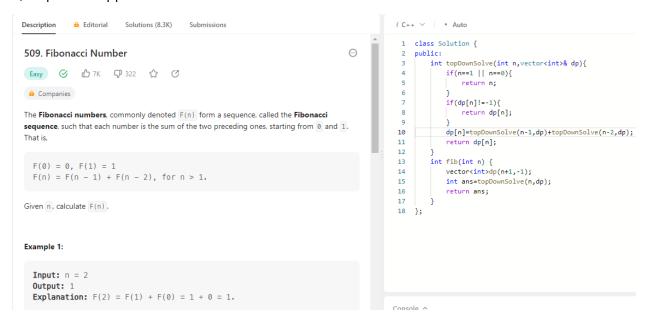
# **Dynamic Programming Class -1**

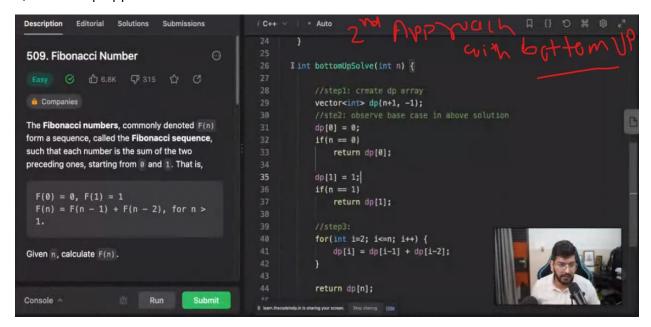
## 1) top down approach



## Tc=O(n)+O(n)

#### Sc=O(n)

#### 2) Bottom up approach



Tc=O(n)

Sc=O(n)

## Space Optimization

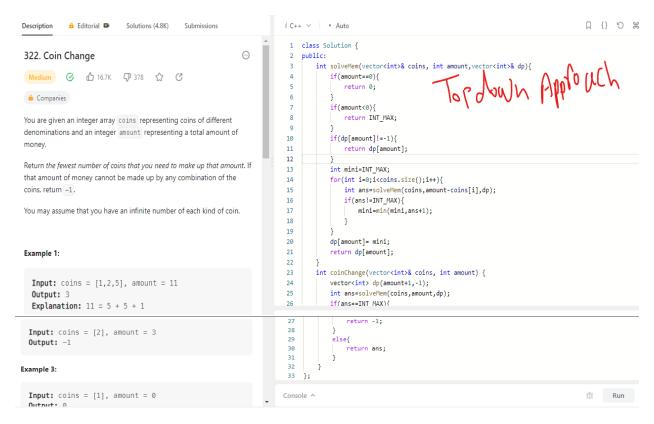
```
Description Editorial Solutions Submissions
                                                               i C++
509. Fibonacci Number
                                                                            int prev2 = 0;
(a) Companies
                                                                            int prev1 = 1;
The Fibonacci numbers, commonly denoted F(n) form a
sequence, called the Fibonacci sequence, such that each
                                                                            if(n==0)
number is the sum of the two preceding ones, starting from 0
                                                                            return prev2;
and 1. That is,
                                                                            return prev1;
                                                                                 curr = prev1 + prev2;
Given n, calculate F(n).
                                                                                 prev2 = prev1;
                                                                                 prev1 = curr;
Example 1:
  Input: n = 2
  Output: 1
                                                                67
Console
```

## **Dynamic Programming Class -2**

Q) coin change using recursion (Important question LeetCode 322)

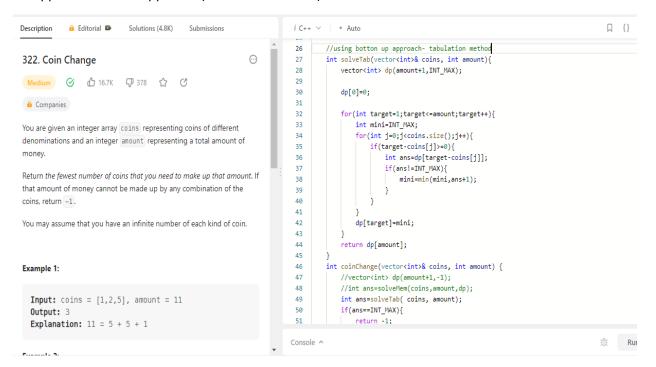
```
#include <iostream>
#include <vector>
#include <limits.h>
using namespace std;
int solveUsingRecursion(vector<int>& coins,int amount){
    if(amount==0){
        return 0;
    if(amount<0){</pre>
        return INT_MAX;
    int mini=INT_MAX;
    for(int i=0;i<coins.size();i++){</pre>
        int ans=solveUsingRecursion(coins,amount-coins[i]);
        if(ans!=INT_MAX){
            mini=min(mini,ans + 1);
    return mini;
int main()
    vector<int>coins={1,2,5};
    int amount=11;
    int ans=solveUsingRecursion(coins,amount);
    cout<<"minimum coin is :"<<ans;</pre>
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
minimum coin is :3
```



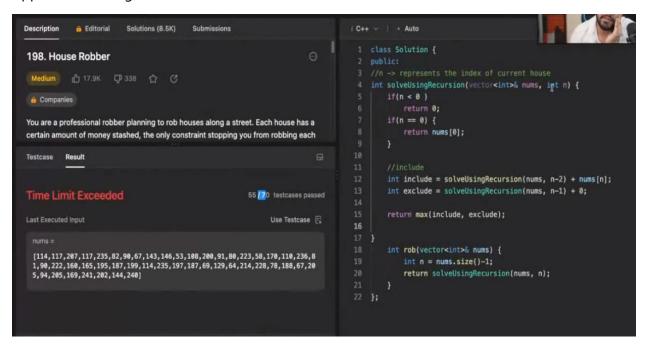
#### Tc=O(amount)

#### 2<sup>nd</sup> approach bottom approach (tabulation method)



## Q) 198. House Robber (Importan Question)

# Approach 1st using recursion



#### Tc=expontial

```
//using memosiation(top down approach - DP)
int solveUsingMem(vector<int>& nums,int n,vector<int>& dp){
    if(n==0){
        return nums[0];
    }
    if(n<0){
        return 0;
    }

    if(dp[n]!=-1){
        return dp[n];
    }
    int include=solveUsingMem(nums,n-2,dp)+nums[n];
    int exclude=solveUsingMem(nums,n-1,dp)+0;

    dp[n]=max(include,exclude);
    return dp[n];
}</pre>
```

## Tc=O(n), Sc=O(n)+O(n)

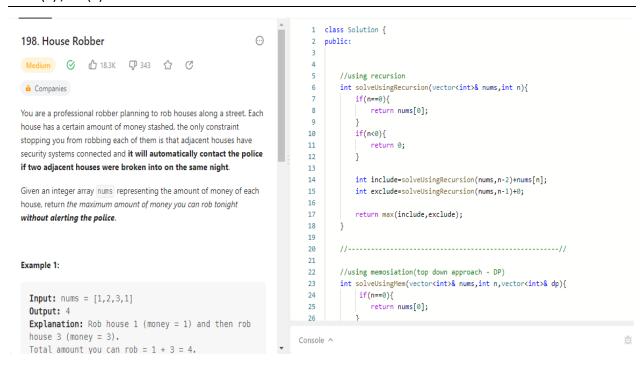
```
//using bottom up Approach
int solveUsingTabulation(vector<int>& nums,int n){
    vector<int>dp(n+1,0);
    dp[0]=nums[0];

for(int i=1;i<=n;i++){
    int temp=0;

    if(i-2>=0){
        temp=dp[i-2];
    }
    int include=temp+nums[i];
    int exclude=dp[i-1]+0;

    dp[i]=max(include,exclude);
}
return dp[n];
}
```

## Tc=O(n),ScO(n)



Tc=O(n), Sc=(1)

# Dynamic Programming Class – 3

Q) Panting fence problem problem using recursion (IMP)

```
#include <iostream>
using namespace std;
int solveUsingRecursion(int n,int k){
    if(n==1){
        return k;
    }
    if(n==2){
        return k+k*(k-1);
    }

    int ans=(solveUsingRecursion(n-2,k)+solveUsingRecursion(n-1,k)) *(k-1);
    return ans;
}
int main()
{
    int n=4;
    int k=3;
    int ans=solveUsingRecursion(n,k);
    cout<<"ans is :"<<ans;
    return 0;
}</pre>
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
ans is :66
```

Time complexity: exponential

2<sup>nd</sup> approach solve panting fence problem using (top dowan - dp)

```
#include <iostream>
#include <vector>
using namespace std;
int solveUsingMem(int n,int k,vector<int>& dp){
    if(n==1){
        return k;
    if(n==2){
        return k+k*(k-1);
    if(dp[n]!=-1){
        return dp[n];
    dp[n]=(solveUsingMem(n-2,k,dp)+solveUsingMem(n-1,k,dp)) *(k-1);
    return dp[n];
int main()
    int n=4;
    int k=3;
    vector<int>dp(n+1,-1);
    int ans=solveUsingMem(n,k,dp);
    cout<<"ans is :"<<ans;</pre>
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
ans is :66
```

Time complexity: O(n)

3<sup>rd</sup> approach solve panting fence problem using (bottom up - dp)

```
#include <iostream>
#include <vector>
using namespace std;
int solveUsingTab(int n,int k){
    vector<int>dp(n+1,0);
    dp[1]=k;
    dp[2]=k+k*(k-1);
    for(int i=3;i<=n;i++){</pre>
        dp[i]=(dp[i-2]+dp[i-1]) *(k-1);
    return dp[n];
int main()
    int n=4;
    int k=3;
    vector<int>dp(n+1,-1);
    int ans=solveUsingTab(n,k);
    cout<<"ans is :"<<ans;</pre>
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
ans is :66
```

4<sup>th</sup> approach solve panting fence problem using (space optimization - dp)

```
#include <iostream>
#include <vector>
using namespace std;
int solveUsingSpaceOptimization(int n,int k){
    vector<int>dp(n+1,0);
    int prev2=k;
    int prev1=k+k*(k-1);
    for(int i=3;i<=n;i++){</pre>
        int curr=(prev2+prev1) *(k-1);
        prev2=prev1;
        prev1=curr;
    return prev1;
int main()
    int n=4;
    int k=3;
    int ans=solveUsingSpaceOptimization(n,k);
    cout<<"ans is :"<<ans;</pre>
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
ans is :66
```

Time complexity : O(n)

Space complexity: O(1)

