

# Task 3: Statistical Estimation of Response Time

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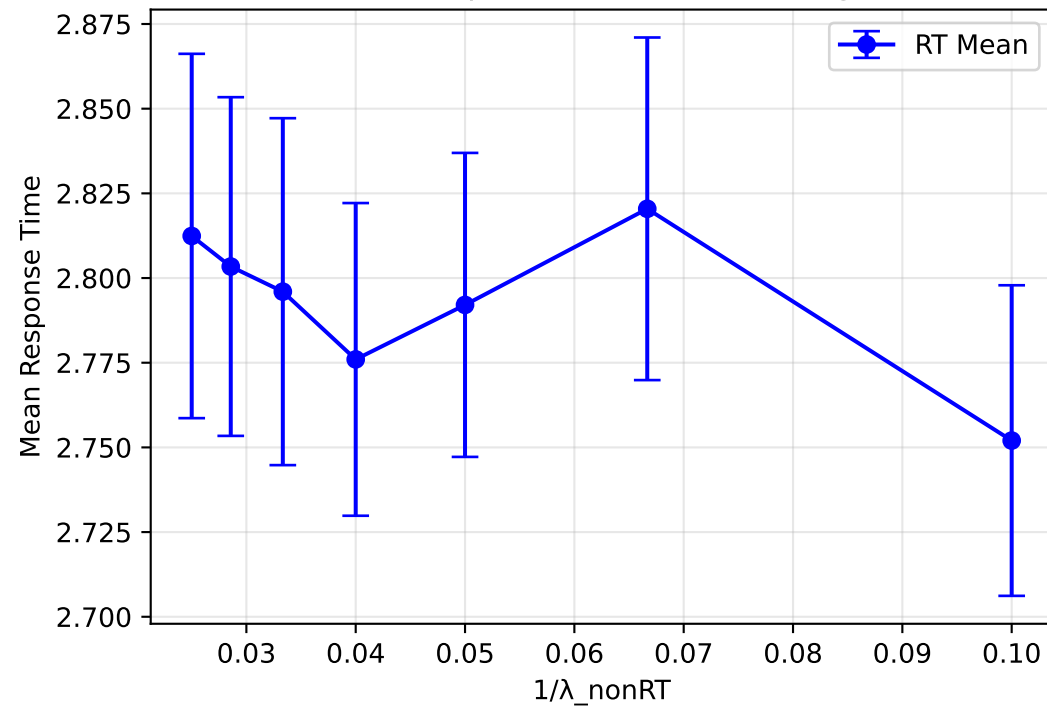
Parameters:  $MST_{RT}=2$ ,  $MST_{nonRT}=4$ ,  $MIAT_{RT}=7$   
Varying  $MIAT_{nonRT}$  from 10 to 40 in increments of 5

Batch Means Method:  $m=51$  batches,  $b=1000$  observations per batch

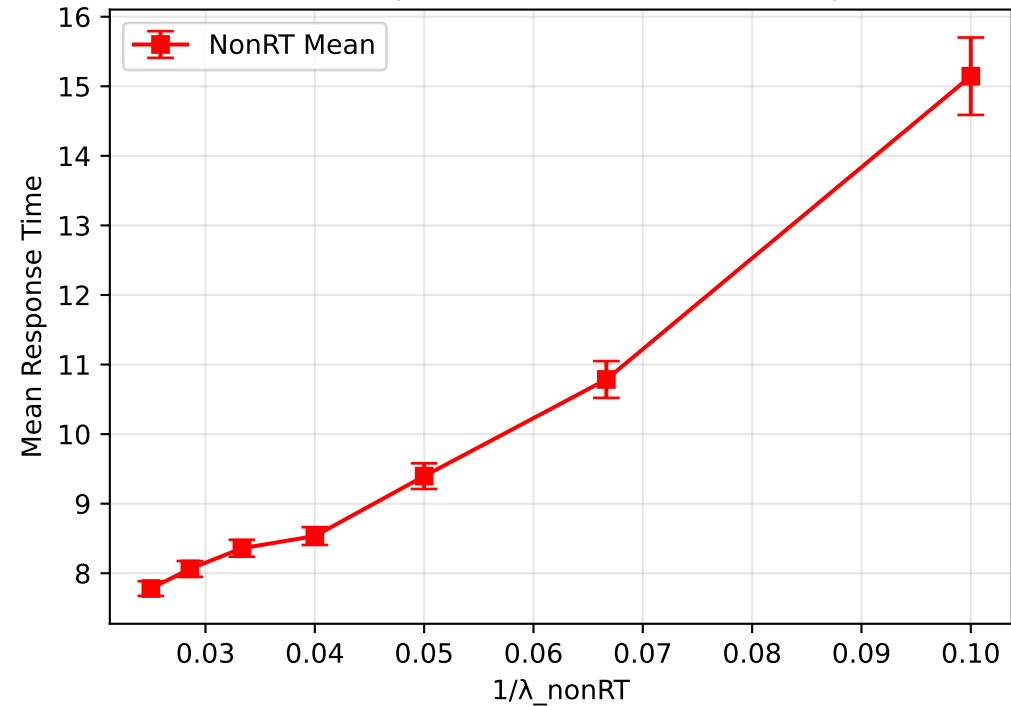
First batch ignored, using remaining 50 batches for statistics

