

# Week 7 Reading Notes: NLP 1 - Distributions & Key Research Directions

Name: Ananya and Apoorva

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## Overview

Week 7 covers four main topics:

1. Choosing appropriate regression analysis methods
  2. Statistical distributions and Poisson Random Fields
  3. Climate change data analysis
  4. Introduction to NLP with Count Vectors and TF-IDF
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## 1. Choosing the Right Regression Analysis

Source: Statistics By Jim

### Types of Regression Models

#### Linear Regression

- For continuous dependent variables with linear relationships
- Assumptions: linearity, homoscedasticity, independence, normality
- Example: Predicting house prices

#### Logistic Regression

- For binary outcomes (yes/no, 0/1)
- Output: Probability between 0 and 1
- Example: Customer churn prediction, spam detection

#### Polynomial Regression

- For non-linear curved relationships
- Uses polynomial terms ( $x^2$ ,  $x^3$ )
- Risk of overfitting with high degrees

#### Poisson Regression

- For count data (non-negative integers)
- Assumption: Variance equals mean
- Example: Number of customer visits, accident counts

### **Negative Binomial Regression**

- For count data with overdispersion
- Use when variance exceeds mean

### **Decision Framework**

Questions to ask when choosing regression:

1. What type is my dependent variable?
  2. What is the relationship shape?
  3. Are model assumptions met?
  4. Is there overdispersion in count data?
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## **2. Distributions & Poisson Random Fields**

### **Key Distributions**

#### **Normal Distribution**

- Bell curve, symmetric
- Parameters: mean and standard deviation
- Common in natural phenomena

#### **Poisson Distribution**

- Models count of events in fixed interval
- Parameter:  $\lambda$  (average rate)
- Mean equals variance
- Good for rare events

#### **Binomial Distribution**

- Number of successes in  $n$  trials
- Parameters:  $n$  (trials),  $p$  (probability)

#### **Exponential Distribution**

- Time between events in Poisson process
- Example: Time until next customer arrival

## Poisson Random Fields

### Concept:

- Extension of Poisson processes to spatial domains
- Models discrete events distributed across space or time
- Used for feature selection in high-dimensional data

### Dynamic Feature Models:

- Features can appear or disappear over time
- Allows sparse, dynamic feature sets
- Applications: time-series, gene expression, topic modeling

### Key Innovation:

- Traditional models assume fixed features
  - Poisson Random Fields enable flexible feature selection
  - Better for high-dimensional sparse data
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## 3. Climate Change Data Analysis

### Types of Climate Data

- Temperature records
- Precipitation measurements
- Sea level data
- Ice core samples
- Satellite observations
- Atmospheric CO<sub>2</sub> levels

### Statistical Challenges

#### Temporal Autocorrelation

- Climate measurements correlated over time
- Requires time-series models (ARIMA, SARIMA)

#### Spatial Autocorrelation

- Nearby locations have similar climates
- Requires spatial statistics

## **Non-stationarity**

- Climate patterns change over time
- Requires detrending or differencing

## **Missing Data**

- Historical records incomplete
- Requires imputation techniques

## **Regression Applications**

- Linear regression for temperature trends
- Polynomial regression for non-linear patterns
- Poisson regression for extreme event counts
- Machine learning for climate forecasting

## **Key Points**

- Climate change detection requires 30+ years of data
  - Natural variability must be separated from human impact
  - Multiple data sources strengthen conclusions
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# **4. Introduction to NLP: Count Vectors and TF-IDF**

## **Text Preprocessing Pipeline**

### **Step 1: Text Cleaning**

- Remove punctuation and special characters
- Convert to lowercase
- Handle contractions

### **Step 2: Tokenization**

- Split text into individual words
- Example: "I love NLP" → ["I", "love", "NLP"]

### **Step 3: Stop Word Removal**

- Remove common words: "the", "is", "at", "a"
- Reduces dimensionality

### **Step 4: Stemming/Lemmatization**

- Stemming: Crude chopping (running → run)
- Lemmatization: Dictionary-based (better → good)

## Count Vectors (Bag of Words)

### Concept:

- Represent text as vector of word frequencies
- Each unique word is one dimension
- Value is count of word in document

### Example:

Document 1: "I love dogs"

Document 2: "I love cats"

Vocabulary: [I, love, dogs, cats]

Count Vectors:

Doc1: [1, 1, 1, 0]

Doc2: [1, 1, 0, 1]

### Advantages:

- Simple and interpretable
- Captures word importance by frequency

### Disadvantages:

- Ignores word order
- Treats all words equally
- High dimensionality

## TF-IDF (Term Frequency - Inverse Document Frequency)

### Concept:

- Weighs words by importance across documents
- Down-weights common words, up-weights rare words

### Formula:

$$\text{TF-IDF} = \text{TF} \times \text{IDF}$$

$$\text{TF} = (\text{Count of word in document}) / (\text{Total words in document})$$

$$\text{IDF} = \log(\text{Total documents} / \text{Documents containing word})$$

**Intuition:**

- High TF: Word appears frequently in this document
- High IDF: Word is rare across all documents
- High TF-IDF: Word is important to this specific document

**Advantages:**

- Reduces impact of common words
- Highlights discriminative terms
- Better for classification and search

**Disadvantages:**

- Still ignores word order
- More complex than count vectors
- Requires entire corpus for calculation

**Applications**

- Text classification (spam detection, sentiment analysis)
- Information retrieval (search engines)
- Document similarity (plagiarism detection)

**Python Implementation****Count Vectorizer:**

```
from sklearn.feature_extraction.text import CountVectorizer
vectorizer = CountVectorizer()
X = vectorizer.fit_transform(corpus)
```

**TF-IDF Vectorizer:**

```
from sklearn.feature_extraction.text import TfidfVectorizer
vectorizer = TfidfVectorizer()
X = vectorizer.fit_transform(corpus)
```

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**Connections Between Topics**

### **Regression + Climate Data:**

- Poisson regression for extreme weather events
- Linear regression for temperature trends

### **Distributions + NLP:**

- Word frequencies follow power-law distributions
- Topic modeling uses Dirichlet distributions

### **NLP + Regression:**

- TF-IDF features as predictors
- Sentiment scores predicting outcomes

### **Dynamic Features + NLP:**

- Poisson Random Fields for topic evolution
  - Sparse feature selection in text data
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## **Key Takeaways**

### **Regression Analysis**

- Choose regression based on dependent variable type
- Always validate model assumptions
- Start simple, add complexity as needed

### **Statistical Distributions**

- Poisson for count data with rare events
- Poisson Random Fields enable dynamic models
- Distribution choice affects model performance

### **Climate Data**

- Long-term trends require careful analysis
- Account for temporal and spatial autocorrelation
- Multiple data sources strengthen conclusions

### **NLP Basics**

- Count Vectors: Simple frequency-based representation
- TF-IDF: Weights words by importance

- Preprocessing is critical for success
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## **Tools & Libraries**

- scikit-learn: CountVectorizer, TfidfVectorizer, regression models
- NLTK: Natural language toolkit
- spaCy: Industrial NLP
- statsmodels: Advanced statistical models
- pandas: Data manipulation