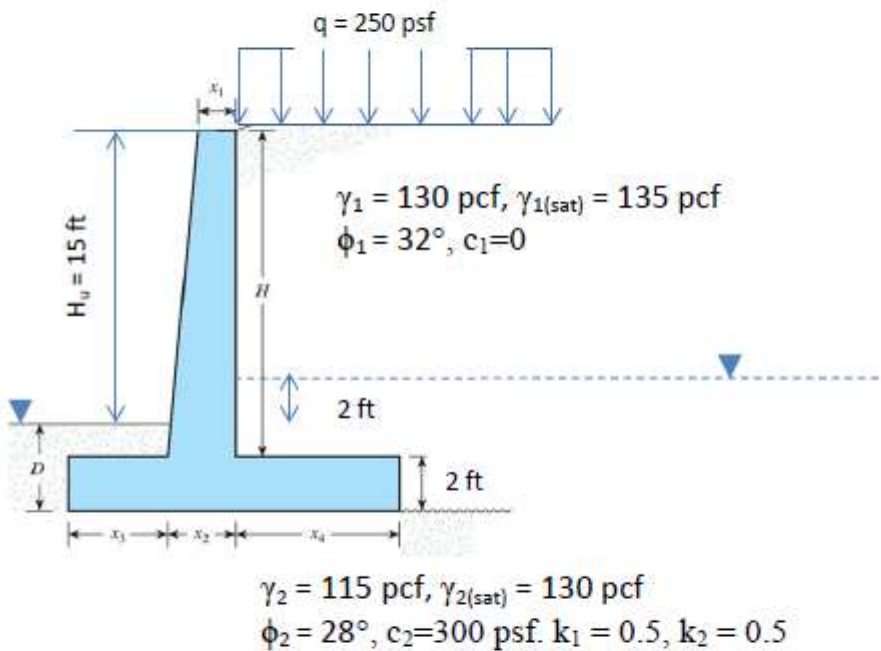


**Given:**

As foundation engineer, you are required to determine the preliminary dimensions of a reinforced concrete cantilever retaining wall, which will support a new roadway. The adjacent highway surcharge load is shown in the figure below. The unsupported height of the retaining wall ( $H_u$ ) is 15 ft. and the foundation must be embedded a depth ( $D$ ) of 5 ft. below the adjacent grade. Due to site flooding conditions, design flood level is at grade in front of the wall is expected to be two (2) feet higher behind the wall as shown in the figure below. Assume unit weight of concrete is 150 pcf. All soil properties are given in the figure. Use Rankine Active Earth Pressures and ignore passive earth pressure effects.



**Find:**

- Using Figure 8.3b in your textbook, determine the preliminary unknown dimension of the retaining wall ( $x_1$ ,  $x_2$ ,  $x_3$ , and  $x_4$ ) round to nearest 0.25 ft.. Using these preliminary dimensions and determine:
  - Factor of Safety for Overturning Stability.
  - Factor of Safety for Sliding Stability.
  - Factor of Safety for Bearing Capacity.
- What is the critical mode of failure for the preliminary design?

GIVEN	Wall dimensions	$\gamma_c := 150$ pcf	$H_u := 15$ ft	$D := 5$ ft	Since horizontal granular backfill: $\alpha := 0^\circ$
		$x_5 := 2$ ft	Surcharge $q := 250$ psf		
Soil properties	$\gamma_1 := 130$ pcf	$\gamma_2 := 115$ pcf	$k_1 := \frac{1}{2}$	$k_2 := \frac{1}{2}$	height of water behind the wall $h_{wb} := 7$ ft
	$\gamma_{1sat} := 135$ pcf	$\gamma_{2sat} := 130$ pcf			
	$\phi'_1 := 32^\circ$	$\phi'_2 := 28^\circ$	$\gamma_w := 62.4$ pcf		
	$c'_1 := 0$	$c'_2 := 300$ psf			
			$H_w := H_u + D - x_5 = 18$ ft		

METHOD 1 Use Figure 8.3b to determine initial proportioning

A) OVERTURNING STABILITY:

1. Determine the Rankine Active Force per unit length of Wall
  - 1.1 Determine  $K_a$  (active earth pressure coefficient) using EQ 7.1
  - 1.2 The force  $P_a$  can be obtained by adding stresses and the effects of hydrostatic pressure can be lumped into  $P_a$
3. Determine the overturning moment
  - 3.2 Determine horizontal component of  $P_a$  and moment caused by it ( $M_o$ )
4. Determine the resisting forces and its corresponding moments
  - 4.1 For the areas of concrete below the water, a specific effective weight of concrete is used in order to represent the effect of water buoyancy on the structure
  - 4.2 The forces are tabled and vertical forces summed, as well as moments
4. Determine  $F_{\text{Soverturning}}$  (Use EQN 8.5)

- B) SLIDING      Determine  $K_p$  (Use equation on page 385)  
Sliding Factor of Safety can be calculated with EQ 8.11

C) BEARING CAPACITY FAILURE

0. Determine eccentricity and maximum and minimum pressures (pressures at the toe and heel of wall) (EQNS 8.18 & 8.21)
1. Use Table 3.3 to determine Bearing Capacity Factors
2. Use Table 3.4 to determine Depth and Inclination Factors
3. Use Meyerhoff's Equation 8.22 to determine bearing capacity  $q_u$
4. Determine Bearing Capacity using EQ 8.23

