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## Review Article

# List Decoding of Generalized Reed-Solomon Codes by Using a Modified Extended Key Equation Algorithm

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This work presents a modified extended key equation algorithm in list decoding of generalized Reed-Solomon (GRS) codes. A list decoding algorithm of generalized Reed-Solomon codes has two steps, interpolation and factorization. The extended key equation algorithm (EKE) is an interpolation-based approach with a lower complexity than Sudan's algorithm. To increase the decoding speed, this work proposes a modified EKE algorithm to perform codeword checking prior to such an interpolation process. Since the evaluation mapping is engaged in encoding, a codeword is not generated systematically. Thus, the transmission information is not directly obtained from a received codeword. Therefore, the proposed algorithm undertakes a matrix operation to obtain the transmission information once a received vector has been checked to be error-free. Simulation results demonstrate that the modified EKE algorithm in list decoding of a GRS code provides low complexity, particularly at high signal-to-noise ratios.

## 1. Introduction

Reed-Solomon (RS) codes are currently used in a wide variety of applications, ranging from data storage systems, mobile communications, to satellite communications. The third-generation (3G) wireless standard utilizes RS codes as outer codes. For CDMA2000 high-rate broadcast packet data air interface [1], they are expected to be adopted as outer codes in concatenated coding schemes for future fourth-generation (4G) wireless systems.

Algorithms for hard decision decoding of RS codes are typically classified into two well-known types, namely, syndrome-based decoding and interpolation-based decoding. Well-developed algorithms in the first category include the Peterson-Gorenstein-Zierler algorithm [2], Berlekamp-Massey algorithm [2, 3], Euclidean algorithm [2, 3], frequency domain algorithm [2, 3], and step-by-step algorithm [4–7]. Algorithms in the second category include the Welch-Berlekamp algorithms [8, 9] and list decoding algorithms

[10–12], as Koetter-Vardy algorithm [13] is also a list decoding algorithm but with soft decision approaching.

Sudan's algorithm [10] decodes GRS codes in two steps involved, namely, interpolation and factorization. An interpolation is performed on a received word  $\bar{r} = (r_0, r_1, \dots, r_{n-1})$ , producing a nonzero bivariate polynomial  $Q(x, y) = \sum_{t=0}^l Q^{(t)}(x)y^t = \sum_{i=0}^n a_i \phi(x, y)$  with at least  $n - \tau$  points  $(\alpha^i, r_i)$ , such that  $Q(\alpha^i, r_i) = 0$  and  $i \in [n - 1] = \{0, 1, \dots, n - 1\}$ . Factorization is then performed on  $Q(x, y)$ , yielding linear factors (or called  $y$ -root polynomials)  $y - f(x)$ . The codewords are then generated from these distinct factors  $f(x)$  via an evaluation mapping. A decoded codeword  $\bar{c}^*$  is chosen if the Hamming distance between  $\bar{c}^*$  and  $\bar{r}$  is  $\tau$  or less.

Because solving these interpolation equations of Sudan's algorithm with a naïve Gaussian elimination requires the time complexity  $O(n^3)$ , an EKE algorithm has been presented to decrease this complexity [12]. The EKE algorithm employs generalized Berlekamp-Massey algorithm (or the Feng-Tzeng algorithm in [14]) that obtains the shortest recurrence that

generates a given sequence, and the time complexity of EKE to solve these interpolation equations is  $O(l(n-k)^2)$ .  $l$  represents a design parameter, typically a small constant, which is an upper bound on the size of the list of decoded codewords.

