## EE380 (Control Systems) Pre-Lab work of Experiment 5

Student Name	Roll No.	Bench No.
You should use your values of $R_{\Sigma}$ , $B$ , $K_t$ ,	$K_b$ , $J$ , etc in the m-files e5q4	.m and e5q5easysim.m.

**Q1** Using the voltage equation  $V = L\frac{di}{dt} + Ri + E$ , the fundamental torque equation  $J\frac{d\omega}{dt} = -B\omega + T - T_L$ ,  $E = K_b\omega$ , and  $T = K_ti$ , determine the current at steady-state speed with V = 7 V and  $T_L = 0$ . Call this current  $i_{d1}$ . See the lecture slides.

*Note:* The figure  $i_{d1}$  is the maximum value that we wish to specify as reference for the current control at  $T_L = 0$ . Any greater value of reference current at  $T_L = 0$  will require the H-bridge to apply a voltage V > 7 V, and thereby go into voltage saturation. We wish to avoid saturation so that we may work with an approximately linear plant.

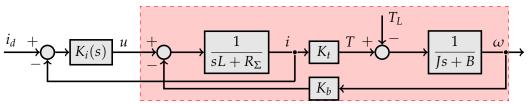
**Q2** Using the voltage equation, the fundamental torque equation,  $E = K_b \omega$ , and  $T = K_t i$ , determine the current at steady-state speed with V = 7 V and  $T_L = 0.003$  N·m. Call this current  $i_{d2}$ . See the lecture slides.

*Note:* This value of  $T_L = 0.003 \text{ N} \cdot \text{m}$  has been arrived at as follows. The radius of the pulley where the string winds is approximately r = 1.25 cm. The mass of the load is in the range m = 1.5 - 2 kg, but we assume that it is 1.5 kg. Acceleration due to gravity  $g = 9.8 \text{ m/s}^2$ . The gear ratio is  $R_g = 62$ . Then,  $T_L = mgr/R_g \approx 0.003$ . *But wait!* Don't we need to divide the answer by the efficiency of the gear  $\eta \approx 0.59$ ? Then,  $T_L \approx 0.005 \text{ N} \cdot \text{m}$ .

*Note:* This  $i_{d2}$  is the maximum value that we wish to specify as reference for the current control at  $T_L = 0.003 \text{ N} \cdot \text{m}$ . Any greater value of reference current at  $T_L = 0.003 \text{ N} \cdot \text{m}$  will require the H-bridge to apply a voltage V > 7 V, and thereby go into voltage saturation. We avoid saturation to have an approximately linear plant. The minimum value of  $i_{d2}$  is  $T_L/K_t$ . When we apply the load and require the motor to track a value of  $i_d$  that is less than this minimum value of  $i_{d2}$ , the load will drive the motor, rather than the motor driving the load.

**Q3** Determine the TF from u to i for the PMDC motor in preparation for the design of a proportional-integral (PI) controller. Use the values of  $R_{\Sigma}$  and B from the experiment where they were calculated from the experimentally-determined  $K_m$  and  $\tau_m$ .

The armature inductance  $L_a$  is negligible (see footnote in lab manual, Ch. 2).



Plant: The part outside dsPIC30F4012

**Q4** We wish to work out a controller  $K_p + K_I/s$  with the best settling time we can achieve for the <u>unloaded motor</u>, while keeping the control effort u out of saturation. Provided to you is an m-file e5q4.m for this purpose. Run this m-file and document in the table the effect of varying  $K_p$  and  $K_I$ .

Values of $(K_p, K_I)$	(20,0)	(250,0)	(250, 100	) (20, 100)	(20,500)	(20, 1500)	(0,1500)
Approx. settling time $t_s$ [s]							
Tracking error $e_{0+} = i_d(0+) - i(0+)$ [A] using intial value theorem $\lim_{t\to 0+} y(t) = \lim_{s\to \infty} sY(s)$							
Tracking error $e_0 = i_d(0+) - i(0+)$ [A] from plot							
Steady state error $e_{ss}$ [A]							
Max. control effort [V]							

**Q5** Provided to you is e5q5easysim.m, which is a modified version of easysim.m. Simulate the CL system of the above figure for  $i_d = i_{d1}$  and fill the below table.

Values of $(K_p, K_I)$	(20,0)	(250,0)	(250, 100)	(20, 100)	(20,500)	(20, 1500)	(0,1500)
Approx. settling time $t_s$ [s]							
Tracking error $e_{0+} = i_{d1}(0+) - i(0+)$ [A]							
Steady state error $e_{ss}$ [A]							
Max. control effort [V]							

**Q6** Do the results of Q5 match those from Q4? Explain the differences. (Hint: A thought on the two questions asked in e5q4.m might reveal the answer).

**Q7** With  $T_L = 0.003 \text{ N} \cdot \text{m}$  and  $i_d = i_{d2}$ , perform a simulation of the digital control of the motor using e5q5easysim.m and the controllers from the above tables. Write down a controller that you will use in the lab.