

4.3 Refer to Figure 4.2. Given: $B = L = 1.75$ m, $D_f = 1$ m, $H = 1.75$ m, $\gamma = 17$ kN/m³, $c' = 0$, and $\phi' = 30^\circ$. Using Eq. (4.6) and FS = 4, determine the gross allowable load the foundation can carry.

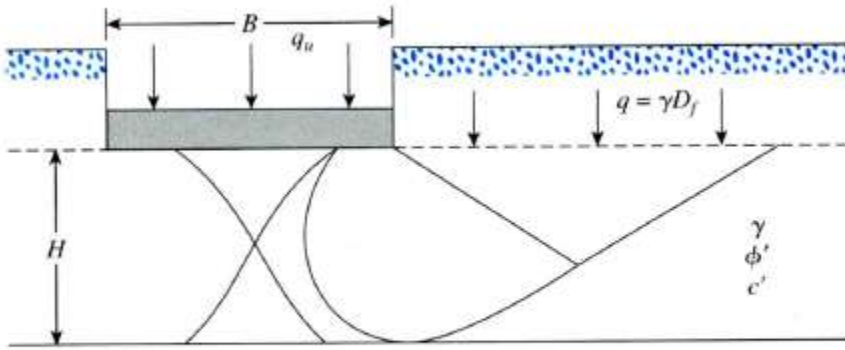
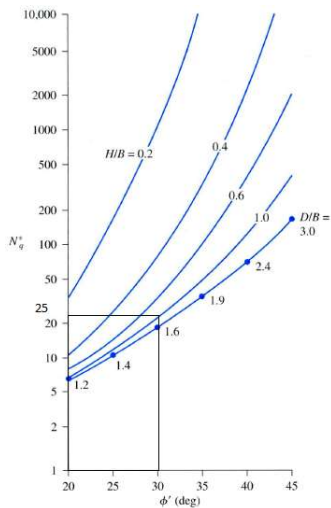


Figure 4.2 Failure surface under a rough, continuous foundation with a rigid, rough base located at a shallow depth

Given: $B := 1.75$ m $L := 1.75$ m $D_f := 1$ m $H := 1.75$ m $\gamma := 17 \frac{\text{kN}}{\text{m}^3}$ $c' := 0$ $\phi' := 30^\circ$ FS := 4

Required: determine the gross allowable load the foundation can carry

$$\frac{H}{B} = 1 \quad q := \gamma \cdot D_f = 17$$



From Figure 4.7, N'_y :

$$N'_y \gamma := 78$$

$$N'_q := 22$$

$$q_u := q \cdot N'_q + .4 \cdot \gamma \cdot B \cdot N'_y = 1.302 \frac{\text{kN}}{\text{m}^3}$$

$$q_a := \frac{q_u}{\text{FS}} = 325.55$$

Equ 4.6 p 187

$$Q_{all} := q_a \cdot B \cdot L = 996.997$$

4.5 Refer to Figure 4.8. For a strip foundation in two-layered clay, given:

- $\gamma_1 = 115 \text{ lb/ft}^3$, $c_1 = 1200 \text{ lb/ft}^2$, $\phi_1 = 0$
- $\gamma_2 = 110 \text{ lb/ft}^3$, $c_2 = 600 \text{ lb/ft}^2$, $\phi_2 = 0$
- $B = 3 \text{ ft}$, $D_f = 2 \text{ ft}$, $H = 2 \text{ ft}$

Find the gross allowable bearing capacity. Use a factor of safety of 3.

$$\begin{aligned} \text{FS} &:= 3 & \pi &:= 3.1415 & B &:= 3 \text{ ft} & D_f &:= 2 \text{ ft} & H &:= 2 \text{ ft} & L &:= \infty & \text{FS} &:= 3 \\ \gamma_1 &:= 115 \frac{\text{lb}}{\text{ft}^3} & c_1 &:= 1200 \frac{\text{lb}}{\text{ft}^2} & \phi_1 &:= 0^\circ \\ \gamma_2 &:= 110 \frac{\text{lb}}{\text{ft}^3} & c_2 &:= 600 \frac{\text{lb}}{\text{ft}^2} & \phi_2 &:= 0^\circ \\ & & & & \text{bearing capacity factors Table 3.3 p 144} \\ N_{q1} &:= 1 & N_{c1} &:= 5.14 & N_{\gamma1} &:= 0 & N_{q2} &:= 1 & N_{c2} &:= 5.14 & N_{\gamma2} &:= 0 \end{aligned}$$