Guruswami and Sudan (GS) presented an improvement on Sudan's algorithm [11], by introducing a multiplicity  $u$  at each interpolation point. A nonzero  $Q(x, y)$  polynomial exists that interpolates the points  $(x_i, y_i)$ ,  $i \in [n-1]$  with multiplicity  $u$ , and is formed by  $Q(x, y) = \sum_{i=0}^c a_i \phi(x, y)$ , where  $c = n \binom{u+1}{2}$ , and the expression of  $\binom{I}{J}$  denotes the number of ways to choose  $J$  from  $I$ . In comparison with Sudan's work, the GS algorithm provides more  $n \binom{u+1}{2} - n$  linear homogeneous equations in interpolation, thus improving the decoding correction distance. Increasing  $u$  improves the decoding performance but also increases the required complexity. The asymptotical decoding correction fraction is given by  $1 - \sqrt{R}$ , and the code rate  $R$  is given by  $R = k/n$ . The increase in decoding capability is substantial, especially for low-rate GRS codes.

Koetter and Vardy [13] extended the GS algorithm by incorporating the soft information received from a channel into the interpolation process. With a complexity that is a polynomial of the code length, the Koetter-Vardy (KV) algorithm can achieve a substantial coding gain over the GS algorithm. For instance, at a frame-error-rate (FER) of  $10^{-5}$ , the KV algorithm can achieve a coding gain of about 1 dB over the GS algorithm, for a (255, 144) GRS code transmitted over an additive white Gaussian noise (AWGN) channel using 256-QAM modulation [13].

However, those approaches have a drawback, that is codeword checking is absent during decoding. In other words, regardless of whether the received sequence is correct or not, the decoding algorithm proceeds to decode it. This work overcomes this drawback by presenting a modified EKE algorithm with codeword checking. Additionally, a matrix operation is also proposed to obtain the transmission information from the received codeword. As in syndrome-based decoding, if the syndrome vector is all-zero, then the decoding process is terminated and the received sequence is output as a decoded codeword. The rest of this paper is organized as follows. Section 2 introduces the EKE algorithm. Section 3 then presents the modified EKE algorithm with the proposed codeword checking method and the matrix operation to obtain the transmission information from the received codeword. Finally, simulations and conclusions are presented in Section 4.

## 2. Extended Key Equation Algorithm

Consider an evaluation mapping  $f(x) = m_0 + m_1x + \dots + m_{k-1}x^{k-1}$  and  $n = 2^m - 1$ . A codeword in an  $[n, k]$  GRS code over  $\text{GF}(2^m)$  is generated as

$$\begin{aligned} \bar{c} &= (c_0, c_1, \dots, c_{n-1}) \\ &= (f(\alpha^0), f(\alpha), \dots, f(\alpha^{n-1})) \end{aligned}$$

$$\begin{aligned} &= (m_0, m_1, \dots, m_{k-1}) \begin{pmatrix} 1 & 1 & \dots & 1 \\ 1 & \alpha & \dots & \alpha^{n-1} \\ \vdots & \vdots & \dots & \vdots \\ 1 & \alpha^{k-1} & \dots & \alpha^{(n-1)(k-1)} \end{pmatrix} \\ &= \bar{m} \cdot \mathbf{G}, \end{aligned} \quad (1)$$

where the information vector is  $\bar{m} = (m_0, m_1, \dots, m_{k-1})$ , the generator matrix is

$$\mathbf{G} = \begin{pmatrix} 1 & 1 & \dots & 1 \\ 1 & \alpha & \dots & \alpha^{n-1} \\ \vdots & \vdots & \dots & \vdots \\ 1 & \alpha^{k-1} & \dots & \alpha^{(n-1)(k-1)} \end{pmatrix}, \quad (2)$$

and  $\alpha$  is a primitive element in  $\text{GF}(2^m)$ .

The term  $l$  is the upper bound of the number of consistent codewords, which are at Hamming distance  $\leq \tau$  from any received word. For an  $(n, k)$  GRS code, Sudan's algorithm corrects any error pattern of up to  $\tau$  errors for

$$\tau = n - (h+1) - l(k-1), \quad (3)$$

where  $h$  denotes the smallest nonnegative integer holding the following equation:

$$(h+1)(l+1) + (k-1) \binom{l+1}{2} > n. \quad (4)$$

Assuming that  $k \leq (n+1)/3$ , the value of  $\tau$  becomes

$$\tau = \left\lfloor \frac{2(n+1)}{3} \right\rfloor - k. \quad (5)$$

Let  $F$  be a field, and let  $F_k[x]$  represent the set of all polynomials of degree  $< k$  in the variable  $x$  over  $F$ . Sudan's algorithm consists of the following steps.