## Q) 0/1 Knapsack Problem and Dynamic Programming (Imp)

1<sup>st</sup> approach using recursion

```
#include <iostream>
using namespace std;
int solveUsingRecursion(int weight[],int value[],int index,int capacity){
    if(index==0){
        if(weight[0]<=capacity){</pre>
            return value[0];
        else{
            return 0;
    int include =0;
    if(weight[index]<=capacity){</pre>
        include=value[index]+solveUsingRecursion(weight, value, index-1, capacity-
weight[index]);
    int exclude=0+solveUsingRecursion(weight, value, index-1, capacity);
    int ans=max(include,exclude);
    return ans;
int main()
    int weight[]={4,5,1};
    int value[]={1,2,3};
    int n=3;
    int capacity=4;
    int ans=solveUsingRecursion(weight, value, n-1, capacity);
    cout<<"knapsack ans:"<<ans;</pre>
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
knapsack ans:3
```

```
#include <iostream>
#include <vector>
using namespace std;
int solveUsingMem(int weight[],int value[],int index,int capacity,vector
vector<int> >&dp){
    if(index==0){
        if(weight[0]<=capacity){</pre>
            return value[0];
        else{
            return 0;
    if(dp[index][capacity]!=-1){
        return dp[index][capacity];
    int include =0;
    if(weight[index]<=capacity){</pre>
        include=value[index]+solveUsingMem(weight,value,index-1,capacity-
weight[index],dp);
    int exclude=0+solveUsingMem(weight,value,index-1,capacity,dp);
    dp[index][capacity]=max(include,exclude);
    return dp[index][capacity];
int main()
    int weight[]={4,5,1};
    int value[]={1,2,3};
    int n=3;
    int capacity=4;
```

```
vector< vector<int> >dp(n,vector<int>(capacity+1,-1));
int ans=solveUsingMem(weight,value,n-1,capacity,dp);
cout<<"knapsack ans:"<<ans;
return 0;
}</pre>
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
knapsack ans:3
```

```
#include <iostream>
#include <vector>
using namespace std;
int solveUsingTabulation(int weight[],int value[],int n,int capacity){
    vector< vector<int> >dp(n,vector<int>(capacity+1,0));
    for(int w=weight[0];w<=capacity;w++){</pre>
        if(weight[0]<=capacity){</pre>
            dp[0][w]=value[0];
        else{
            dp[0][w]=0;
    for(int index=1;index<n;index++){</pre>
        for(int wt=0;wt<=capacity;wt++){</pre>
             int include=0;
            if(weight[index]<=wt){</pre>
                 include=value[index]+dp[index-1][wt-weight[index]];
            int exclude=0+dp[index-1][wt];
            dp[index][wt]=max(include,exclude);
    return dp[n-1][capacity];
int main()
    int weight[]={4,5,1};
    int value[]={1,2,3};
    int n=3;
    int capacity=4;
    int ans=solveUsingTabulation(weight,value,n,capacity);
    cout<<"knapsack ans:"<<ans;</pre>
    return 0;
```

PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
knapsack ans:3

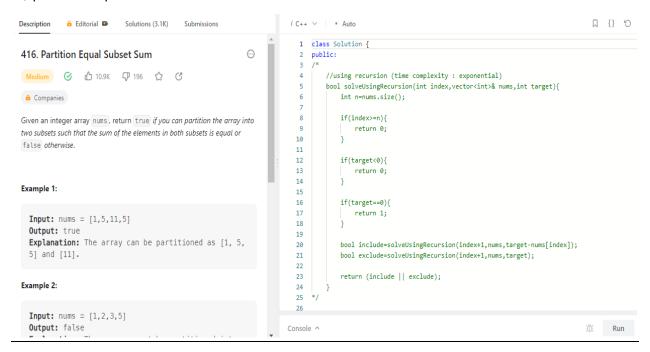
```
#include <iostream>
#include <vector>
using namespace std;
int solveUsingSpaceOptimization(int weight[],int value[],int n,int capacity){
    vector<int>prev(capacity+1,0);
    vector<int>curr(capacity+1,0);
    for(int w=weight[0];w<=capacity;w++){</pre>
        if(weight[0]<=capacity){</pre>
             prev[w]=value[0];
        else{
             prev[w]=0;
    for(int index=1;index<n;index++){</pre>
        for(int wt=0;wt<=capacity;wt++){</pre>
             int include=0;
             if(weight[index]<=wt){</pre>
                 include=value[index]+prev[wt-weight[index]];
             int exclude=0+prev[wt];
             curr[wt]=max(include,exclude);
        prev=curr;
    return prev[capacity];
int main()
    int weight[]={4,5,1};
    int value[]={1,2,3};
    int n=3;
    int capacity=4;
    int ans=solveUsingSpaceOptimization(weight, value, n, capacity);
    cout<<"knapsack ans:"<<ans;</pre>
    return 0;
```

PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
knapsack ans:3

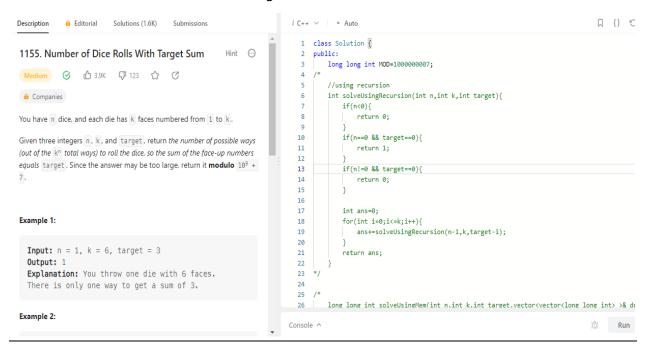
```
#include <iostream>
#include <vector>
using namespace std;
int solveUsingSpaceOptimization(int weight[],int value[],int n,int capacity){
    //vector<int>prev(capacity+1,0);
    vector<int>curr(capacity+1,0);
    for(int w=weight[0];w<=capacity;w++){</pre>
        if(weight[0]<=capacity){</pre>
             curr[w]=value[0];
        else{
            curr[w]=0;
    for(int index=1;index<n;index++){</pre>
        for(int wt=capacity;wt>=0;wt--){
            int include=0;
            if(weight[index]<=wt){</pre>
                 include=value[index]+curr[wt-weight[index]];
            int exclude=0+curr[wt];
             curr[wt]=max(include,exclude);
        //prev=curr;
    return curr[capacity];
int main()
    int weight[]={4,5,1};
    int value[]={1,2,3};
    int n=3;
    int capacity=4;
    int ans=solveUsingSpaceOptimization(weight, value, n, capacity);
    cout<<"knapsack ans:"<<ans;</pre>
    return 0;
```

## **Dynamic Programming Class - 4**

### Q) partition equal subset sum

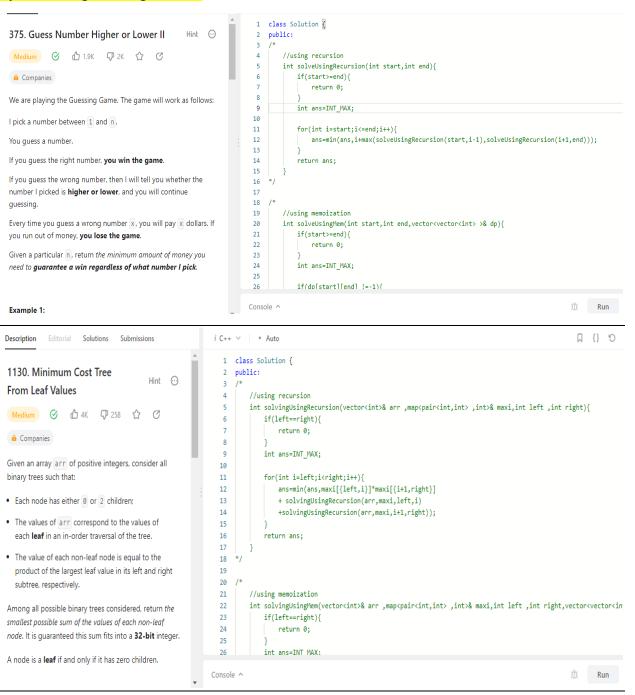


## Q) 1155. Number of Dice Rolls With Target Sum

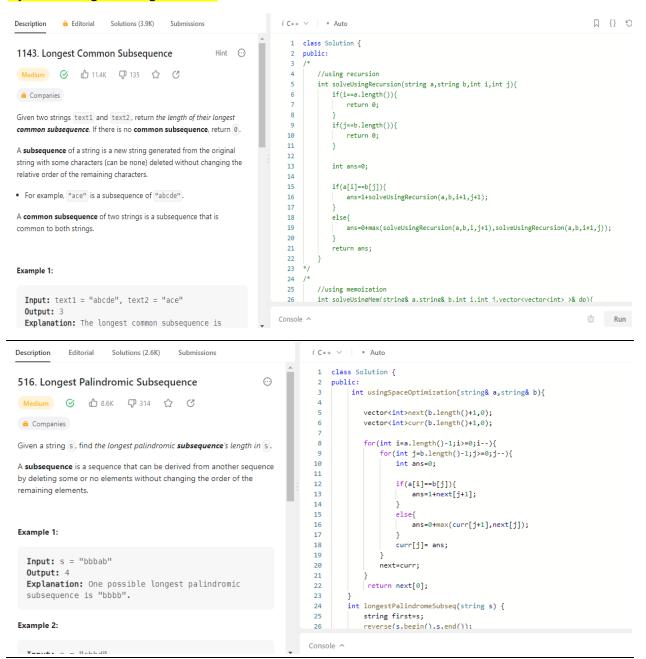


## Dynamic Programming - II

## **Dynamic Programming Class -5**



# Dynamic Programming Class – 6



```
1 class Solution {
                                                                    \odot
                                                                                      public:
/*
72. Edit Distance
Medium ⊗ 🖒 13.1K 🖓 155 🏠 ♂
                                                                                          //using recursion
                                                                                          int solveUsingRecursion(string& a, string& b,int i,int j){
                                                                                              if(i==a.length()){
    return b.length()-j;
♠ Companies
Given two strings word1 and word2, return the minimum number of operations
required to convert word1 to word2.
                                                                                  10
                                                                                              if(j==b.length()){
                                                                                  11
                                                                                                 return a.length()-i;
You have the following three operations permitted on a word:
                                                                                  12
                                                                                  13

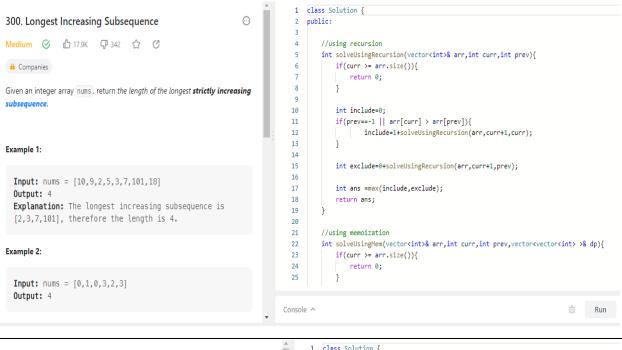
    Insert a character

                                                                                  14
                                                                                               int ans=0;
                                                                                  15

    Delete a character

                                                                                              if(a[i]==b[j]){
    ans=solveUsingRecursion(a,b,i+1,j+1);
                                                                                  16
                                                                                  17
· Replace a character
                                                                                  18
                                                                                  19
                                                                                               else{
                                                                                                  int insert=1+solveUsingRecursion(a,b,i,j+1);
                                                                                  20
                                                                                  21
                                                                                                   int deleted=1+solveUsingRecursion(a,b,i+1,j);
Example 1:
                                                                                  22
                                                                                                   int replace=1+solveUsingRecursion(a,b,i+1,j+1);
                                                                                  23
                                                                                                  ans=min(insert,min(deleted,replace));
  Input: word1 = "horse", word2 = "ros"
                                                                                  24
  Output: 3
                                                                                  25
                                                                                               return ans;
  Explanation:
  horse -> rorse (replace 'h' with 'r')
                                                                               Console ^
  rorse -> rose (remove 'r')
```

