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Section: B

Skill Lab

Group Activity

Topic :01

Array

"FIND LARGEST SUM CONTIGUOUS SUBARRAY"

Here, the problem statement "Find largest sum contiguous subarray" says that - Among all the subarrays of an array find the subarray that gives maximum sum.

Example:

Let us consider an array:
 $arr = [-2, -3, 4, -1, -2, 1, 5, -3]$

Possible subarrays are:-

$[-2], [-3], [4], [-1], [-2], [1], [5], [-3]$

$[-2, -3], [4, -1], [-2, 1], [5, -3]$

$[-2, -3, 4], [4, -1, -2], [-2, -3, 4, -1],$
 $[4, -1, -2, 1, 5]$

Sum of elements in subarray:-

$-2 + (-3) = -5$ $4 + (-1) = 3$

.

$-2 + (-3) + 4 + (-1) = -2$ $4 + (-1) + (-2) + 1 + 5 = 7$

Here the largest sum of a subarray is

$$[4, -1, -2, 1, 5] = 7$$

This is the solution.

- In order to find the solution for the problem statement "Find the largest sum contiguous subarray" there are many ways. One of the best solution approach is by using "Kadane's algorithm".

KADANE'S ALGORITHM

Kadane's Algorithm is a dynamic programming technique, to find the largest sum of a contiguous subarray within 1-Dimensional array of elements.

- * Kadane's Algorithm can also be used to find largest sum of submatrix within 2-Dimensional or multi-dimensional array.

Steps in Kadane's Algorithm:

Step 1: Initialize variables

- $\text{max_so_far} = -\infty$ → To keep track of the maximum sum found so far
- max_ending_far here $= 0$ → To keep track of the sum of the

current subarray.

Step 2: Iterate through the array.

• For each element num in the array:

1. Add num to max_ending_here .
2. If max_ending_here is greater than max_so_far , update max_so_far .
3. If $max_so_ending_here$ becomes negative, reset it to 0.

Step 3:

Return max_so_far as the maximum sum of the contiguous subarray.

Algorithm (Pseudocode):

Initialize $max_so_far = -\infty$

Initialize $max_ending_here = 0$

For each element num in the array:

add num to max_ending_here

If $max_ending_here > max_so_far$:

update $max_so_far = max_ending_here$

If $max_ending_here \leq 0$:

Reset $max_ending_here = 0$

Return max_so_far

Let us take program example and understand Kadane's algorithm:
The following code is written in python programming language.

Code:

```
def max_subarray_sum_kadane(arr):  
    max_so_far = float('-inf')  
    max_ending_here = 0  
  
    for num in arr:  
        max_ending_here += num  
        max_so_far = max(max_so_far, max_ending_here)  
  
        if max_ending_here < 0:  
            max_ending_here = 0  
  
    return max_so_far  
  
# Example usage  
arr = [-2, -3, 4, -1, -2, +1, 5, -3]  
print("Largest sum:", max_subarray_sum_kadane(arr))
```

Output:-

Largest sum(Kadane's Algorithm): 7

Step by Step Execution of program:

The above code of Kadane's algorithm to find largest sum subarray works in the following ways:-

The input given is
 $arr = [-2, -3, 4, -1, -2, 1, 5, -3]$
 Execution is as follows:-

Index	Element	max ending here (current sum)	max so far (Max sum found)
0	-2	-2	-2
1	-3	-3	-2
Since sum can be $-ve$, the above will be reset to 0			
2	4	4	4
3	-1	$4 + (-1) = 3$	4
4	-2	$4 + (-1) + (-2) = 1$	4
5	1	$4 + (-1) + (-2) + 1 = 2$	4
6	5	$4 + (-1) + (-2) + 1 + 5 = 7$	7 (updated)
7	-3	$4 + (-1) + (-2) + 1 + 5 - 3 = 4$	7

Here, the largest sum is 7.
 Therefore the variable max so far will return 7.

The subarray that gives largest sum is
 $[4, -1, -2, 1, 5] = 7$