#### **AC – Aprendizagem Computacional / Machine Learning**

# P4b – Multilayer neural networks

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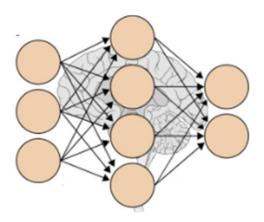
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- 1 Objectives
- 2 | Datasets
- 3 | Tasks
- 4 | Conclusions

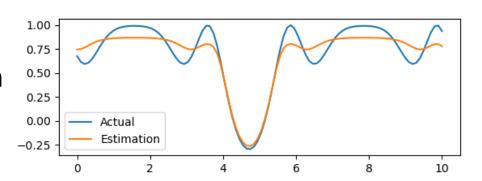
- MLNN Multi Layer neural networks
  - Concepts
  - Implement BackPropagation from scratch
    - Regression Approximate a non-linear function
  - Use python/scikit learning functionalities
    - Classification
    - Regression
  - Evaluation the performance of the MLNN classifier/regressor
    - SE, SP, F1score (classification)
    - MSE, R2 (regression)

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#### Datasets

- 1 | Function approximation
  - Simple problem regression
  - P4\_function.csv



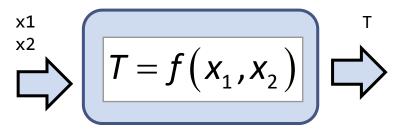
- 2 | Cardiac Risk
  - Classification
  - P4\_cardiacRiskClassification.csv
  - Output = {0,1} {event, NO event}
- 3 | Cardiac Risk
  - Regression
  - P4\_cardiacRiskRegresssion.csv
  - Output = [0..1] probability to have an event

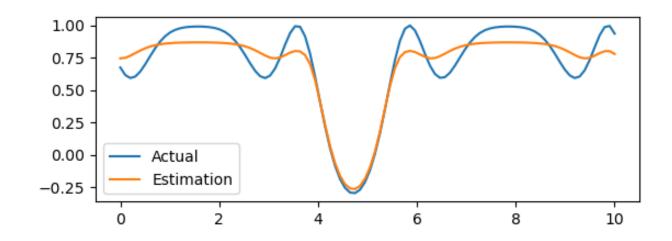


# 1 Datasets – function approximation

Non-linear function

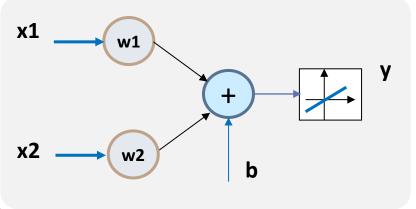
P4\_function.csv

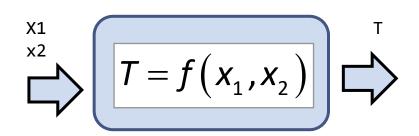


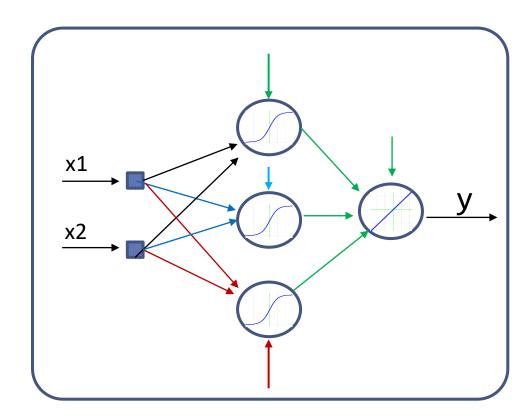


# 1 | Function approximation

- Two possible structures
  - 1. Adaline : one layer
  - 2. MLNN: hidden layer
- Learning:
  - 1. RMLSE
  - 2. Backpropagation



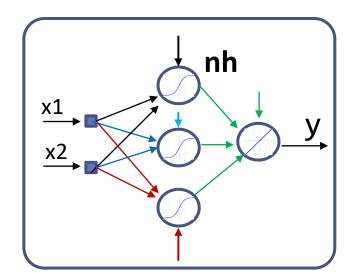




- 2 Datasets Cardiac Risk
  - Use of scikit learning functionalities
    - Structure: MLNN one hidden layer
    - Activation functions
      - Hidden layer sigmoidal (nh neurons)
      - Output layer linear (one neuron)

- Classification T={0,1}
- Regression T=[0..1]





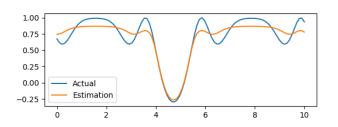
# JH AC P4. MLNN

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# 1 | Function approximation

P4\_function.csv



# 1.1 | Structure

#### **Activation function**

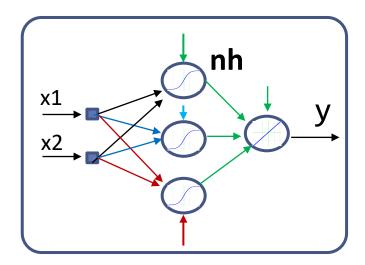
Sigmoidal / Linear

# Number of hidden layers

• nh = ?