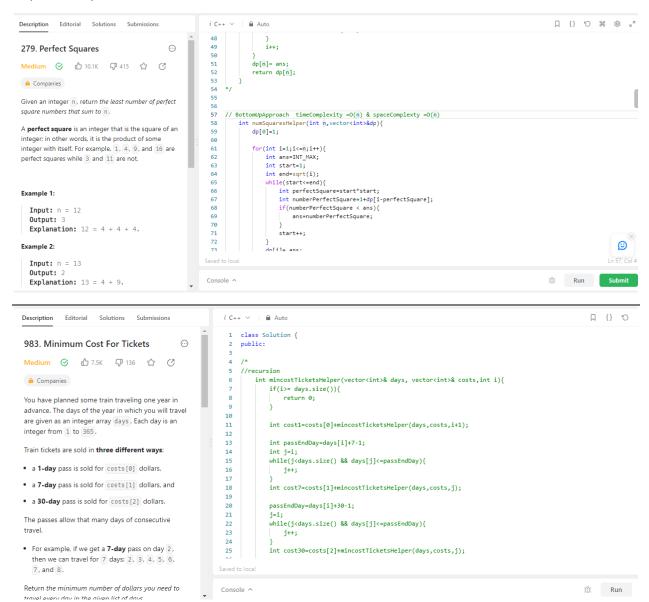
## Dynamic Programming Class – 7

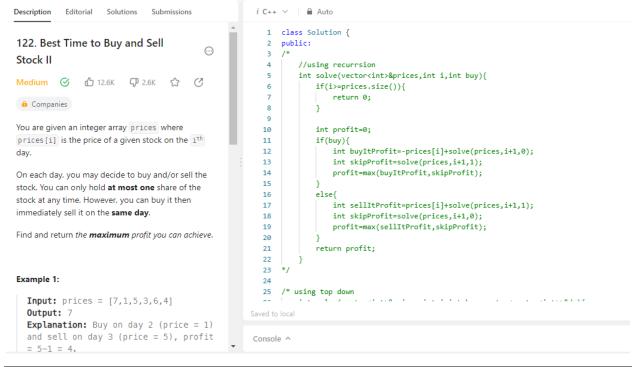




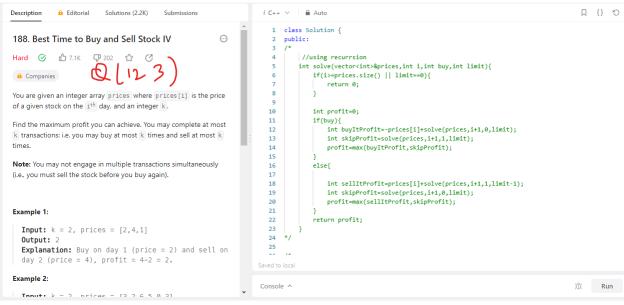
### **DP** – Assignments

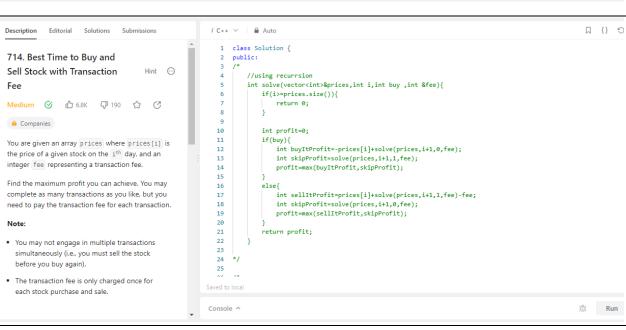
## Q)perfect squares





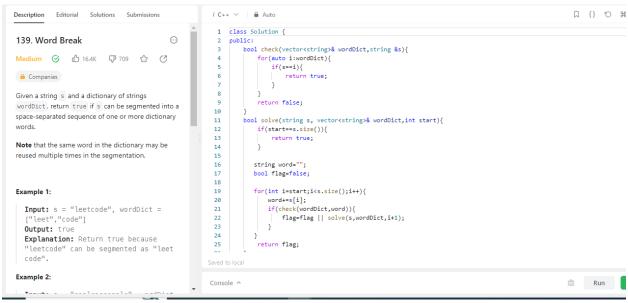
```
Description Editorial Solutions Submissions
                                                                                                                                                               C' {} []
                                                        class Solution {
123. Best Time to Buy and Sell
                                                              public:
/*
                                            0
Stock III
                                                               //using recurrsion
                                                                  int solve(vector<int>&prices,int i,int buy,int limit){
Hard ⊘ 🖒 9.1K 🖓 165 🏠 ♂
                                                                      if(i>=prices.size() || limit==0){
                                                                         return 0;
You are given an array prices where prices[i] is
                                                                      int profit=0;
                                                                      if(buy){
  int buyItProfit=-prices[i]+solve(prices,i+1,0,limit);
the price of a given stock on the ith day.
                                                          11
                                                          12
                                                                         int skipProfit=solve(prices,i+1,1,limit);
profit=max(buyItProfit,skipProfit);
Find the maximum profit you can achieve. You may
                                                          13
                                                          14
complete at most two transactions.
                                                          15
                                                                      else{
                                                          16
Note: You may not engage in multiple transactions
simultaneously (i.e., you must sell the stock before
                                                                          int sellItProfit=prices[i]+solve(prices,i+1,1,limit-1);
                                                          18
you buy again).
                                                          19
                                                                          int skipProfit=solve(prices,i+1,0,limit);
                                                          20
                                                                          profit=max(sellItProfit,skipProfit);
                                                                      return profit;
                                                          22
Example 1:
                                                          24 */
  Input: prices = [3,3,5,0,0,3,1,4]
                                                          25
  Output: 6
   Explanation: Buy on day 4 (price = 0)
   and sell on day 6 (price = 3), profit
   = 3-0 = 3.
                                                       Console ^
                                                                                                                                                             Ω Run
   Then huv on day 7 (nrice - 1) and
```