SOLUTION      Given the general dimensions we can obtain  $H_t$ :       $H_t := H_u + D = 20 \text{ ft}$

$$1 \quad x_3 := 0.1 \cdot H_t = 2 \text{ ft} \quad x_2 := 0.1 \cdot H_t = 2 \text{ ft} \quad B := 0.6 \cdot H_t = 12 \text{ ft} \quad x_4 := B - (x_3 + x_2) = 8 \text{ ft}$$

$$x_1 := 1.5 \text{ ft} \quad \theta := \text{atan}\left[\frac{(x_2 - x_1)}{18}\right] = 0.028$$

DETERMINING RANKINE ACTIVE FORCE:

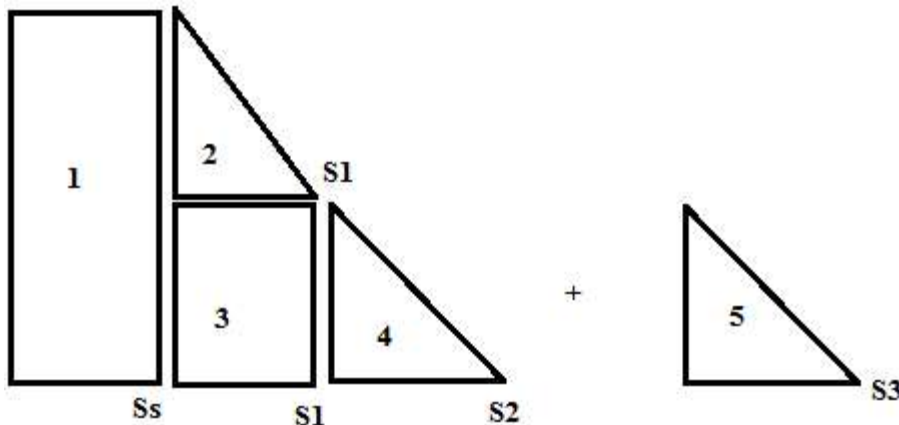
$$K_a := \tan\left(45 \cdot \text{deg} - \frac{\phi'1}{2}\right)^2 = 0.307$$

Stress Due to the surcharge:       $S_s := q \cdot K_a = 76.815 \text{ psf}$

Stress @       $z_1 := H_t - h_{wb} = 13 \text{ ft} \quad S_1 := K_a \cdot \gamma_1 \cdot z_1 = 519.267 \text{ psf}$

Stress @       $z_2 := H_t - z_1 = 7 \text{ ft} \quad S_2 := K_a \cdot (\gamma_{1\text{sat}} - \gamma_w) \cdot z_2 = 156.149 \text{ psf}$

Hydrostatic Pressure       $z_2 = 7 \text{ ft} \quad S_3 := z_2 \cdot \gamma_w = 436.8 \text{ psf}$



The stress areas in the picture are equal to:

$$A_1 := H_t \cdot S_s = 1.536 \times 10^3 \text{ plf}$$

$$A_2 := 0.5 \cdot z_1 \cdot S_1 = 3.375 \times 10^3 \text{ plf}$$

$$A_3 := z_2 \cdot S_1 = 3.635 \times 10^3 \quad A_4 := 0.5 \cdot z_2 \cdot S_2 = 546.521$$

$$A_5 := 0.5 \cdot z_2 \cdot S_3 = 1.529 \times 10^3$$

$$A_{5w} := A_5 = 1.529 \times 10^3$$

Figure 3.1 - Stresses Areas and its Force Equivalents

The total rankine active pressure is equal to the sum of the areas above:

$$P_a := A1 + A2 + A3 + A4 + A5 = 1.062 \times 10^4 \text{ plf}$$

### Overturning components:

$$P_h := P_a \cdot \cos(\alpha) = 1.062 \times 10^4 \text{ plf} \quad M_o := P_h \cdot (H') = 7.118 \times 10^4 \text{ lb} - \frac{\text{ft}}{\text{ft}} \quad \text{CCW}$$

The hydrostatic pressure (and force Fbw) behind the wall also causes an overturning moment, however it has already been accounted within  $P_a$ .

To determine the height of concrete that is submerged:  $h_b := 6 \text{ ft} \quad h_{bs} := 6 - x_5 = 4$

The location of the force (to the bottom of the wall) is equal to:

$$H' := \frac{\left[ A1 \cdot \frac{H_t}{2} + A2 \cdot \left( z_2 + \frac{z_1}{3} \right) + A3 \cdot \frac{z_2}{2} + (A4 + A5) \cdot \frac{z_2}{3} \right]}{P_a} = 6.701 \text{ ft}$$

### RESISTING COMPONENTS

$$P_v := P_a \cdot \sin(\alpha) = 0$$

Obs for the table below:

1. The suffix b (below) refers to areas submerged (below the water)
2. The vertical component of the surcharge is taken into consideration as a resisting force (See 7 below)
3. The vertical component of the hydrostatic pressure in the front of the wall causes a resisting moment (See 6 below)
4.  $P_p$  also causes a resisting moment, however, we'll assume it equal to zero for a conservative approach

