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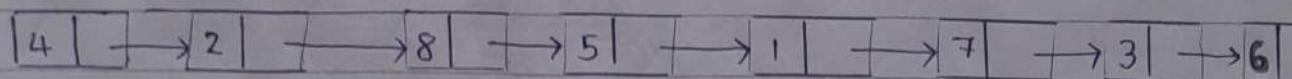
IRIV24MC017

MCA 'E' semester 'A' section

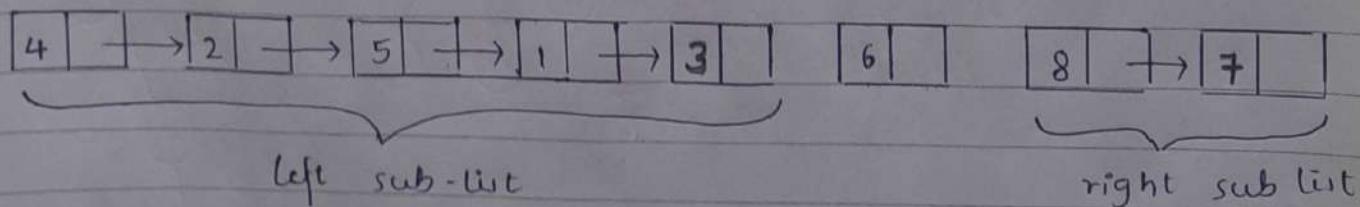
Sort a linked list using quick sort

Quick sort is a sorting algorithm that follows the divide and conquer approach to sort a given array or any contiguous data structure. It works by selecting a pivot element from the list and comparing it with each element in the list. If an element is less than pivot element it will go to the left sub-list and if its greater it will be put into right sub-list. Quick sort repeatedly partitions the current list until it can be no longer divided. At this point all the values will be in a sorted manner and we put this into new linked list which will be the sorted linked list.

Expt Example: Sorting below linked list using quick sort

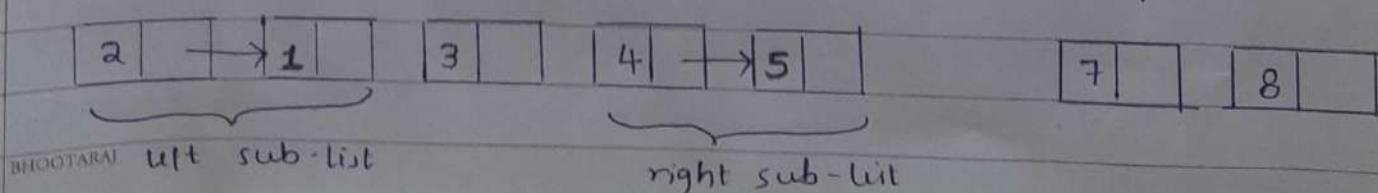


Iteration 1: choose 6 (last element as pivot)



Iteration 2: pivot = 3

pivot = 7

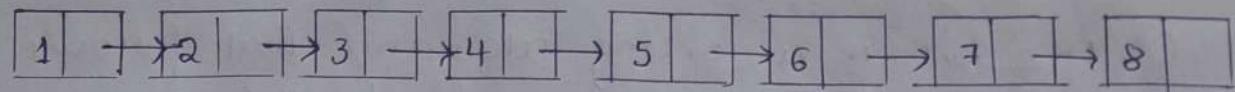


Iteration 3: pivot=1, pivot = 5

1	2
---	---

4	5
---	---

Now we can no longer divide the sub partitions any further.
Combining these sublists into one linked list -