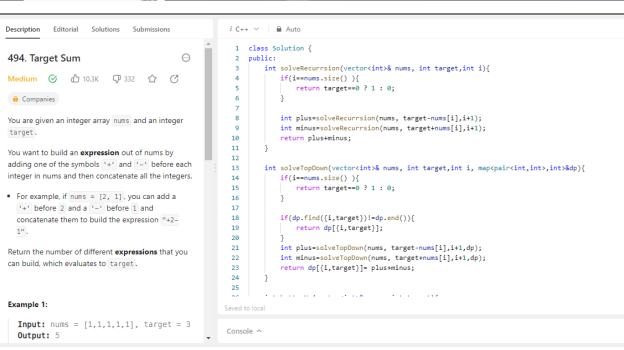


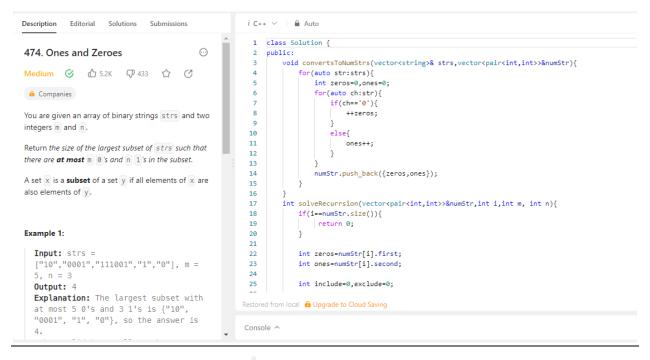


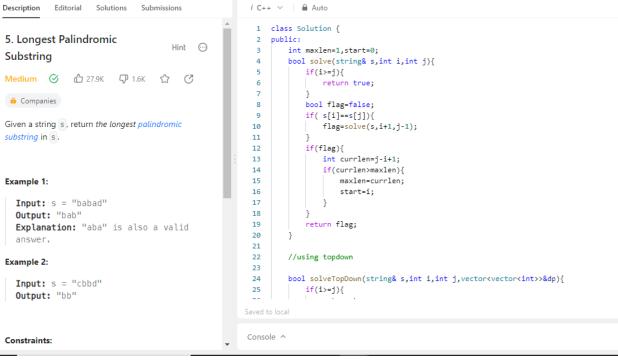


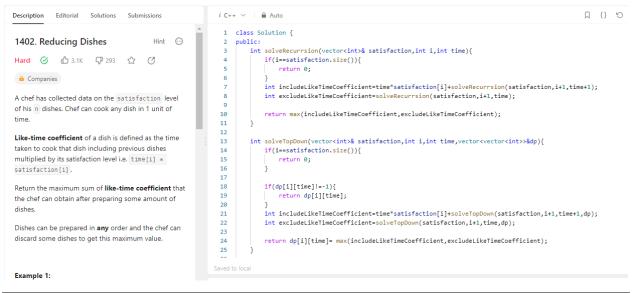




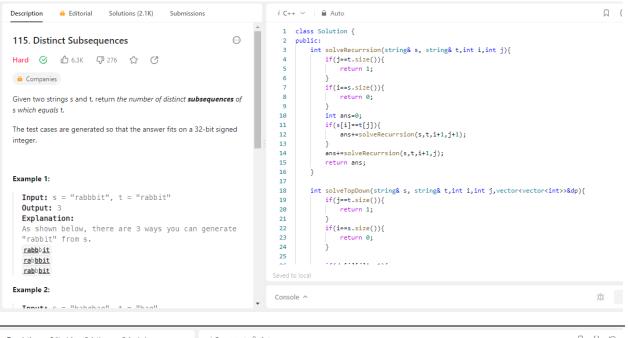




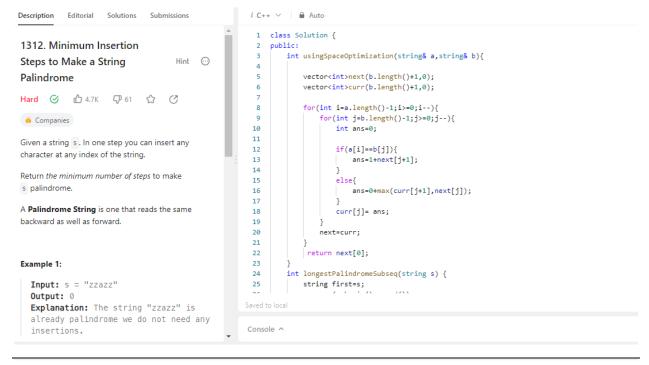


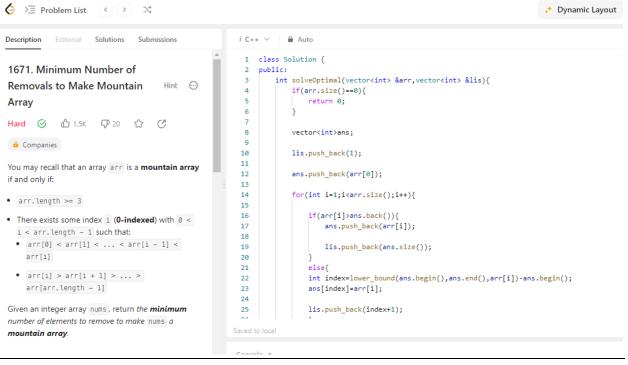


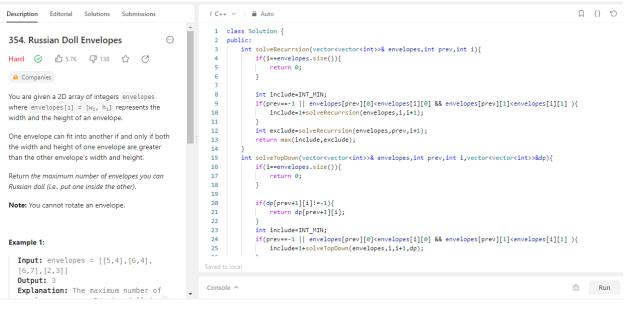


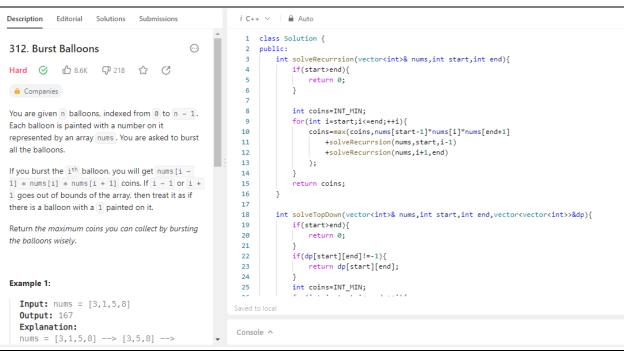


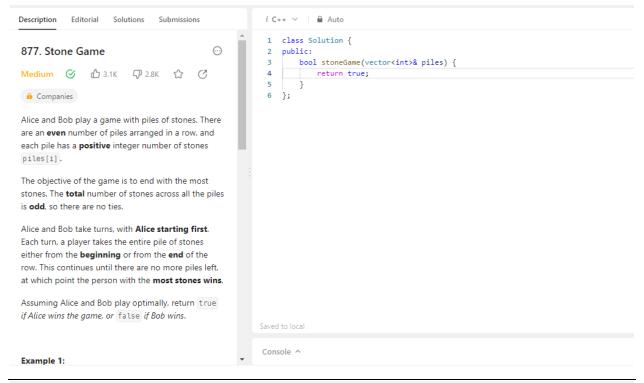


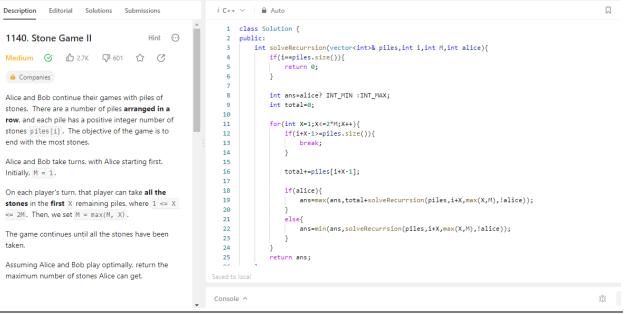


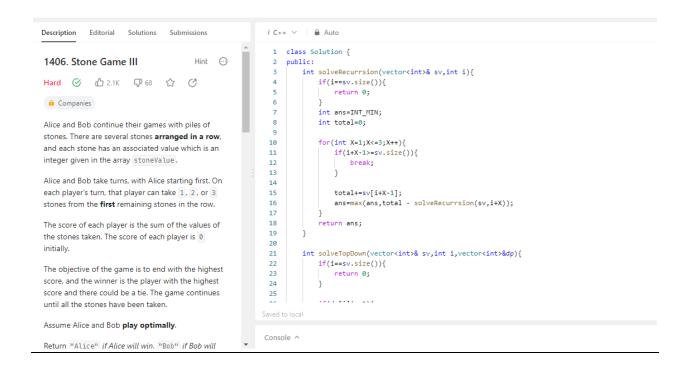












Graphs-I 9/11/23

# Graphs Class - 1

Q) Write a program for adjacency matrix

```
#include <iostream>
#include <queue>
using namespace std;
int main()
    cout<<"enter the number of nodes :"<<endl;</pre>
    cin>>n;
    vector<vector<int> >adj(n,vector<int>(n,0));
    int e;
    cout<<"enter the number of edges :"<<endl;</pre>
    cin>>e;
    for(int i=0;i<e;i++){</pre>
        int u,v;
         cin>>u>>v;
         adj[u][v]=1;
    cout<<"print the adjance: "<<endl;</pre>
    for(int i=0;i<n;i++){</pre>
         for(int j=0;j<n;j++){</pre>
             cout<<adj[i][j]<<" ";</pre>
         cout<<endl;</pre>
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
enter the number of nodes:
3
enter the number of edges:
6
0 1
1 0
1 2
2 1
0 2
2 0
print the adjance:
0 1 1
1 0 1
1 1 0 1
```

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
using namespace std;
class Graph{
    public:
    unordered_map<int,list<int> >adjList;
    void addEdge(int u,int v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
};
int main()
    Graph g;
    g.addEdge(0,1,0);
    g.addEdge(1,2,0);
    g.addEdge(0,2,0);
    g.printAdjacencyList();
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
2-> 1, 0,
1-> 0, 2,
0-> 1, 2,
```

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
using namespace std;
class Graph{
    public:
    unordered_map<int,list<int> >adjList;
    void addEdge(int u,int v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
};
int main()
    Graph g;
    g.addEdge(0,1,1);
    g.addEdge(1,2,1);
    g.addEdge(0,2,1);
    g.printAdjacencyList();
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
1-> 2,
0-> 1, 2,
```

#### Q)write program for weighted graph

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
using namespace std;
class Graph{
    public:
    unordered_map<int,list<pair<int,int> > >adjList;
    void addEdge(int u,int v,int weight,bool direction){
        adjList[u].push_back({v,weight});
        if(direction==0){
            adjList[v].push_back({u,weight});
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<"("<<neighbours.first<<", "<<neighbours.second<<"),";</pre>
            cout<<endl;</pre>
};
int main()
    Graph g;
    g.addEdge(0,1,5,1);
    g.addEdge(1,2,8,1);
    g.addEdge(0,2,6,1);
    g.printAdjacencyList();
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
1-> (2, 8),
0-> (1, 5),(2, 6),
```

#### Q) write program for Generic Type

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
};
int main()
    Graph <char>g;
    g.addEdge('a','b',0);
    g.addEdge('b','c',0);
    g.addEdge('a','c',0);
    g.printAdjacencyList();
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
c-> b, a,
b-> a, c,
a-> b, c,
```

Adjacency matrix : space complexity : worst case O(n²)

space complexity: Average case O(v²)

Adjacency List : space complexity : worst case  $O(v^2)$ 

space complexity : Average case O(v + e)

### Q) write program for BFS Traversal

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
    void bfs(T src){
        queue<T>q;
        unordered_map<T,bool>visited;
        q.push(src);
        visited[src]=true;
```

```
while(!q.empty()){
            int frontNode=q.front();
            q.pop();
            cout<<frontNode<<", ";</pre>
            for(auto neighbours : adjList[frontNode]){
                 if(!visited[neighbours]){
                     q.push(neighbours);
                     visited[neighbours]=true;
};
int main()
    Graph <int>g;
    g.addEdge(0,1,0);
    g.addEdge(1,2,0);
    g.addEdge(1,3,0);
    g.addEdge(3,5,0);
    g.addEdge(3,7,0);
    g.addEdge(7,6,0);
    g.addEdge(7,4,0);
    g.printAdjacencyList();
    cout<<endl<<"print bfs "<<endl;</pre>
    g.bfs(0);
    return 0;// time Complexity :0(v+e)//v is number of node,e is number of edge
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
4-> 7,
6-> 7,
7-> 3, 6, 4,
5-> 3,
0-> 1,
1-> 0, 2, 3,
2-> 1,
3-> 1, 5, 7,

print bfs
0, 1, 2, 3, 5, 7, 6, 4,
```

Q) write program for two different graph connected (BFS)

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
    void bfs(T src,unordered_map<int,bool>& visited){
        queue<T>q;
        q.push(src);
        visited[src]=true;
```

```
while(!q.empty()){
             int frontNode=q.front();
            q.pop();
             cout<<frontNode<<", ";</pre>
             for(auto neighbours : adjList[frontNode]){
                 if(!visited[neighbours]){
                     q.push(neighbours);
                     visited[neighbours]=true;
};
int main()
    Graph <int>g;
    int n=8;
    g.addEdge(0,1,0);
    g.addEdge(1,2,0);
    g.addEdge(1,3,0);
    g.addEdge(3,5,0);
    g.addEdge(3,7,0);
    g.addEdge(7,6,0);
    g.addEdge(7,4,0);
    g.printAdjacencyList();
    cout<<endl<<"print two different graph connected :"<<endl;</pre>
    unordered_map<int,bool>visited;
    for(int i=0;i<n;i++){</pre>
        if(!visited[i]){
            g.bfs(i,visited);
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
4-> 7,
6-> 7,
7-> 3, 6, 4,
5-> 3,
0-> 1,
1-> 0, 2, 3,
2-> 1,
3-> 1, 5, 7,

print two different graph connected:
0, 1, 2, 3, 5, 7, 6, 4,
```

