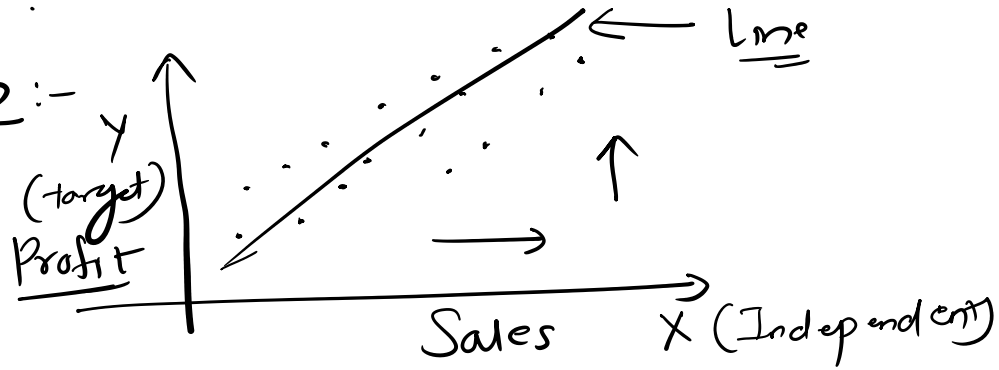


Regression :-

Goal :- To predict a continuous target variables based on the available independent variable.

Linear Regression :-

Simple Straight
line



Linear Regression :- To establish a relation between the target and independent variable using a straight line:

$$y = b_0 + b_1 x$$

y = target variable
 x = Independent variable

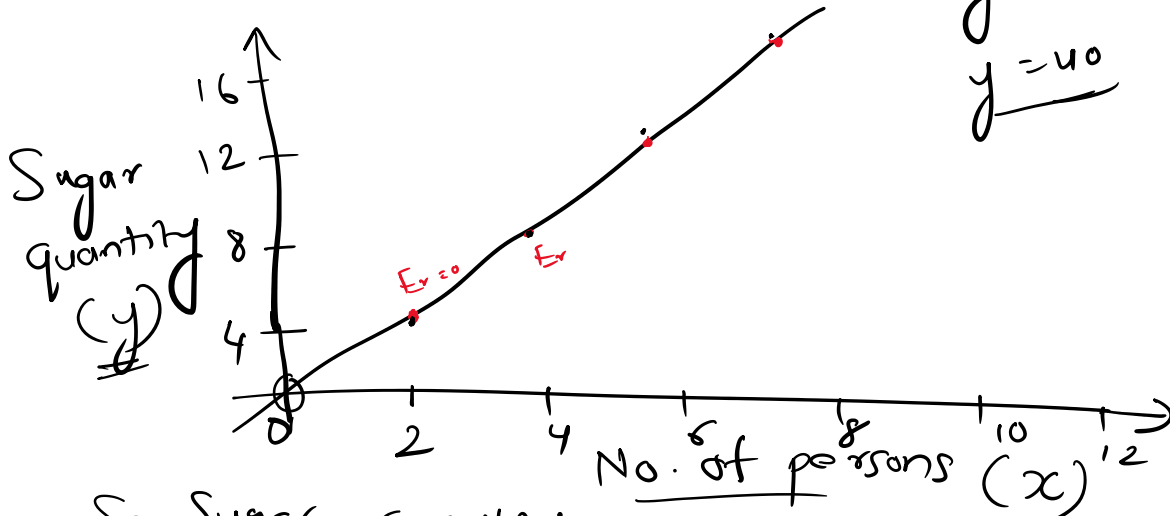
$b_0 \rightarrow$ Intercept
 $b_1 \rightarrow$ Slope