# Response Time Statistics

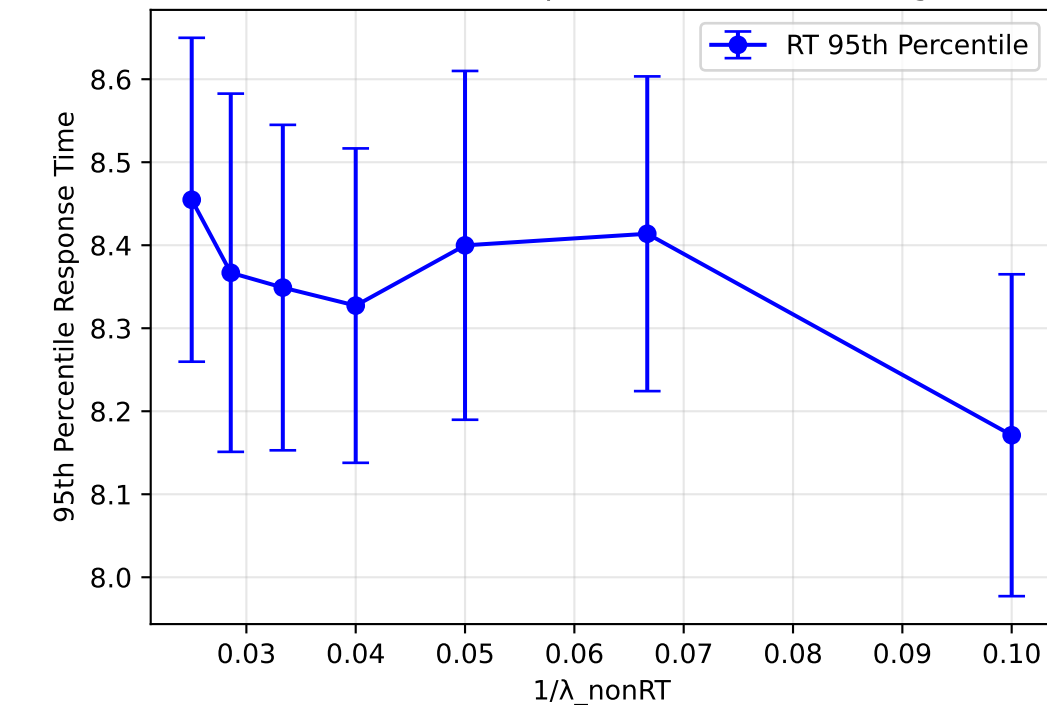
## Mean Response Time - RT Messages



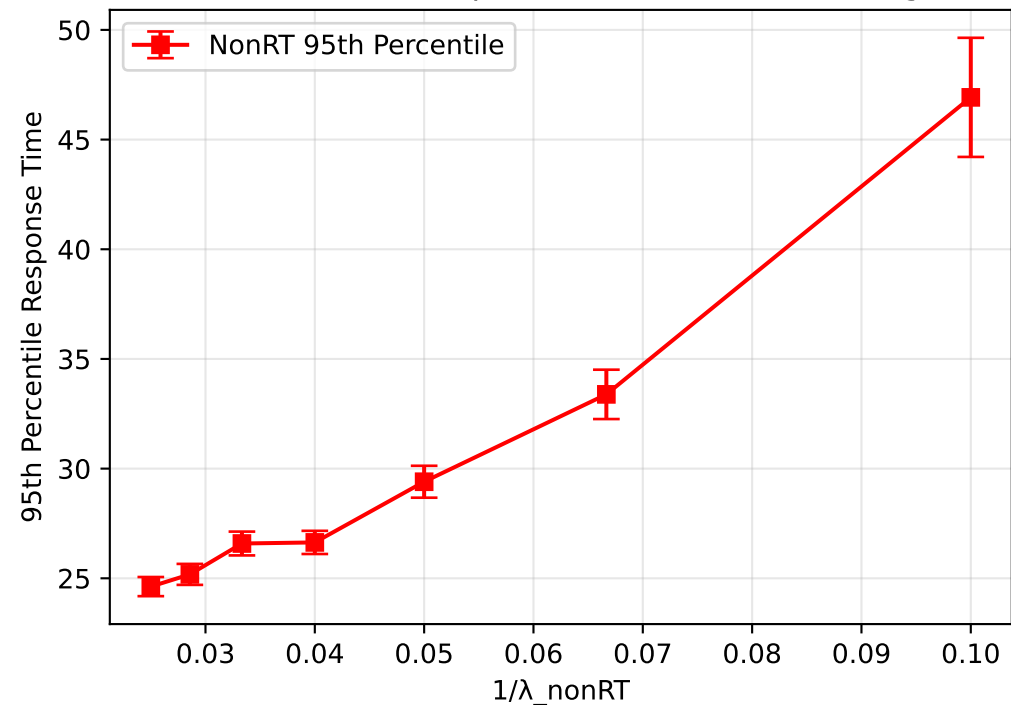
## Mean Response Time - NonRT Messages



## 95th Percentile Response Time - RT Messages



## 95th Percentile Response Time - NonRT Messages



Results Summary Table

MIAT_nonRT	1/λ_nonRT	RT Mean	RT 95th %	NonRT Mean	NonRT 95th %
10.0	0.1000	2.7520	8.1711	15.1451	46.9242
15.0	0.0667	2.8204	8.4138	10.7856	33.3846
20.0	0.0500	2.7921	8.3999	9.3959	29.4019
25.0	0.0400	2.7760	8.3273	8.5343	26.6359
30.0	0.0333	2.7960	8.3490	8.3594	26.5862
35.0	0.0286	2.8034	8.3669	8.0622	25.1783
40.0	0.0250	2.8124	8.4548	7.7802	24.6222

Confidence Intervals (95%)

MIAT\_nonRT = 10.0:

- RT Mean CI: [2.7062, 2.7979]
- RT 95th % CI: [7.9772, 8.3650]
- NonRT Mean CI: [14.5886, 15.7015]
- NonRT 95th % CI: [44.2089, 49.6395]

MIAT\_nonRT = 15.0:

- RT Mean CI: [2.7699, 2.8710]
- RT 95th % CI: [8.2242, 8.6034]
- NonRT Mean CI: [10.5212, 11.0500]
- NonRT 95th % CI: [32.2595, 34.5097]

MIAT\_nonRT = 20.0:

- RT Mean CI: [2.7472, 2.8369]
- RT 95th % CI: [8.1898, 8.6100]
- NonRT Mean CI: [9.2116, 9.5801]
- NonRT 95th % CI: [28.6746, 30.1292]

MIAT\_nonRT = 25.0:

- RT Mean CI: [2.7298, 2.8221]
- RT 95th % CI: [8.1379, 8.5166]
- NonRT Mean CI: [8.4061, 8.6624]
- NonRT 95th % CI: [26.1077, 27.1640]

MIAT\_nonRT = 30.0:

- RT Mean CI: [2.7448, 2.8472]
- RT 95th % CI: [8.1529, 8.5450]
- NonRT Mean CI: [8.2373, 8.4815]
- NonRT 95th % CI: [26.0436, 27.1289]

MIAT\_nonRT = 35.0:

- RT Mean CI: [2.7534, 2.8534]
- RT 95th % CI: [8.1511, 8.5826]
- NonRT Mean CI: [7.9485, 8.1758]
- NonRT 95th % CI: [24.6999, 25.6567]

MIAT\_nonRT = 40.0:

- RT Mean CI: [2.7586, 2.8662]
- RT 95th % CI: [8.2597, 8.6499]
- NonRT Mean CI: [7.6749, 7.8855]
- NonRT 95th % CI: [24.1855, 25.0589]

