         75.50         415.19         134.32         1159.18         0.34         0.330           MN         1677.14         187.37         206.34         -177.23         522.92         0.34         0.330           MS         1122.35         110.09         350.56         102.90         636.51         0.34         0.330           MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330	0.150
KY       1535.39       48.95       358.66       246.42       1382.33       0.70       0.150         LA       1712.72       57.20       452.73       -39.53       1235.86       0.70       0.150         ME       1594.78       107.60       345.89       214.93       1399.30       0.70       0.150         MD       701.06       63.82       522.92       -151.95       280.03       0.34       0.330         MA       1029.61       145.55       325.05       279.57       784.94       0.34       0.330         MI       2538.05       75.50       415.19       134.32       1159.18       0.34       0.330         MN       1677.14       187.37       206.34       -177.23       522.92       0.34       0.330         MS       1122.35       110.09       350.56       102.90       636.51       0.34       0.330         MO       1032.29       119.12       452.46       -129.18       410.42       0.34       0.330         MT       1620.01       97.69       290.73       -157.86       521.12       0.34       0.330         NV       733.30       87.25       411.85       -109.82       304.21	0.150
LA         1712.72         57.20         452.73         -39.53         1235.86         0.70         0.150           ME         1594.78         107.60         345.89         214.93         1399.30         0.70         0.150           MD         701.06         63.82         522.92         -151.95         280.03         0.34         0.330           MA         1029.61         145.55         325.05         279.57         784.94         0.34         0.330           MI         2538.05         75.50         415.19         134.32         1159.18         0.34         0.330           MN         1677.14         187.37         206.34         -177.23         522.92         0.34         0.330           MS         1122.35         110.09         350.56         102.90         636.51         0.34         0.330           MO         1032.29         119.12         452.46         -129.18         410.42         0.34         0.330           MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330           NE         258.94         186.39         337.28         -128.88         131.97         0.34         0.330	0.150
ME         1594.78         107.60         345.89         214.93         1399.30         0.70         0.150           MD         701.06         63.82         522.92         -151.95         280.03         0.34         0.330           MA         1029.61         145.55         325.05         279.57         784.94         0.34         0.330           MI         2538.05         75.50         415.19         134.32         1159.18         0.34         0.330           MN         1677.14         187.37         206.34         -177.23         522.92         0.34         0.330           MS         1122.35         110.09         350.56         102.90         636.51         0.34         0.330           MO         1032.29         119.12         452.46         -129.18         410.42         0.34         0.330           MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330           NE         258.94         186.39         337.28         -128.88         131.97         0.34         0.330           NV         733.30         87.25         411.85         -109.82         304.21         0.34         0.330	0.150
MD         701.06         63.82         522.92         -151.95         280.03         0.34         0.330           MA         1029.61         145.55         325.05         279.57         784.94         0.34         0.330           MI         2538.05         75.50         415.19         134.32         1159.18         0.34         0.330           MN         1677.14         187.37         206.34         -177.23         522.92         0.34         0.330           MS         1122.35         110.09         350.56         102.90         636.51         0.34         0.330           MO         1032.29         119.12         452.46         -129.18         410.42         0.34         0.330           MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330           NE         258.94         186.39         337.28         -128.88         131.97         0.34         0.330           NV         733.30         87.25         411.85         -109.82         304.21         0.34         0.330           NH         699.78         72.22         590.32         185.31         641.87         0.34         0.330 </td <td>0.150</td>	0.150
MA         1029.61         145.55         325.05         279.57         784.94         0.34         0.330           MI         2538.05         75.50         415.19         134.32         1159.18         0.34         0.330           MN         1677.14         187.37         206.34         -177.23         522.92         0.34         0.330           MS         1122.35         110.09         350.56         102.90         636.51         0.34         0.330           MO         1032.29         119.12         452.46         -129.18         410.42         0.34         0.330           MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330           NE         258.94         186.39         337.28         -128.88         131.97         0.34         0.330           NV         733.30         87.25         411.85         -109.82         304.21         0.34         0.330           NH         699.78         72.22         590.32         185.31         641.87         0.34         0.330           NJ         1172.15         99.46         583.98         38.91         662.98         0.34         0.330 <td>0.330</td>	0.330
