2018 AP® CALCULUS AB FREE-RESPONSE QUESTIONS

Version # 15

CALCULUS AB
SECTION II, Part A

Time—30 minutes

Number of questions—2

A GRAPHING CALCULATOR IS REQUIRED FOR THESE QUESTIONS.

1. People enter a line for an escalator at a rate modeled by the function r given by

$$r(t) = \begin{cases} 78 \left(\frac{t}{100}\right)^3 \left(1 - \frac{t}{152}\right)^1 & \text{for } 0 \le t \le 300\\ 0 & \text{for } t > 300, \end{cases}$$

where r(t) is measured in people per second and t is measured in seconds. As people get on the escalator, they exit the line at a constant rate of 0.6 person per second. There are 92 people in line at time t = 0.

- (a) How many people enter the line for the escalator during the time interval $0 \le t \le 300$?
- (b) During the time interval $0 \le t \le 300$, there are always people in line for the escalator. How many people are in line at time t = 300?
- (c) For t > 300, what is the first time t that there are no people in line for the escalator?
- (d) For $0 \le t \le 300$, at what time t is the number of people in line a minimum? To the nearest whole number, find the number of people in line at this time. Justify your answer.