

```
import numpy as np
a = np.arange(6)
b = np.arange(5)
c = np.arange(5)
np.hstack((a,b)) → o/p
np.hstack((a,c)) → o/p
```

```
import numpy as np
a = np.array([[1,2],[3,4]])
b = np.array([[5,6]])
np.concatenate((a,b.T), axis=1)
np.hstack((a,b.T))
```

Same.

vstack → 1d → same shape ⇒ 2d as o/p  
 ↘ 2d, 2d → same as concatenation, axis=0

hstack → 1d → any shape → it will join  
 → 2d, 3d → same as concatenation, axis=1

splitting:-

split() → subarray.  
 np.split(array, section, axis=0)

```
import numpy as np
a = np.arange(1,10)
np.split(a,3) → 3 sub arrays
np.split(a,4) → error
```

```
import numpy as np
a = np.arange(1,13).reshape(6,2)
a →
np.split(a,2) → o/p
```

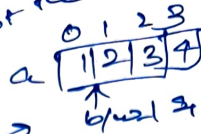
np.vsplit(a,2)  
 np.hsplit(a,3)  
 (or)  
 np.

numpy.hsplit(array, section)  
 numpy.vsplit(array, section)

## Array manipulation

- insert
- delete

insert:-  $\rightarrow$  copy of the array not the original.



insert()

np.insert(array, object, values, axis=None)  
=1  $\rightarrow$  row value

import numpy as np

a = np.arange(1, 11)

a

np.insert(a, 1, 50)  $\rightarrow$  d/p

np.insert(a, 1, 50.5)  $\rightarrow$  convert to float then it will insert

np.insert(a, (1, 3), 50)  
 $\swarrow$  1st index  $\searrow$  3rd index

import numpy as np

a = np.array([[1, 2], [3, 4]])

a

np.insert(a, 1, 23)  $\rightarrow$  whatever the dimension it will flatten then modify  $\rightarrow$  (2D, 3D, ...)

np.insert(a, 1, 23, axis=0)  $\rightarrow$  2D format

np.insert(a, 1, 23, axis=1)  $\rightarrow$  2D format

np.insert(a, 1, [1, 2], axis=0)  $\rightarrow$  d/p

np.insert(a, 1, [1, 2, 3], axis=0)  $\rightarrow$  error  
 $\rightarrow$  dimension change

append  $\rightarrow$  if I need to add some no at the end of the array.

append()

np.append(array, values, axis=None)

import numpy as np

a = np.arange(1, 11)

a

np.append(a, 3452)  $\rightarrow$  o/p

a  $\rightarrow$  it is just copied

import numpy as np

a = np.array([[1,2],[3,4]])

np.append(a, [[4,5]], axis=0) =   
 (4,5)

np.append(a, [[4,5]], axis=1) → error

1	2	4	5
3	4		

np.append(a, [[4],[5]]) → 1d array as no axis

np.append(a, [[4],[5]], axis=1) → o/p

1	2	4
3	4	5

Delete:

delete()

np.delete(array, obj, axis=None)

import numpy as np

a = np.arange(1,11)

a

np.delete(a, 2)   
 index position

a → original not deleted.

import numpy as np

a = np.array([[1,2],[3,4]])

a

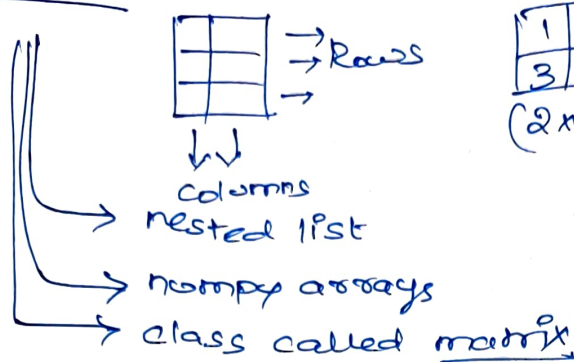
np.delete(a, 2) → 124 (no axis)

np.delete(a, 2, axis=0) → error

np.delete(a, 1, axis=0) → o/p

np.delete(a, 1, axis=1) → o/p.

MATRIX → Rectangular arrangement of data/no.