Effective Concrete Weight

$$\gamma_{c'} := \gamma_c - \gamma_w = 87.6$$

Effective Soil Weight

$$\gamma_{l'} := \gamma_l - \gamma_w = 67.6$$

Height above water table  $H_w := H_t - 7 = 13 \text{ ft}$

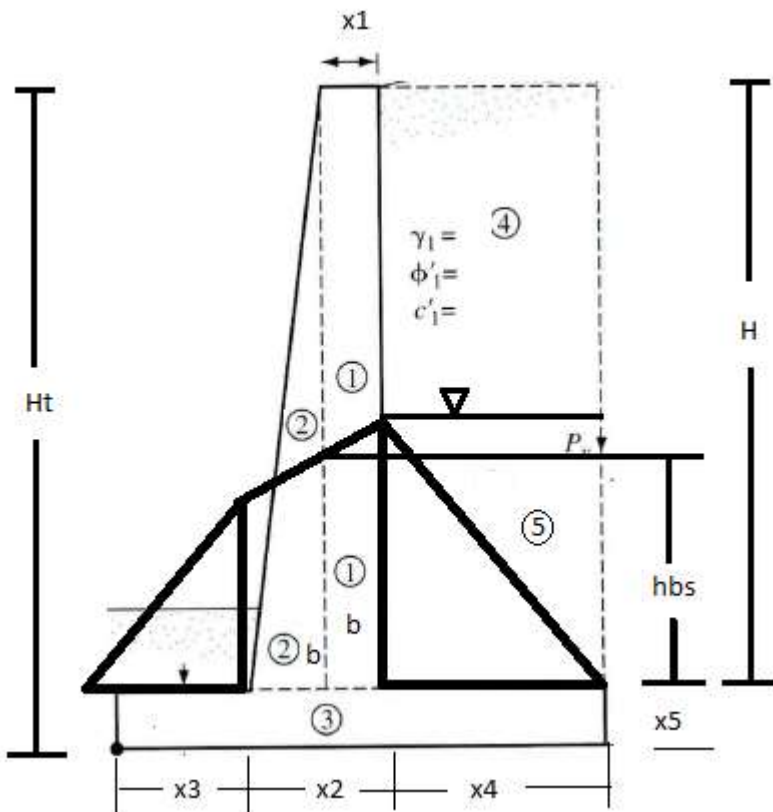


Figure 3.1 - Area distribution for the table below

SEC	AREA (ft <sup>2</sup> )	W/unit length (plf)	M. Arm to C (ft)	Moment lb-ft/ft
1	$A1 := x1 \cdot (H - h_{bs}) = 21$	$w1 := \gamma_c \cdot A1 = 3.15 \times 10^3$	$B1 := x3 + x2 - \frac{x1}{2} = 3.25$	$M1 := w1 \cdot B1 = 1.024 \times 10^4$
	$A1b := x1 \cdot h_{bs} = 6$	$w1b := (\gamma_{c'}) \cdot A1b = 525.6$	$B1b := B1 = 3.25$	$M1b := w1b \cdot B1b = 1.708 \times 10^3$

$$2 \quad \underline{A2} := (x2 - x1) \cdot \frac{(H - hbs)^2}{2 \cdot H} = 2.722 \quad w2 := \gamma_c \cdot A2 = 408.333 \quad B2 := x3 + \frac{2}{3} \left( x2 - \frac{x1}{2} \right) = 2.833 \quad M2 := w2 \cdot B2 = 1.157 \times 10^3$$

$$A2b := (x2 - x1) \cdot \frac{(H)}{2} - A2 = 1.778 \quad w2b := \gamma_c' \cdot A2b = 155.733 \quad B2b := B2 = 2.833 \quad M2b := w2b \cdot B2b = 441.244$$

$$3 \quad \underline{A3} := x5 \cdot B = 24 \quad w3 := \gamma_c' \cdot A3 = 2.102 \times 10^3 \quad B3 := \frac{B}{2} = 6 \quad M3 := w3 \cdot B3 = 1.261 \times 10^4$$

$$4 \quad \underline{A4} := x4 \cdot (Hw) = 104 \quad w4 := \gamma_1 \cdot A4 = 1.352 \times 10^4 \quad B4 := B - \frac{x4}{2} = 8 \quad M4 := w4 \cdot B4 = 1.082 \times 10^5$$

$$5 \quad \underline{A5} := x4 \cdot hbs = 32 \quad w5 := \gamma_1' \cdot A5 = 2.163 \times 10^3 \quad B5 := B4 = 8 \quad M5 := w5 \cdot B5 = 1.731 \times 10^4$$

$$6 \quad \text{Hydrostatic Force Front} \quad Ffw := 0.5 \cdot \gamma_w \cdot D^2 = 780 \text{ plf} \quad B6 := 0.333 \cdot D = 1.665 \quad M6 := Ffw \cdot B6 = 1.299 \times 10^3$$

$$\text{Surcharge Vertical Component} \quad Qq := q \cdot x4 = 2 \times 10^3 \text{ plf} \quad \underline{Bq} := B - \frac{x4}{2} = 8 \quad M7 := Qq \cdot Bq = 1.6 \times 10^4$$

$$\Sigma V := w1 + w1b + w2b + Qq + w2 + w3 + w4 + w5 = 2.403 \times 10^4 \frac{\text{lb}}{\text{ft}}$$

$$\Sigma Mr := M1 + M1b + M2b + M2 + M3 + M4 + M5 + M6 + M7 = 1.689 \times 10^5 \text{ lb} - \frac{\text{ft}}{\text{ft}}$$

$$FS_{\text{overturning}} := \frac{\Sigma Mr}{M_o} = 2.373$$

$$\text{if}(FS_{\text{overturning}} > 2, \text{"OK!"}, \text{"No Good"}) = \text{"OK!"}$$

