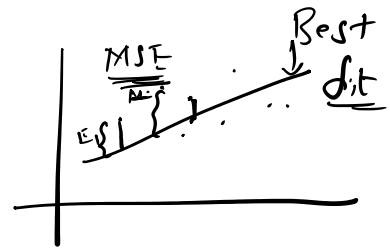


Linear Regression :- Cost function of linear Regression  
is MSE

$$\underline{\underline{MSE}} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

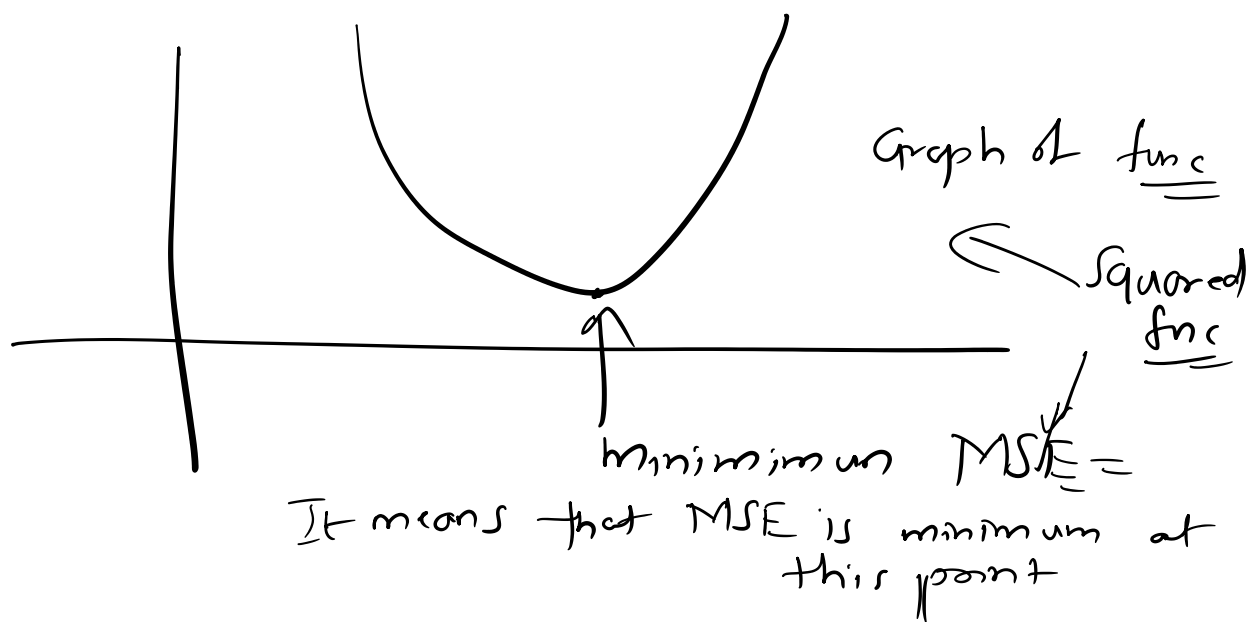
constant  $\leftarrow$   $\underbrace{\quad\quad\quad}_{\text{Squared function.}}$



Goal of LR is to minimize the cost function  
which is the Mean Squared Error.

When I say, I want to minimize the MSE,  
It means that I want to find the minimum  
value of MSE.

## Graph of MSE :-



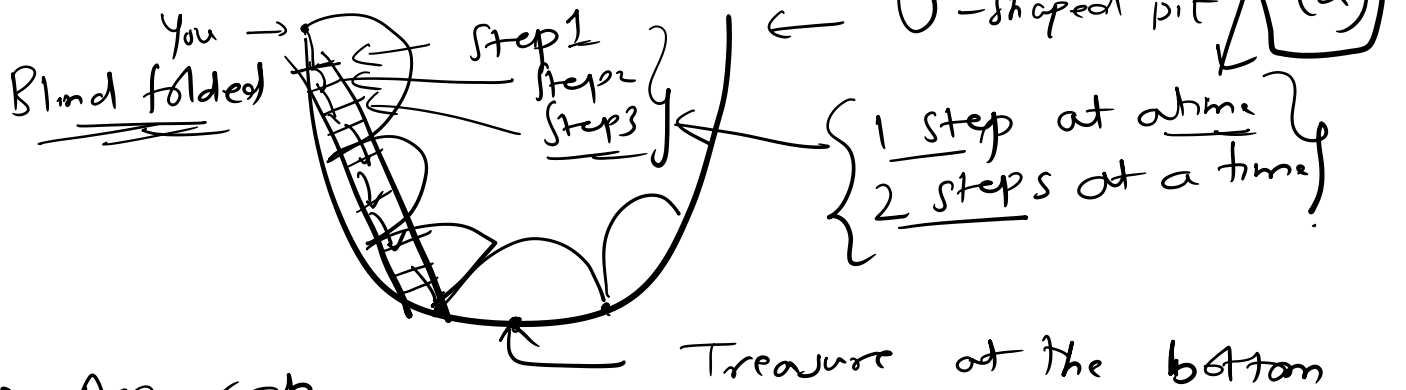
Q. How to reach the minimum point ?

If I want to reach min point there is a  
step by step process.