Method Stronger clay over soft clay gives us special case 3, thus: Eq (4.29), (4.30) and (4.31) will apply:

Determine c_2/c_1 to obtain the value of c_a from Figure 4.10

Apply equations cited above and obtain allowable load by using equation (3.12)

Solution

$$\frac{c_2}{c_1} = 0.5$$

Thus

$$c'_a := c_1 \cdot 0.94 = 1.128 \times 10^3$$

4.3 Bearing Capacity of Layered Soils: Stronger Soil Underlain by Weaker Soil 19

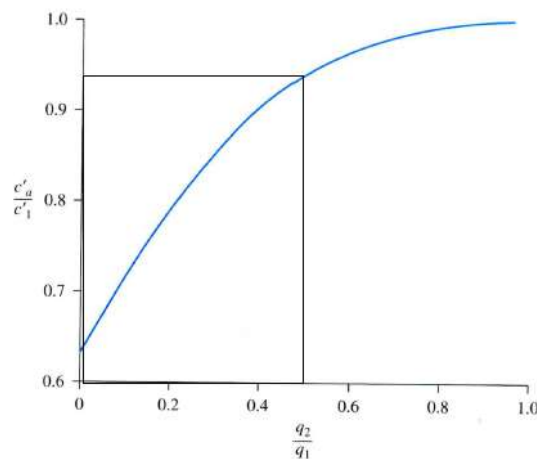


Figure 4.10 Variation of c'_a/c'_1 with q_2/q_1 based on the theory of Meyerhof and Hanna (1978)

$$q_u := \left(1 + .2 \frac{B}{L}\right) \cdot 5.14 \cdot c_2 + \left(1 + \frac{B}{L}\right) \left(\frac{2c'_a \cdot H}{B}\right) + \gamma_1 \cdot D_f = 4.818 \times 10^3$$

Eq 4.29 p195

$$q_t := \left(1 + .2 \frac{B}{L}\right) 5.14 c_1 + \gamma_1 \cdot D_f = 6.398 \times 10^3$$

Eq 4.30 p195

$$\text{solution: } q_{all} := \frac{\min(q_u, q_t)}{\text{FS}} = 1.606 \times 10^3$$

4.7 Refer to Figure 4.8. For a square foundation on layered sand, given:

- $B = 1.5 \text{ m}$, $D_f = 1.5 \text{ m}$, $H = 1 \text{ m}$
- $\gamma_1 = 18 \text{ kN/m}^3$, $\phi'_1 = 40^\circ$, $c'_1 = 0$
- $\gamma_2 = 16.7 \text{ kN/m}^3$, $\phi'_2 = 32^\circ$, $c'_2 = 0$

Given: $B := 1.5$ $D_f := 1.5$ $H := 1$ $L := 1.5$

Find: determine the gross allowable load the foundation can carry

$\gamma_1 := 18$ $c_1 := 0$ $\phi'_1 := 40\text{deg}$ $\gamma_2 := 16.7$ $c_2 := 0$ $\phi'_2 := 32\text{deg}$ $FS := 4$

Method Case 2 Special Cases, thus use equations (4.26 and 4.27)
Determine factors for each of the layers, using table 3.3 and table 3.4

Table 3.3

$N_{q1} := 64.2$ $N_{q2} := 23.18$
 $N_{\gamma 1} := 109.41$ $N_{\gamma 2} := 30.22$

