EA 2023/2024 PL exercises

Exercise 1 Show by induction:

```
a) 1^2 + 2^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}
```

b) For any  $n \geq 7$ , we have that  $n! > 3^n$ 

**Exercise 2** Show that the following recursive algorithm computes correctly the factorial of a number. Assume that  $n \ge 0$ .

```
Function F(n)

if n = 0 then

s = 1

else

s = n \cdot F(n - 1)

return s
```

**Exercise 3** Show that the following insertion sort algorithm is able to sort a list A of n numbers in nondecreasing order.

```
Function IS(n,A)

if n \geq 2 then

IS(n-1,A)

i=n-1

while i \geq 1 and A[n] < A[i] do

i=i-1

i=i+1

p=A[n]

j=n-1

while j \geq i do

A[j+1] = A[j]

j=j-1

A[i] = p
```

**Exercise 4** Read the problem *A new chess game* in Mooshak. Consider a recursive approach to solve it.