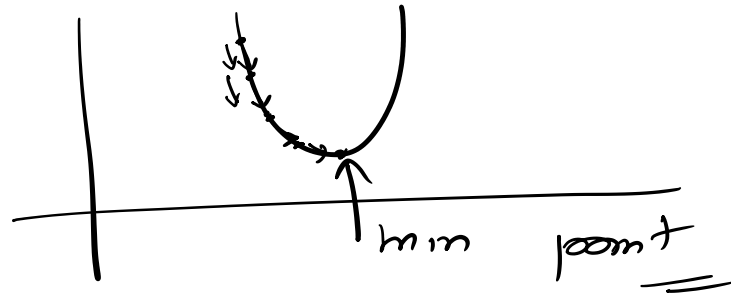
Gradient Descent Algorithm :- It is an  
Optimization algorithm to find the minimum value  
of my cost function

GDA :- Image the scenario;



② Approach :-

- ① Step by step descend using some ladder
- ② Directly jump to the bottom X

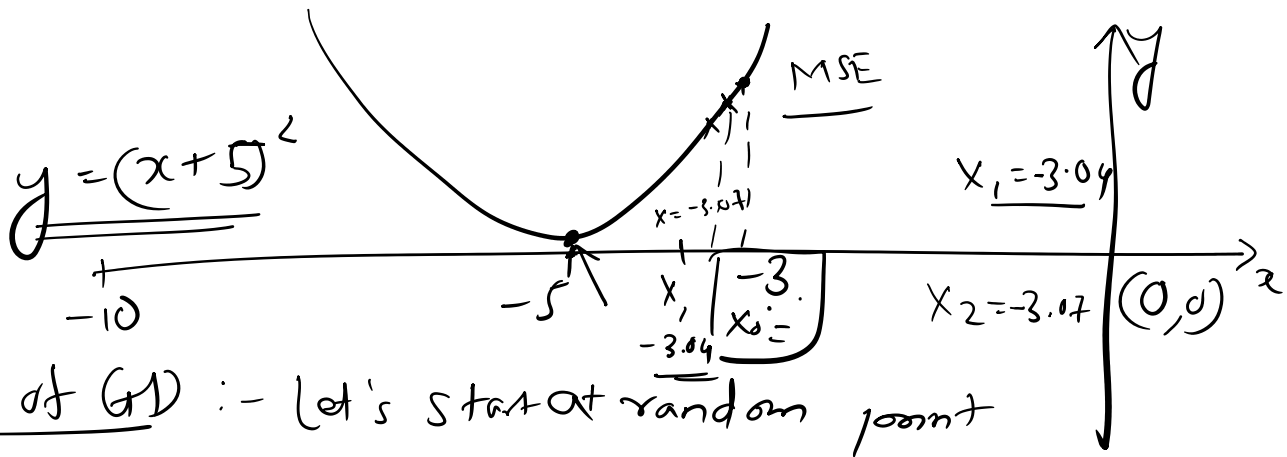


Learning rate( $\alpha$ ) :- The  $\alpha$  decides how fast  
the algorithm reaches the minimum  
point.

eg: -

CF: -

$$y = (x+5)^2$$



Step 1 of GD :- Let's start at random point

$$x = -3$$

Step 2 of GD :- Move in the negative direction of the gradient (derivative)

$$y = (x+5)^2 \Rightarrow \frac{dy}{dx} = 2(x+5)$$

$$y = \underline{x}^2 = \frac{dy}{dx} = \underline{2x}$$

Q. But how much to move? For this we have our learning rate ( $\alpha$ ) = 0.01  $\leftarrow$  Assumption

Step 3 :- Perform 2 iterations of ~~GL~~ GL to understand how GD works.



# Initialize Parameters:-

$$X_0 = -3$$

$$\frac{dy}{dx} = 2(x+5) \quad \alpha = 0.01$$

Iteration 1 :-

$$X_1 = X_0 - \alpha * \left(\frac{dy}{dx}\right)$$

$$X_1 = (-3) - (0.01) * (2 * (-3) + 5)$$

$$\boxed{X_1 = -3.04}$$

Iteration 2:-  $x_1 = -3.04$   $\alpha = 0.01$   $\frac{dy}{dx} = 2(x+5)$

$$x_2 = x_1 - \alpha \times \frac{dy}{dx}$$

$$= (-3.04) - (0.01) \times 2 (0.01 + 5)$$

$$x_2 = -3.07$$

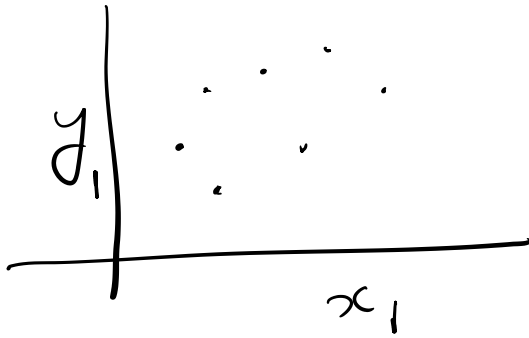
## Multiple Linear Regression :-

- ① Many Independent Variables
- ② 1 Dependent or target variable.

The eqn of MLR :-

$$y = b_0 + b_1 x_1 + b_2 x_2 + b_3 x_3 + \dots$$

Q. What is important condition for Linear Regression?



The problem arises when there are multiple independent variables!

Q What is the problem.

For real estate dataset,

① Lin Rel<sup>n</sup> between house age & price is ok

② Lin Rel<sup>n</sup> between MRT stores & price is ok

But

① Lin Rel<sup>n</sup> between house age & MRT store is a problem because both have & MRT store are independent variables

MLR :- (1) Lin Rel<sup>n</sup> bet<sup>n</sup> target & independent variables should be present

(2) Lin Rel<sup>n</sup> bet<sup>n</sup> any 2 independent variable should not be present

Multicollinearity :- Lin Rel<sup>n</sup> bet<sup>n</sup> 2 independent variables is called Multicollinearity

Q How to check Multicollinearity?

Ans :- (1) Scatter plot (2) Correlation Map