Table 3.4 $F_{\gamma s1} := 1 - 0.4 \cdot \left(\frac{B}{L}\right) = 0.6$

$F_{\gamma s2} := 1 - 0.4 \cdot \left(\frac{B}{L}\right) = 0.6$

$F_{qs1} := 1 + 1 \cdot \tan(\phi'_1) = 1.839$

$F_{qs2} := (1 + 1 \cdot \tan(\phi'_2)) = 1.625$

Determine K_s , using angle of friction on the top layer (layer 1), Figure 4.9 and from equations (4.15) & (4.16):

Eq 4.15 p192

Eq 4.16 p192

$$q_1 := c_1 \cdot N_{c1} + 0.5 \cdot \gamma_1 \cdot B \cdot N_{\gamma 1} = 1.477 \times 10^3$$

$$q_2 := c_2 \cdot N_{c2} + 0.5 \cdot \gamma_2 \cdot B \cdot N_{\gamma 2} = 378.505$$

$$\frac{q_2}{q_1} = 0.256$$

$K_s := 5$

$$\frac{B}{L} = 1$$

Determine $Q_{all} = q_{all} \cdot A$

Solution

$$q_u := [\gamma_1 \cdot (D_f + H) N_{q2} \cdot F_{qs2} + .5 \gamma_2 \cdot B \cdot N_{\gamma 2} \cdot F_{\gamma s2}] + H^2 \cdot \gamma_1 \left(1 + \frac{B}{L}\right) \left(1 + \frac{2D_f}{H}\right) \left(\frac{K_s \cdot \tan(\phi'_1)}{B}\right) - \gamma_1 \cdot H = 2.307 \times 10^3 \quad \text{eqn 4.26 p 194}$$

$$q_t := \gamma_1 \cdot D_f \cdot N_{q1} \cdot F_{qs1} + .5 \gamma_1 \cdot B \cdot N_{\gamma 1} \cdot F_{\gamma s1} = 4.074 \times 10^3$$

$$q_{all} := \frac{\min(q_u, q_t)}{FS} = 576.693$$

$$q := D_f \cdot \gamma = 25.5$$

$$q_{net} := q_{all} - q$$

$$Q_{net} := q_{net} \cdot B \cdot L = 1.24 \times 10^3$$

4.9 Given: $B := 1.2$ $D_f := 1$ $x := 2$ $\phi'_1 := 35\text{deg}$ $FS := 4$ $\gamma := 16.8$ $L := \infty$ $FS = 4$

Find: Determine the net allowable bearing capacity of the foundation can carry

Method 1. Use table 3.3 to determine N_q and N_y , and Figure 4.13 p202 to determine ζ_q ζ_y
2. Apply equation 4.36 to determine ultimate bearing
3. Determine $q_{net} = q_u - q$

Solution 1. $N_q := 12.75$ $N_{\gamma} := 8.35$ $\frac{x}{B} = 1.667$ $\zeta_q := 1.4$ $\zeta_{\gamma} := 2.4$

$$q_u := q \cdot N_q \cdot \zeta_q + .5 \cdot \gamma \cdot B \cdot N_{\gamma} \cdot \zeta_{\gamma} = 657.178$$

$$q := \gamma \cdot D_f = 16.8$$

$$q_{net} := q_u - q = 640.378 \quad \frac{\text{kN}}{\text{m}^2}$$

$$q_{all} := \frac{q_{net}}{FS} = 160.095$$

Given :

$$B := 1 \text{ m} \quad H := 4 \text{ m} \quad b := 2 \text{ m} \quad c' := 68 \text{ kN/m}^2$$

$$\gamma := 16.8 \text{ kN/m}^3 \quad \phi := 0^\circ \quad \beta := 60^\circ$$

$$FS := 3 \quad D_f := 1 \text{ m}$$

$$\gamma = 16.8 \text{ kN/m}^3$$

4.10 A continuous foundation with a width of 1 m is located on a slope made of clay soil. Refer to Figure 4.14 and let $D_f = 1 \text{ m}$, $H = 4 \text{ m}$, $b = 2 \text{ m}$, $\gamma = 16.8 \text{ kN/m}^3$, $c = 68 \text{ kN/m}^2$, $\phi = 0$, and $\beta = 60^\circ$.

