

Name: \_\_\_\_\_

ID: \_\_\_\_\_

**1.)** Please consider the differential equation below:

$$\frac{d^2y}{dt^2} + 6 \frac{dy}{dt} + 5y = u$$

**a) (10 pts)** Obtain the transfer function  $Y(s)/U(s)$  for this system.

**b) (10 pts)** Find the free response of this differential equation analytically using Laplace transform with initial conditions:  $y(0) = 1$  and  $\dot{y}(0) = 0$ . Please plot the response for 10 seconds using MATLAB.

**c) (10 pts)** Plot the free response to this differential equation by numerical solution using MATLAB. Compare graphically this numerical solution to the analytical solution in (a).

Name: \_\_\_\_\_

ID: \_\_\_\_\_

**2.) (10 pts)** Please solve Problem B-3-6 from Ogata (page 98).

Name: \_\_\_\_\_

ID: \_\_\_\_\_

**3.) (10 pts)** Please solve Problem B-3-9 from Ogata (page 99), except for the analogous mechanical system.

Name: \_\_\_\_\_

ID: \_\_\_\_\_

**4.) (10 pts)** Please find the inverse Laplace transform of:

$$G(s) = \frac{2s + 4}{s^2 + 6s + 10}$$

Name: \_\_\_\_\_

ID: \_\_\_\_\_

**5.) (10 pts)** Please find the inverse Laplace transform of:

$$G(s) = \frac{s^2 + s + 2}{(s + 1)^3}$$