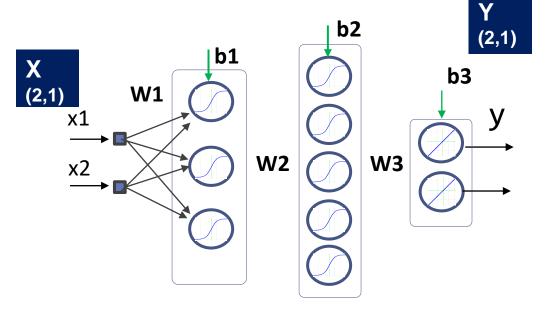
# 1.2 | Learning: Back Propagation

Perform the computations by hand!



### 1 BP: example

**FORWARD** 



$$a^0 = x$$

$$n^1 = W^1 a^0 + b^1$$

$$a^1 = f^1(n^1)$$

$$n^2 = W^2 q^1 + b^2$$
 (5,3)(3,1)+(5,1)

$$^{2}a^{1} + b^{2} \frac{(5,3)}{(5,3)}$$

$$a^2 = f^2(n^2)$$

$$(5,3)(3,1)+(5,1)$$

$$n^3 = W^3 a^2 + b^3$$

$$n^{\circ} = VV^{\circ}a^{-} + b^{\circ}$$

$$a^3=f^3(n^3)$$

$$(2,5)(5,1)+(2,1)$$

$$y = a^3$$

# Last layer (m=3)

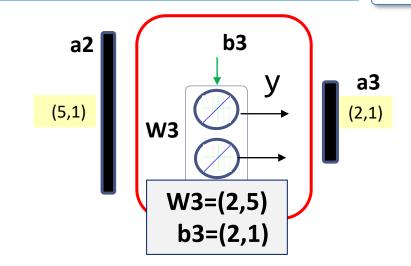
$$n^3 = W^3 a^2 + b^3$$
$$a^3 = f^3(n^3)$$

$$e = e^3 = t - a^3 = t - y$$

$$\left| \dot{f}(n^3) = df^3(\cdot) \right|$$

$$\left| \frac{dE}{dw^3} = \frac{d(e^3)^2}{dw^3} = -2 e^3 f^3(\cdot)(a^2)^T \right|$$

$$\frac{dE}{db^{3}} = \frac{d(e^{3})^{2}}{db^{3}} = -2 f^{3}(\cdot)e^{3}$$



$$s^3 = e^3 \otimes df^3(\cdot)$$
 (2,1)\omega (2,1)\omega (2,1)

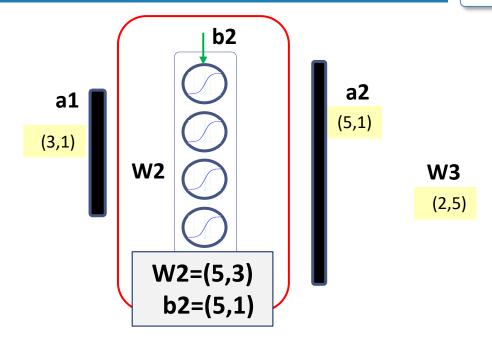
$$dW^{3} = s^{3} \left(a^{2}\right)^{T}$$
 (2,1) (1,5)

$$db^3 = s^3$$
 (2,1)