- Determine the allowable bearing capacity of the foundation. Let $FS = 3$.
- Plot a graph of the ultimate bearing capacity q_u if b is changed from 0 to 6 m.

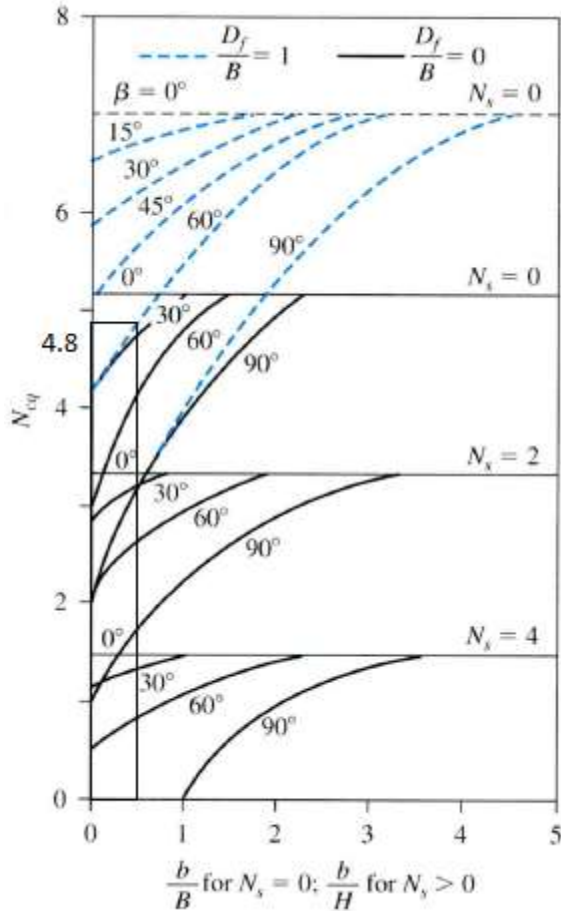


Figure 4.16 Meyerhof's bearing capacity factor N_{cq} for purely cohesive soil

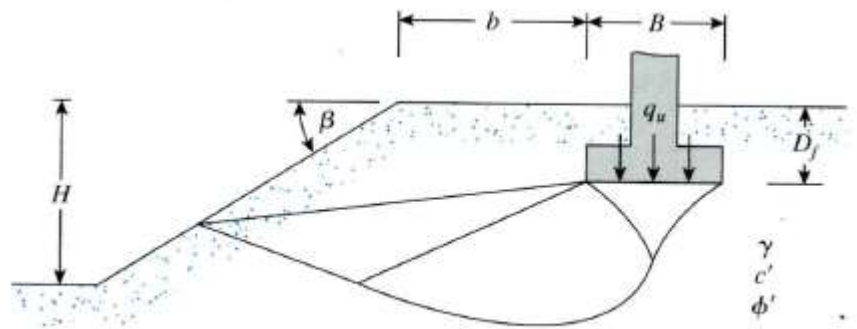


Figure 4.14 Shallow foundation on top of a slope

- Method**
- N_s must be obtained using equation 4.40
If $N_s = 0$ use b/B and if $N_s > 0$ use b/H on Figure 4.16
 - Determine ultimate bearing capacity with eq 4.39
 - Determine $q_{all} = q_u / FS$ eq 3.12

