

Authors' response

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Title: Operationally-Safe Peer-to-Peer Energy Trading in Distribution Grids: A Game-Theoretic Market-Clearing Mechanism

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The authors would like to thank the Reviewers and the Associate Editor for their comments, which have helped us to improve the manuscript. We do hope that all the points raised have been addressed. To help reviewing the revised manuscript, the points have been divided up and marked AE, R1, R2, R3, and R4, for comments from Associate Editor, Reviewers 1, 2, 3, and 4, respectively. When appropriate, the corresponding marks can be found within the manuscript and the modifications according to the comments are highlighted in blue. In addition, the cross references of equation labels, as mentioned by the reviewers and used in the answers, are adapted based on the revised manuscript.

Answers to Associate Editor

AE-1: *This paper proposes a generalized Nash game model for P2P energy trading in a distribution network considering network constraints and DNO. A distributed algorithm is developed to seek the equilibrium of the game. The topic is relevant and timely. However, the reviewers raised some concerns. The authors should carefully consider all the comments and make a corresponding improvement.*

Answer: To be answered!

Answers to Reviewer 1

R1-1: *This paper proposed a peer-to-peer energy market for prosumers as a generalized aggregative game. The paper is well written, and the research may be of value. The reviewer mainly concerns about the proposed algorithm.*

Answer: We thank the reviewer for the positive comment.

The comments are as follows:

R1-2: *The feasibility of such scenarios still remains further discussions considering the capital costs of energy storage, interests conflicts of current electrical roles, and the engineering implementations involving such accurate models.*

Answer: We agree with the Reviewer. This work shows how peer-to-peer market scenarios in theory can be beneficial.

R1-3: *The charging and discharging efficiency are not considered in (5), which is sometimes acceptable, but requires explanations.*

Answer: In the first version of the manuscript, we did not consider the charging and discharging efficiency as we assume the simplest model of the storage since component model is not the main focus of this work. However, based on this reviewer comment, we now update the storage dynamics, which include the charging and discharging efficiencies. Therefore, for each storage unit, we consider two decision variables, i.e., the charging and discharging powers. The storage unit is now modeled as follows:

“The battery charging and discharging profiles, $p_i^{\text{ch}} = \text{col}((p_{i,h}^{\text{ch}})_{h \in \mathcal{H}})$ and $p_i^{\text{ds}} = \text{col}((p_{i,h}^{\text{ds}})_{h \in \mathcal{H}})$, respectively, are constrained by the battery dynamics

$$\left. \begin{aligned} x_{i,h+1} &= \eta_i^{\text{st}} x_{i,h} + \frac{T_s}{e_i^{\text{cap}}} (\eta_i^{\text{ch}} p_{i,h}^{\text{ch}} - (\frac{1}{\eta_i^{\text{ds}}}) p_{i,h}^{\text{ds}}), \\ \underline{x}_i &\leq x_{i,h+1} \leq \bar{x}_i, \\ p_i^{\text{ch}} &\in [0, \bar{p}_i^{\text{ch}}], \quad p_i^{\text{ds}} \in [0, \bar{p}_i^{\text{ds}}], \\ p_i^{\text{ch}} &= 0, \quad p_i^{\text{ds}} = 0, \end{aligned} \right\} \begin{aligned} &\forall i \in \mathcal{N}^{\text{st}}, \\ &\forall h \in \mathcal{H}, \\ &\forall i \notin \mathcal{N}^{\text{st}}, \end{aligned} \quad (1)$$

where $x_{i,h}$ denotes the state of charge (SoC) of the storage unit at time $h \in \mathcal{H}$, $\eta_i^{\text{st}}, \eta_i^{\text{ch}}, \eta_i^{\text{ds}} \in (0, 1]$ denote the leakage coefficient of the storage, charging, and discharging efficiencies, respectively, while T_s and e_i^{cap} denote sampling time and maximum capacity of the storage, respectively. Moreover, $\underline{x}_i, \bar{x}_i \in [0, 1]$ denote the minimum and the maximum SoC of the storage unit of prosumer i , respectively, whereas $\bar{p}_i^{\text{ch}} \geq 0$ and $\bar{p}_i^{\text{ds}} \geq 0$ denote the maximum charging and discharging power of the storage unit. Finally, we denote by $\mathcal{N}^{\text{st}} \subseteq \mathcal{N}$ the set of prosumers that own a storage unit.”