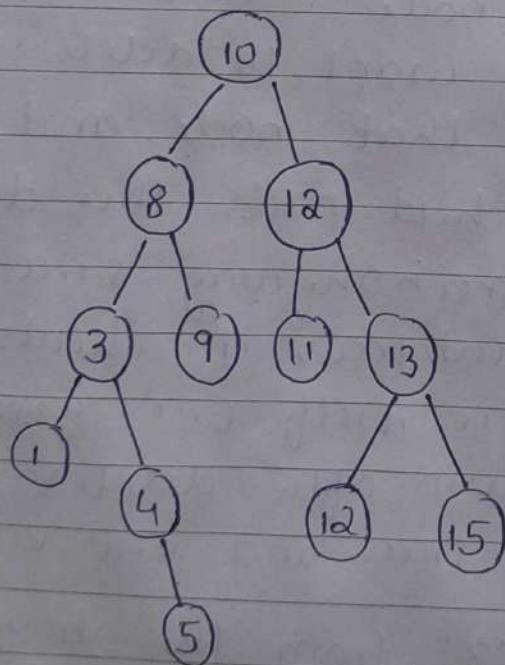
Which is a sorted list.

Time complexity : $O(n \log n)$

Deletion of a node in Binary Search Tree

'Binary Search Tree' is a tree data structure (i.e.) consists of root element / node and descendants of root node (child nodes) and leaf nodes where each node has either 0, 1 or 2 children such that all the nodes on the left of that node (left sub-tree) are lesser than the value of that node, and all the nodes on the right (right sub-tree) are greater than that node.

example:



* All the nodes on the right sub-tree are greater and left sub tree are lesser at every level.

Binary Search Tree

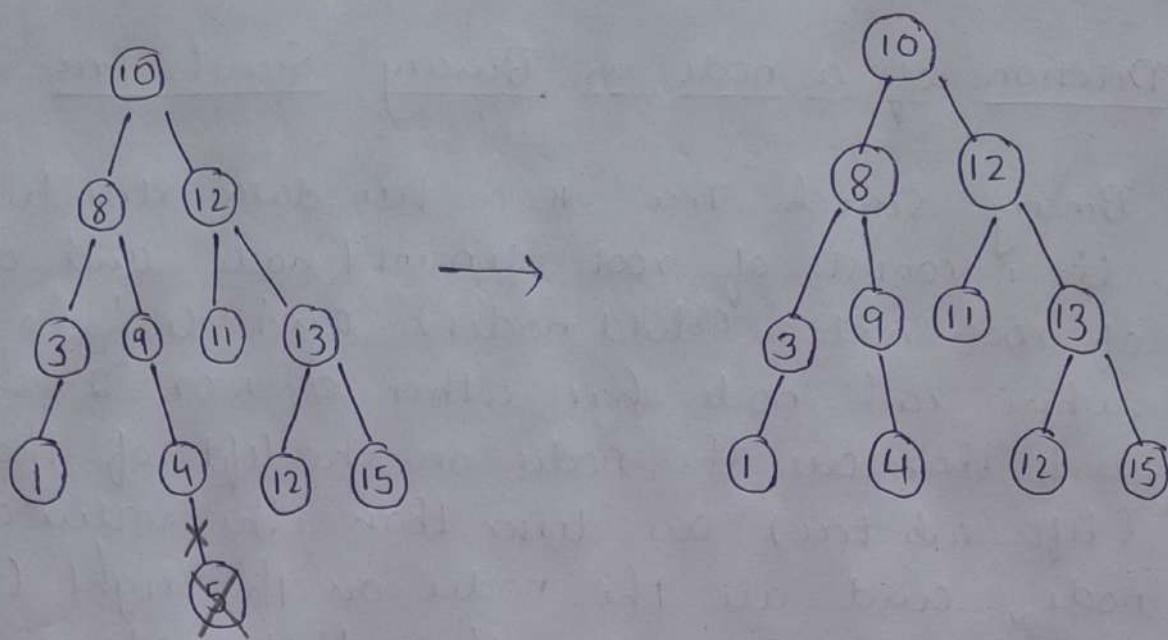
→ Deleting a node from Binary search Tree

→ Case 1: Deleting a node that has no child.

This is the simplest case of deletion in BST. If a node is a leaf node (has no child)

we can simply remove the node by deleting the reference of that node and reclaiming the memory allocated.

example: Deleting '5' from the above BST.

