

α_{11}	0	\cdots	0
α_{21}	α_{22}	\cdots	0
α_{31}	α_{32}	\ddots	0
$\alpha_{T_N 1}$	$\alpha_{T_N 2}$	\cdots	$\alpha_{T_N T_N}$

Attention weights (masked) ($T_N \times T_N$)

$$\longrightarrow \times \longrightarrow V = \begin{pmatrix} v_{11} & v_{12} & \cdots & v_{1d} \\ v_{21} & v_{22} & \cdots & v_{2d} \\ \vdots & \vdots & \ddots & \vdots \\ v_{T_N 1} & v_{T_N 2} & \cdots & v_{T_N d} \end{pmatrix} \longrightarrow \begin{pmatrix} \sum_k \alpha_{1k} v_{k1} & \cdots & \sum_k \alpha_{1k} v_{kd} \\ \sum_k \alpha_{2k} v_{k1} & \cdots & \sum_k \alpha_{2k} v_{kd} \\ \vdots & \ddots & \vdots \\ \sum_k \alpha_{T_N k} v_{k1} & \cdots & \sum_k \alpha_{T_N k} v_{kd} \end{pmatrix}$$

Value ($T_N \times d$)

Head 1 Output ($T_N \times d$)

α'_{11}	0	\cdots	0
α'_{21}	α'_{22}	\cdots	0
α'_{31}	α'_{32}	\ddots	0
$\alpha'_{T_N 1}$	$\alpha'_{T_N 2}$	\cdots	$\alpha'_{T_N T_N}$

Attention weights (masked) ($T_N \times T_N$)

$$\longrightarrow \times \longrightarrow V = \begin{pmatrix} v'_{11} & v'_{12} & \cdots & v'_{1d} \\ v'_{21} & v'_{22} & \cdots & v'_{2d} \\ \vdots & \vdots & \ddots & \vdots \\ v'_{T_N 1} & v'_{T_N 2} & \cdots & v'_{T_N d} \end{pmatrix} \longrightarrow \begin{pmatrix} \sum_k \alpha'_{1k} v'_{k1} & \cdots & \sum_k \alpha'_{1k} v'_{kd} \\ \sum_k \alpha'_{2k} v'_{k1} & \cdots & \sum_k \alpha'_{2k} v'_{kd} \\ \vdots & \ddots & \vdots \\ \sum_k \alpha'_{T_N k} v'_{k1} & \cdots & \sum_k \alpha'_{T_N k} v'_{kd} \end{pmatrix}$$

Value ($T_N \times d$)

Head 2 Output ($T_N \times d$)

$\alpha_{11}^{(N)}$	0	\cdots	0
$\alpha_{21}^{(N)}$	$\alpha_{22}^{(N)}$	\cdots	0
$\alpha_{31}^{(N)}$	$\alpha_{32}^{(N)}$	\ddots	0
$\alpha_{T_N 1}^{(N)}$	$\alpha_{T_N 2}^{(N)}$	\cdots	$\alpha_{T_N T_N}^{(N)}$

Attention weights (masked) ($T_N \times T_N$)

$$\longrightarrow \times \longrightarrow V = \begin{pmatrix} v_{11}^{(N)} & v_{12}^{(N)} & \cdots & v_{1d}^{(N)} \\ v_{21}^{(N)} & v_{22}^{(N)} & \cdots & v_{2d}^{(N)} \\ \vdots & \vdots & \ddots & \vdots \\ v_{T_N 1}^{(N)} & v_{T_N 2}^{(N)} & \cdots & v_{T_N d}^{(N)} \end{pmatrix} \longrightarrow \begin{pmatrix} \sum_k \alpha_{1k}^{(N)} v_{k1}^{(N)} & \cdots & \sum_k \alpha_{1k}^{(N)} v_{kd}^{(N)} \\ \sum_k \alpha_{2k}^{(N)} v_{k1}^{(N)} & \cdots & \sum_k \alpha_{2k}^{(N)} v_{kd}^{(N)} \\ \vdots & \ddots & \vdots \\ \sum_k \alpha_{T_N k}^{(N)} v_{k1}^{(N)} & \cdots & \sum_k \alpha_{T_N k}^{(N)} v_{kd}^{(N)} \end{pmatrix}$$

Value ($T_N \times d$)

Head N Output ($T_N \times d$)

$$\underbrace{\begin{pmatrix} \sum_k \alpha_{1k} v_{k1} & \cdots & \sum_k \alpha_{1k} v_{kd} \\ \sum_k \alpha_{2k} v_{k1} & \cdots & \sum_k \alpha_{2k} v_{kd} \\ \vdots & \ddots & \vdots \\ \sum_k \alpha_{T_N k} v_{k1} & \cdots & \sum_k \alpha_{T_N k} v_{kd} \end{pmatrix}}_{\text{Head}_1} \quad \underbrace{\begin{pmatrix} \sum_k \alpha'_{1k} v'_{k1} & \cdots & \sum_k \alpha'_{1k} v'_{kd} \\ \sum_k \alpha'_{2k} v'_{k1} & \cdots & \sum_k \alpha'_{2k} v'_{kd} \\ \vdots & \ddots & \vdots \\ \sum_k \alpha'_{T_N k} v'_{k1} & \cdots & \sum_k \alpha'_{T_N k} v'_{kd} \end{pmatrix}}_{\text{Head}_2} \quad \underbrace{\begin{pmatrix} \sum_k \alpha_{1k}^{(N)} v_{k1}^{(N)} & \cdots & \sum_k \alpha_{1k}^{(N)} v_{kd}^{(N)} \\ \sum_k \alpha_{2k}^{(N)} v_{k1}^{(N)} & \cdots & \sum_k \alpha_{2k}^{(N)} v_{kd}^{(N)} \\ \vdots & \ddots & \vdots \\ \sum_k \alpha_{T_N k}^{(N)} v_{k1}^{(N)} & \cdots & \sum_k \alpha_{T_N k}^{(N)} v_{kd}^{(N)} \end{pmatrix}}_{\text{Head}_N}$$

$\{\text{Head}_1 | \text{Head}_2 | \cdots | \text{Head}_N\}$

Concatenated MHA Output ($T_N \times N \cdot d$)