MI         2538.05         75.50         415.19         134.32         1159.18         0.34         0.330           MN         1677.14         187.37         206.34         -177.23         522.92         0.34         0.330           MS         1122.35         110.09         350.56         102.90         636.51         0.34         0.330           MO         1032.29         119.12         452.46         -129.18         410.42         0.34         0.330           MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330           NE         258.94         186.39         337.28         -128.88         131.97         0.34         0.330           NV         733.30         87.25         411.85         -109.82         304.21         0.34         0.330           NH         699.78         72.22         590.32         185.31         641.87         0.34         0.330           NJ         1172.15         99.46         583.98         38.91         662.98         0.34         0.330           NM         521.42         80.62         429.80         218.22         633.16         0.60         0.200	0.330
MN         1677.14         187.37         206.34         -177.23         522.92         0.34         0.330           MS         1122.35         110.09         350.56         102.90         636.51         0.34         0.330           MO         1032.29         119.12         452.46         -129.18         410.42         0.34         0.330           MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330           NE         258.94         186.39         337.28         -128.88         131.97         0.34         0.330           NV         733.30         87.25         411.85         -109.82         304.21         0.34         0.330           NH         699.78         72.22         590.32         185.31         641.87         0.34         0.330           NJ         1172.15         99.46         583.98         38.91         662.98         0.34         0.330           NM         521.42         80.62         429.80         218.22         633.16         0.60         0.200           NY         556.41         165.97         366.54         -69.08         371.27         0.60         0.200	0.330
MS         1122.35         110.09         350.56         102.90         636.51         0.34         0.330           MO         1032.29         119.12         452.46         -129.18         410.42         0.34         0.330           MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330           NE         258.94         186.39         337.28         -128.88         131.97         0.34         0.330           NV         733.30         87.25         411.85         -109.82         304.21         0.34         0.330           NH         699.78         72.22         590.32         185.31         641.87         0.34         0.330           NJ         1172.15         99.46         583.98         38.91         662.98         0.34         0.330           NM         521.42         80.62         429.80         218.22         633.16         0.60         0.200           NY         556.41         165.97         366.54         -69.08         371.27         0.60         0.200           NC         517.26         68.15         445.26         -9.63         403.41         0.60         0.200	0.330
MO         1032.29         119.12         452.46         -129.18         410.42         0.34         0.330           MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330           NE         258.94         186.39         337.28         -128.88         131.97         0.34         0.330           NV         733.30         87.25         411.85         -109.82         304.21         0.34         0.330           NH         699.78         72.22         590.32         185.31         641.87         0.34         0.330           NJ         1172.15         99.46         583.98         38.91         662.98         0.34         0.330           NM         521.42         80.62         429.80         218.22         633.16         0.60         0.200           NY         556.41         165.97         366.54         -69.08         371.27         0.60         0.200           NC         517.26         68.15         445.26         -9.63         403.41         0.60         0.200           ND         438.47         186.50         151.41         -43.78         286.88         0.60         0.200 <td>0.330</td>	0.330
MT         1620.01         97.69         290.73         -157.86         521.12         0.34         0.330           NE         258.94         186.39         337.28         -128.88         131.97         0.34         0.330           NV         733.30         87.25         411.85         -109.82         304.21         0.34         0.330           NH         699.78         72.22         590.32         185.31         641.87         0.34         0.330           NJ         1172.15         99.46         583.98         38.91         662.98         0.34         0.330           NM         521.42         80.62         429.80         218.22         633.16         0.60         0.200           NY         556.41         165.97         366.54         -69.08         371.27         0.60         0.200           NC         517.26         68.15         445.26         -9.63         403.41         0.60         0.200           ND         438.47         186.50         151.41         -43.78         286.88         0.60         0.200	0.330
