

```

Exchange economy invariant
Exchange economy pairwise
Competitive economy invariant
---
Exchange economy
---
Two goods x and y, firm i and consumer j
Firm-consumer, consumer-firm, firm-firm, consumer-consumer to obtain mutual
advantage
---
i, j
x, y
 $q_x > 0$ 
 $q_y > 0$ 
 $p_{xm} > 0$ 
 $p_{ym} > 0$ 
 $p_x > 0$ 
 $p_y > 0$ 
 $m \sim R$ 
---
i -  $q_x, p_{xm} / j - q_x, p_{xm}$ 
i -  $q_y, p_{ym} / j - q_y, p_{ym}$ 
(a) [Isolated]
 $m_i = q_x p_{xm} + q_y p_{ym} > 0$ 
 $m_j = - q_x p_{xm} - q_y p_{ym} < 0$ 
(b) [Non-isolated]
 $m_i = q_x p_x + q_x p_{xm} + q_y p_y + q_y p_{ym} = q_x (p_x + p_{xm}) + q_y (p_y + p_{ym}) > 0$ 
 $m_j = - q_x p_x - q_x p_{xm} - q_y p_y - q_y p_{ym} = - q_x (p_x + p_{xm}) - q_y (p_y + p_{ym}) < 0$ 
---
 $m_i + m_j = 0$ 
Exchange economy invariant
---
i -  $q_y, p_{ym} / j - q_x, p_{xm}$ 
i -  $q_x, p_{xm} / j - q_y, p_{ym}$ 
(1)
(a)
 $m_i = q_y p_{ym} > 0$ 
 $m_j = - q_x p_{xm} < 0$ 
(b)
 $m_i = q_y p_y + q_y p_{ym} = q_y (p_y + p_{ym}) > 0$ 
 $m_j = - q_x p_x - q_x p_{xm} = - q_x (p_x + p_{xm}) < 0$ 
(2)
(a)
 $m_i = q_x p_{xm} > 0$ 
 $m_j = - q_y p_{ym} < 0$ 
(b)
 $m_i = q_x p_x + q_x p_{xm} = q_x (p_x + p_{xm}) > 0$ 
 $m_j = - q_y p_y - q_y p_{ym} = - q_y (p_y + p_{ym}) < 0$ 
---
 $m_{i1} + m_{j2} = 0$ 
 $m_{i2} + m_{j1} = 0$ 
Exchange economy pairwise
---
Competitive economy
---
Firm i, consumer j, good x
Firm and consumer do not consider
their actions to have any effect on prices
---
i, j
x
 $q > 0$ 
 $p_m > 0$ 
 $p > 0$ 

```

$m \sim R$

(a)

$$m_i = q^* p > 0$$

$$m_j = -q^* p < 0$$

(b)

$$m_i = q^* p + q^* p_m = q^* (p + p_m) > 0$$

$$m_j = -q^* p - q^* p_m = -q^* (p + p_m) < 0$$

$$m_i + m_j = 0$$

Competitive economy invariant