- (1) Find a nonzero bivariate polynomial  $Q(x, y)$  over  $F$  with at least  $n - \tau$  points  $(\alpha^i, r_i)$ , such that  $Q(\alpha^i, r_i) = 0$  and  $i \in [n-1]$ , for a received vector  $\bar{r} = (r_0, r_1, \dots, r_{n-1})$ .
- (2) Output all polynomials  $f(x) \in F_k[x]$  for which  $y - f(x)$  is a factor of  $Q(x, y)$  and  $f(\alpha^i) = r_i$  for at least  $n - \tau$  locators  $\alpha^i$ .

In [2, 3], for an  $(n, k)$  RS code, the error-locator polynomial  $\Lambda(x)$  and the error-evaluator polynomial  $\Omega(x)$  are computed in the following key equation (KE):

$$\Lambda(x) \cdot S(x) \equiv \Omega(x) \pmod{x^{n-k}}. \quad (6)$$

In [12], based on the linear factors of bivariate polynomials  $Q(x, y)$  where the polynomial arithmetic is carried out

modulo a power of  $x$  in Sudan's algorithm, an EKE algorithm is derived as follows:

$$\sum_{t=1}^l \Lambda^{(t)}(x) x^{(t-1)(k-1)} \cdot S^{(t)}(x) \equiv \Omega(x) \pmod{x^{n-k}}, \quad (7)$$

where  $\Lambda^{(t)}(x)$ ,  $t \in \{1, 2, \dots, l\}$ , and  $\Omega(x)$  are polynomials that satisfy certain degree constraints and  $S^{(t)}(x)$  are syndrome polynomials computed as follows:

$$S^{(t)}(x) = \sum_{i=0}^{n-2-t(k-1)} S_i^{(t)} x^i, \quad S_i^{(t)} = \sum_{j=0}^{n-1} r_j^t \eta_j \alpha^{i \cdot j}, \quad (8)$$

$$\eta_j^{-1} = \prod_{\gamma \in [n-1] \setminus \{j\}} (\alpha^j - \alpha^\gamma). \quad (9)$$

Furthermore, the above equation can be obtained as follows:

$$\sum_{t=1}^l \sum_{s=0}^{N_t-1} Q_s^{(t)} S_{i+s}^{(t)} = 0, \quad 0 \leq i < \tau, \quad (10)$$

which is denoted as

$$\begin{pmatrix} S_0^{(1)} & \dots & S_{N_1-1}^{(1)} & S_0^{(2)} & \dots & S_{N_1-1}^{(2)} \\ S_1^{(1)} & \dots & S_{N_1}^{(1)} & S_1^{(2)} & \dots & S_{N_1}^{(2)} \\ \vdots & & \vdots & \vdots & & \vdots \\ S_\tau^{(1)} & \dots & S_{N_1+\tau-1}^{(1)} & S_\tau^{(2)} & \dots & S_{N_1+\tau-1}^{(2)} \end{pmatrix} \cdot \begin{pmatrix} Q_0^{(1)} \\ \vdots \\ Q_{N_1-1}^{(1)} \\ Q_0^{(2)} \\ \vdots \\ Q_{N_1-1}^{(2)} \end{pmatrix} = \begin{pmatrix} 0 \\ \vdots \\ 0 \end{pmatrix}. \quad (11)$$