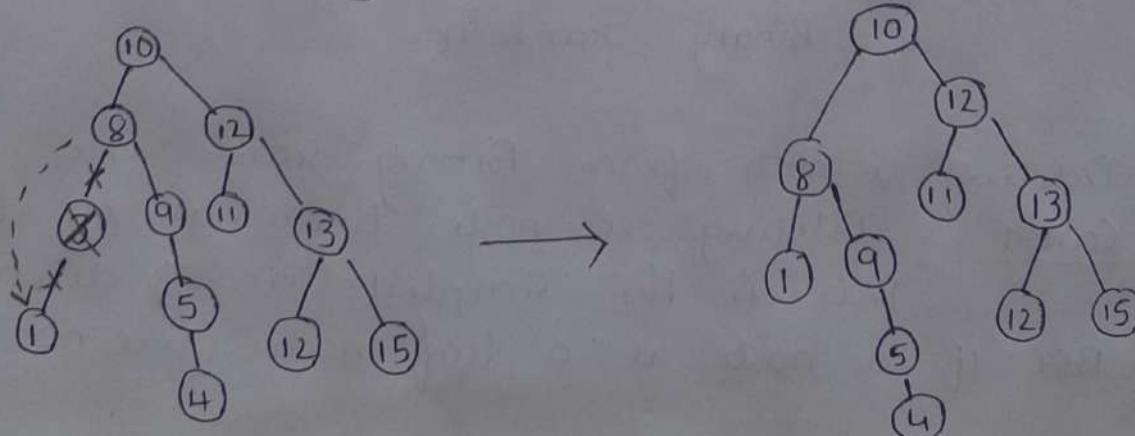


1, 11, 12, 15 are all leaf nodes and can be deleted this way.

→ Case 2: Single child node

When the node we want to delete has a one child we can delete that node, and link its parent to its only child node. This does not exploit the binary search tree in any way since - if the node is on the left sub-tree, its children will also be on the left sub-tree itself (i.e., lesser than the parent node). Hence even after deletion, it would still be a binary search tree and vice versa.

example: Deleting '3' from the above BST



9 and 5 are also single child nodes and can be deleted this way.

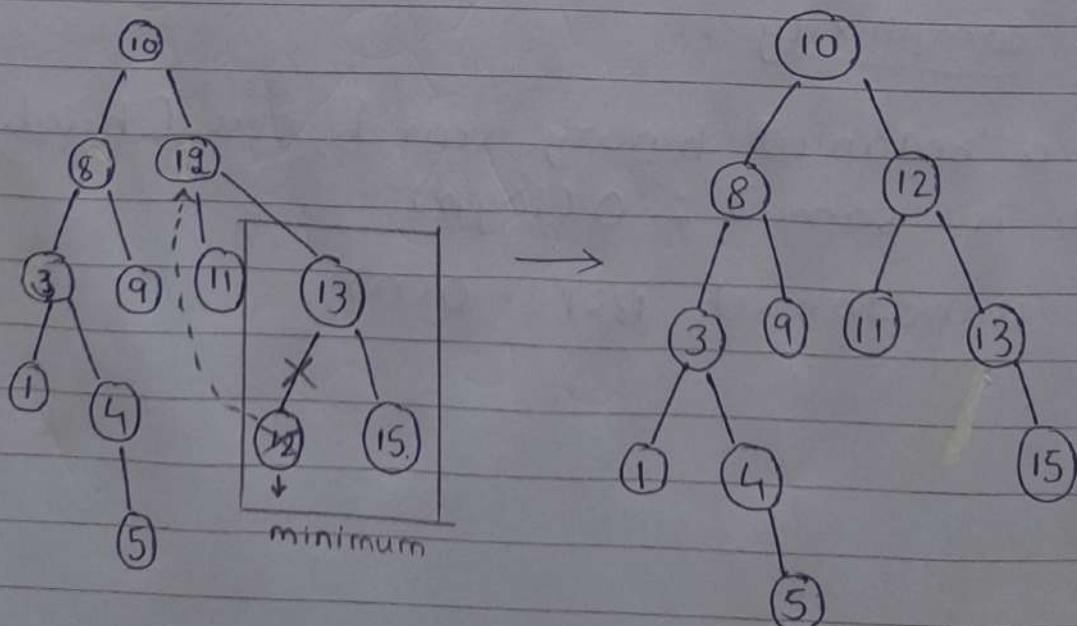
→ Case 3: 2 children node

Solution 1: Find the minimum node in the right subtree, copy the value in the node you want to delete. Delete the duplicate value in the right sub tree.

