ML0101EN-Reg-NoneLinearRegression-py-v1

December 5, 2018

#

Non Linear Regression Analysis

If the data shows a curvy trend, then linear regression will not produce very accurate results when compared to a non-linear regression because, as the name implies, linear regression presumes that the data is linear. Let's learn about non linear regressions and apply an example on python. In this notebook, we fit a non-linear model to the datapoints corrensponding to China's GDP from 1960 to 2014.

Importing required libraries

Though Linear regression is very good to solve many problems, it cannot be used for all datasets. First recall how linear regression, could model a dataset. It models a linear relation between a dependent variable y and independent variable x. It had a simple equation, of degree 1, for example y = 2x + 3.

```
In []: x = np.arange(-5.0, 5.0, 0.1)

##You can adjust the slope and intercept to verify the changes in the graph
y = 2*(x) + 3
y_noise = 2 * np.random.normal(size=x.size)
ydata = y + y_noise
#plt.figure(figsize=(8,6))
plt.plot(x, ydata, 'bo')
plt.plot(x,y, 'r')
plt.ylabel('Dependent Variable')
plt.xlabel('Indepdendent Variable')
plt.show()
```

Non-linear regressions are a relationship between independent variables x and a dependent variable y which result in a non-linear function modeled data. Essentially any relationship that is not linear can be termed as non-linear, and is usually represented by the polynomial of k degrees (maximum power of x).

$$y = ax^3 + bx^2 + cx + d$$

Non-linear functions can have elements like exponentials, logarithms, fractions, and others. For example:

$$y = \log(x)$$

Or even, more complicated such as:

$$y = \log(ax^3 + bx^2 + cx + d)$$

Let's take a look at a cubic function's graph.

```
In []: x = np.arange(-5.0, 5.0, 0.1)

##You can adjust the slope and intercept to verify the changes in the graph
y = 1*(x**3) + 1*(x**2) + 1*x + 3
y_noise = 20 * np.random.normal(size=x.size)
ydata = y + y_noise
plt.plot(x, ydata, 'bo')
plt.plot(x, y, 'r')
plt.ylabel('Dependent Variable')
plt.xlabel('Indepdendent Variable')
plt.show()
```

As you can see, this function has x^3 and x^2 as independent variables. Also, the graphic of this function is not a straight line over the 2D plane. So this is a non-linear function.

Some other types of non-linear functions are:

0.0.1 Quadratic

$$Y = X^2$$

```
In []: x = np.arange(-5.0, 5.0, 0.1)

##You can adjust the slope and intercept to verify the changes in the graph

y = np.power(x,2)
y_noise = 2 * np.random.normal(size=x.size)
ydata = y + y_noise
plt.plot(x, ydata, 'bo')
plt.plot(x,y, 'r')
plt.ylabel('Dependent Variable')
plt.xlabel('Indepdendent Variable')
plt.show()
```

0.0.2 Exponential

An exponential function with base c is defined by

$$Y = a + bc^X$$

where b 0, c > 0, c 1, and x is any real number. The base, c, is constant and the exponent, x, is a variable.

```
In []: X = np.arange(-5.0, 5.0, 0.1)

##You can adjust the slope and intercept to verify the changes in the graph

Y= np.exp(X)

plt.plot(X,Y)
    plt.ylabel('Dependent Variable')
    plt.xlabel('Indepdendent Variable')
    plt.show()
```

0.0.3 Logarithmic

The response y is a results of applying logarithmic map from input x's to output variable y. It is one of the simplest form of log(): i.e.

$$y = \log(x)$$

Please consider that instead of x, we can use X, which can be polynomial representation of the x's. In general form it would be written as

$$y = \log(X) \tag{1}$$

```
In []: X = np.arange(-5.0, 5.0, 0.1)

Y = np.log(X)

plt.plot(X,Y)
    plt.ylabel('Dependent Variable')
    plt.xlabel('Indepdendent Variable')
    plt.show()
```

0.0.4 Sigmoidal/Logistic

$$Y = a + \frac{b}{1 + c^{(X-d)}}$$

```
In []: X = np.arange(-5.0, 5.0, 0.1)

Y = 1-4/(1+np.power(3, X-2))

plt.plot(X,Y)
    plt.ylabel('Dependent Variable')
    plt.xlabel('Indepdendent Variable')
    plt.show()
```

Non-Linear Regression example

For an example, we're going to try and fit a non-linear model to the datapoints corresponding to China's GDP from 1960 to 2014. We download a dataset with two columns, the first, a year

between 1960 and 2014, the second, China's corresponding annual gross domestic income in US dollars for that year.

```
In []: import numpy as np
    import pandas as pd

#downloading dataset
!wget -nv -0 china_gdp.csv https://s3-api.us-geo.objectstorage.softlayer.net/cf-courses-
    df = pd.read_csv("china_gdp.csv")
    df.head(10)
```

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0.0.5 Plotting the Dataset

This is what the datapoints look like. It kind of looks like an either logistic or exponential function. The growth starts off slow, then from 2005 on forward, the growth is very significant. And finally, it decelerate slightly in the 2010s.

0.0.6 Choosing a model

From an initial look at the plot, we determine that the logistic function could be a good approximation, since it has the property of starting with a slow growth, increasing growth in the middle, and then decreasing again at the end; as illustrated below:

The formula for the logistic function is the following:

$$\hat{Y} = \frac{1}{1 + e^{\beta_1(X - \beta_2)}}$$

 β_1 : Controls the curve's steepness,

 β_2 : Slides the curve on the x-axis.

0.0.7 Building The Model

Now, let's build our regression model and initialize its parameters.

Lets look at a sample sigmoid line that might fit with the data:

```
In []: beta_1 = 0.10
    beta_2 = 1990.0

#logistic function
Y_pred = sigmoid(x_data, beta_1 , beta_2)

#plot initial prediction against datapoints
plt.plot(x_data, Y_pred*150000000000000)
plt.plot(x_data, y_data, 'ro')
```

Our task here is to find the best parameters for our model. Lets first normalize our x and y:

How we find the best parameters for our fit line? we can use curve_fit which uses non-linear least squares to fit our sigmoid function, to data. Optimal values for the parameters so that the sum of the squared residuals of sigmoid(xdata, *popt) - ydata is minimized.

popt are our optimized parameters.

Now we plot our resulting regression model.

0.1 Practice

Can you calculate what is the accuracy of our model?

```
In [ ]: # write your code here
```

Double-click **here** for the solution.

0.2 Want to learn more?

IBM SPSS Modeler is a comprehensive analytics platform that has many machine learning algorithms. It has been designed to bring predictive intelligence to decisions made by individuals, by groups, by systems – by your enterprise as a whole. A free trial is available through this course, available here: SPSS Modeler.

Also, you can use Watson Studio to run these notebooks faster with bigger datasets. Watson Studio is IBM's leading cloud solution for data scientists, built by data scientists. With Jupyter notebooks, RStudio, Apache Spark and popular libraries pre-packaged in the cloud, Watson Studio enables data scientists to collaborate on their projects without having to install anything. Join the fast-growing community of Watson Studio users today with a free account at Watson Studio

0.2.1 Thanks for completing this lesson!

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