# Analysis and Comments

## Task 3.1 Results Analysis:

As  $1/\lambda_{\text{nonRT}}$  increases (i.e.,  $\text{MIAT}_{\text{nonRT}}$  increases), the nonRT arrival rate decreases.

This means fewer nonRT messages compete for server resources, leading to:

1. Lower mean response time for nonRT messages (less queueing)
2. Lower 95th percentile for nonRT messages
3. Potentially lower response times for RT messages as well, since there's less preemption and interference from nonRT messages

The confidence intervals show the uncertainty in our estimates. Wider intervals indicate higher variance in the response times, which could be due to:

- High variability in inter-arrival times (exponential distribution)
- High variability in service times
- System approaching saturation

## Task 3.2 Results Analysis:

With fixed  $\text{MST}_{\text{RT}}=2$ ,  $\text{MST}_{\text{nonRT}}=4$ , and  $\text{MIAT}_{\text{RT}}=7$ , and varying  $\text{MIAT}_{\text{nonRT}}$ :

**RT Messages:** RT messages have priority and can preempt nonRT messages.

Their response time is primarily affected by:

- Their own arrival rate (fixed at  $\text{MIAT}_{\text{RT}}=7$ )
- Service time (fixed at  $\text{MST}_{\text{RT}}=2$ )
- Interference from nonRT messages (decreases as  $\text{MIAT}_{\text{nonRT}}$  increases)

**NonRT Messages:** NonRT messages experience:

- Direct impact from their own arrival rate ( $\text{MIAT}_{\text{nonRT}}$ )
- Preemption by RT messages
- As  $\text{MIAT}_{\text{nonRT}}$  increases, fewer nonRT messages arrive, reducing both queue length and preemption frequency

**Expected Trends:**

1. NonRT mean and 95th percentile should decrease as  $1/\lambda_{\text{nonRT}}$  increases
2. RT response times may show slight improvement as nonRT interference decreases
3. Confidence intervals should be relatively stable if batch size is adequate