We have also modified our game formulation and proposed algorithm in Section III to take into account this storage model update.

R1-4: *The energy loss of the distribution network is also not considered.*

Answer: We do not include energy loss of the distribution network in the current setup and leave it for future work. In this manuscript, we focus on the game-theoretic formulation of the interaction among prosumers and the network operator and show that the problem can be solved efficiently. Based on the formulation in our manuscript, the energy loss can be included as long as it is formulated as [continue depending whether this appears in the cost function or constraints]

R1-5: *The individual variables, coupled relationships for these energy roles, and the corresponding dual variables should be explained specifically, along with the whole framework structure for equilibrium. The rationalities of the framework is not clear. At least, the current presentation is hard to*

follow.

Answer: To be answered!

R1-6: *The P2P trading prices are given parameters, which are quite unreasonable. In fact, the P2P prices are the key variable in most literature.*

Answer: In this manuscript, we want to consider the most general problem formulation available in the literature. Following [Sorin et al., 2019, Cadre et al., 2020, Sousa et al., 2019], a linear trading cost function is introduced in the problem formulation to describe [continue]. Furthermore, [?] also adds a trading tariff encoded as a 1-norm cost function. Furthermore, we may set $c_{\{i,j\}}^{\text{tr}} = 0$, and thus only consider the dual variable associated with the reciprocity constraints (Eq. (xx) in the revised manuscript) as the shadow price of trading. Indeed the proposed algorithm can handle any case where $c_{\{i,j\}}^{\text{tr}} \geq 0$, for all $\{i, j\} \in \mathcal{E}$.

R1-7: *The algorithm requires too many iterations, which leads to poor feasibility in real applications, especially in distributed environment.*

Answer: [for day-ahead or intra-day markets (with sufficiently large sampling time), our numerical experience shows the algorithm is tractable.]

Answers to Reviewer 2

R2-1: *This manuscript proposes a game model for P2P energy trading in a distribution network considering network constraints and the DNO agent. The game model is a generalized game in which agents have coupled objectives and constraints. A distributed algorithm is developed to seek the equilibrium of the game. The topic of this manuscript is interesting, and the presentation is clear in general. The reviewer has some comments on the model and algorithm.*

Answer: We thank the Reviewer for the positive comment.

R2-2: *In common energy storage models, efficiency is usually a coefficient of the charging/discharging power. The storage model in (5) is uncommon as the authors take the efficiency a_i as a coefficient of energy state $x_{i,h}$. In related works (such as (6) in <https://ieeexplore.ieee.org/document/8919970>), the coefficient of energy states is usually called a leakage coefficient, describing energy leakage over time. References may be needed for (5), and please explain in what sense this storage model (5) is practical.*

Answer: We thank the reviewer for raising this point and suggesting the reference. In the first version of the manuscript, we did not consider the charging and discharging efficiency as we assume the simplest model of the storage since component model is not the main focus of this work. However, based on this reviewer comment, we now update the storage dynamics, which include the charging and discharging efficiencies. Therefore, for each storage unit, we consider two decision variables, i.e., the charging and discharging powers. The storage unit is now modeled as follows:

“The battery charging and discharging profiles, $p_i^{\text{ch}} = \text{col}((p_{i,h}^{\text{ch}})_{h \in \mathcal{H}})$ and $p_i^{\text{ds}} = \text{col}((p_{i,h}^{\text{ds}})_{h \in \mathcal{H}})$, respectively, are constrained by the battery dynamics

$$\left. \begin{aligned} x_{i,h+1} &= \eta_i^{\text{st}} x_{i,h} + \frac{T_s}{e_i^{\text{cap}}} (\eta_i^{\text{ch}} p_{i,h}^{\text{ch}} - (\frac{1}{\eta_i^{\text{ds}}}) p_{i,h}^{\text{ds}}), \\ \underline{x}_i &\leq x_{i,h+1} \leq \bar{x}_i, \\ p_i^{\text{ch}} &\in [0, \bar{p}_i^{\text{ch}}], \quad p_i^{\text{ds}} \in [0, \bar{p}_i^{\text{ds}}], \\ p_i^{\text{ch}} &= 0, \quad p_i^{\text{ds}} = 0, \end{aligned} \right\} \begin{aligned} &\forall i \in \mathcal{N}^{\text{st}}, \\ &\forall h \in \mathcal{H}, \\ &\forall i \notin \mathcal{N}^{\text{st}}, \end{aligned} \quad (2)$$

