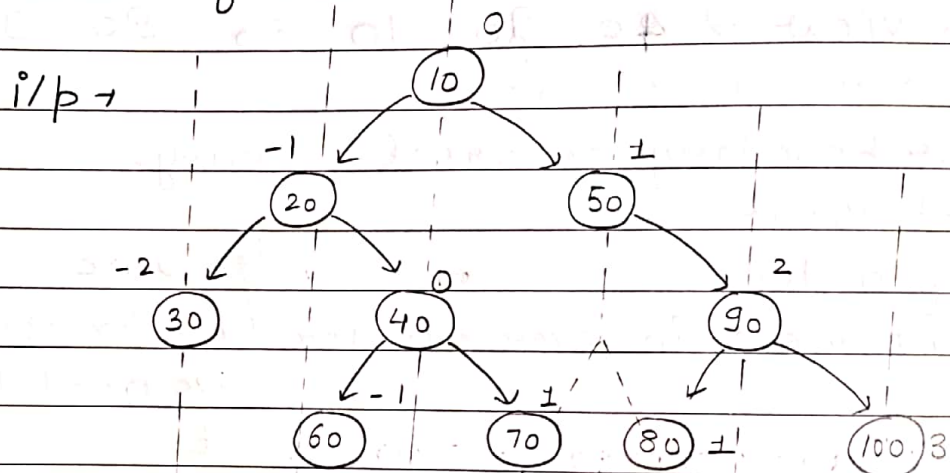


13/05/2023

Q1 Top view of tree

O/p  $\rightarrow$  30 20 10 50 90 100

The above question can be done with the help of horizontal distance from the root node. If we go towards left, reduce by 1 & if we go towards right then increment by 1.

If for a particular answer is stored already, then don't store else store the node. Here the traversal that we have to follow is level order traversal as in this higher level is processed first.

<u>Stored</u>	<u>Not stored</u>
0 $\rightarrow$ 10	
-1 $\rightarrow$ 20	40
1 $\rightarrow$ 50	60
-2 $\rightarrow$ 30	70, 80
	-
2 $\rightarrow$ 90	-
3 $\rightarrow$ 100	-

Code

```
void printTopView (Node * root){
    // Tree empty
    if (root == NULL){
        return;
    }
    // Map which stores horizontal distance &
    // node data
    map<int, int> topNode;
    // Level order traversal
    // Create queue consisting of pair having
    // Node * & horizontal distance
    queue<pair<Node *, int>> q;
    // Push root & hd of root
    q.push(make_pair(root, 0));
    while (!q.empty()){
        pair<Node *, int> temp = q.front();
        q.pop();
        Node* frontNode = temp.first;
        int hd = temp.second;
        // Check whether any node is already
        // present for hd.
        if (topNode.find(hd) == topNode.end()){
            // Not present & hence store
            topNode[hd] = frontNode->data;
        }
        // Push left child & also hd
        if (frontNode->left){
            q.push(make_pair(frontNode->left, hd-1));
        }
        // Push right child & also hd
```



```

    if (frontNode → right) {
        q.push(make_pair(frontNode → right, hd+1));
    }
}

```

```

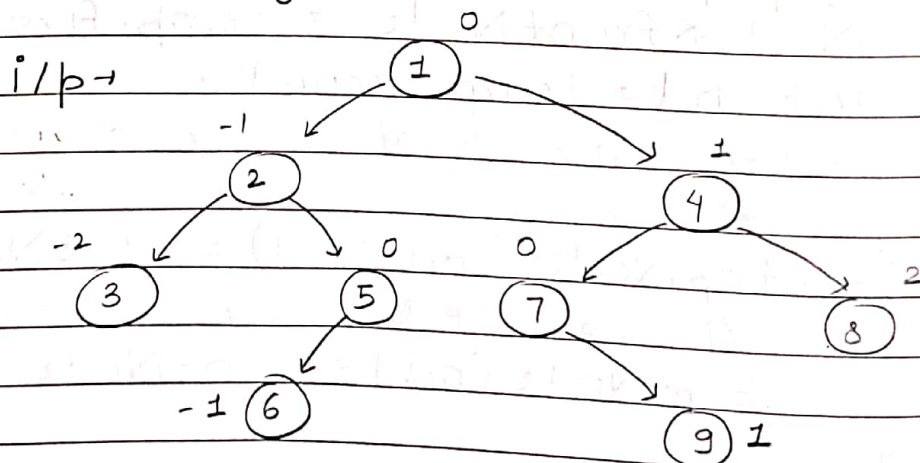
// Top view stored in the map topNode
for (auto i : topNode) {
    cout << i.second << endl;
}
}

```

Note →  $\text{topNode.find(hd)} == \text{topNode.end()} \Rightarrow$   
While searching for  $hd$ , we have reached the end and this means  $hd$  was not found.