### FACTOR OF SAFETY AGAINST SLIDING:

$$\text{We must obtain } K_p \quad K_p := \tan \left( 45 \cdot \text{deg} + \frac{\phi_1'}{2} \right) = 3.255 \quad Pp := 0.5 \cdot K_p \cdot \gamma_2 \cdot D^2 + 2 \cdot c'2 \cdot \sqrt{K_p} \cdot D = 1.009 \times 10^4$$

$$\text{EQ 8.11} \quad FS_{\text{sliding}} := \frac{(\Sigma V \cdot \tan(k1 \cdot \phi_2') + B \cdot k2 \cdot c'2 + Pp + Ffw)}{(Pa \cdot \cos(\alpha))} = 1.757 \quad \text{if}(FS_{\text{sliding}} > 1.5, \text{"okay"}, \text{"not good"}) = \text{"okay"}$$

### FACTOR OF SAFETY AGAINST BEARING CAPACITY FAILURE

$$\underline{e} := \frac{B}{2} - \frac{(\Sigma Mr - M_o)}{\Sigma V} = 1.932 \text{ ft} \quad \text{EQ 8.16, 8.17 and 8.18} \quad \text{if} \left( e < \frac{B}{6}, \text{"okay"}, \text{"not good"} \right) = \text{"okay"}$$

$$q_{toe} := \frac{\Sigma V}{B} \cdot \left( 1 + 6 \cdot \frac{e}{B} \right) = 3.936 \times 10^3 \text{ psf} \quad q_{heel} := \frac{\Sigma V}{B} \cdot \left( 1 - 6 \cdot \frac{e}{B} \right) = 68.395 \text{ psf} \quad q_{max} := \max(q_{toe}, q_{heel})$$

$$\text{Using Table 3.3 we have: } \underline{\phi_2'} := 28 \cdot \text{deg} \quad N_c := 25.8 \quad N_q := 14.72 \quad N_\gamma := 16.72 \quad B' := (B - 2e) = 8.137 \text{ ft}$$

$$p := \frac{D}{B'} = 0.615 \quad F_{\gamma d} := 1 \quad F_{qd} := 1 + 2 \cdot \tan(\phi_2') \cdot (1 - \sin(\phi_2'))^2 \cdot \left( \frac{D}{B'} \right) = 1.184 \quad F_{cd} := F_{qd} - \frac{(1 - F_{qd})}{N_c \cdot \tan(\phi_2')} = 1.197$$

$$\psi := \text{atan} \left[ \frac{(Pa \cdot \cos(\alpha))}{\Sigma V} \right] = 0.416 \quad F_{ci} := \left( 1 - \frac{\psi}{90 \cdot \text{deg}} \right)^2 = 0.54 \quad F_{qi} := F_{ci} = 0.54 \quad F_{\gamma i} := \left( 1 - \frac{\psi}{\phi_2'} \right)^2 = 0.022$$

$$q_u := (\gamma_2 - \gamma_w) \cdot D = 263$$

$$q_u := c' \cdot 2 \cdot N_c \cdot F_{cd} \cdot F_{ci} + q \cdot N_q \cdot F_{qd} \cdot F_{qi} + .5 \cdot \gamma_2 \cdot B' \cdot N_\gamma \cdot F_{\gamma d} \cdot F_{\gamma i} = 7.654 \times 10^3$$