where $x_{i,h}$ denotes the state of charge (SoC) of the storage unit at time $h \in \mathcal{H}$, $\eta_i^{\text{st}}, \eta_i^{\text{ch}}, \eta_i^{\text{ds}} \in (0, 1]$ denote the leakage coefficient of the storage, charging, and discharging efficiencies, respectively, while T_s and e_i^{cap} denote sampling time and maximum capacity of the storage, respectively. Moreover, $\underline{x}_i, \bar{x}_i \in [0, 1]$ denote the minimum and the maximum SoC of the storage unit of prosumer i , respectively, whereas $\bar{p}_i^{\text{ch}} \geq 0$ and $\bar{p}_i^{\text{ds}} \geq 0$ denote the maximum charging and discharging power of the storage unit. Finally, we denote by $\mathcal{N}^{\text{st}} \subseteq \mathcal{N}$ the set of prosumers that own a storage unit.”

We have also modified our game formulation and proposed algorithm in Section III to take into account this storage model update.

R2-3: *In (9), the electricity price is defined to depend on the total consumption. This setting is often used in local energy systems (community or microgrid) but rarely used in wide-area energy networks (distribution networks). In real situations, the electricity prices in a power network are different at different buses and are determined by generation costs, power line congestion, power loss, etc. The reviewer understands that the authors deliberately use (9) to make the agents’ objectives coupled with each other. But the authors must explain why (9) is practical in the proposed model.*

Answer: [Wicak] [check price formulation in distribution networks]

R2-4: *In the proposed model, the DNO is considered a game player. This setting is also used in some other related works (such as <https://ieeexplore.ieee.org/document/9223743>). The authors may need a more comprehensive review on this aspect.*

Answer: [improve literature survey]

R2-5: *The property of the game equilibrium is not clear enough. It is unclear what is the difference between v-GNE and GNE. The authors may need to formally (mathematically) define the variational GNE that the proposed game will reach.*

Answer: [add explanation about v-GNE]

R2-6: *Algorithm 1 looks unfriendly to readers. The explanation for the algorithm (section III-A) is also unclear. In this current version, readers may have no clue to follow the formulation/notations in the algorithm and Fig. 2. For example, what are the dual variables used for? What is the intuitive idea behind the algorithm? What are the step sizes used for? The authors are suggested to separate Algorithm 1 into several parts and explain each part.*

Answer: [Improve explanation of algorithm 1. Apply comments.]

Answers to Reviewer 3

This paper presents an interesting work dealing with the clearing of P2P energy markets while also considering technical constraints of the distribution network. From my point of view, some issues need to be further clarified:

R3-1: *Papers dealing with P2P markets are quite numerous recently. Literature review section is well structured and provides a fair number of works in this area, however the research gaps are not clearly stated. As a consequence, the contributions of the paper are quite generic. Please, consider to state, in a more specific way, the contributions of the paper. In particular, why the GNE approach is advantageous with respect to other decentralized frameworks proposed in the literature.*

Answer: [rephrase research gaps]

R3-2: *From the modeling point of view, a linear approximation of the power-flow is considered. It is known that this approximation is weak in distribution systems. I would suggest to include some references and analysis of convex approximations, if any, that might be compatible with the Assumption 1 of this paper.*

Answer: We agree with the assessment of the Reviewer on the linear approximation of the power flow equations. Based on Assumption 1, nonlinear but convex approximation of the power flow equations such as a second order cone programming or semi-definite programming relaxation as discussed in [Molzahn et al., 2017, Sect. II-A] can be considered instead of a linear one. Furthermore, since the power flow constraints are handled fully by the distribution network operator, a reformulation of these constraints does not require any modification of Algorithm 1 but only on the local constraint set of the DNO, i.e., \mathcal{U}_{N+1} . In this regard, the ad-hoc algorithm that we proposed to perform the projection onto \mathcal{U}_{N+1} must be adjusted accordingly. We leave out the task of improving the model as future work as this is not the focus and contribution of this work. Furthermore, as suggested by the reviewer, we have modified Remark 1 based on the preceding explanation:

“... remain satisfied. In addition, instead of considering linear power flow equations in (14), a nonlinear convex relaxation, such as a second order cone or semi-definite programming as discussed in [Molzahn et al., 2017, Sect. II-A] can be considered since it still satisfies Assumption 1. In this case, only the definition of \mathcal{U}_{N+1} differs from the current formulation.”