Time complexity :O(v+e) //liner time complexity

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
    void bfs(T src,unordered_map<int,bool>& visited){
        queue<T>q;
        q.push(src);
        visited[src]=true;
```

```
while(!q.empty()){
            int frontNode=q.front();
            q.pop();
            cout<<frontNode<<", ";</pre>
            for(auto neighbours : adjList[frontNode]){
                 if(!visited[neighbours]){
                     q.push(neighbours);
                     visited[neighbours]=true;
    void dfs(T src,unordered_map<int,bool>& visited){
        cout<<src<<", ";</pre>
        visited[src]=true;
        for(auto neighbour: adjList[src]){
            if(!visited[neighbour]){
                dfs(neighbour, visited);
};
int main()
    Graph <int>g;
    int n=5;
    g.addEdge(0,1,0);
    g.addEdge(1,3,0);
    g.addEdge(0,2,0);
    g.addEdge(2,4,0);
    g.printAdjacencyList();
    cout<<endl<<"print two different graph connected (BFS TRAVERSAL):"<<endl;</pre>
    unordered_map<int,bool>visited;
    for(int i=0;i<n;i++){</pre>
        if(!visited[i]){
            g.bfs(i,visited);
```

```
cout<<endl<<"print two different graph connected (DFS TRAVERSAL):"<<endl;
unordered_map<int,bool>visited2;
for(int i=0;i<n;i++){
    if(!visited2[i]){
        g.dfs(i,visited2);
    }
}
return 0;
}</pre>
```

```
print two different graph connected :
0, 1, 2, 3, 5, 7, 6, 4,
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
4-> 2,
0-> 1, 2,
1-> 0, 3,
3-> 1,
2-> 0, 4,

print two different graph connected (BFS TRAVERSAL):
0, 1, 2, 3, 4,
print two different graph connected (DFS TRAVERSAL):
0, 1, 3, 2, 4,
```

# Graphs Class – 2

Q) write program for check cycle graph using BFS (undirect graph)

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
    bool checkCyclicUsingBfs(int src,unordered_map<int,bool>& visited){
        queue<int>q;
        unordered_map<int,bool>parent;
        q.push(src);
        visited[src]=true;
        parent[src]=-1;
```

```
while(!q.empty()){
            int frontNode=q.front();
            q.pop();
            for(auto neighbour : adjList[frontNode]){
                if(!visited[neighbour]){
                    q.push(neighbour);
                    visited[neighbour]=true;
                    parent[neighbour]=frontNode;
                else{
                    if(visited[neighbour] && neighbour!=parent[frontNode]){
                        return true;
        return false;
};
int main()
    Graph <int>g;
    int n=5;
    g.addEdge(0,1,0);
    g.addEdge(1,2,0);
    g.addEdge(2,3,0);
    g.addEdge(3,4,0);
    g.addEdge(4,0,0);
    g.printAdjacencyList();
    cout<<endl;</pre>
    bool ans=false;
    unordered_map<int,bool>visited;
```

```
for(int i=0;i<n;i++){
    if(!visited[i]){
        ans=g.checkCyclicUsingBfs(i,visited);
        if(ans==true){
            break;
        }
    }
}

if(ans=true){
    cout<<"cycle is present"<<endl;
}
else{
    cout<<"cycle is NOT present"<<endl;
}
return 0;
}</pre>
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
4-> 3, 0,
0-> 1, 4,
1-> 0, 2,
2-> 1, 3,
3-> 2, 4,

cycle is present
```

Time complexity=O(v+e)

Q) write program for check cycle graph using BFS & DFS (undirect graph)

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
    bool checkCyclicUsingBfs(int src,unordered_map<int,bool>& visited){
        queue<int>q;
        unordered_map<int,bool>parent;
        q.push(src);
        visited[src]=true;
        parent[src]=-1;
```

```
while(!q.empty()){
            int frontNode=q.front();
            q.pop();
            for(auto neighbour : adjList[frontNode]){
                if(!visited[neighbour]){
                    q.push(neighbour);
                    visited[neighbour]=true;
                    parent[neighbour]=frontNode;
                else{
                    if(visited[neighbour] && neighbour!=parent[frontNode]){
                        return true;
    bool checkCyclicUsingDfs(int src,unordered_map<int,bool>& visited,int
parent){
        visited[src]=true;
        for(auto neighbour : adjList[src]){
            if(!visited[neighbour]){
                bool checkAageKaAns=checkCyclicUsingDfs(neighbour, visited, src);
                if(checkAageKaAns==true){
                    return true;
                if(visited[neighbour] && neighbour!=parent){
                    return true;
        return false;
};
```

```
int main()
    Graph <int>g;
    int n=5;
    g.addEdge(0,1,0);
    g.addEdge(1,2,0);
    g.addEdge(2,3,0);
    g.addEdge(3,4,0);
    g.addEdge(4,0,0);
    g.printAdjacencyList();
    cout<<endl;</pre>
    bool ans=false;
    unordered_map<int,bool>visited;
    for(int i=0;i<n;i++){</pre>
        if(!visited[i]){
             ans=g.checkCyclicUsingBfs(i,visited);
             if(ans==true){
                 break;
    if(ans=true){
        cout<<"cycle is present"<<endl;</pre>
    else{
        cout<<"cycle is NOT present"<<endl;</pre>
    //check cycle using DFS
    bool ans2=false;
    unordered_map<int,bool>visited2;
    for(int i=0;i<n;i++){</pre>
        if(!visited2[i]){
             ans2=g.checkCyclicUsingDfs(i,visited,-1);
             if(ans2==true){
                 break;
```

```
if(ans2=true){
    cout<<"cycle is present"<<endl;
}
else{
    cout<<"cycle is NOT present"<<endl;
}
return 0;
}</pre>
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
4-> 3, 0,
0-> 1, 4,
1-> 0, 2,
2-> 1, 3,
3-> 2, 4,

cycle is present
cycle is present
```

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
    bool checkCyclicDirectGraphUsingDfs(int src,unordered_map<int,bool>&
visited,unordered_map<int,bool> dfsVisited){
        visited[src]=true;
        dfsVisited[src]=true;
```

```
for(auto neighbour: adjList[src]){
            if(!visited[neighbour]){
aageKaAns=checkCyclicDirectGraphUsingDfs(neighbour, visited, dfsVisited);
                if(aageKaAns==true){
            if(visited[neighbour]==true && dfsVisited[neighbour]==true){
                return true;
        dfsVisited[src]=false;
        return false;
};
int main()
    Graph <int>g;
    int n=5;
    g.addEdge(0,1,1);
    g.addEdge(1,2,1);
    g.addEdge(2,3,1);
    g.addEdge(3,4,1);
    g.addEdge(4,0,1);
    g.printAdjacencyList();
    cout<<endl;</pre>
    bool ans=false;
    unordered_map<int,bool>visited;
    unordered_map<int,bool>dfsVisited;
```

```
for(int i=0;i<n;i++){
    if(!visited[i]){
        ans=g.checkCyclicDirectGraphUsingDfs(i,visited,dfsVisited);
        if(ans==true){
            break;
        }
    }
}

if(ans == true)
    cout << "Cycle is Present" << endl;
else
    cout << "Cycle Absent" << endl;
return 0;
}</pre>
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
4-> 0,
0-> 1,
1-> 2,
2-> 3,
3-> 4,

Cycle is Present
```

# Graphs Class – 3

Q) write program for Topological Sort Order using DFS

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
#include <stack>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
    void topologicalSortUsingDFS(int src,unordered_map<int,bool>&
visited,stack<int>& ans){
        visited[src]=true;
```

```
for(auto neighbour :adjList[src]){
            if(!visited[neighbour]){
                 topologicalSortUsingDFS(neighbour, visited, ans);
        ans.push(src);
};
int main()
    Graph <int>g;
    int n=8;
    g.addEdge(0,1,1);
    g.addEdge(1,2,1);
    g.addEdge(2,3,1);
    g.addEdge(3,4,1);
    g.addEdge(3,5,1);
    g.addEdge(4,6,1);
    g.addEdge(5,6,1);
    g.addEdge(6,7,1);
    g.printAdjacencyList();
    cout<<endl;</pre>
    unordered_map<int,bool>visited;
    stack<int> ans;
    for(int i=0;i<n;i++){</pre>
        if(!visited[i]){
            g.topologicalSortUsingDFS(i,visited,ans);
    }
    cout << "topological sort order :"<<endl;</pre>
    while(!ans.empty()){
        cout<<ans.top()<<" ,";</pre>
        ans.pop();
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
6-> 7,
5-> 6,
4-> 6,
0-> 1,
1-> 2,
2-> 3,
3-> 4, 5,

topological sort order :
0 ,1 ,2 ,3 ,5 ,4 ,6 ,7 ,
```

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
#include <stack>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
    void topologicalSortUsingDFS(int src,unordered_map<int,bool>&
visited,stack<int>& ans){
        visited[src]=true;
```

```
for(auto neighbour :adjList[src]){
            if(!visited[neighbour]){
                topologicalSortUsingDFS(neighbour, visited, ans);
        ans.push(src);
    void topologicalSortUsingBFS(int n,vector<int>& ans){
        queue<int>q;
        unordered_map<int,int> indegree;
        for(auto i: adjList){
            int src=i.first;
            for(auto neighbour: i.second){
                indegree[neighbour]++;
        for(int i=0;i<n;i++){</pre>
            if(indegree[i]==0){
                q.push(i);
        while(!q.empty()){
            int fNode=q.front();
            q.pop();
            ans.push_back(fNode);
            for(auto neighbour :adjList[fNode]){
                indegree[neighbour]--;
                if(indegree[neighbour]==0){
                     q.push(neighbour);
};
```

```
int main()
    Graph <int>g;
    int n=8;
    g.addEdge(2,4,1);
    g.addEdge(2,5,1);
    g.addEdge(4,6,1);
    g.addEdge(5,3,1);
    g.addEdge(3,7,1);
    g.addEdge(6,7,1);
    g.addEdge(7,0,1);
    g.addEdge(7,1,1);
    g.printAdjacencyList();
    cout<<endl;</pre>
    vector<int>ans;
    g.topologicalSortUsingBFS(n,ans);
    cout << "topological sort order using BFS :"<<endl;</pre>
    for(int i=0;i<ans.size();i++){</pre>
        cout<<ans[i]<<", ";</pre>
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
7-> 0, 1,
6-> 7,
2-> 4, 5,
4-> 6,
5-> 3,
3-> 7,

topological sort order using BFS :
2, 4, 5, 6, 3, 7, 0, 1,
```