eg:- Let consider an example $x = \underline{\underline{20}}$

$$y = 2 \times 20 \Downarrow$$

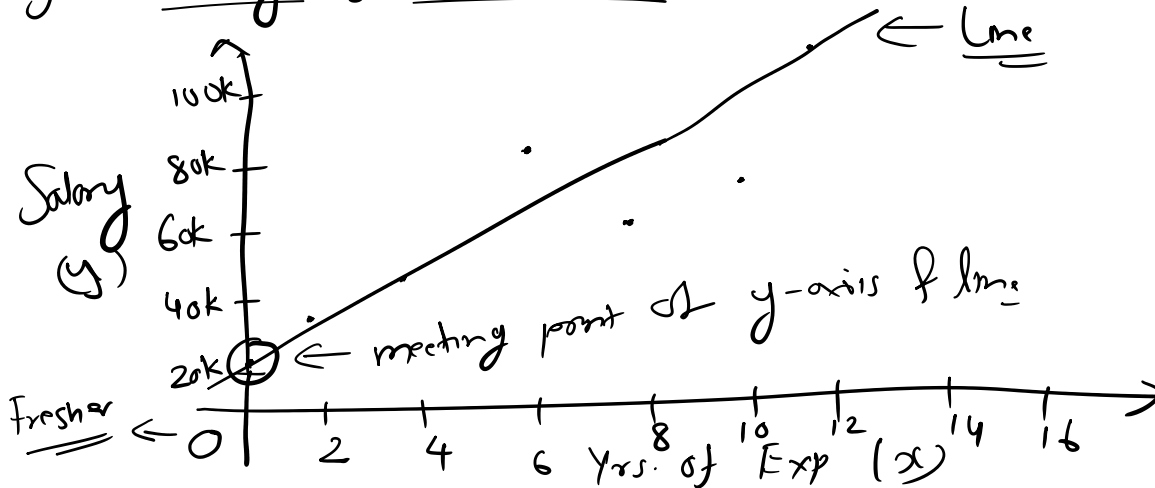
$$y = 40$$

2 x times
the sugar
of No. of
persons



Sugar quantity = $2 \times$ No. of persons.

eg:- Salary & Yrs of Exp



Freshers
Salary =
25K

$$y = b_0 + b_1 x$$

b_0 = intercept

b_1 = Slope

$$\text{Salary} = \boxed{25K} + (\underline{b_1}) \text{ Yrs. of Exp}$$

Slope figure out

Intercept (b_0):- The meeting point of Linear Regression Line & Y-axis is called intercept.

Tea ex:- $y = 2x \Rightarrow$

$$y = 2x + \underline{\underline{0}}$$

\downarrow \downarrow

b_1 Intercept.

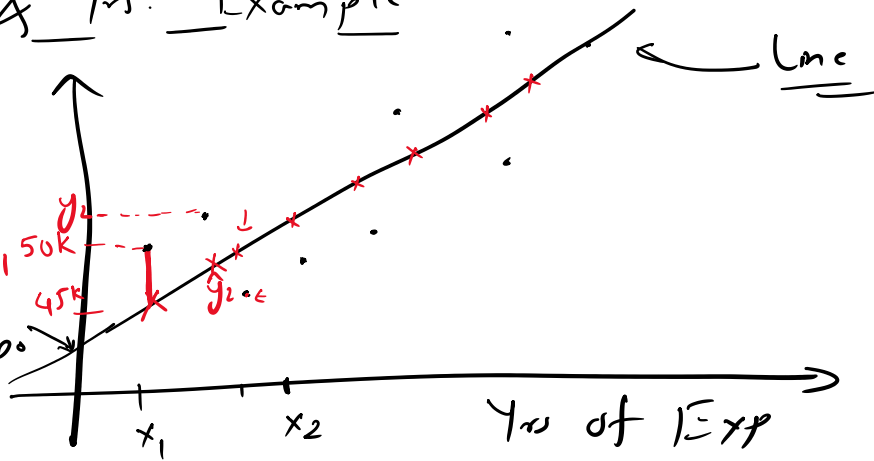
slope

Salary & Yrs. Example

Salary

$$\frac{50k - 45k}{45k} = \text{Error}$$

$$\text{Error} = 5K$$



• \leftarrow represent actual salary values

$x \leftarrow$ represent the predicted value.

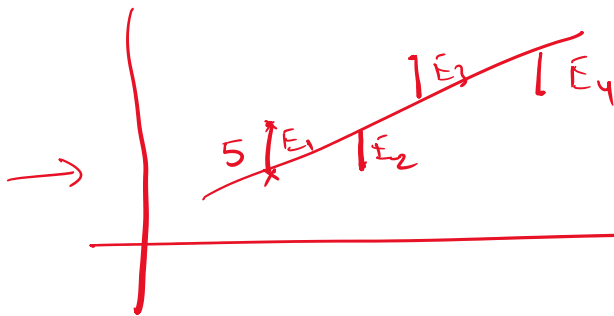
$y_i =$ actual salary
 $\hat{y}_i =$ predicted salary

$$\begin{aligned} \text{Error} &= y_1 - \hat{y}_1 \\ \text{Error} &= y_2 - \hat{y}_2 \end{aligned}$$

$$\text{Error} = y_3 - \hat{y}_3$$

$$\boxed{\text{Error} = y_i - \hat{y}_i} \quad \text{where } i = 1 \text{ to } n$$

$$\boxed{\text{Sum of Error} = \sum_{i=1}^n (y_i - \hat{y}_i)}$$



$$\leftarrow \text{Error} = \cancel{5} + \cancel{(-5)} + \cancel{8} + \cancel{(-8)}$$

$$E_1 = 5$$

$$E_3 = 8$$

$$E_2 = -5$$

$$E_4 = -8$$

$$\boxed{\text{Error} = 0}$$

$$\boxed{\text{Squared Error} = \sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

$$\begin{aligned} E_1 = 5 \quad E_3 = 8 &= (5)^2 + (-5)^2 + (8)^2 + (-8)^2 \\ E_2 = -5 \quad E_4 = -8 &= 25 + 25 + 64 + 64 \end{aligned}$$

$$\boxed{\text{Squared Error} = 178}$$

$$\boxed{\text{Mean Squared Error} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

$$\text{Sq. Error} = 178$$

$$\text{MSE} = \frac{178}{4}$$

$$\boxed{\text{MSE} = \underline{\underline{44.23}}}$$

* Mean Squared Error is called as the cost function for Linear Regression problems