$\text{topNode.find(hd)} \neq \text{topNode.end()} \Rightarrow$   
This means entry was found i.e  $hd$  is present in the map.

Q2 Bottom view of the tree



O/p → 3 6 7 9 8

↳ Not 5 as given in question

Again we will be using the concept of horizontal distance from root node.

0 → ~~1~~ ~~5~~ 7

-1 → ~~2~~ 6

1 → ~~4~~ 9

-2 → 3

2 → 8

Here we have to do the updations in map even if the entry is present in the map.

-2	-1	0	1	2	
↓	↓	↓	↓	↓	
3	6	7	9	8	} <u>Ans</u>

Note → What if question said to store 5 instead of 7? In this case we would be storing the hd and vector and as we go on to next level remove previous answer.

Level-0 ⇒ 0 → {1}

Level-1 ⇒ -1 → {2}, 1 → {4}

Level-2 ⇒ -2 → {3}, 0 → {5, 7}, 2 → {8}

Level-3 ⇒ -1 → {6}, 1 → {9} 1st value will be considered.

Code

Instead of

```
if (topNode.find(hd) == topNode.end()) {
    topNode[hd] = frontNode->data;
}
```

}

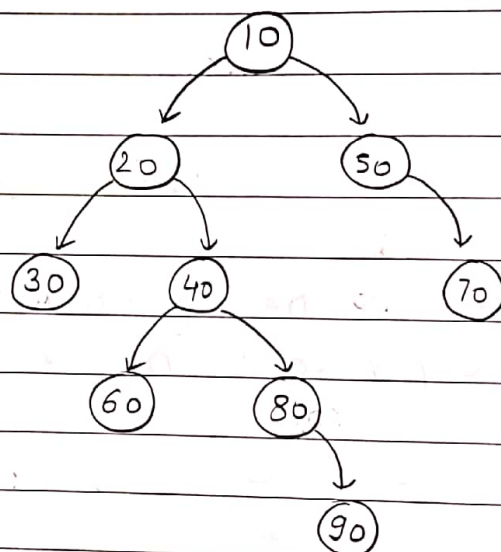
⇓

```
topNode[hd] = frontNode->data;
```

Here no if condition is used.

### Q3 Left view of tree

i/p →



O/p → 10 20 30 60 90

This question is very simple when level order traversal is used but here we will be solving it with the help of recursion. Here we will be storing the answer only when for that particular level, no node is present. If node is present for that level, then do not update it.

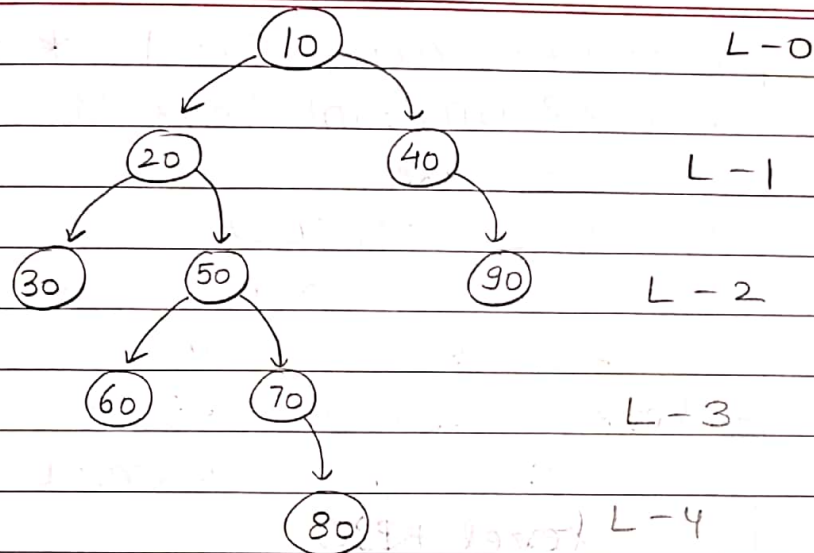
Not stored

0 → 10	-
1 → 20	50
2 → 30	40, 70
3 → 60	80
4 → 90	-

Ans → 10, 20, 30, 60, 90

The above method is also simple. Let's do it with recursion.