Let

$$Q^{(t)}(x) = \sum_{s=0}^{N_t-1} Q_s^{(t)} x^s, \quad (12)$$

where  $N_t = n - \tau - t(k-1)$  and  $t \in \{1, 2, \dots, l\}$ . After these polynomials  $Q^{(t)}(x)$ ,  $t \in \{1, 2, \dots, l\}$ , have been computed in (11) by using the Feng-Tzeng algorithms [14] or a similar algorithm mentioned in [12], the polynomial  $Q^{(0)}(x)$  is obtained as follows:

$$Q^{(0)}(x) + \sum_{t=1}^l Q^{(t)}(x) y^t = Q(x, y) \quad (13)$$

and satisfies

$$Q^{(0)}(\alpha^j) = - \sum_{t=1}^l Q^{(t)}(\alpha^j) r_j^t, \quad j \in [n-1]. \quad (14)$$

A design parameter  $l$  in [12] is an upper bound on the size of the list of decoded codewords. For code rate  $R \leq 1/3$ , from (4), the value of  $l$  is determined by the following range:

$$\frac{2n - 2\tau - k + 1 - \sqrt{(2n - 2\tau - k + 1)^2 - 8\tau(k-1)}}{2(k-1)} < l < \frac{2n - 2\tau - k + 1 + \sqrt{(2n - 2\tau - k + 1)^2 - 8\tau(k-1)}}{2(k-1)}. \quad (15)$$

The EKE algorithm employs the Feng-Tzeng algorithm [14] to decode GRS codes. The dimensions of the  $S$ -matrix in (11) are  $\tau$  by  $l(n - \tau - (k-1)(l+1)/2)$ . Since the Feng-Tzeng algorithm is run column by column in a matrix, therefore the column length dominates the decoding complexity. Reducing the column length lowers the complexity of locating the smallest set of linear dependent coefficients. The algorithm of [12] requires the solving of  $\tau$  homogeneous linear equations in (11) and then finding the corresponding coefficients of  $Q^{(0)}(x)$  in (14). Hence, the time complexity is  $O(l(n-k)^2)$ , which is less than the time complexity of  $O(n^3)$  of Sudan's algorithm. Consequently, the EKE algorithm is more attractive than the algorithm of [10].

### 3. Modified Extended Key Equation Algorithm

Since the polynomial  $f(x) = \sum_{i=0}^{n-1} m_i x^i$  is associated with a codeword  $\bar{c} \in C$ , which has zeros  $1, \alpha, \alpha^2, \dots, \alpha^{n-k}$  [15], a parity-check matrix for  $C$  is given by [16, 17]

$$\mathbf{H} = \begin{pmatrix} 1 & \alpha & \dots & \alpha^{n-1} \\ 1 & \alpha^2 & \dots & \alpha^{2(n-1)} \\ \vdots & & \dots & \vdots \\ 1 & \alpha^{n-k} & \dots & \alpha^{(n-k)(n-1)} \end{pmatrix}. \quad (16)$$

**Theorem 1.** For a received vector  $\bar{r} = (r_0, r_1, \dots, r_{n-1})$ , codeword checking  $\bar{w}$  is equal to the computation of  $\bar{S}^{(1)}$ , which is

$$\begin{aligned} \bar{w} &= (w_0, w_1, \dots, w_{n-k-1}) \\ &= \bar{r} \cdot \mathbf{H}^T \\ &= \bar{S}^{(1)}, \end{aligned} \quad (17)$$

where  $T$  denotes the matrix transpose.

*Proof.* For computing the value of  $\eta_j$  in (9), a different element  $\gamma \in [n-1] \setminus \{j\}$  should yield a different result for  $\alpha^j - \alpha^\gamma$ . Consequently, the value of  $\prod_{\gamma \in [n-1] \setminus \{j\}} (\alpha^j - \alpha^\gamma)$  can be simplified as

$$\begin{aligned} \prod_{\gamma \in [n-1] \setminus \{j\}} (\alpha^j - \alpha^\gamma) &= \frac{\prod_{s \in [n-1] \setminus \{j\}} \alpha^s}{\alpha^j} \\ &= \alpha^{n(n-1)/2-j} \\ &= \alpha^{-j}. \end{aligned} \quad (18)$$