# ■ Hidden layer (*m*=2)

$$n^2 = W^2 a^1 + b^2$$
$$a^2 = f^2(n^2)$$

$$s^{m-1} \equiv (w^m)^T s^m \dot{f}(n^{m-1})$$



$$|f(n^2) = df^2(\cdot)|$$
 (5,1)

$$s^2 = (w^3)^T s^3 \otimes df^2(\cdot)$$

$$((5,2)(2,1)) \otimes (5,1)$$

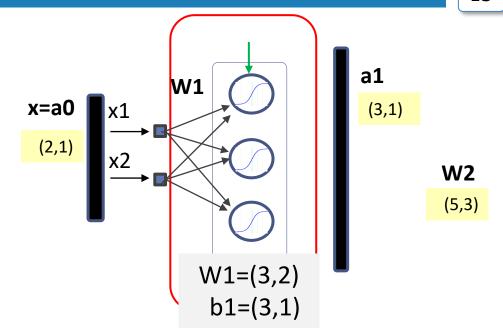
$$dW^{2} = s^{2} (a^{1})^{T}$$
(5,1) (1,3) = (5,3)

$$db^2 = s^2$$
 (5,1)

# ■ First layer (*m*=1)

$$n^1 = W^1 a^0 + b^1$$
$$a^1 = f^1(n^1)$$

$$s^{m-1} \equiv (w^m)^T s^m \dot{f}(n^{m-1})$$



$$f(n^1) = df^1(\cdot)$$
 (3,1)

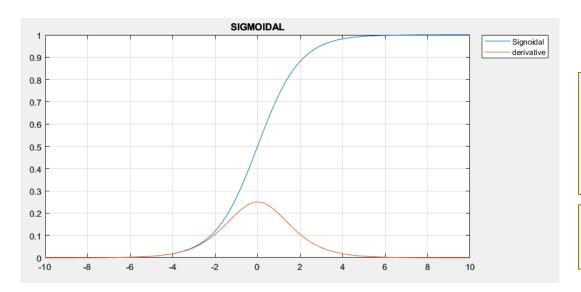
$$s^1 = (w^2)^T s^2 \otimes df^1(\cdot)$$

$$((3,5)(5,1)) \otimes (3,1)$$

$$dW^{1} = s^{1} \left(a^{0}\right)^{T}$$
(3,1) (1,2) = (3,2)

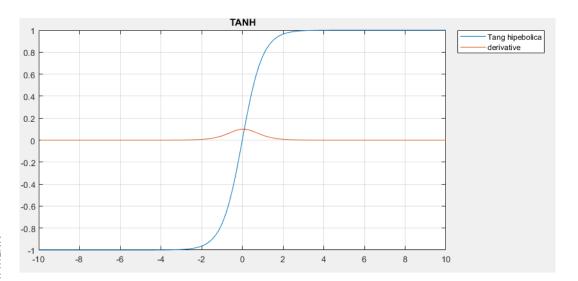
$$db^1 = s^1$$

# 3 | Tasks



$$f(x) = \frac{1}{1 + \exp(-x)}$$

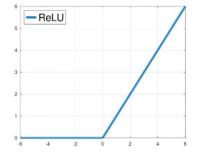
$$df(x) = f(x)(1-f(x))$$

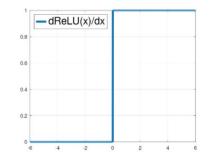


$$f(x) = \frac{\exp(x) - \exp(-x)}{\exp(x) + \exp(-x)}$$

# RLU

# $f(x) = \max(0,x) = egin{cases} x & ext{if } x > 0, \ 0 & ext{otherwise.} \end{cases} f'(x) = egin{cases} 1 & ext{if } x > 0, \ 0 & ext{if } x < 0. \end{cases}$





#### Properties

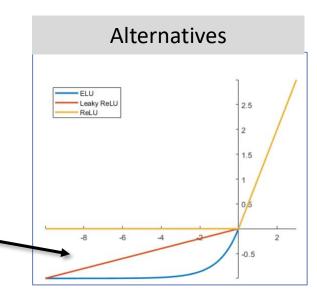
- Linear for positive values
- Non-linear for negative values

#### Advantages

- Avoids vanish gradient: unlike sigmodal does not saturate for positive values
- Simple, fast, efficient

#### Disadvantages

- Non-zero centered output
- Dead neurons: always zero (consistently negative values)



# Tasks

#### 1 | Function approximation

P4 function.csv

```
alfa=0.001
W2=np.random.random((ny, nh1))
B2=np.random.random((ny,
                          1))
W1=np.random.random((nh1, nx))
B1=np.random.random((nh1, 1))
MI=np.ones(n,1)
```