Why it works?

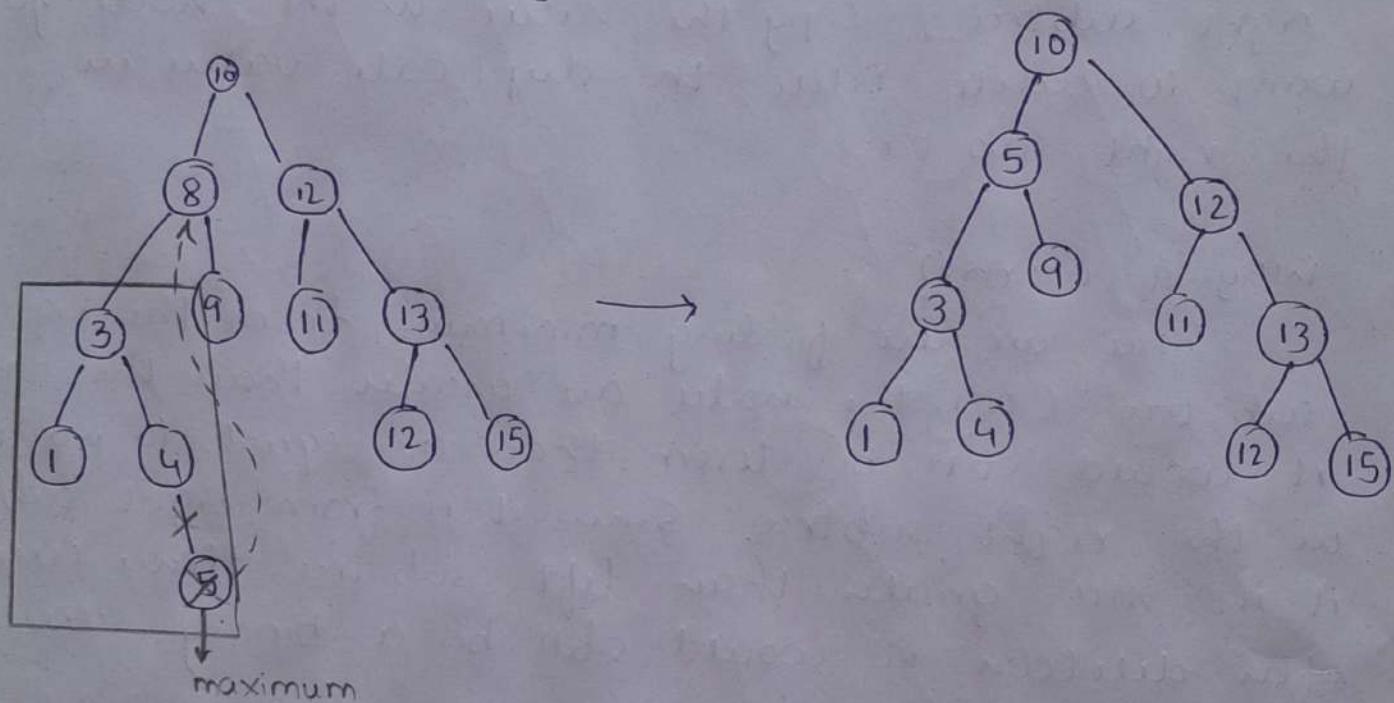
Since we are finding minimum from the right sub tree all the nodes are greater than the nodes in the right subtree. Since it is from right subtree it is still greater than left subtree hence even after deletion it would still be a binary search tree.