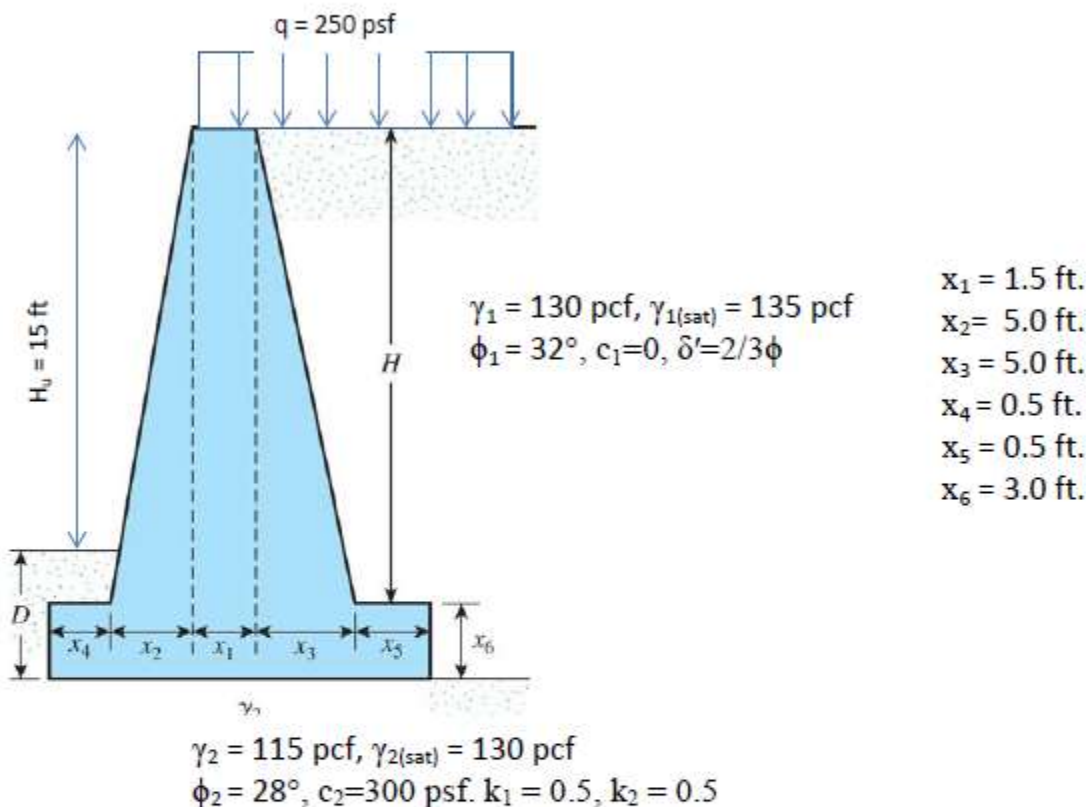
$$FS_{\text{bearing}} := \frac{q_u}{q_{\text{max}}} = 1.945$$

if( $FS_{\text{bearing}} > 3$ , "okay", "not good") = "not good"

**PART B** In the preliminary design Bearing Capacity is the critical mode of failure.

**Given:**

You are requested evaluate a massive gravity wall option using dimensions shown in the figure below for the same site conditions described in Problem 3. Use Coulomb Active Earth Pressures and ignore passive earth pressure effects.



**Find:**

- Using these preliminary dimensions determine:
  - Factor of Safety for Overturning Stability.
  - Factor of Safety for Sliding Stability.
  - Factor of Safety for Bearing Capacity.
- What is the critical mode of failure for the massive gravity wall option?
- Which option would you recommend for the final design? **Cantilever/Massive Gravity**
  - Explain your preferred choice and discuss how you would improve the design to achieve the following minimum requirements:
    - Factor of Safety for Overturning Stability = 2.0
    - Factor of Safety for Sliding Stability = 1.5
    - Factor of Safety for Bearing Capacity = 3.0

GIVEN	Wall dimensions	$\gamma_c := 150 \text{ pcf}$	$H_u := 15 \text{ ft}$	$D := 5 \text{ ft}$	Since horizontal granular backfill:		
		$x_5 := 2 \text{ ft}$	Surcharge $q := 250 \text{ psf}$	$\alpha := 0 \text{ deg}$			
	$x_1 := 1.5 \text{ ft}$	$x_2 := 5 \text{ ft}$	$x_3 := 5 \text{ ft}$	$x_4 := 0.5 \text{ ft}$	$x_5 := 0.5 \text{ ft}$	$x_6 := 3.0 \text{ ft}$	$B := x_4 + x_2 + x_1 + x_3 + x_5 = 12.5$
Soil properties	$\gamma_1 := 130 \text{ pcf}$	$\gamma_2 := 115 \text{ pcf}$	$k_1 := \frac{1}{2}$	$k_2 := \frac{1}{2}$	height of water behind the wall		
	$\gamma_{1sat} := 135 \text{ pcf}$	$\gamma_{2sat} := 130 \text{ pcf}$			$h_{wb} := 7 \text{ ft}$		
	$\phi'_1 := 32 \text{ deg}$	$\phi'_2 := 28 \text{ deg}$	$\gamma_w := 62.4 \text{ pcf}$				
	$c'_1 := 0$	$c'_2 := 300 \text{ psf}$	$H := H_u + D - x_6 = 17 \text{ ft}$				
	$\delta' := \frac{2}{3} \cdot \phi'_1 = 0.372$						

## METHOD

### A) OVERTURNING STABILITY:

- Determine the Coulomb Active Force per unit length of Wall using Equation 7.27
  - Determine  $K_a$  using EQ 7.26  
The angles can be obtained through the geometry of the wall
  - Determine the  $y_{eq}$  due to the surcharge using EQN 7.28  
This equation will take in consideration the effects due to the surcharge into  $P_a$
- Determine the location of the Coulomb Active force (a) using statics concepts
- Determine the overturning moment
  - Determine angle that the force  $P_a$  is applied to the wall using geometry
  - Determine horizontal component and moment caused by
  - Determine the horizontal hydrostatic force caused by the water in the soil, and the corresponding overturning moment it causes
  - The total overturning moment will be equal to the sum of the two moments calculated in 3.2 and 3.3
- Determine the resisting forces and its corresponding moments
  - For the areas of concrete below the water, an specific effective weight of concrete is used in order to represent the effect of water buoyancy on the structure
  - The forces are tabled and vertical forces summed, as well as moments
- Determine  $F_{S_{overturning}}$  (Use EQN 8.5)