Level  $\rightarrow 0$ , vector size = 0 ] matching  
vector  $\rightarrow \{10\}$

Level-1, vector size = 1 ] matching  
vector  $\rightarrow \{10, 20\}$

Level-2, vector size = 2 ] matching  
vector  $\rightarrow \{10, 20, 30\}$

Level-2, vector size = 3 ] not matching  
vector  $\rightarrow \{10, 20, 30\}$

Level-3, vector size = 3 ] matching  
vector  $\rightarrow \{10, 20, 30, 60\}$

Level-3, vector size = 4 ] not matching  
vector  $\rightarrow \{10, 20, 30, 60\}$

Level-4, vector size = 4 ] matching  
vector  $\rightarrow \{10, 20, 30, 60, 80\}$

Level-1, vector size = 5 ] not matching  
vector  $\rightarrow \{10, 20, 30, 60, 80\}$

Level-2, vector size = 5 ] not matching  
vector  $\rightarrow \{10, 20, 30, 60, 80\}$

If level and size of vector is matching, Then  
only insert element in the vector.

Code

```
void printLeftView (Node * root,
vector <int> & ans, int level){
```

```
    // Base case
```

```
    if (root == NULL)
```

```
        return;
```

```
    // level & size are same, then insert
```

```
    if (level == ans.size()){
```

```
        ans.push_back (root->data);
```

```
    }
```

```
    // left subtree
```

```
    printLeftView (root->left, ans, level+1);
```

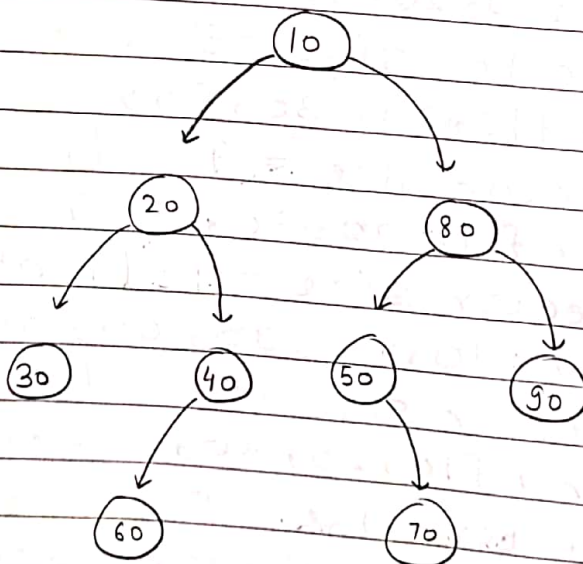
```
    // Right subtree
```

```
    printLeftView (root->right, ans, level+1);
```

```
}
```

Q4 Right view of tree.

i/p →



o/p → 10 80 90 70

Here first we need to go to the right & then left.



