

# LAB ASSIGNMENT

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## MONTE-CARLO SIMULATION OF RADIOACTIVE RADIOACTIVE DECAY

### AIM

- Implement a simulation of radioactive decay in python
- Provide initial conditions (number of particles, decay constant) and analyse the results, including plotting the decay curve over time)
- Calculate the half-life of the radioactive substance based on the simulation results and check how it compares to the theoretically expected half-life

Provide information about a specific radioactive isotope with a known half-life to simulate the decay of this isotope and compare the simulation results with the expected decay

### PRINCIPLE

The decay of an unstable nucleus is entirely random in time so it is impossible to predict when a particular atom will decay. But the number of decay events  $dN$  expected to in a small interval of time  $dt$  is proportional to the number of atoms present  $N$ , given by the equation

$$\frac{dN}{dt} = -\lambda N$$

where  $\lambda$  is the decay constant. Analytically solving it shows that decay is exponential

### THEORY

Radioactive decay is a spontaneous and process where in unstable nuclei disintegrate over time, following an exponential decay law.

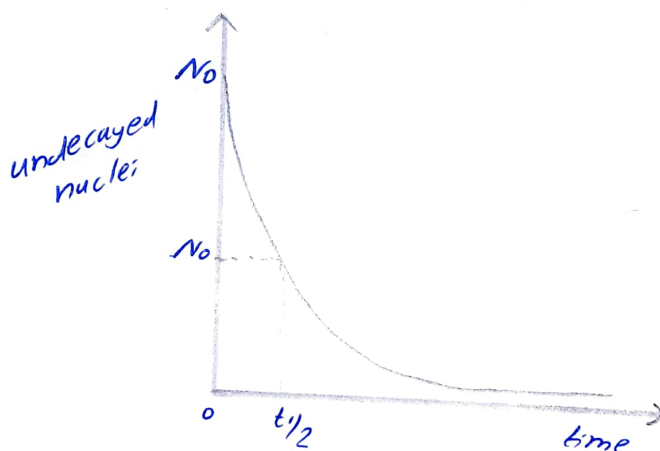
The number of undecayed nuclei at any time  $t$  is given by solving the above differential equation,  $N(t) = N_0 e^{-\lambda t}$  where  $N_0$  is the initial number of nuclei and  $\lambda$  is the decay constant. The decay constant physically signifies the probability that are

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particular atom undergoes radioactive decay in a infinitesimal time step  $\Delta t$

In this experiment, probabilistic decay is modelled using Monte-Carlo method. At each time step, each nucleus is assumed to have a fixed probability of decaying. By simulating a large number of such decay ~~events~~ <sup>events</sup> are successive intervals, the aggregate behaviour statistically approximates the exponential decay curve

Graph of analytical solution (expected)



Algorithm and flowchart

Step 1: Import required libraries

Step 2: Set initial parameters

Step 3: calculate theoretical half-life  
 $N_0 = 1000, \lambda = 0.06966 \text{ (s}^{-1}\text{)}, \text{steps} = 100$

$$t_{1/2} = \frac{0.693}{\lambda}$$

Step 4: Initialize array & variable  
decay\_mc to store remaining particles after each step

t\_half\_mc = None

Step 5: Monte-Carlo simulation of decay  
for each time  $t$  from 0 to step 1

- i) generate  $N$  random numbers from 0 to 1
- ii) count how many are less than  $\lambda$ . There present decayed ~~from~~ particles
- iii) subtract the number of decayed from  $N$

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iv) store the current  $N$  in  $\text{decay\_mc}[t]$

v) If  $\text{half\_mc}$  hasn't been set and  $N$  has dropped below half of  $N_0$ , set  $t_{\text{half\_mc}} = t$