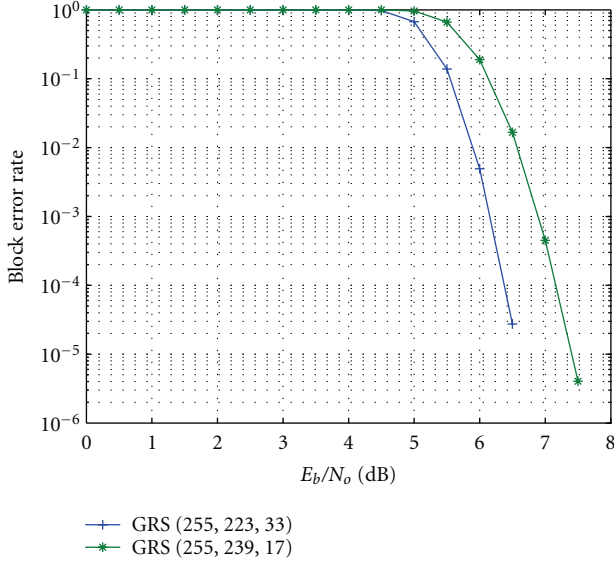


FIGURE 1: Performance of listing decoding with the modified EKE algorithm, when a (255, 233, 33) GRS code and a (255, 239, 17) GRS code are transmitted with BPSK signaling over AWQN channels.

Equation (9) becomes

$$\eta_j = \alpha^j. \quad (19)$$

For the vector  $\bar{S}^{(1)} = (S_0^{(1)}, S_1^{(1)}, \dots, S_{n-k-1}^{(1)})$ , the calculation of each  $S_i^{(1)}$  can be denoted as follows:

$$S_i^{(1)} = \sum_{j=0}^{n-1} r_j \alpha^{(i+1) \cdot j}, \quad (20)$$

and the vector  $\bar{S}^{(1)}$  becomes

$$\begin{aligned} \bar{S}^{(1)} &= (S_0^{(1)}, S_1^{(1)}, \dots, S_{n-k-1}^{(1)}) \\ &= (r_0, r_1, \dots, r_{n-1}) \cdot \begin{pmatrix} 1 & 1 & \dots & 1 \\ \alpha & \alpha^2 & \dots & \alpha^{n-k} \\ \vdots & \dots & \vdots & \\ \alpha^{n-1} & \alpha^{2(n-1)} & \dots & \alpha^{(n-k)(n-1)} \end{pmatrix} \\ &= \bar{r} \cdot \mathbf{H}^T. \end{aligned} \quad (21)$$

□

**Theorem 2.** The codeword checking  $\bar{w}$  is checked to be all-zero, and then the transmission message is given by

$$\bar{m} = \bar{m}' \cdot \mathbf{M}, \quad (22)$$

where  $\bar{m}'$  is the last  $k$ -tuple of  $\bar{r}$  and  $\mathbf{M}$  is a  $k \times k$  matrix such that  $\mathbf{G}' = \mathbf{M} \cdot \mathbf{G}$  is a systematical matrix.

*Proof.* The proof is quite trivial. In the expression of (1),

$$\begin{aligned} \bar{c} &= \bar{m} \cdot \mathbf{G} \\ &= \bar{m} \mathbf{M}^{-1} \cdot \mathbf{M} \mathbf{G} \\ &= \bar{m}' \cdot \mathbf{G}'. \end{aligned} \quad (23)$$