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
#include <stack>
using namespace std;
template <typename T>
class Graph{
    public:
    unordered_map<T,list<T> > adjList;
    void addEdge(T u,T v,bool direction){
        adjList[u].push_back(v);
        if(direction==0){
            adjList[v].push_back(u);
    void printAdjacencyList(){
        for(auto node :adjList){
            cout<<node.first<<"-> ";
            for(auto neighbours: node.second){
                cout<<neighbours<<", ";</pre>
            cout<<endl;</pre>
```

```
void topologicalSortUsingDFS(int src,unordered_map<int,bool>&
visited,stack<int>& ans){
        visited[src]=true;
        for(auto neighbour :adjList[src]){
            if(!visited[neighbour]){
                topologicalSortUsingDFS(neighbour, visited, ans);
        ans.push(src);
    void topologicalSortUsingBFS(int n,vector<int>& ans){
        queue<int>q;
        unordered_map<int,int> indegree;
        for(auto i: adjList){
            int src=i.first;
            for(auto neighbour: i.second){
                indegree[neighbour]++;
        for(int i=0;i<n;i++){</pre>
            if(indegree[i]==0){
                q.push(i);
        while(!q.empty()){
            int fNode=q.front();
            q.pop();
            ans.push_back(fNode);
            for(auto neighbour :adjList[fNode]){
                indegree[neighbour]--;
                if(indegree[neighbour]==0){
                    q.push(neighbour);
```

```
int main()
    Graph <int>g;
    int n=8;
    g.addEdge(0,1,1);
    g.addEdge(1,2,1);
    g.addEdge(2,3,1);
    g.addEdge(3,1,1);
    g.printAdjacencyList();
    cout<<endl;</pre>
    vector<int>ans;
    g.topologicalSortUsingBFS(n,ans);
    if(ans.size()==n){
        cout<<"It is a valid topo sort "<<endl;</pre>
    else{
        cout<<"cycle preesnt or invalid topological sort"<<endl;;</pre>
    cout << "topological sort order using BFS :"<<endl;</pre>
    for(int i=0;i<ans.size();i++){</pre>
        cout<<ans[i]<<", ";</pre>
    return 0;
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
3-> 1,
2-> 3,
1-> 2,
0-> 1,

cycle preesnt or invalid topological sort

topological sort order using BFS :
0, 4, 5, 6, 7,
```

### Graphs Class – 4

Q) write program for find shortest path using BFS

```
#include<iostream>
#include<unordered map>
#include<list>
#include<queue>
#include<stack>
using namespace std;
class Graph{
    public :
    unordered_map<int, list<pair<int,int> > >adjList;
    void addEdge(int u,int v,int wt,bool direction){
        //dircttion = 1-> undirected graph
        //dircttion = 0-> directed graph
        adjList[u].push_back({v,wt});
        if(direction==0){
            adjList[v].push_back({u,wt});
    void printAdjList(){
        for(auto i: adjList){
            cout<<i.first<<"->";
            for(auto j : i.second){
                cout<<"("<<j.first<<", "<<j.second<<") ";</pre>
            cout<<endl;</pre>
    void shortestPathBfs(int src,int dest){
        queue<int>q;
        unordered_map<int,bool>visited;
        unordered_map<int,int>parent;
        q.push(src);
        visited[src]=1;
        parent[src]=-1;
        while(!q.empty()){
```

```
int fNode=q.front();
            q.pop();
            for(auto neighbour :adjList[fNode]){
                if(!visited[neighbour.first]){
                    q.push(neighbour.first);
                    visited[neighbour.first]=1;
                    parent[neighbour.first]=fNode;
        stack<int>st;
        int node=dest;
        while (node!=-1)
            st.push(node);
            node=parent[node];
        cout<<"printing ans: "<<endl;</pre>
        while(!st.empty()){
            cout<<st.top()<<"->";
            st.pop();
};
int main(){
    Graph g;
    g.addEdge(0,1,1,1);
    g.addEdge(1,2,1,1);
    g.addEdge(2,3,1,1);
    g.addEdge(3,4,1,1);
    g.addEdge(0,5,1,1);
    g.addEdge(5,4,1,1);
    g.addEdge(0,6,1,1);
    g.addEdge(6,7,1,1);
    g.addEdge(7,8,1,1);
    g.addEdge(8,4,1,1);
```

```
g.printAdjList();
int src=0;
int dest=4;

g.shortestPathBfs(src,dest);
return 0;
}
```

```
PS C:\Users\home\Desktop\DSA Code> g++ .\f77.cpp
PS C:\Users\home\Desktop\DSA Code> .\a.exe
8->(4, 1)
7->(8, 1)
6->(7, 1)
5->(4, 1)
0->(1, 1) (5, 1) (6, 1)
1->(2, 1)
2->(3, 1)
3->(4, 1)
printing ans:
0->5->4->
```

Time complexity: O(n)

```
#include<iostream>
#include<unordered map>
#include<list>
#include<queue>
#include<stack>
#include<limits.h>
using namespace std;
class Graph{
    public :
    unordered_map<int, list<pair<int,int> > >adjList;
    void addEdge(int u,int v,int wt,bool direction){
        //dircttion = 1-> undirected graph
        //dircttion = 0-> directed graph
        adjList[u].push_back({v,wt});
        if(direction==1){
            adjList[v].push_back({u,wt});
    void printAdjList(){
        for(auto i: adjList){
            cout<<i.first<<"->";
            for(auto j : i.second){
                cout<<"("<<j.first<<", "<<j.second<<") ";</pre>
            cout<<endl;</pre>
    void topSortDfs(int src ,unordered_map<int,bool>& visited,stack<int>& ans){
        visited[src]=true;
        for(auto neighbour : adjList[src]){
            if(!visited[neighbour.first] ){
                topSortDfs(neighbour.first, visited, ans);
        ans.push(src);
```

```
void shortestPathDfs(int dest,stack<int>topOrder,int n){
        vector<int>dist(n,INT_MAX);
        int src=topOrder.top();
        topOrder.pop();
        dist[src]=0;
        for(auto neighbour:adjList[0]){
            if(dist[0]+neighbour.second < dist [neighbour.first] ){</pre>
                dist [neighbour.first] = dist[0]+neighbour.second;
        while(!topOrder.empty()){
            int topElment=topOrder.top();
            topOrder.pop();
            if(dist[topElment]!=INT_MAX){
                for(auto neighbour:adjList[topElment]){
                     if(dist[topElment]+neighbour.second < dist [neighbour.first]</pre>
){
                         dist [neighbour.first] =
dist[topElment]+neighbour.second;
        cout<<"printing ans :"<<endl;</pre>
        for(int i=0;i<n;i++){
            cout<<i<<"->"<<dist[i]<<endl;</pre>
};
int main(){
    Graph g;
    g.addEdge(0,1,5,0);
    g.addEdge(0,2,3,0);
    g.addEdge(2,1,2,0);
    g.addEdge(1,3,3,0);
    g.addEdge(2,3,5,0);
    g.addEdge(2,4,6,0);
```

```
g.addEdge(4,3,1,0);

g.printAdjList();

stack<int>topOrder;
unordered_map<int,bool>visited;
g.topSortDfs(0,visited,topOrder);

g.shortestPathDfs(3,topOrder,5);
return 0;
}
```

```
PS C:\Users\home\Desktop\DSA Code> g++ .\f77.cpp
PS C:\Users\home\Desktop\DSA Code> .\a.exe
4->(3, 1)
1->(3, 3)
2->(1, 2) (3, 5) (4, 6)
0->(1, 5) (2, 3)
printing ans:
0->0
1->5
2->3
3->8
4->9
```

Q) write program for find shortest path distance using dijkstra's algorithm (Imp)

```
#include<iostream>
#include<unordered_map>
#include<list>
#include<queue>
#include<stack>
#include<set>
#include<limits.h>
using namespace std;
class Graph{
    public :
    unordered_map<int, list<pair<int,int> > >adjList;
    void addEdge(int u,int v,int wt,bool direction){
        //dircttion = 0-> directed graph
        adjList[u].push_back({v,wt});
        if(direction==1){
            adjList[v].push_back({u,wt});
    void printAdjList(){
        for(auto i: adjList){
            cout<<i.first<<"->";
            for(auto j : i.second){
                cout<<"("<<j.first<<", "<<j.second<<") ";</pre>
            cout<<endl;</pre>
```

