

① For Tuple T

$$\text{Info}(T) = - \sum_{i=1}^n P_i \log_2(P_i)$$

$$\text{Info}(T) = -5/10 \log_2(5/10) - 5/10 \log_2(5/10) \\ = 1.0 \text{ bit}$$

②
$$\text{Info}_{\text{VD}}(T) = 3/10 * (-3/3 \log_2 3/3) + 4/10 * (-2/4 \log_2 2/4 \\ - 2/4 \log_2 2/4) + 3/10 * (-3/3 \log_2 3/3) \\ = 0.4 \text{ bits}$$

$$\text{Info}(T) - \text{Info}_{\text{VD}}(T) = 1.0 - 0.4 = 0.6 \text{ bits}$$

Gain

③ None Observation = 4
Many Observation = 3
Some Observation = 3

Total Observation = 10

Using Simple log-Algebra Method

$$\text{Entropy} + I(\text{Taste/Visual Defect} = \text{some}) = -3/3 \log_2(3/3) - 0 \log_2(0) \\ = 0$$

$$\text{Entropy} + I(\text{Taste/Visual Defect} = \text{none}) \\ = -2/4 \log_2(2/4) - 2/4 \log_2(2/4) \\ = -1/2 - 1/2 \\ = -1$$