Then,

$$\bar{m} = \bar{m}' \cdot \mathbf{M}. \quad (24)$$

□

*Example 1.* For a (7, 3) GRS code over  $\text{GF}(2^3)$  generated by the polynomial  $p(X) = 1 + X + X^3$ , a codeword  $\bar{v} = (1, \alpha^6, \alpha^5, \alpha^5, 1, \alpha^3, \alpha^6)$  is given by the evaluation mapping provided as the transmission message  $\bar{m} = (\alpha^3, \alpha^2, \alpha^4)$ . If the codeword is transmitted over an error-free channel, then  $\bar{S}^{(1)}$  is checked to be all-zero by (17) and the transmission message is computed by (22) as follows:

$$\begin{aligned} \bar{m} &= \bar{m}' \mathbf{M} \\ &= (1 \quad \alpha^3 \quad \alpha^6) \cdot \begin{pmatrix} \alpha & \alpha^5 & \alpha^4 \\ \alpha^2 & \alpha^2 & \alpha^6 \\ \alpha^5 & \alpha^3 & \alpha^3 \end{pmatrix} \\ &= (\alpha^3 \quad \alpha^2 \quad \alpha^4), \end{aligned} \quad (25)$$

where

$$\begin{aligned} \mathbf{M} &= \begin{pmatrix} \alpha & \alpha^5 & \alpha^4 \\ \alpha^2 & \alpha^2 & \alpha^6 \\ \alpha^5 & \alpha^3 & \alpha^3 \end{pmatrix}, \\ \mathbf{G} &= \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & \alpha & \alpha^2 & \alpha^3 & \alpha^4 & \alpha^5 & \alpha^6 \\ 1 & \alpha^2 & \alpha^4 & \alpha^6 & \alpha & \alpha^3 & \alpha^5 \end{pmatrix}, \\ \mathbf{G}' &= \mathbf{M} \cdot \mathbf{G} = \begin{pmatrix} \alpha^3 & \alpha & 1 & \alpha^3 & 1 & 0 & 0 \\ \alpha^6 & \alpha^6 & 1 & \alpha^2 & 0 & 1 & 0 \\ \alpha^5 & \alpha^4 & 1 & \alpha^4 & 0 & 0 & 1 \end{pmatrix}. \end{aligned} \quad (26)$$

With the above theorems, the list decoding algorithm [12] of an  $[n, k]$  GRS code is adjusted as follows.

- (1) Perform codeword-checking,  $\bar{S}^{(1)} = \bar{r} \mathbf{H}^T$ , for a received vector  $\bar{r} = (r_0, r_1, \dots, r_{n-1})$ . If  $\bar{S}^{(1)}$  is an all-zero vector, then output the corresponding message vector  $\bar{m}$  determined as  $\bar{m} = \bar{m}' \cdot \mathbf{M}$ , where a vector  $\bar{m}'$  is the last  $k$ -tuple of  $\bar{r}$ . Then, go to step 5.
- (2) Perform the EKE interpolation:
  - (a) compute the syndrome polynomials in parallel:  $S^{(t)}(x) = \sum_{i=0}^{n-2-t(k-1)} S_i^{(t)} x^i$  and  $S_i^{(t)} = \sum_{j=0}^{n-1} r_j^t \alpha^{(i+1)j}$  and  $t \in \{2, \dots, l\}$ ,

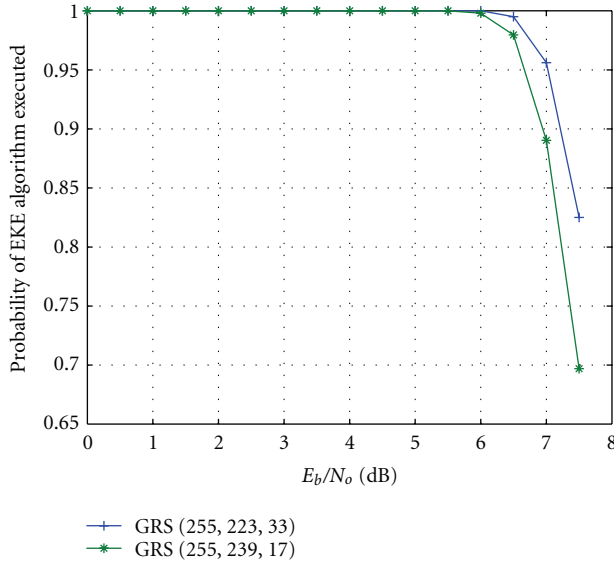


FIGURE 2: Probability of the EKE algorithm in listing decoding, when a (255, 233, 33) GRS code and a (255, 239, 17) GRS code are transmitted with BPSK signaling over AWGN channels.