### B) SLIDING

Determine  $K_p$  (Use equation on page 385)  
Sliding Factor of Safety can be calculated with EQ 8.11  
The values that represent the hydrostatic pressure vertically resisting sliding and contributing to it are added to the equation

### C) BEARING CAPACITY FAILURE

- Determine eccentricity and maximum and minimum pressures (pressures at the toe and heel of wall) (EQNS 8.18 & 8.21)
  - Use Table 3.3 to determine Bearing Capacity Factors
  - Use Table 3.4 to determine Depth and Inclination Factors
  - Use Meyerhoff's Equation 8.22 do determine bearing capacity  $q_u$
  - Determine Bearing Capacity using EQ 8.23

SOLUTION Given the general dimensions we can obtain  $H_t$ :  $H_t := H_u + D = 20 \text{ ft}$

$$\beta := \text{atan}\left(\frac{H}{x_3}\right) = 1.285 \quad \text{Angle of the backfill: } \alpha := 0 \cdot \text{deg}$$

$$K_a := \frac{(\sin(\beta + \phi'_1))^2}{\sin(\beta)^2 \cdot \sin(\beta - \delta') \cdot \left[ 1 + \sqrt{\frac{(\sin(\phi'_1 + \delta') \cdot \sin(\phi'_1 - \alpha))}{\sin(\beta - \delta') \cdot \sin(\alpha + \beta)}} \right]^2} = 0.417 \quad \text{Eqn 7.26}$$



$$\gamma_{eq} := \gamma_1 + \left( \frac{\sin(\beta)}{\sin(\beta + \alpha)} \right) \cdot \left( 2 \cdot \frac{q}{H} \right) = 159.412$$

$$P_a := .5 \cdot \gamma_{eq} \cdot H^2 \cdot K_a = 1.329 \times 10^4 \text{ plf} \quad \text{EQ 7.27}$$

Location of the line of action of the resultant:

from the bottom of the wall

$$z := \frac{\left[ 0.5 \cdot K_a \cdot \gamma_1 \cdot \frac{H^3}{6} + K_a \cdot \frac{H^2}{2} \cdot q \cdot \left( \frac{\sin(\beta)}{\sin(\beta + \alpha)} \right) \right]}{P_a} = 4.287 \text{ ft}$$

AS SEEN IN EXAMPLE 7.7 page 347

Angle for the force  $P_a$

$$\alpha_2 := 90 - \frac{\beta}{\text{deg}} + \frac{\delta'}{\text{deg}} = 37.723 \quad \alpha := 37.723 \cdot \text{deg} = 0.658$$

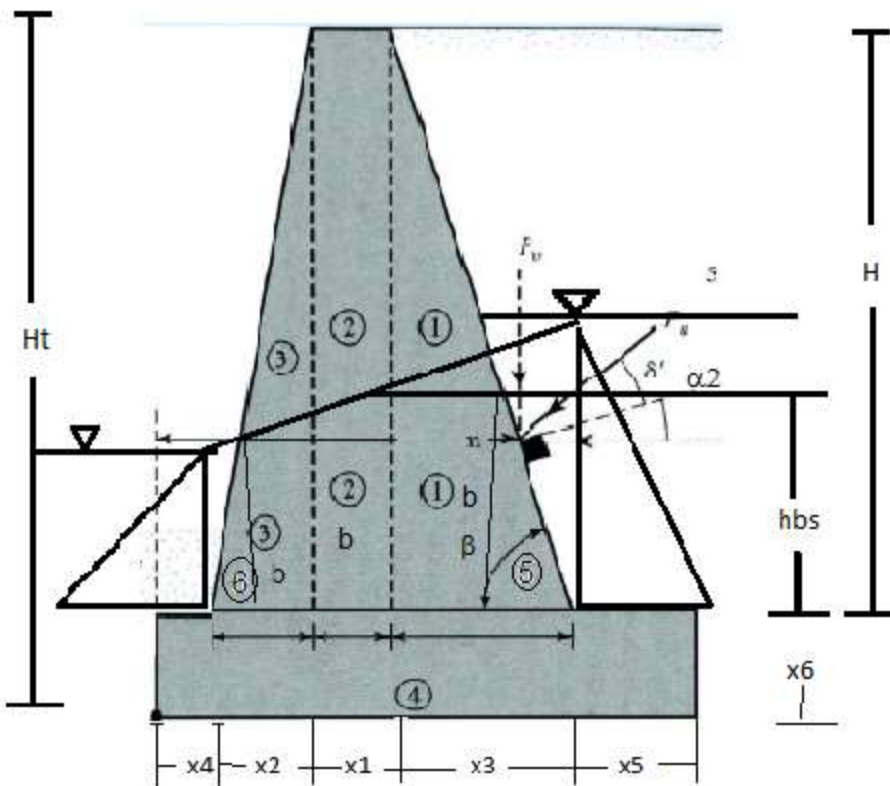
### Overturning components:

$$P_h := P_a \cdot \cos(\alpha_2) = 1.328 \times 10^4 \text{ plf} \quad M_{o1} := P_h \cdot (z) = 5.695 \times 10^4 \text{ lb} - \frac{\text{ft}}{\text{ft}} \quad \text{CCW}$$