R3-3: *As well pointed by the authors, this is a semi-decentralized approach where a coordinator is needed. Please, provide some discussion on how this is different with community-based local markets.*

Answer: As discussed in [Sousa et al., 2019, Sect. 3.2], in community-based local markets, each prosumer does not know with which other prosumers it trades energy. The power balance of the whole network (all prosumers) is considered. Our setup considers full P2P markets where each prosumer knows its trading partners and, thus, negotiates directly with them. The coordinator in our setup plays a role in handling the physical constraints of the network as well as the aggregated power bought from the main grid.

R3-4: *The proposed algorithm relies on several dual variables. Please, elaborate on the meaning of this dual variables and their interpretation as economic outputs of the clearing process.*

Answer: [apply comment]

R3-5: *As to the results section, I miss some analysis of trading prices. Please consider to add some information about transactions prices among peers and compare them with grid prices. This analysis might be interesting in both storage and non-storage situations.*

Answer: [apply comment]

R3-6: *Please, check Figure 7. The authors claim that storage help in shaving the peak of total power*

imported from the main grid, but this looks the same in both figures.

Answer: We thank the Reviewer for providing this observation. What we claim is that the storage shaves the peak of the sum of the total power imported from the main grid and that of locally generated power. Indeed, due to the choice of the cost parameters, which follows [Atzeni et al., 2013], local generation costs are cheaper than importing cost. We have redone the simulations where we readjust the cost parameters and introduce a positive quadratic coefficient on f_i^{di} . Due to this adjustment, we can now see in Figure xx in the revised manuscript (as also shown below) that the storage particularly shaves the peak of total power imported from the main grid. [\[show the new figure\]](#)

R3-7: *As a conclusion, the paper presents an interesting mathematical approach for clearing P2P markets. On the another hand, some relevant topics in this area remain uncovered and highlighted as future work. All in all, in my opinion, is a very good work, and should be considered for publication if the issues raised during revision are handled.*

Answer: We thank the Reviewer for the positive comment and recommendation.

Answers to Reviewer 4

This paper presents a mathematical model for a P2P energy market formulated as a generalized game. They introduce in the game a new agent, a Distribution Network Operator (DNO), who is responsible of ensure the operational constraints of the market. Further, they propose a semi-decentralized algorithm to solve the problem, ensuring convergence to a Nash equilibrium. Finally, a numerical study is used to show the relevance of the market framework and the scalability of the algorithm.

R4-1: *In my opinion, the paper is clearly written, with a detailed explanation of the mathematical aspects, and introduces some relevant results. However, some questions need to be addressed in order to improve the quality of the work.*

Answer: We thank the Reviewer for the positive comment.

Comments and suggestions:

R4-2: *The authors state that due to the presence of coupling objective and constraints in the formulation, this implies the inapplicability of other decentralized algorithms employed in the literature (lines 54-57, page 2). This is not strictly true, since it is straightforward to reformulate the problem to decompose the objective function, just by replicating the variables avoiding the decomposition, and introduce new complicating constraints to coordinate these variables. Reformulate this sentence.*

Answer: [rephrase sentence. Not as straightforward.]

R4-3: *In the introduction, the authors assert that they extend a preliminary work by including nonlinear operational constraints, which complicate the analysis. However, they consider a linear approximation of power-flow equations (equations (13)). In fact, it seems that the only nonlinear constraint in the model is (15a), although some quadratic terms appear in the objective function. Is there any justification for this? Probably, the statement must be relaxed.*

Answer: [Wicak] [apply comment]

R4-4: *Related to the previous comment, one of the nonlinearities appears in the objective function related to dispatchable units (equation (2)). However, in the numerical studies the parameter Q_i^{di} is taken as zero, becoming a linear objective function, and simplifying the model. The same happens with the objective function associated to storage units (equation (4)). Have you tested the effect of these parameters in the model? Further, if these parameters take a positive value, some of the conclusions presented in the numerical study could change. I suggest the authors to analyze this issue.*

Answer: [Wicak] [nonlinear objective function is not an issue. Show simulation results here when we have strongly convex cost of storage and dispatchable units. We follow existing paper for the parameters of problem.]