```
void shortestDistDijkstra(int src,int n){
        vector<int>dist(n,INT_MAX);
        set<pair<int,int> >st;
        dist[src]=0;
        st.insert(make_pair(0,src));
        while(!st.empty()){
             auto topElement=*(st.begin());
            int nodeDistance=topElement.first;
            int node=topElement.second;
            st.erase(st.begin());
             for(auto neighbour:adjList[node]){
                 if(nodeDistance+neighbour.second < dist[neighbour.first]){</pre>
result=st.find(make_pair(dist[neighbour.first],neighbour.first));
                     if(result!=st.end()){
                         st.erase(result);
                     dist[neighbour.first]=nodeDistance+neighbour.second;
                     st.insert(make_pair(dist[neighbour.first],neighbour.first));
        cout<<"printing ans :"<<endl;</pre>
        for(int i=0;i<n;i++){</pre>
             cout<<dist[i]<<" ";</pre>
        cout<<endl;</pre>
    }
};
int main(){
    Graph g;
```

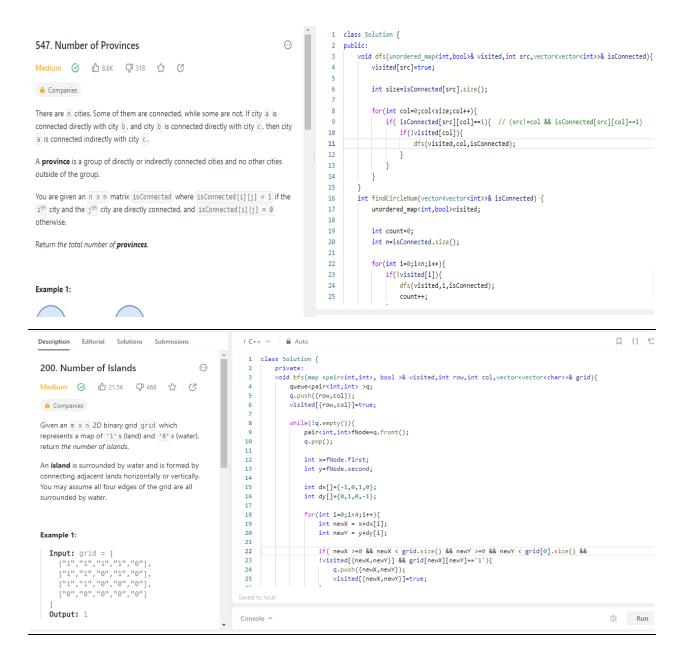
```
g.addEdge(6,3,2,1);
g.addEdge(3,1,9,1);
g.addEdge(3,2,10,1);
g.addEdge(3,2,7,1);
g.addEdge(1,2,7,1);
g.addEdge(2,4,15,1);
g.addEdge(4,3,11,1);
g.addEdge(6,5,9,1);
g.addEdge(4,5,6,1);
g.printAdjList();
g.shortestDistDijkstra(6,7);
return 0;
}
```

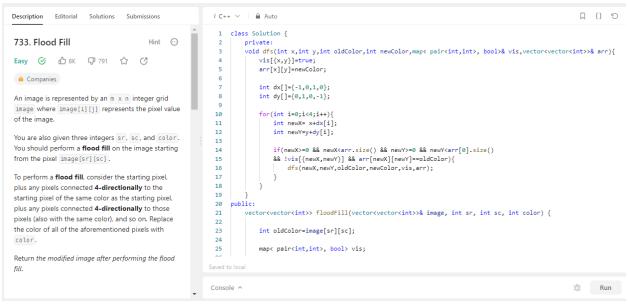
```
PS C:\Users\home\Desktop\DSA Code_Next_Part> g++ .\f77.cpp
PS C:\Users\home\Desktop\DSA Code_Next_Part> .\a.exe
5->(6, 9) (4, 6)
4->(2, 15) (3, 11) (5, 6)
6->(3, 2) (1, 14) (5, 9)
1->(6, 14) (3, 9) (2, 7)
3->(6, 2) (1, 9) (2, 10) (4, 11)
2->(3, 10) (1, 7) (4, 15)
printing ans :
2147483647 11 12 2 13 9 0
```

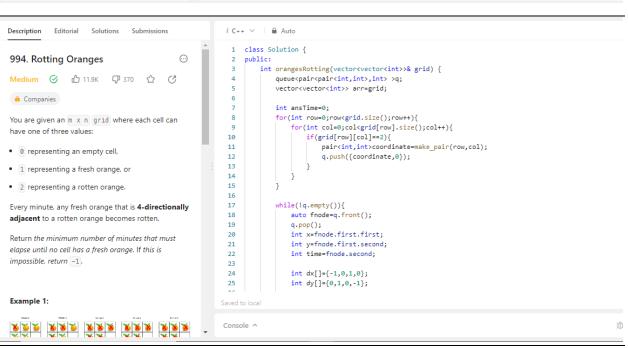
Time complexity : O(e log v)

### Graphs - II

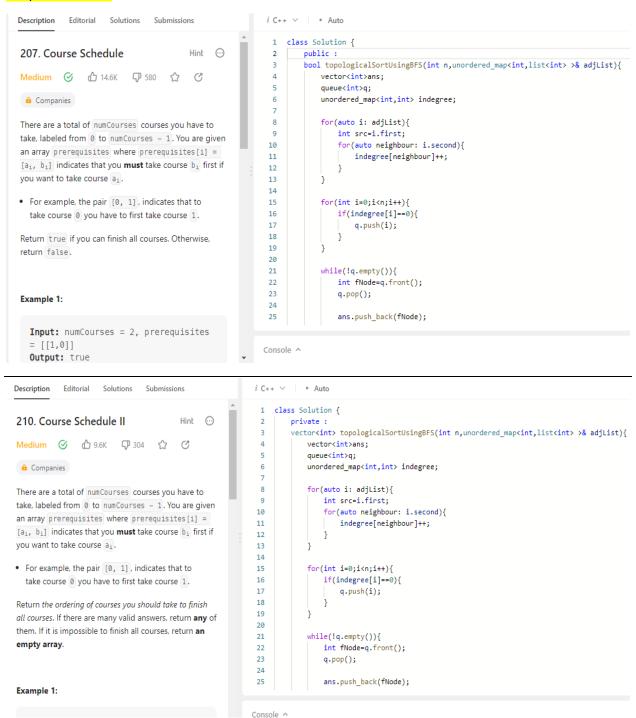
## Graphs Class - 5

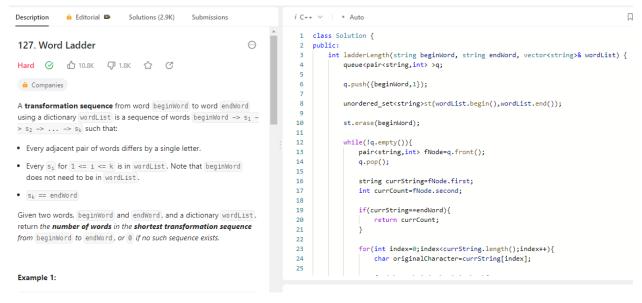


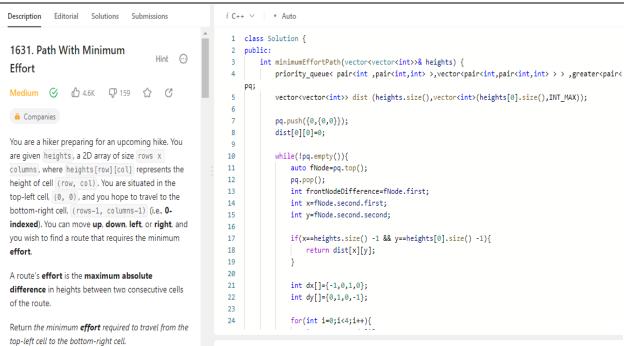




### Graphs Class - 6







## Graphs Class – 7

## Q) write bellman ford algorithms

```
#include<iostream>
#include<unordered_map>
#include<list>
#include<queue>
#include<stack>
#include<set>
#include<limits.h>
using namespace std;
class Graph{
    public :
    unordered_map<int, list<pair<int,int> > >adjList;
    void addEdge(int u,int v,int wt,bool direction){
        //dircttion = 1-> undirected graph
        //dircttion = 0-> directed graph
        adjList[u].push_back({v,wt});
        if(direction==1){
            adjList[v].push_back({u,wt});
    void printAdjList(){
        for(auto i: adjList){
            cout<<i.first<<"->";
            for(auto j : i.second){
                cout<<"("<<j.first<<", "<<j.second<<") ";
            cout<<endl;</pre>
```

```
void bellmanForAlgo(int n,int src){
        vector<int>dist(n,INT MAX);
        dist[src]=0;
        for(int i=0;i<n-1;i++){</pre>
            for(auto t:adjList){
                 for(auto neighbour:t.second){
                     int u=t.first;
                     int v=neighbour.first;
                     int wt=neighbour.second;
                     if(dist[u]!=INT_MAX && dist[u]+wt < dist[v]){</pre>
                         dist[v]=dist[u]+wt;
        cout<<"printing Bellman Ford Algorithms ans :"<<endl;</pre>
        for(auto i: dist){
            cout<<i<< ";</pre>
};
int main(){
    Graph g;
    g.addEdge(0,1,-1,0);
    g.addEdge(0,2,4,0);
    g.addEdge(1,2,3,0);
    g.addEdge(1,3,2,0);
    g.addEdge(1,4,2,0);
    g.addEdge(3,1,2,0);
    g.addEdge(3,2,5,0);
    g.addEdge(4,3,-3,0);
    g.printAdjList();
    g.bellmanForAlgo(5,0);
    //g.shortestDistDijkstra(6,7);
    return 0;
```

```
PS C:\Users\home\Desktop\DsaCodeNewNext> g++ .\f77.cpp
PS C:\Users\home\Desktop\DsaCodeNewNext> .\a.exe
4->(3, -3)
3->(1, 2) (2, 5)
1->(2, 3) (3, 2) (4, 2)
0->(1, -1) (2, 4)
printing Bellman Ford Algorithms ans:
0 -1 2 -2 1
```

Q) write program to check –ve cycle is present or absen using bellman ford algorithms

```
#include<iostream>
#include<unordered_map>
#include<list>
#include<queue>
#include<stack>
#include<set>
#include<limits.h>
using namespace std;
class Graph{
    public :
    unordered_map<int, list<pair<int,int> > >adjList;
    void addEdge(int u,int v,int wt,bool direction){
        //dircttion = 1-> undirected graph
        //dircttion = 0-> directed graph
        adjList[u].push_back({v,wt});
        if(direction==1){
            adjList[v].push_back({u,wt});
    void printAdjList(){
        for(auto i: adjList){
            cout<<i.first<<"->";
            for(auto j : i.second){
                cout<<"("<<j.first<<", "<<j.second<<") ";</pre>
            cout<<endl;</pre>
```

```
void bellmanFordAlgo(int n,int src){
    vector<int>dist(n,INT MAX);
    dist[src]=0;
    for(int i=0;i<n-1;i++){</pre>
        for(auto t:adjList){
             for(auto neighbour:t.second){
                 int u=t.first;
                 int v=neighbour.first;
                 int wt=neighbour.second;
                 if(dist[u]!=INT MAX && dist[u]+wt < dist[v]){</pre>
                     dist[v]=dist[u]+wt;
    bool negativeCycle=false;
    for(auto t:adjList){
             for(auto neighbour:t.second){
                 int u=t.first;
                 int v=neighbour.first;
                 int wt=neighbour.second;
                 if(dist[u]!=INT_MAX && dist[u]+wt < dist[v]){</pre>
                     negativeCycle=true;
                     break;
    if(negativeCycle==true){
        cout<<"-ve cycle is present";</pre>
    else{
        cout<<"-ve cycle is absent";</pre>
    cout<<endl;</pre>
    cout<<"printing Bellman Ford Algorithms ans :"<<endl;</pre>
    for(auto i: dist){
        cout<<i<< ";</pre>
```

```
int main(){
    Graph g;

    g.addEdge(0,1,-1,0);
    g.addEdge(0,2,4,0);
    g.addEdge(1,2,3,0);

    g.addEdge(1,3,2,0);
    g.addEdge(1,4,2,0);
    g.addEdge(3,1,2,0);

    g.addEdge(3,1,2,0);

    g.addEdge(4,3,-3,0);

    g.printAdjList();

    g.bellmanFordAlgo(5,0);
    //g.shortestDistDijkstra(6,7);
    return 0;
}
```

```
PS C:\Users\home\Desktop\DsaCodeNewNext> g++ .\f77.cpp
PS C:\Users\home\Desktop\DsaCodeNewNext> .\a.exe
4->(3, -3)
3->(1, 2) (2, 5)
1->(2, 3) (3, 2) (4, 2)
0->(1, -1) (2, 4)
-ve cycle is absent
printing Bellman Ford Algorithms ans :
0 -1 2 -2 1
```

## Q) write Floyd Warshall algorithms