**b1** W2 W<sub>1</sub> **b2** x1

```
FORWARD
```

$$f_1 = sigmoidal(x)$$
  
 $f_1 = f_1(1 - f_1) = 1 - f_1^2$ 

```
element by element
= np.dot(.)
                 multiplication
```

for numEP in range(EPOCHS): **FORWARD** a0 = Xa1 = np.dot(W1,a0) + B1y1 = sigmoid(a1); # sigmoidal a2 = np.dot(W2,a1) + B2# linear y2 = a2ERROR e2 = T - v2erro = np.dot( e2, e2.transpose()) # for each EPOCH **BACKPROPAGATIN** dy2 = 1S2 = e2\*dy2dW2 = alfa\*np.dot(S2, a1.transpose()) dB2 = alfa\*np.dot(S2, MI) W2 = W2 + dW2B2 = B2 + dB2dy1 = y1\*(1-y1)S1 = np.dot( W2.transpose(), S2)\*dy1 dW1 = alfa\* np.dot(S1, a0.transpose()) dB1 = alfa\*np.dot(S1, MI) W1 = W1 + dW1B1 = B1 + dB1

1H AC | P4. MLNN

- **2 | Dataset: Cardiac risk /** P4\_cardiacRiskClassification.csv
- 2.1 | Implement MLNN classification
  - Structure
    - Number of neurons = ?
    - Activation functions: Hidden layer / Output layer (sigmoidal/linear)
  - Training / test data
    - Learning algorithm (adam)

- 2 Dataset: Cardiac risk / P4\_cardiacRiskClassification.csv
- 2.2 Evaluation
  - SE, SP, F1score, ?

```
from sklearn.metrics import confusion_matrix

cm = confusion_matrix(Ttest, Ytest)
TN, FP, FN, TP = cm.ravel()
SE = TP/(TP+FN)
SP = TN/(TN+FP)
F1 = ...
```

- 3 | Cardiac risk / P4\_cardiacRiskRegression.csv
- 3.1 | Implement MLNN Regression
  - Structure
    - Number of neurons = ?
    - Activation functions: Hidden layer / Output layer (sigmoidal/linear)
  - Training / test data
    - Learning algorithm (adam)

- **3 | Dataset: Cardiac risk /** P4\_cardiacRiskRegression.csv
- ■3.2 | Evaluation
  - Mean squared Error

```
from sklearn.metrics import mean_squared_error

Etrain = mean_squared_error(Ttrain, Ytrain)
Etest = mean_squared_error(Ttest, Ytest)
```

- 3 | Cardiac risk / P4\_cardiacRiskRegression.csv
- Output activation function

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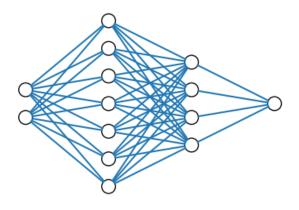
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# • N

- Multi Layer Neural Networks
  - Implement by hand the BP algorithm
    - Function approximation
  - Implement a MLNN
    - Classification
    - Regression problem
  - Evaluation
    - SE, SP classification
    - Error regression

#### Improvements

- Function approximation
  - 2 hidden layers ?



- MLNN Cardiac Risk
  - Activation functions: Hidden layer / Output layer ??
  - Learning algorithm ?
- Other ideas ?
  - Use of keras / tensorflow (more general tool)

# Scikit / Keras

```
KERAS=0 from sklearn.neural_network import MLPClassifier sklearn.neural_network import MLPRegressor

from keras.models import Sequential keras.layers import Dense
```

# Scikit / Keras

```
if KERAS==1:
   model = Sequential()
    if regression:
       model.add(Dense(32,activation='sigmoid'))
       model.add(Dense(18,activation='sigmoid'))
       model.add(Dense( 1,activation='linear'))
       model.compile(
                       loss='mse', optimizer='adam',
                        metrics=['mse'])
   else:
       model.add(Dense(33,activation='sigmoid')
       model.add(Dense(12,activation='sigmoid')
       model.add(Dense( 4,activation='sigmoid')
       model.add(Dense( 1,activation='sigmoid'))
       model.compile(
                        loss='binary crossentropy', optimizer='adam',
                        metrics=['accuracy'])
   model.fit(Xtrain, Ttrain, batch size=40, epochs=125, verbose=1)
```

# Scikit / Keras

```
history=model.fit(
                         Xtrain, Ttrain, validation split=0.3,
                         batch size=40, epochs=125, verbose=1)
if KERAS==1:
   #df = pd.DataFrame.from_dict(history.history)
   print(history.history.keys())
   plt.plot(history.history['loss'])
   plt.plot(history.history['val loss'])
   plt.title(' Training error')
   plt.ylabel('Error')
   plt.xlabel('epoch')
   plt.legend(['train', 'test'], loc='upper left')
   plt.show()
```