Clever Randomization and Ensembling Strategies for Accommodating Multiple Data Pathologies in Conjoint Studies

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October 15, 2019

Outline

Conjoint Analysis

Ensembles

Data Pathologies

Model Development

Conclusion

Conjoint Analysis in Marketing

- Products are defined by attributes, each with a number of levels
- Individuals choose from among a number of alternatives
- We infer individual-level preferences for each attribute level
- ► Market simulators make use of individual-level preference estimates to forecast the demand for **potential products** compared with the competition
- ► This can inform **new product development**, **pricing**, product line optimization, and go-no-go decision-making

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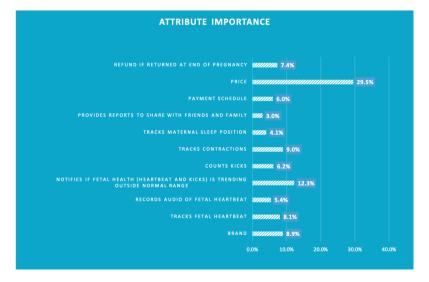
Conjoint Analysis Example - Choice Task

Taking into consideration all of the features presented, please pick the **pregnancy monitoring device** that you would be **most likely to buy**.

	Option 1	Option 2	Option 3	Options 4
Tracks fetal heart rate	summer infant	MOTOROLA	& bloomlife	Owlet
Tracks fetal heart rate	•	8	•	8
Records fetal heartbeat	•	•	8	8
Notifies if fetal health (heartbeat and kicks) is trending outside normal range	0	•	Ø	•
Counts kicks	•	Ø	8	Ø
Tracks contractions	8	Ø	8	0
Tracks maternal sleep position	•	0	•	•
Provides reports to share with friends and family	8	•	•	•
Payment Schedule	Rental	1 time payment	Rental	Monthly payments
Total Price	\$174	\$399	\$374	\$374
Refund if returned at end of pregnancy	\$20	\$60	\$80	\$10
	0	0		0

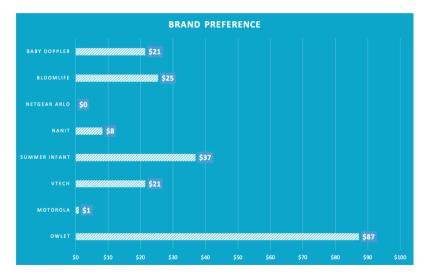
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Conjoint Analysis Example - Attribute Importance



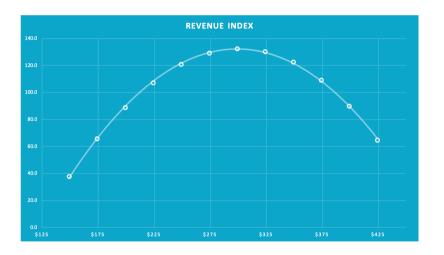
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Conjoint Analysis Example - Brand Premium



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Conjoint Analysis Example - Optimal Price



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Motivation: Ensemble Approaches to Prediction

1. Ensemble-based approaches currently dominate the world of **competitive prediction** (e.g., Kaggle, Netflix Prize, etc.)

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Wisdom from a Kaggle Superstar

No matter how faithful and well-tuned your individual models are, you are likely to improve the accuracy with ensembling. Ensembling works best when the individual models are less correlated. Throwing a multitude of mediocre models into a blender can be counterproductive. Combining a few well-constructed models is likely to work better.

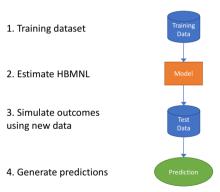
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Motivation: Ensemble Approaches to Conjoint Prediction

- 1. Ensemble-based approaches currently dominate the world of competitive prediction (e.g., Kaggle, Netflix Prize, etc.)
- 2. With a few notable exceptions, most conjoint projects are still conducted using a **single model** for both inference and simulation

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The Current Approach to Prediction



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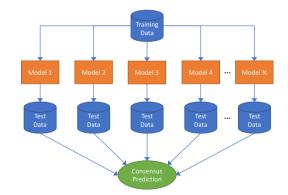
Motivation: Ensemble Approaches to Conjoint Prediction

- 1. Ensemble-based approaches currently dominate the world of competitive prediction (e.g., Kaggle, Netflix Prize, etc.)
- 2. With a few notable exceptions, most conjoint projects are still conducted using a single model for both inference and simulation
- 3. A notable exception is Kevin Lattery's Sawtooth 2015 presentation and paper, "A Machine Learning Approach to Conjoint"

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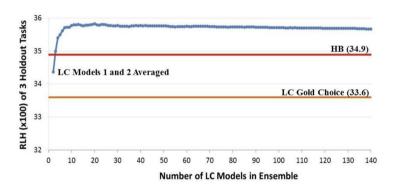
An Ensemble Approach to Conjoint Prediction

- 1. Training dataset
- 2. Estimate different types of models
- 3. Simulate outcomes on new data
- 4. Generate a consensus prediction



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Results from Kevin Lattery's 2015 Paper



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Why Do Ensembles Perform So Well?