The hydrostatic pressure (and force  $F_{bw}$ ) behind the wall also causes an overturning moment:

$$F_{bw} := A_{5w} = 1.529 \times 10^4 \text{ plf} \quad M_{o2} := F_{bw} \cdot \frac{z^2}{3} = 3.567 \times 10^3 \text{ CCW} \quad M_o := M_{o1} + M_{o2} = 6.051 \times 10^4 \text{ plf} \quad \text{CCW}$$

Resisting Components:



To determine the height of concrete that is submerged:

$$h_b := 6 \text{ ft} \quad h_{bs} := 6 - x_6 = 3$$

Obs for the table below:

1. The suffix b (below) refers to areas submerged (below the water)
2. The vertical component of the surcharge is taken into consideration as a resisting force (See 7 below)
3. The vertical component of the hydrostatic pressure in the front of the wall causes a resisting moment (See 6 below)
4.  $P_p$  also causes a resisting moment, however, we'll assume it equal to zero for a conservative approach
5. Although the moments below are shown as positive they are in fact clockwise (thus negative)

Effective Concrete Weight At  $z=13 \text{ x}$  for the triangle (A1 & A3)

$$\gamma_{c'} := \gamma_c - \gamma_w = 87.6$$

$$x_{in} := x_3 \cdot \frac{(H - h_{bs})}{H}$$

Effective Soil Weight

$$\gamma_{s'} := \gamma_1 - \gamma_w = 67.6$$

Height above water table  $H_w := H_t - 7 = 13 \text{ ft}$

**Figure 4.1** - Area distribution and location of important geometrical variables for table 4.1 below

SEC	AREA (ft <sup>2</sup> )	W/unit length (plf)	M. Arm to C (ft)	Moment lb-ft/ft
1	$A1 := x_{in} \cdot \frac{(H - hbs)}{2} = 28.824$ $A1b := (x_{in}) \cdot hbs = 12.353$	$w1 := \gamma_c \cdot A1 = 4.324 \times 10^3$ $w1b := \gamma_c' \cdot A1b = 525.6$	$B1 := x4 + x2 + x1 + .667 \cdot x_{in} = 9.746$ $B1b := x4 + x2 + x1 + .5 \cdot x_{in} = 9.059$	$M1 := w1 \cdot B1 = 4.214 \times 10^4$ $M1b := w1b \cdot B1b = 4.761 \times 10^3$
2	$A2 := (x1) \cdot (H - hbs) = 21$ $A2b := (x1) \cdot (hbs) = 4.5$	$w2 := \gamma_c \cdot A2 = 3.15 \times 10^3$ $w2b := \gamma_c' \cdot A2b = 394.2$	$B2 := x3 + x2 + .5x1 = 10.75$ $B2b := B2 = 10.75$	$M2 := w2 \cdot B2 = 4.39 \times 10^3$ $M2b := w2b \cdot B2b = 4.238 \times 10^3$
3	$A3 := x_{in} \cdot \frac{(H - hbs)}{2} = 28.824$ $A3b := (x_{in}) \cdot hbs = 12.353$	$w3 := (\gamma_c) \cdot A3 = 4.324 \times 10^3$ $w3b := \gamma_c' \cdot A3b = 1.082 \times 10^3$	$B3 := x4 + x2 - .667 \cdot x3 = 2.165$ $B3b := x4 + x2 - .5x3 = 3$	$M3 := w3 \cdot B3 = 9.36 \times 10^3$ $M3b := w3b \cdot B3b = 3.246 \times 10^3$
4	$A4 := x6 \cdot B = 37.5$	$w4 := \gamma_c' \cdot A4 = 3.285 \times 10^3$	$B4 := 0.5 \cdot B = 6.25$	$M4 := w4 \cdot B4 = 2.053 \times 10^4$
5	$A5 := (x3 - x_{in}) \cdot \frac{hbs}{2} = 1.324$	$w5 := \gamma_c' \cdot A5 = 115.941$	$B5 := x4 + x2 + x1 + \frac{2}{3}x3 + \frac{1}{3} \cdot x_{in} = 11.706$	$M5 := w5 \cdot B5 = 1.357 \times 10^3$
6	$A6 := (x3 - x_{in}) \cdot \frac{hbs}{2} = 1.324$	$w6 := \gamma_c' \cdot A6 = 115.941$	$B6 := x4 + .333 \cdot (x2 - x_{in}) = 0.794$	$M6 := w6 \cdot B6 = 92.037$
7	Hydrostatic Force Front	$F_{fw} := 0.5 \cdot \gamma_w \cdot D^2 = 780 \text{ plf}$ $P_v := P_a \cdot \sin(\alpha_2) = 315.729$	$B7 := 0.333 \cdot D = 1.665$ $B8 := B - \frac{(z - x6)}{\tan(\beta)} - x5 = 11.622$	$M7 := F_{fw} \cdot B6 = 619.182$ $M8 := P_v \cdot B8 = 3.669 \times 10^3$
$\Sigma V := w1 + w1b + w2b + w2 + w3 + w3b + w4 + w5 + w6 + P_v = 1.763 \times 10^4 \frac{\text{lb}}{\text{ft}}$				
$\Sigma M_r := M1 + M1b + M2b + M2 + M3 + M3b + M4 + M5 + M6 + M7 + M8 = 9.44 \times 10^4 \text{ lb} - \frac{\text{ft}}{\text{ft}}$				
$F_{S_{\text{overturning}}} := \frac{\Sigma M_r}{M_o} = 1.56$ if( $F_{S_{\text{overturning}}} > 2$ , "OK!" , "No Good") = "No Good"				