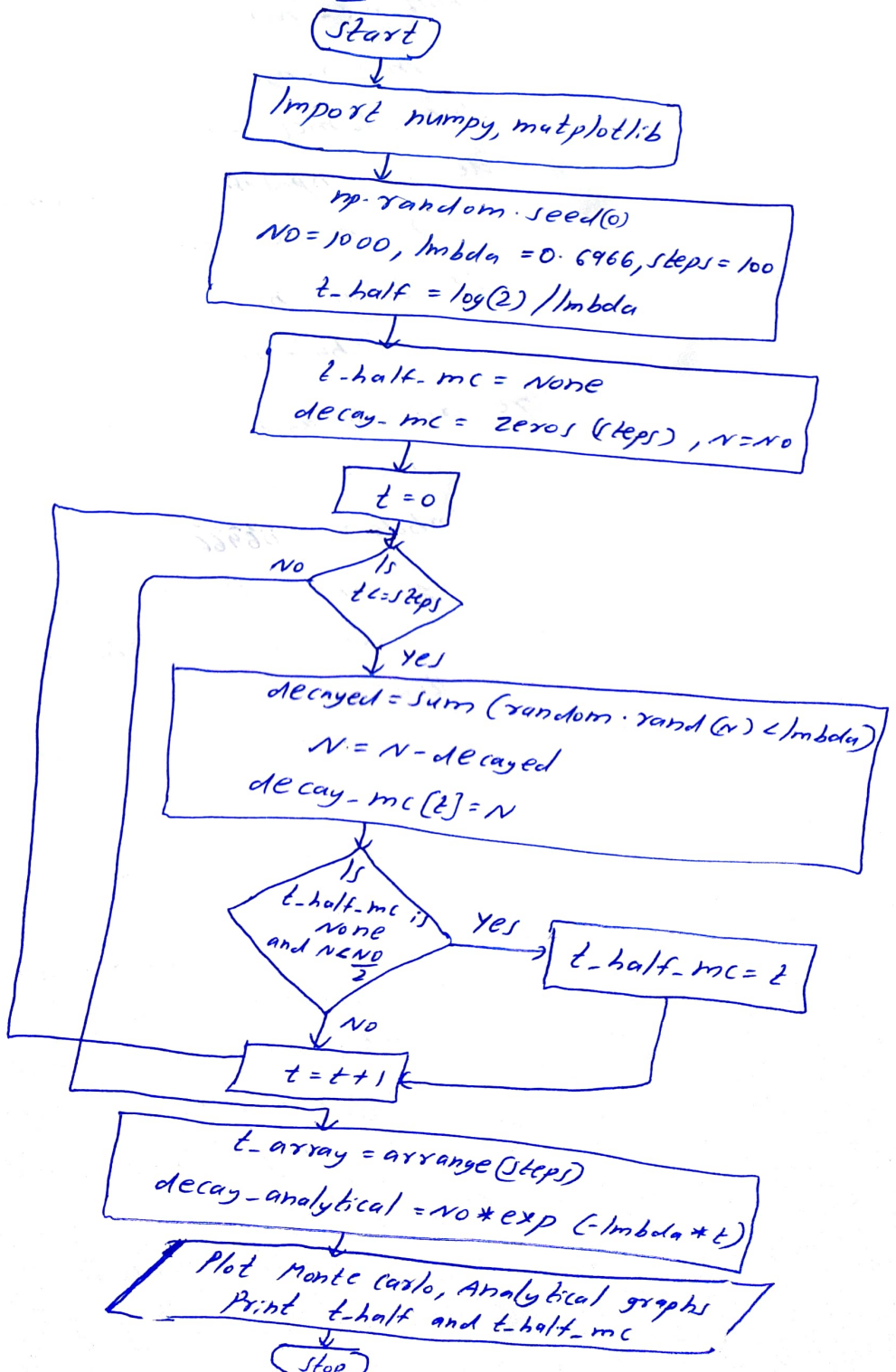
step 6: Analytical solution  

$$N(t) = N_0 e^{-\lambda t}$$

step 7: Plot the results

step 8: Compare theoretically obtained half-life & Monte-carlo half-life

flowchart





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PROCEDURE - CODE

```

import numpy as np
import matplotlib.pyplot as plt

np.random.seed(0)

def monte-carlo-decay-simulation(no n0, lambda, steps):
    decay_mc = np.zeros(steps)
    n = n0
    t_half_mc = None
    for t in range(steps):
        decayed_mc[t] = n
        decayd = np.sum(np.random.rand(n) < lambda)
        n = n - decayd
        if t_half_mc is None and n < n0/2:
            t_half_mc = t
    return decay_mc, t_half_mc

n0 = 1000
lambda = 0.01023

# decay constant of N-13 = 0.06966
# decay constant of Ga-68 = 0.01023
steps = 1000