- ► They strike an optimal trade-off on the bias/variance frontier
 - Wisdom of the Crowd
- ▶ They allow for efficient exploration of the model space
 - All models are wrong, but some models are useful
- ► They provide a hedge against data conditions that are pathological with respect to a single model (our hypothesis)

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What is a Data Pathology?

Pathology: Structural and functional **deviations from the normal** that constitute disease or characterize a particular disease

Data Pathology: Any **respondent-level behavior** that deviates from the **normative model** of consumer choice, thus impeding accurate out-of-sample prediction

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What is the Normative Model of Consumer Choice? (In Math)

For a given individual and choice task:

$$y \in \{1, 2, \cdots, J\}$$
 $U_j = V_j + \varepsilon_j$
 $V_j = \beta_1 x_{1j} + \beta_2 x_{2j} + \beta_k x_{kj}$
 $\varepsilon_j \sim \mathsf{iid} \; \mathsf{Gumbel}$

Across respondents:

$$\beta \sim N\left(\bar{\beta}, \Sigma\right)$$

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What is the Normative Model of Consumer Choice? (In Words)

- Consumers are able to assess the "utility" of each alternative in a choice set
- They pick the alternative that provides the greatest level of utility
- Utility is made up of two components: A deterministic component and a random (to the researcher) component
- ► The deterministic component is expressed as a (linear, compensatory) function of the design of the alternative
- ► The random component is assumed to come from an independent and identically distributed Gumbel distribution
- While we estimate preferences at the individual level, we assume that the preferences of all individuals are drawn from a common Multivariate Normal Distribution

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Models of Data Pathologies

- Most innovations in the academic conjoint literature focus on addressing specific data pathologies
- ▶ These models fit better and provide marginal improvements in predictive fit
- ► Although prospectively useful, these models are rarely used in practice

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Examples of Data Pathologies

- Attribute Non-Attendance
- Screening Rules
- Poor Respondent Quality
- Respondent Fatigue
- ► Alternative Decision Rules (e.g., Regret Minimization)

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Why Aren't These Models Used in Practice?

- 1. They are theoretically and computationally complex (i.e., difficult to understand and time-consuming to estimate and simulate)
- We don't have high-quality commercial software that can be used to fit these models
- 3. Each model deals with a single data pathology
 - A priori how do I know which pathology will prove problematic (i.e., which model should I fit)?
 - What if multiple pathologies are present in a single dataset?

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Our Proposed Approach

- Create an ensemble of models where diversity in the ensemble is created through various forms of (clever) randomization
- Induce diversity in the ensemble by thinking about how specific forms of randomization are related to specific data pathologies
- Generate a consensus prediction from the set of models in the ensemble

Note: Our focus in this study is to improve **out-of-sample predictive validity**!

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A Summary Thus Far...

- Conjoint analysis is a powerful tool
- Decisions are informed based on predictions using a market simulator
- Ensembles are cool and powerful for prediction
- We don't use them in the world of conjoint
- Data pathologies can lead to bad inference and prediction
- Cleverly designed ensembles of models might help hedge against data pathologies
 - We don't have to fit complicated models, but we do need to fit a lot of models!
 - Trade-off between model complexity and computational intensity

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Pathology 1: Attribute Non-Attendance (ANA)

Attribute Non-Attendance: Respondents ignore subsets of attributes when making decisions (i.e., $\beta = 0$ for all levels of the attribute)

Randomization Strategy for the Ensemble: Create an ensemble where we randomly set the coefficients for a full attribute to 0

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Ensemble Algorithm for Attribute Non-Attendance

- 1. Estimate an HB MNL on training data
- 2. Loop over respondent-level estimates $(\hat{\beta}_h)$
 - randomly select an attribute
 - with probability heta set all coefficients for that attribute to 0
- 3. Predict first choices (e.g., max utility) for each choice set in the out-of-sample holdout (test) data
- 4. Repeat 2 and 3 many times
- 5. Generate a consensus (e.g., most commonly selected) prediction