### Factor of Safety against Sliding

We must obtain  $K_p$

$$K_p := \tan\left(45 \cdot \text{deg} + \frac{\phi'_1}{2}\right)^2 = 3.255 \quad P_p := 0.5 \cdot K_p \cdot \gamma_2 \cdot D^2 + 2 \cdot c'_2 \cdot \sqrt{K_p} \cdot D = 1.009 \times 10^4$$

$$\text{EQ 8.11} \quad F_{S_{\text{sliding}}} := \frac{(\Sigma V \cdot \tan(k1 \cdot \phi'_2) + B \cdot k2 \cdot c'_2 + P_p + F_{fw})}{(P_a \cdot \cos(\alpha) + F_{bw})} = 1.424 \quad \text{if}(F_{S_{\text{sliding}}} > 1.5, \text{"okay"} , \text{"not good"}) = \text{"not good"}$$

### FACTOR OF SAFETY AGAINST BEARING CAPACITY FAILURE



$$e := \frac{B}{2} - \frac{(\sum M_r - M_o)}{\sum V} = 4.328 \text{ ft} \quad \text{EQ 8.16, 8.17 and 8.18} \quad \text{if} \left( e < \frac{B}{6}, \text{"okay"} , \text{"not good"} \right) = \text{"not good"}$$

$$q_{toe} := \frac{\sum V}{B} \cdot \left( 1 + 6 \cdot \frac{e}{B} \right) = 4.341 \times 10^3 \text{ psf} \quad q_{heel} := \frac{\sum V}{B} \cdot \left( 1 - 6 \cdot \frac{e}{B} \right) = -1.52 \times 10^3 \text{ psf} \quad q_{max} := \max(q_{toe}, q_{heel})$$

Using Table 3.3 we have:  $\phi'2 := 28 \cdot \text{deg}$   $N_c := 25.8$   $N_q := 14.72$   $N_\gamma := 16.72$   $B' := (B - 2e) = 3.844 \text{ ft}$

$$p := \frac{D}{B'} = 1.301 \quad F_{\gamma d} := 1 \quad F_{qd} := 1 + 2 \cdot \tan(\phi'2) \cdot (1 - \sin(\phi'2))^2 \cdot \left( \frac{D}{B'} \right) = 1.389 \quad F_{cd} := F_{qd} - \frac{(1 - F_{qd})}{N_c \cdot \tan(\phi'2)} = 1.418$$

$$\psi := \frac{180}{\pi} \cdot \text{atan} \left[ \frac{(P_a \cdot \cos(\alpha) + F_{bw})}{\sum V} \right] = 34.327 \quad \psi := 23.119 \text{ deg} \quad F_{ci} := \left( 1 - \frac{\psi}{90 \cdot \text{deg}} \right)^2 = 0.552 \quad F_{qi} := F_{ci} = 0.552$$

$$F_{\gamma i} := \left( 1 - \frac{\psi}{\phi'2} \right)^2 = 0.03 \quad q := (\gamma_2 - \gamma_w) \cdot D = 263$$

$$q_u := c'2 \cdot N_c \cdot F_{cd} \cdot F_{ci} + q \cdot N_q \cdot F_{qd} \cdot F_{qi} + .5 \cdot \gamma_2 \cdot B' \cdot N_\gamma \cdot F_{\gamma d} \cdot F_{\gamma i} = 9.142 \times 10^3$$

$$FS_{bearing} := \frac{q_u}{q_{max}} = 2.106 \quad \text{if}(FS_{bearing} > 3, \text{"okay"} , \text{"not good"}) = \text{"not good"}$$

**PART B** In the analysis of the gravity wall, it is conservative to not account for the resisting moment given the soil behind the wall. In this case, however, the design becomes unsafe and fails in overturning and bearing capacity.

**PART C** I would recommend the cantilever as a preferred design. I am more confident in its design calculations, I believe it is likely easier to be constructed (instead of sloping walls) which would likely reduce in construction time and cost. The simplicity also shows that it will likely require less material while maintaining satisfactory levels of safety, which also represent a reduced value in cost.

The current design already satisfies overturning and sliding, thus, to improve and achieve final factor of safety of design I would recommend to increase the value of  $q_u$  and/or decrease the value of  $q_{max}$ .

To increase the value of  $q_u$ , one possible modification is to add soil to the front of the retaining wall. By increasing the dimension  $D$  we increase the value of  $q_u$ . That, however, has costs included to it.

Another option is to increase the width of the base  $B$ . By increasing  $B$ , we reduce eccentricity  $e$ , increase effective width  $B'$ , which increases the final value of  $q_u$ . At the same time, this increase in  $B$ , also reduces the value of  $q_{max}$ , probably being more effective in reaching the factor of safety sought. It is necessary to take into account that the increase in  $B$ , will also increase in costs.

Thus a cost-analysis is necessary in order to obtain which one of the methods would be more effective and desired.