R4-5: *The objective function associated to the power traded with the main grid seems not so natural. If the electricity unit price, c_h^{mg} in equation (9) is considered linear (instead of quadratic) with respect to the total consumption, this would simplify this term, further becoming (11) a decomposable function. Could the authors elaborate what is the advantage of using a quadratic term here? Is worth the improvement it could add with respect to the difficulty it brings to the model?*

Answer: [Wicak] [correspond to linear inverse demand function]

R4-6: *Taking into account comment 1, suppose that we consider a reformulation of the problem to avoid coupling objective functions, and we employ the Alternating Direction Methods of Multipliers (ADMM) to solve the P2P market game in (1). Could the authors elaborate if this would be possible? Would the application of the ADDM also guarantees the convergence to a variational GNE of the P2P market game? What are the advantages of using Algorithm 1 proposed in the paper to solve the problem?*

Answer: To be answered!

R4-7: *Regarding to the scalability of the algorithms, the author evaluates the convergence of the algorithm with respect to the number of agents and the connectivity, but they do not provide any information about the computational times. This is relevant to evaluate if it could be applied in a real large-scale system.*

Answer: We thank the Reviewer for raising this point. We agree that the computational time is relevant in practice and thus we have added the plots of the total computational time/agent in the scalability test section (Figure xx in the revised manuscript as also shown below). Since at each iteration, each agent only needs to update its own decision variable and some dual variables associated with the coupling constraints, we can see that the total computational time/agent is relatively low as the day-ahead problem is only solved once per day. [show the new figure]

R4-8: *Given a prosumer i , when Algorithm 1 is applied, in order to update the dual variable related to reciprocity constraints, the value of the power traded with neighbors plays an important role. In detail, I mean $\{p_{(j,i)}^{tr}\}_{j \in \mathcal{N}_i}$, the forward trade estimate to prosumer i . It seems that, depending on the order the prosumers are considered, the coordination of these variables could change, so that the convergence of the algorithm. Hence, it could be interesting to analyze how this affect to the behavior of the algorithm. For example, could it benefit to consider first prosumers with less neighbors, since maybe they reach faster an equilibrium?*

Answer: [prosumers update in parallel, not sequentially.]

Minor comments:

R4-9: *The notation used to define the quadratic terms of the objective functions must be introduced previously as “Basic notation”.*

Answer: We thank the reviewer for this suggestion and we have introduced the notation as follows:

“Given $x \in \mathbb{R}^n$, $\|x\|_A^2 = x^\top A x$, with square matrix $A \succ 0$.”

R4-10: *The references to the lines of Algorithm 1 (in page 7) appearing in the text must be revised. For example, in item (iv) of Remark 2 (page 6), it must appear “....(lines: 28-31)”. In the box related to dual variable update of prosumer i , in Figure 2 (page 6), the line references must be: lines 19-24.*

Answer: We thank the reviewer for noticing this errors and we have updated the references to the lines of Algorithm 1 in Remark 2 and Figure 2.

References

- [Atzeni et al., 2013] Atzeni, I., Ordóñez, L. G., Scutari, G., Palomar, D. P., and Fonollosa, J. R. (2013). Demand-side management via distributed energy generation and storage optimization. *IEEE Transactions on Smart Grid*, 4(2):866–876.
- [Cadre et al., 2020] Cadre, H. L., Jacquot, P., Wan, C., and Alasseur, C. (2020). Peer-to-peer electricity market analysis: From variational to generalized Nash equilibrium. *European Journal of Operational Research*, 282(2):753–771.
- [Molzahn et al., 2017] Molzahn, D. K., Dörfler, F., Sandberg, H., Low, S. H., Chakrabarti, S., Baldick, R., and Lavaei, J. (2017). A survey of distributed optimization and control algorithms for electric power systems. *IEEE Transactions on Smart Grid*, 8(6):2941–2962.
- [Sorin et al., 2019] Sorin, E., Bobo, L., and Pinson, P. (2019). Consensus-based approach to peer-to-peer electricity markets with product differentiation. *IEEE Transactions on Power Systems*,

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[Sousa et al., 2019] Sousa, T., Soares, T., Pinson, P., Moret, F., Baroche, T., and Sorin, E. (2019). Peer-to-peer and community-based markets: A comprehensive review. *Renewable and Sustainable Energy Reviews*, 104:367–378.