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Pathology 2: Screening Behavior

Screening Behavior: Respondents use certain attribute levels to screen out alternatives from consideration (i.e., $\beta \approx -\infty$ for levels being screened on)

Randomization Strategy for the Ensemble: Create an ensemble where we randomly set the coefficients for attribute levels to $\approx -\infty$

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Ensemble Algorithm for Screening Behavior

- 1. Estimate HB MNL on training data
- 2. Loop over respondent-level estimates $(\hat{\beta}_h)$
 - randomly select an attribute level
 - with probability ψ set the coefficient for that attribute level to $pprox -\infty$
- 3. Predict first choices (e.g., max utility) for each choice set in the validation data
- 4. Repeat 2 and 3 many times
- 5. Generate a consensus (e.g., most commonly selected) prediction

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Joint Ensemble Algorithm for Attribute Non-Attendance and Screening

- 1. Estimate HB MNL on training data
- 2. Loop over respondent-level estimates $(\hat{\beta}_h)$
 - randomly select an attribute level
 - with probability ψ set the coefficient for that attribute level to $\approx -\infty$
 - randomly select an attribute
 - with probability θ set all coefficients for that attribute to 0
- 3. Predict first choices (e.g., max utility) for each choice set in the validation data
- 4. Repeat 2 and 3 many times
- 5. Generate a consensus (e.g., most commonly selected) prediction

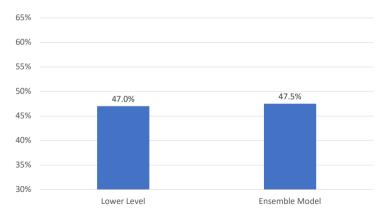
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Simulation Study

- Simulate data with the presence or absence of pathologies: attribute non-attendance and/or screening
- ▶ 500 respondents; 12 choice tasks; 6 attributes
- Generate prediction from standard HBMNL results (lower level) and the ANA, Screening, or joint ANA + Screening Ensemble

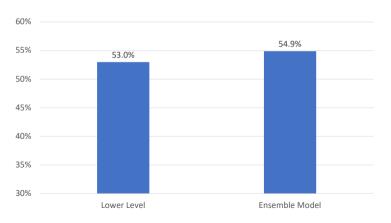
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Simulated Data: No ANA + No Screening



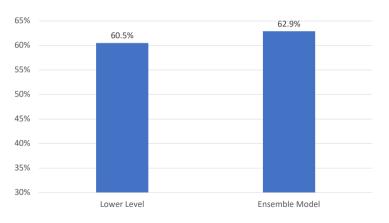
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Simulated Data: ANA without Screening



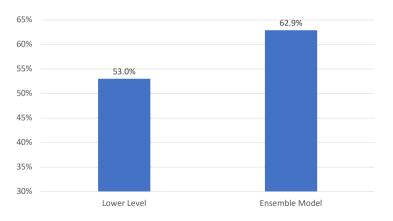
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Simulated Data: Screening without ANA



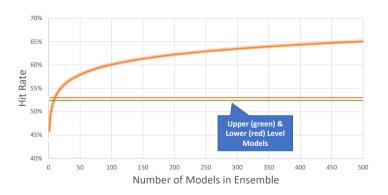
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Simulated Data: ANA + Screening



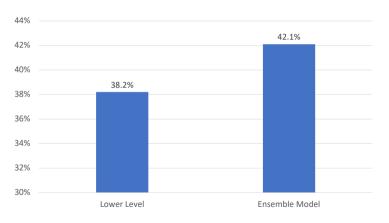
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Predictive Fit as a Function of Ensemble Size



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Performance on Actual Data - Interior Paint



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Conclusion

- Cleverly designed ensembles of models appear to help hedge against data pathologies and improve prediction
- ► The ensemble approach is especially powerful in the presence of multiple data pathologies

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Next Steps

- 1. Faster computation (Stan)
- 2. More pathologies
- 3. Smarter ensembles: Can we employ principles of experimental design to (cleverly) cover the design space of multiple pathologies?
- 4. Better aggregation of prediction (e.g., model stacking via a meta-learner rather than consensus predictions)
- 5. Ensembles for inference: Can we learn about the severity of a particular pathology by examining the relative fit of ensemble members?

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Thank You!

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