$$\frac{D_f}{B} = 1$$

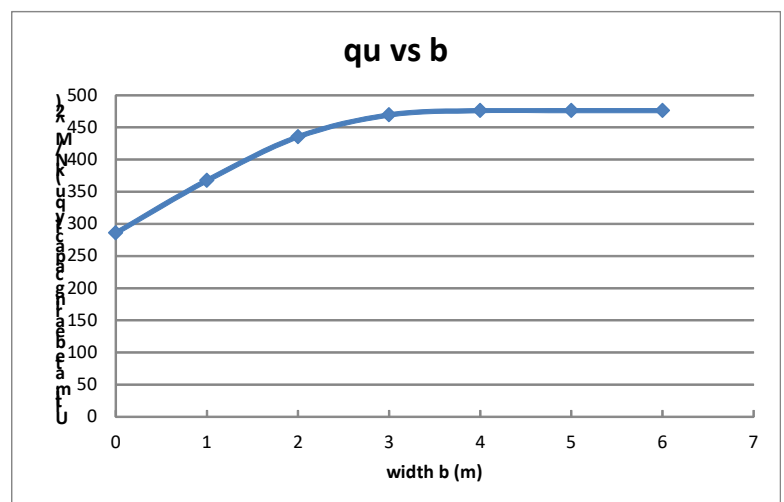
Solution

- $N_s := \frac{\gamma \cdot H}{c} = 2.242 \times 10^{-7} \frac{s}{m} \quad \frac{b}{B} = 2 \quad N_{cq} := 6.5$

- $q_u := c' \cdot N_{cq} = 442$ eq 4.39 p 203

- $q_{all} := \frac{q_u}{FS} = 147.333$

Part B)



Given $\frac{FS}{\gamma} := 3$ $\frac{Df}{\gamma} := 4$

$\frac{B}{\gamma} := 4$ $\frac{H}{\gamma} := 15$ $\frac{b}{\gamma} := 6$ $\frac{c}{\gamma} := 0$

$\frac{FS}{\gamma} := 4$ $\gamma := 110$ $\phi := 40$ $\beta := 30\text{deg}$

4.11 A continuous foundation is to be constructed near a slope made of granular soil (see Figure 4.14). If $B = 4$ ft, $b = 6$ ft, $H = 15$ ft, $D_f = 4$ ft, $\beta = 30^\circ$, $\phi' = 40^\circ$, and $\gamma = 110$ lb/ft³, estimate the ultimate bearing capacity of the foundation. Use Meyerhof's solution.

- Method 1. $N_{\gamma q}$ must be obtained using Figure 4.15
2. Determine ultimate bearing capacity with eq 4.38

Solution 1. $\frac{Df}{B} = 1$ $\frac{b}{B} = 1.5$ $N_{\gamma q} := 135$ $\frac{N_{eq}}{\gamma} := 4.8$

2. $q_u := .5 \cdot \gamma \cdot B \cdot N_{\gamma q} = 2.97 \times 10^4$ eq 4.38 p 203 3. $q_{all} := \frac{q_u}{FS} = 7.425 \times 10^3$

4.12 A square foundation in a sand deposit measures 4 ft \times 4 ft in plan. Given: $D_f = 5$ ft, soil friction angle = 35° , and unit weight of soil = 112 lb/ft³. Estimate the ultimate uplift capacity of the foundation.

Given: $\frac{B}{\gamma} := 4$ $\frac{L}{\gamma} := 4$ $\frac{Dfl}{\gamma} := 5$ $\phi' := 35\text{deg}$ $\gamma := 112$ $\frac{\text{lb}}{\text{ft}^3}$ Granular soil, $c'=0$ $\frac{A}{\gamma} := B \cdot L = 16$

Find: Ultimate uplift capacity of the foundation

- Method: 1. Determine the type of foundation dealt
1.1 (Calculate Df/B)

1.2. Using Table 4.3 and Eq 4.55 determine Df/B , or

2. Determine the breakout factor F_q (using either 4.53/4.54) given the factor calculated above
3. Obtain Q_u using formula 4.52

Solution: 1.1 $\frac{Dfl}{B} = 1.25$ 1.2 $K_u := 0.936$ $\frac{m}{\gamma} := 0.25$ $\frac{Dcr}{B} := 5$

Since 1.1 < 1.2 $\frac{Df}{B} := \frac{Dfl}{B}$

2 square foundation $F_q := 1 + 2 \left[1 + m \cdot \left(\frac{Dfl}{B} \right) \right] \left(\frac{Dfl}{B} \right) \cdot K_u \cdot \tan(\phi') = 3.151$ eq 4.54 p 214

3 $Q_u := F_q \cdot A \cdot \gamma \cdot Dfl = 2.823 \times 10^4$ lb