1	2
3	4

(2x2)

1	2	3
4	5	6

(2x3)

### ① numpy array:-

matrix addition  $a + b$

import numpy as np

$a = \text{np.array}([ [1, 2], [3, 4] ])$

$b = \text{np.array}([ [10, 20], [30, 40] ])$

$a + b$  (element by element)

matrix multiplication  $a * b$  (array)

$a \cdot b$  (dot)

a

1	2
3	4

b

10	20
30	40

⇒ o/p

10	40
90	160

element  
by element

$1 \times 10 + 2 \times 30$      $1 \times 20 + 2 \times 40$

70	100
150	220

$3 \times 10 + 4 \times 30$      $3 \times 20 + 4 \times 40$

import numpy as np

$a = \text{np.array}([ [10, 20], [30, 40] ])$

$b = \text{np.array}([ [1, 2], [3, 4] ])$

$a * b$  → element by element

$a \cdot b$  → matrix multiplication

help(np.dot)

### transpose

import numpy as np

$a = \text{np.array}([ [1, 2, 3], [4, 5, 6] ])$

a

$\text{np.transpose}(a)$  (or)  $a.\text{transpose}()$



## ② Matrix

`np.matrix(data, dtype=None, copy=True)`

import numpy as np

`a = np.matrix("1 2; 3 4")`

`a`

`b = np.matrix([[10, 20], [30, 40]])`

`b`

addition

`a+b`

multiplication

`a*b`

transpose

`a.T`

`b.T`

Difference with numpy array

① matrix can be created using string notation.

② matrix objects are always 2D

③ can use `*` for matrix multiplication

`help(np.matrix)`

Linear algebra:

`numpy.linalg`

— Invert  
— Power

— linear equation

— determinant of matrix

— eigen values & many more.

Inverse:-

`np.linalg.inv()` → inverse the given matrix

~~np~~ import numpy as np

`a = np.array([[1, 2], [3, 4]])`

`a`

`b = np.linalg.inv(a)`

$$A \cdot A^{-1} = I$$

$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \frac{1}{ad-bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \frac{1}{4-6} \begin{bmatrix} 4 & -2 \\ -3 & 1 \end{bmatrix} = \frac{-1}{2} \begin{bmatrix} 4 & -2 \\ -3 & 1 \end{bmatrix} \Rightarrow \begin{bmatrix} 2 & -1 \\ 1.5 & -0.5 \end{bmatrix}$$

np.dot(a,b)

import numpy as np

a = np.array([1,2,3,4])

np.linalg.inv(a) → error

help(np.linalg.inv)

Power of matrix:- used to find the power of matrix.

np.linalg.matrix\_power(a, n)

n → 0 → identity matrix

n > 0 →

n < 0 → inverse matrix then power

import numpy as np

a = np.array([[1,2],[3,4]])

np.linalg.matrix\_power(a, 2) ← same

np.dot(a, a) ←

np.linalg.matrix\_power(a, 3)

np.linalg.matrix\_power(a, 0) → identity

np.linalg.matrix\_power(a, -2) ←

↓

b = np.linalg.inv(a)

b

np.linalg.matrix\_power(b, 2) ← same

import numpy as np

a = np.array([[1, 2, 3], [4, 5, 6]])

a

np.linalg.matrix\_power(a, 2) → error

Linear equation:

↳ equation of a straight line

$$x + y = 10$$

$$2x + 2y = 20$$

np.linalg.solve(a, b)

$$\begin{array}{ccc} & Ax = B & \\ \swarrow & \downarrow & \searrow \\ \text{values} & \text{variables} & \text{constant} \end{array}$$

$$3x + y = 9$$

$$x + 2y = 8$$

$$3x + y = 9$$

$$y = 9 - 3x$$

$$a = \begin{bmatrix} 3 & 1 \\ 1 & 2 \end{bmatrix}$$

$$b = \begin{bmatrix} 9 & 8 \end{bmatrix}$$

$$x + 2y = 8$$

$$x + 2(9 - 3x) = 8$$

$$x = 2$$

import numpy as np

a = np.array([[3, 1], [1, 2]])

b = np.array([9, 8])

np.linalg.solve(a, b) → (x, y)

$$6x + 2y - 5z = 13$$

$$3x + 3y - 2z = 13$$

$$7x + 5y - 3z = 26$$

$$a = \begin{bmatrix} 6 & 2 & -5 \\ 3 & 3 & -2 \\ 7 & 5 & -3 \end{bmatrix} \quad b = \begin{bmatrix} 13 & 13 & 26 \end{bmatrix}$$

x = np.~~arr~~array([[6, 2, -5], [3, 3, -2], [7, 5, -3]])

y = np.array([13, 13, 26])

np.linalg.solve(x, y) → o/p

Determinant:

$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix} = ad - bc$$

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = 1 \times 4 - 2 \times 3 \rightarrow 4 - 6 \rightarrow -2 //$$

np.linalg.det(a) → square matrix

import numpy as np

a = np.array([[1, 2], [3, 4]])

2D a

np.linalg.det(a)

round(np.linalg.det(a))

b = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])

3D b

np.linalg.det(b)

round(np.linalg.det(b))

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} = a(ei - fh) - b(di - fg) + c(dh - eg)$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} = 1(45 - 48) - 2(36 - 42) + 3(32 - 35) \\ = -3 - 2(-6) + 3(-3) \\ = -3 + 12 - 9 = 0$$

images

from matplotlib.image import imread

picture = imread('a.png')

print(type(picture))

picture

picture.size

picture.shape

picture.ndim