

$$Q = \{x \in \mathbb{R}^2 \mid Ax \leq b\}, \text{ where } A = \begin{bmatrix} a_1^T \\ \vdots \\ a_m^T \end{bmatrix} \in \mathbb{R}^{m \times 2} \text{ and } b = \begin{bmatrix} b_1 \\ \vdots \\ b_m \end{bmatrix} \in \mathbb{R}^m$$

Therefore our polygon will be defined by m equations of the form:

$$\boxed{a_1^T \cdot x \leq b_1} \text{ (for the 1st entry)}$$

$$\hookrightarrow a_{11} \cdot x_1 + a_{12} \cdot x_2 \leq b_1 \Leftrightarrow x_2 \leq -\frac{a_{11}}{a_{12}} \cdot x_1 + \frac{b_1}{a_{12}}$$

$$B = \{x \in \mathbb{R}^2 \mid \|x - c\| \leq r\}$$

The linear problem that needs to be solved is:

$$\begin{array}{l} \max r \\ \text{such that } Ax \leq b \end{array} \Rightarrow c + \frac{a_i}{\|a_i\|_2} \cdot r = x \Rightarrow$$

$$\Leftrightarrow a_i^T \cdot x \leq b_i \Leftrightarrow$$

$$\Leftrightarrow a_i^T \left(c + \frac{a_i}{\|a_i\|_2} r \right) \leq b_i \Rightarrow \boxed{a_i^T \cdot c + \|a_i\|_2 r \leq b_i} \Rightarrow$$

$$\Rightarrow \underline{A - ub} \text{ is: } \begin{bmatrix} a_1^T & \|a_1\|_2 \\ \vdots & \vdots \\ a_m^T & \|a_m\|_2 \end{bmatrix} \text{ and } \underline{b - ub} = b = \begin{bmatrix} b_1 \\ \vdots \\ b_m \end{bmatrix}$$

and \underline{c} is: $[-1, 0, 0]$.

\hookrightarrow these values we fed to the linprog func.