- (b) find polynomial polynomials  $Q^{(t)}(x) = \sum_{s=0}^{N_t-1} Q_s^{(t)} x^s$ , where  $t \in \{1, \dots, l\}$ , by the Feng-Tzeng algorithm such that  $\sum_{s=0}^{N_t-1} Q_s^{(t)} S_{i+s}^{(t)} = 0$ ,  $0 \leq i < \tau$ ,
  - (c) form the bivariate polynomial  $Q(x, y) = \sum_{t=0}^l Q^{(t)}(x) y^t$ , and then obtain the polynomial  $Q^{(0)}(x)$  satisfying  $Q^{(0)}(\alpha^j) = -\sum_{t=1}^l Q^{(t)}(\alpha^j) r_j^t$ ,  $j \in [n-1]$ .
- (3) Perform the factorization on the bivariate polynomial  $Q(x, y) = \sum_{t=0}^l Q^{(t)}(x) y^t$  by employing the reconstruction algorithm [12] to find the  $y$ -root polynomials  $f(x) = m_0 + m_1 x + \dots + m_{k-1} x^{k-1}$ .
  - (4) Generate the corresponding codeword  $\bar{\tau} = (f(1), f(\alpha), \dots, f(\alpha^{n-1}))$  for each polynomial  $f(x)$ . Output the message vectors  $\bar{m}^* = (m_0^*, m_1^*, \dots, m_{k-1}^*)$  of the codewords  $\bar{\tau}^*$  with the Hamming distance to  $\bar{\tau}$  equal to  $\tau$  or less.
  - (5) Terminate decoding

#### 4. Simulations and Conclusions

Figure 1 displays the decoding performance of listing decoding [12] with the modified EKE algorithm as a (255, 223, 33) GRS code and a (255, 239, 17) GRS code are transmitted with BPSK signaling over AWGN channels. Figure 2 illustrates the probability of the EKE algorithm being executed in such a listing decoding. Those simulations demonstrate that codeword checking has little effect on decoding at low signal-to-noise ratios. However, the modified EKE algorithm provides lower decoding complexity when the signal-to-noise is high. At a block error rate (BER) of  $10^{-5}$ , the probabilities of the EKE algorithm being utilized in list decoding of these two GRS codes are 0.98 and 0.75, respectively. This work presents

a modified EKE algorithm, incorporating codeword checking and a matrix operation, which obtains the transmission information from the received codeword. The computation of codeword checking does not increase the complexity of the original EKE algorithm, because it is an item in the original decoding process. The proposed EKE algorithm is beneficial when the signal-to-noise ratio is high.

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- Image and multidimensional signal processing.
- Signal detection and estimation.
- Sensor array and multi-channel signal processing.
- Sensor fusion in networked systems.
- Signal processing for communications.
- Medical imaging and image analysis.
- Non-stationary, non-linear and non-Gaussian signal processing.

## Submissions

Procedures to submit a paper and proposals for special sessions and tutorials will be detailed at [www.eusipco2011.org](http://www.eusipco2011.org). Submitted papers must be camera-ready, no more than 5 pages long, and conforming to the standard specified on the EUSIPCO 2011 web site. First authors who are registered students can participate in the best student paper competition.

## Important Deadlines:



Proposals for special sessions	15 Dec 2010
Proposals for tutorials	18 Feb 2011
<b>Electronic submission of full papers</b>	<b>21 Feb 2011</b>
Notification of acceptance	23 May 2011
Submission of camera-ready papers	6 Jun 2011

Webpage: [www.eusipco2011.org](http://www.eusipco2011.org)

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