decay_mc, t_half_mc = monte-carlo-decay-simulation
(n0, lambda, steps)

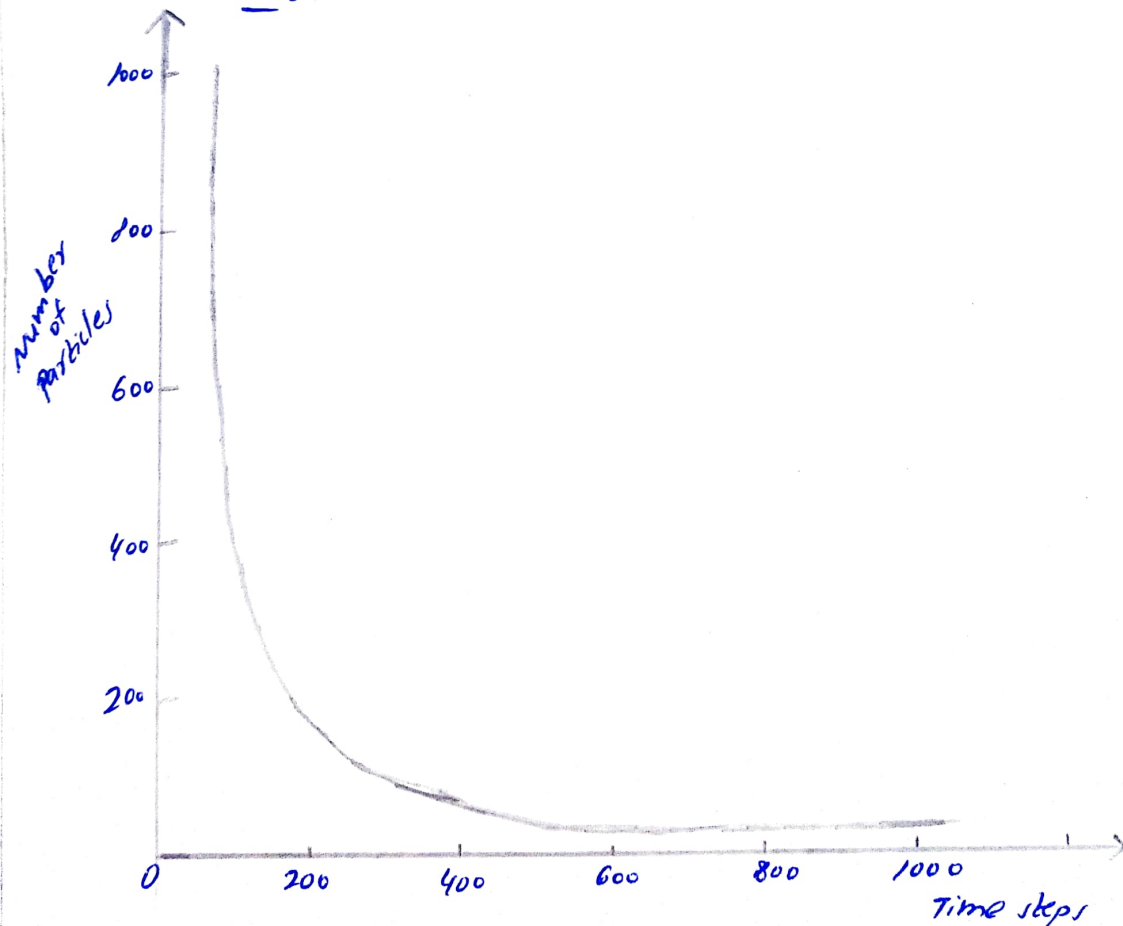
t_half = np.log(2)/lambda
time_array = np.arange(steps)
decay_analytical = n0 * np.exp(-lambda * time_array)
plt.figure(figsize=(10,6))
plt.plot(time_array, decay_mc, label='Monte
carlo simulation', color='blue',
marker='o', marker_size=3)
plt.plot(time_array, decay_analytical,
label='Analytical solution', color='red',
linestyle='--')

```

⑤

```
plt.xlabel('Time steps')  
plt.ylabel('Number of particles')  
plt.title('Monte Carlo Simulation of  
Radioactive Decay')  
plt.xlim(0, 1000)  
plt.grid(True)  
plt.legend()  
plt.show()  
  
print("Simulated Half-life: ", t_half_mc)  
print("Theoretical Half-life: ", t_half)
```

### RESULT



Simulated Half-life : 65  
Theoretical Half-life : 67.7563