NE       258.94       186.39       337.28       -128.88       131.97       0.34       0.330         NV       733.30       87.25       411.85       -109.82       304.21       0.34       0.330         NH       699.78       72.22       590.32       185.31       641.87       0.34       0.330         NJ       1172.15       99.46       583.98       38.91       662.98       0.34       0.330         NM       521.42       80.62       429.80       218.22       633.16       0.60       0.200         NY       556.41       165.97       366.54       -69.08       371.27       0.60       0.200         NC       517.26       68.15       445.26       -9.63       403.41       0.60       0.200         ND       438.47       186.50       151.41       -43.78       286.88       0.60       0.200	0.330
NV       733.30       87.25       411.85       -109.82       304.21       0.34       0.330         NH       699.78       72.22       590.32       185.31       641.87       0.34       0.330         NJ       1172.15       99.46       583.98       38.91       662.98       0.34       0.330         NM       521.42       80.62       429.80       218.22       633.16       0.60       0.200         NY       556.41       165.97       366.54       -69.08       371.27       0.60       0.200         NC       517.26       68.15       445.26       -9.63       403.41       0.60       0.200         ND       438.47       186.50       151.41       -43.78       286.88       0.60       0.200	0.330
NJ     1172.15     99.46     583.98     38.91     662.98     0.34     0.330       NM     521.42     80.62     429.80     218.22     633.16     0.60     0.200       NY     556.41     165.97     366.54     -69.08     371.27     0.60     0.200       NC     517.26     68.15     445.26     -9.63     403.41     0.60     0.200       ND     438.47     186.50     151.41     -43.78     286.88     0.60     0.200	0.330
NJ     1172.15     99.46     583.98     38.91     662.98     0.34     0.330       NM     521.42     80.62     429.80     218.22     633.16     0.60     0.200       NY     556.41     165.97     366.54     -69.08     371.27     0.60     0.200       NC     517.26     68.15     445.26     -9.63     403.41     0.60     0.200       ND     438.47     186.50     151.41     -43.78     286.88     0.60     0.200	0.330
NY     556.41     165.97     366.54     -69.08     371.27     0.60     0.200       NC     517.26     68.15     445.26     -9.63     403.41     0.60     0.200       ND     438.47     186.50     151.41     -43.78     286.88     0.60     0.200	0.330
NY     556.41     165.97     366.54     -69.08     371.27     0.60     0.200       NC     517.26     68.15     445.26     -9.63     403.41     0.60     0.200       ND     438.47     186.50     151.41     -43.78     286.88     0.60     0.200	0.200
ND 438.47 186.50 151.41 -43.78 286.88 0.60 0.200	0.200
ND 438.47 186.50 151.41 -43.78 286.88 0.60 0.200	0.200
OH 331.12 183.50 291.83 104.01 397.75 0.60 0.200	0.200
	0.200
OK 434.05 201.28 240.21 -129.09 219.64 0.60 0.200	0.200
OR 479.14 154.61 476.62 -96.87 316.86 0.60 0.200	0.200
PA 667.03 135.05 369.33 32.55 533.64 0.60 0.200	0.200
RI 516.67 130.18 528.25 294.88 736.57 0.60 0.200	0.200
SC 566.61 59.24 320.34 -256.93 158.95 0.60 0.200	0.200
SD 568.88 113.20 305.38 56.94 481.98 0.60 0.200	0.200
TN 482.11 74.65 464.36 129.79 526.86 0.60 0.200	0.200
TX 700.27 143.84 338.94 -60.33 456.39 0.60 0.200	0.200
UT 621.44 103.06 281.04 240.98 690.66 0.60 0.200	0.200
VT 550.91 115.41 465.21 -52.33 394.34 0.60 0.200	0.200
VA 438.32 144.00 258.52 12.27 355.77 0.60 0.200	0.200
WA 395.00 109.87 420.48 -137.17 205.90 0.60 0.200	0.200
WV 487.61 204.44 376.18 3.43 412.12 0.60 0.200	0.200
WI 664.26 120.95 708.42 -64.96 499.47 0.60 0.200	0.200
WY 469.10 183.22 444.36 150.42 557.40 0.60 0.200	0.200

We are now able to identify a linear model from the above data that depends on variables A,B and C with the results displayed as follows.

```
par(mfrow=c(2,2))
M4<-lm(Total_Cost ~ A+B+C, data = M4_Data)
summary(M4)
##
## Call:
## lm(formula = Total_Cost ~ A + B + C, data = M4_Data)
##
## Residuals:
##
       Min
                1Q Median
                               ЗQ
                                      Max
## -679.24 -146.50
                    23.74 197.25 502.26
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -271.15867 239.40141 -1.133
                                              0.2632
                 0.70815
                            0.07248
                                      9.770 8.48e-13 ***
## B
                 0.58118
                            0.94135
                                              0.5400
                                      0.617
## C
                  0.64641
                            0.37296
                                      1.733
                                              0.0898 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 271.2 on 46 degrees of freedom
## Multiple R-squared: 0.6936, Adjusted R-squared: 0.6737
## F-statistic: 34.72 on 3 and 46 DF, p-value: 7.053e-12
```

plot(M4)



As displayed in the graphs above, the errors and different metrics do not confirm to be unbiased and do not follow Gaussian assumptions. The Residuals vs Fitted display errors with a mean not equal to 0 and showing a fanning effect: larger variance of the residuals for larger values of fitted values. The Normal QQ shows heavy tails suggesting that the model does not follow the Gaussian assumptions, which does not allow us to apply hypothesis tests like *t*-tests. That being said we are still able to retrieve a linear model even without strong assumptions being held.