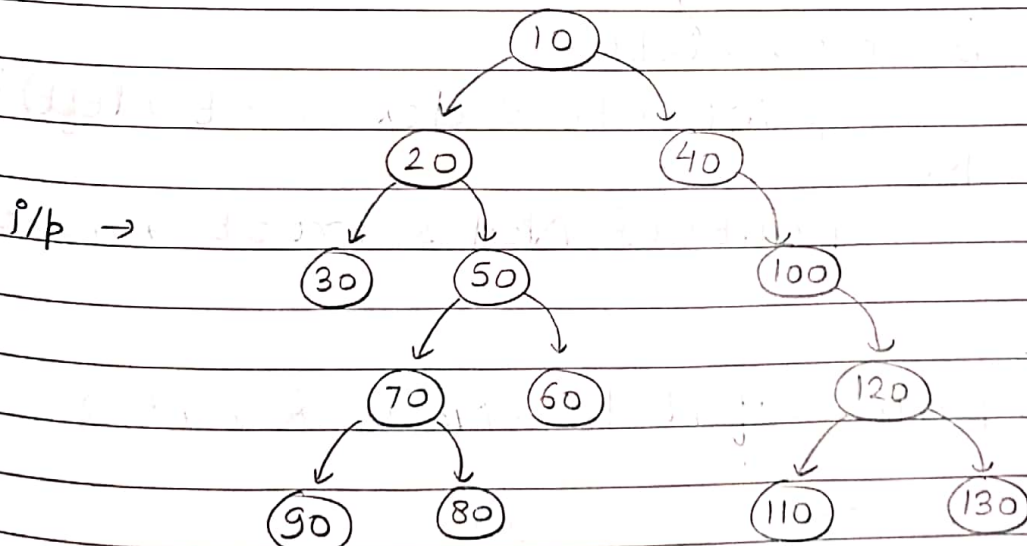
Code

```

void printRightView (Node * root, vector <int> &
ans, int level) {
    // Base case
    if (root == NULL)
        return;
    if (level == ans.size()) {
        // Insert in vector
        ans.push-back (root->data);
    }
    // Right subtree
    printRightView (root->right, ans, level + 1);
    // Left subtree
    printRightView (root->left, ans, level + 1);
}

```

Q5 Boundary traversal.



o/p → 10 20 30 90 80 60 110 130 120  
100 40

- 1) Print left nodes first.
- 2) Print leaf nodes now
- 3) Print right nodes in reverse order.



\* Kind of pre-order traversal to print the left nodes. Stop when leaf node is found.

\* Print leaf nodes

\* Print right nodes while returning from the recursive call.

Code

```
void printLeftNodes (Node * root){
```

```
    // Base case
```

```
    if (root == NULL)
```

```
        return;
```

```
    Leaf node <- if (root->left == NULL && root->right == NULL)
                    return;
```

```
    // Print the data of current node
```

```
    cout << root->data << " ";
```

```
    // Left call first
```

```
    if (root->left)
```

```
        printLeftNodes (root->left);
```

```
    else // Right call
```

```
        printLeftNodes (root->right);
```

```
}
```

```
void printLeafNodes (Node * root){
```

```
    // Base case
```

```
    if (root == NULL){
```

```
        return;
```

```
    }
```

```
    // Leaf node found & hence print
```

```
    if (root->left == NULL && root->right == NULL)
        cout << root->data << " ";
```

```
printLeafNodes (root->left); //Left call  
printLeafNodes (root->right); //Right call
```

3

```
void printRightNodes (Node * root) {  
    // Base case  
    if (root == NULL)  
        return ;  
    // Leaf node found  
    if (root->left == NULL && root->right == NULL)  
        return ;  
    // Right call first  
    if (root->right)  
        printRightNodes (root->right);  
    else // Left call  
        printRightNodes (root->left);  
    // While returning print data of root  
    cout << root->data << " ";  
}
```

3

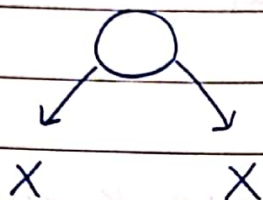
```
void boundaryTraversal (Node * root) {  
    // Empty tree  
    if (root == NULL)  
        return ;  
    // To avoid duplicacy  
    cout << root->data << " ";  
    // Left nodes  
    printLeftNodes (root->left);  
    // Leaf nodes  
    printLeafNodes (root);  
    // Right node  
    printRightNodes (root->right);  
}
```

1



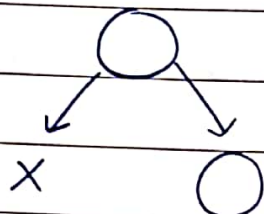
Left Nodes

1)



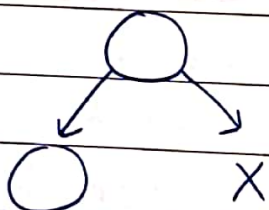
(Return)

2)



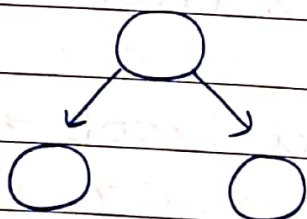
(go to right)

3)



(go to left)

4)



(go to left)

That's why if else has been used.

Time complexity =  $O(n)$