```
#include<iostream>
#include<unordered map>
#include<list>
#include<queue>
#include<stack>
#include<set>
#include<limits.h>
#include<algorithm>
using namespace std;
class Graph{
    public :
    unordered_map<int, list<pair<int,int> > >adjList;
    void addEdge(int u,int v,int wt,bool direction){
        //dircttion = 1-> undirected graph
        //dircttion = 0-> directed graph
        adjList[u].push_back({v,wt});
        if(direction==1){
            adjList[v].push_back({u,wt});
    void printAdjList(){
        for(auto i: adjList){
            cout<<i.first<<"->";
            for(auto j : i.second){
                cout<<"("<<j.first<<", "<<j.second<<") ";</pre>
            cout<<endl;</pre>
```

```
void floydWarshall(int n){
         vector<vector<int> >dist(n,vector<int>(n,1e9));
         for(int i=0;i<n;i++){</pre>
             dist[i][i]=0;
         for(auto t:adjList){
                 for(auto neighbour:t.second){
                      int u=t.first;
                      int v=neighbour.first;
                      int wt=neighbour.second;
                      dist[u][v]=wt;
                 }
         for(int helper=0;helper<n;helper++){</pre>
             for(int src=0;src<n;src++){</pre>
                 for(int dest=0;dest<n;dest++){</pre>
                      dist[src][dest]=min(dist[src][dest],
dist[src][helper]+dist[helper][dest]);
         cout<<endl;</pre>
         cout<<"printing floyd warshall Algorithms ans :"<<endl;</pre>
         for(int i=0;i<n;i++){
             for(int j=0;j<n;j++){</pre>
                 cout<<dist[i][j]<<" ";</pre>
             cout<<endl;</pre>
};
int main(){
    Graph g;
    g.addEdge(0,1,3,0);
    g.addEdge(0,3,5,0);
    g.addEdge(1,0,2,0);
    g.addEdge(1,3,4,0);
    g.addEdge(2,1,1,0);
    g.addEdge(3,2,2,0);
```

```
g.printAdjList();
g.floydWarshall(4);
return 0;
}
```

```
PS C:\Users\home\Desktop\DsaCodeNewNext> g++ .\f77.cpp
PS C:\Users\home\Desktop\DsaCodeNewNext> .\a.exe
3->(2, 2)
2->(1, 1)
1->(0, 2) (3, 4)
0->(1, 3) (3, 5)

printing floyd warshall Algorithms ans:
0 3 7 5
2 0 6 4
3 1 0 5
5 3 2 0
```

## Graphs Class – 8

Q) Strongly Connected Components (Kosaraju's Algo)

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
#include <stack>
using namespace std;
class Graph{
    public:
    unordered_map<int,list<int> > adjList;
    void addEdge(int u,int v,bool direction){
        adjList[u].push_back(v);
        if(direction==1){
            adjList[v].push_back(u);
    void dfs1(int src,stack<int>& s,unordered_map<int,bool>& vis){
        vis[src]=true;
        for(auto neighbour :adjList[src]){
            if(!vis[neighbour]){
                dfs1(neighbour,s,vis);
        s.push(src);
```

```
void dfs2(int src,unordered_map<int,bool>&
visited,unordered_map<int,list<int> >& adjNew){
    visited[src]=true;

    cout<<src<<", ";
    for(auto neighbour :adjNew[src]){
        if(!visited[neighbour]){
            dfs2(neighbour,visited,adjNew);
        }
    }
}</pre>
```

```
int countSSC(int n){
    stack<int>s;
    unordered_map<int,bool>visited;
    for(int i=0;i<n;i++){</pre>
        if(!visited[i]){
            dfs1(i,s,visited);
    unordered_map<int,list<int> > adjNew;
    for(auto t: adjList){
        for(auto neighbour:t.second){
            int u=t.first;
            int v=neighbour;
            adjNew[v].push_back(u);
    int count=0;
    unordered_map<int,bool>visited2;
    while(!s.empty()){
        int node=s.top();
        s.pop();
        if(!visited2[node]){
            cout<<"printing "<<count+1<<" th SSC:";</pre>
            dfs2(node, visited2, adjNew);
            cout<<endl;</pre>
            count++;
    return count;
```

```
int main()
{
    Graph g;
    g.addEdge(0,1,0);
    g.addEdge(1,2,0);
    g.addEdge(2,3,0);
    g.addEdge(3,0,0);
    g.addEdge(3,0,0);
    g.addEdge(4,5,0);
    g.addEdge(4,5,0);
    g.addEdge(5,6,0);
    g.addEdge(6,7,0);

int ans =g.countSSC(8);
    cout<<"number of SSC: "<<ans;
    return 0;
}</pre>
```

```
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> g++ .\f77.cpp
PS E:\C++Code> .\a.exe
printing 1 th SSC:0, 3, 2, 1,
printing 2 th SSC:4, 6, 5,
printing 3 th SSC:7,
number of SSC: 3
```

## Q) Bridges in Graph using Tarjan's Algorithm

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <list>
#include <queue>
#include <stack>
#include <algorithm>

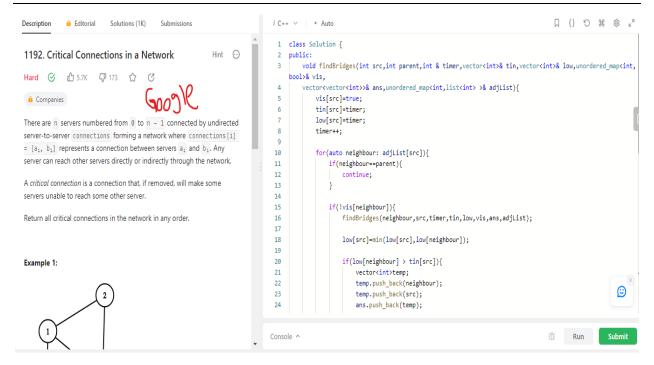
using namespace std;

class Graph{
    public:
    unordered_map<int,list<int> > adjList;

    void addEdge(int u,int v,bool direction){
        adjList[u].push_back(v);
        if(direction==1){
            adjList[v].push_back(u);
        }
    }
}
```

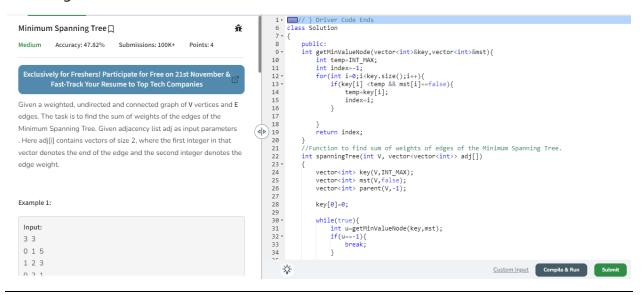
```
void findBridges(int src,int parent,int & timer,vector<int>& tin,vector<int>&
low,unordered_map<int,bool>vis){
        vis[src]=true;
        tin[src]=timer;
        low[src]=timer;
        timer++;
        for(auto neighbour: adjList[src]){
            if(neighbour==parent){
                continue;
            if(!vis[neighbour]){
                findBridges(neighbour, src, timer, tin, low, vis);
                low[src]=min(low[src],low[neighbour]);
                if(low[neighbour] > low[src]){
                     cout<<neighbour<<"--"<<src<<" is a bridge"<<endl;</pre>
            else{
                low[src]=min(low[src],low[neighbour]);
};
int main()
    Graph g;
    g.addEdge(0,1,1);
    g.addEdge(0,2,1);
    g.addEdge(2,1,1);
    g.addEdge(0,3,1);
    g.addEdge(3,4,1);
    int n=5;
    int timer=0;
    vector<int> tin(n);
    vector<int> low(n);
    unordered_map<int,bool>vis;
    g.findBridges(0,-1,timer,tin,low,vis);
    return 0;
```

# PS <u>E:\C++Code</u>> .\a.exe 4--3 is a bridge 3--0 is a bridge

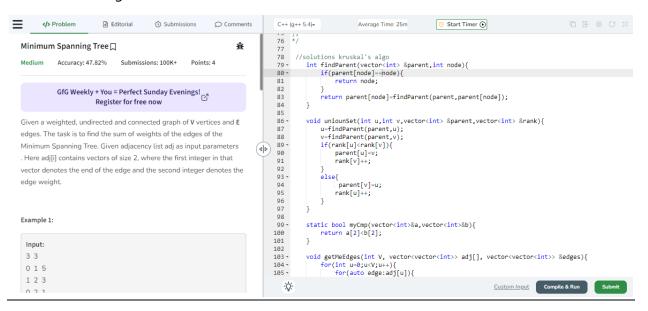


## **Graphs Assignment**

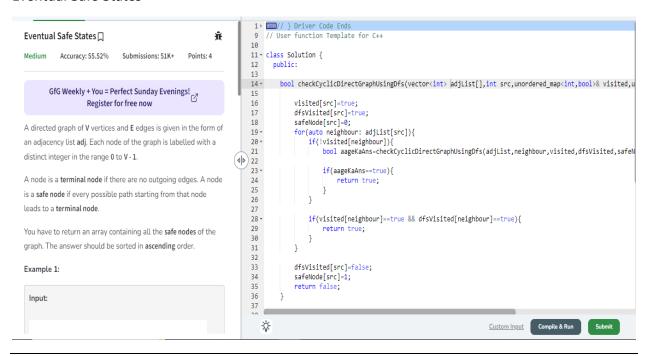
## Prim's Algorithms for MST



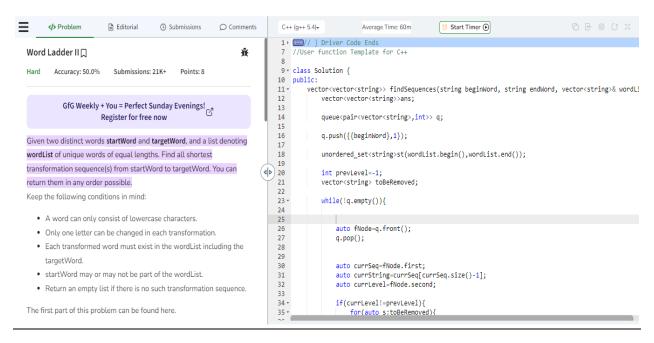
### Kruskal's MST Algorithm



#### **Eventual Safe States**



#### Word Ladder II



## Minimum Multiplications to reach End