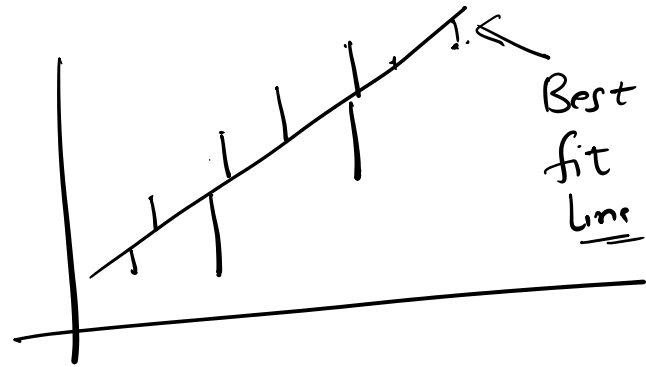
Cost function :- ① It is a function used to measure the performance of a model on any data.

② It measures the error between actual & predicted values & outputs that in the form of a number.

For LR, the cost function is Mean Squared Error

For LR, the MSE should be minimum.

Cost function - performance
For LR, cost function = MSE
 $\text{MSE} = \text{Error of } \underline{\text{LR}}$

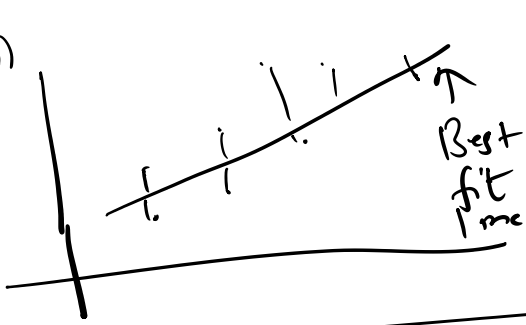


The entire aim of LR model is to find a Best fit line. by minimizing MSE
Q How to find the best fit line?

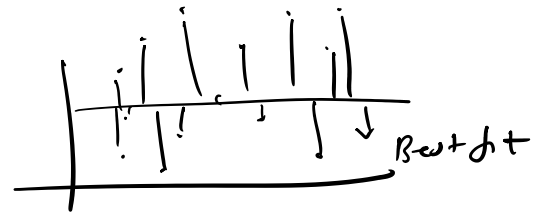
→ By minimizing MSE.

Q. Why minimize MSE?

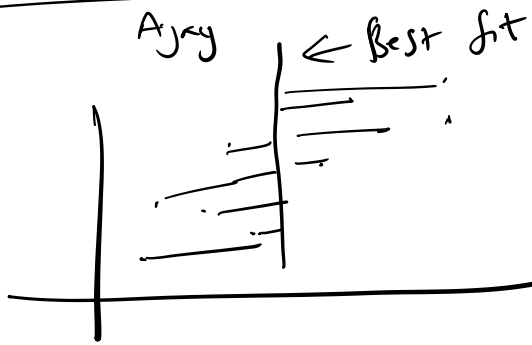
Anil



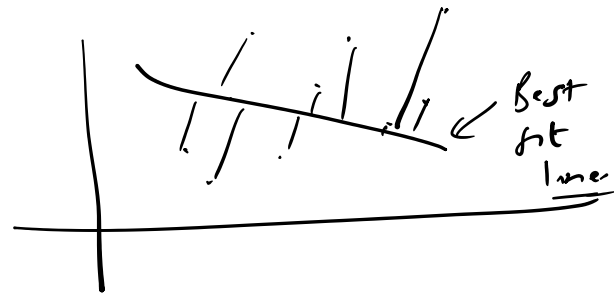
Sunil



Ajay



Sam



Types of Linear Regression

- ① Simple Regression.
 - (a) 1 Independent variable
 - (b) 1 target variable.
- ② Multiple Regression
 - (a) Many Independent variables
 - (b) 1 target variable.

③ Polynomial Linear Regression

④ Lasso Regression.

⑤ Ridge Regression

} When we face a
problem of
overfitting &
underfitting

* Note:- For applying Linear Regression, there should be a linear Relationship between the variables.

If no Linear Relationship, then we cannot apply Linear Regression models.