Example: Deleting '12' from above BST



Solution 2: Find the maximum in the left sub-tree
 copy the value to the node you want to delete
 remove the duplicate node in the left sub-tree.
 This is another possible way to delete a node
 with 2 children, works the way similar to the
 solution proposed in solution 1.

example: deleting '8' in the above BST



* Time complexity

For a balanced binary search tree (height of each node is same) : $O(\log n)$

for unbalanced BST: $O(n)$

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Section: B

Skill Lab

Group Activity

Topic: 01

Array

"FIND LARGEST SUM CONTIGUOUS SUBARRAY"

Here, the problem statement "Find largest sum contiguous subarray" says that - Among all the subarrays of a array find the subarray that gives maximum sum.

Example:

Let us consider an array:
 $arr = [-2, -3, 4, -1, -2, 1, 5, -3]$

Possible subarrays are:-

$[-2]$, $[-3]$, $[4]$, $[-1]$, $[-2]$, $[1]$, $[5]$, $[-3]$

$[-2, -3]$, $[4, -1]$, $[-2, 1]$, $[5, -3]$

$[-2, -3, 4]$, $[4, -1, -2]$, $[-2, -3, 4, -1]$,

$[4, -1, -2, 1, 5]$

Sum of elements in subarray:-

$$-2 + (-3) = -5 \quad 4 + (-1) = 3 \dots$$

$$-2 + (-3) + 4 + (-1) = -2 \quad 4 + (-1) + (-2) + 1 + 5 = 7$$

Here the largest sum of a subarray is

$$[4, -1, -2, 1, 5] = 7$$

This is the solution.

→ In order to find the solution for the problem statement "Find the largest sum contiguous subarray there are many ways.

One of the best solution approach is by using "Kadane's algorithm".

KADANE'S ALGORITHM

Kadane's Algorithm is a dynamic programming technique, to find the largest sum of a continuous subarray within 1-dimensional array of elements.

- * Kadane's Algorithm can also be used to find largest sum of submatrix within 2-Dimensional or multi-dimensional array.

Steps in Kadane's Algorithm:

Step 1: Initialize variables

- max_so_far = $-\infty$ → To keep track of the maximum sum found so far
- max-ending-far here = 0 → To keep track of the sum of the

current subarray.

Step 2: Iterate through the array.

• For each element num in the array:

1. Add num to max. ending here
2. If max. ending here is greater than max so far, update max so far
3. If max. so. ending here becomes negative, reset it to 0.

Step 3:

Return max. so far as the maximum sum of the contiguous subarray.

Algorithm (Pseudocode):

Initialize max_so_far = -∞

Initialize max_ending_here = 0

for each element num in the array :

 add num to max_ending_here

 if max_ending_here > max_so_far :

 update max_so_far =
 max_ending_here

 if max_ending_here < 0 :

 Reset max_ending_here = 0

Return max_so_far

Let us take program example and understand Kadane's algorithm.

The following code is written in python programming language.

Code:

```
def max_subarray_sum_kadane(sum arr):
    max_so_far = float('-inf')
    max_ending_here = 0

    for num in arr:
        max_ending_here += num
        max_so_far = max(max_so_far, max_ending_here)
        if max_ending_here < 0:
            max_ending_here = 0

    return max_so_far

# Example usage
arr = [-2, -3, 4, -1, -2, +1, 5, -3]
print("Largest sum:", max_subarray_sum_kadane(arr))

Output:-
```

Largest sum(Kadane's Algorithm): 7

Step by Step execution of program:

The above code of Kadane's algorithm to find largest sum subarray works in the following ways:-

The input given is

$$arr = [-2, -3, 4, -1, -2, 1, 5, -3]$$

Execution is as follows:-

Index	Element	max ending here (current subarray)	max so far (Max sum found)
0	-2	-2	-2
1	-3	-3	-2

Since sum can be $-ve$, the above will be reset to 0

2	4	4	4
3	-1	$4 + (-1) = 3$	3
4	-2	$4 + (-1) + (-2) = 1$	1
5	1	$4 + (-1) + (-2) + 1 = 2$	2
6	5	$4 + (-1) + (-2) + 1 + 5 = 7$	7
7	-3	$4 + (-1) + (-2) + 1 + 5 - 3 = 4$	7 (updated)

Here, the largest sum is 7.
Therefore the variable max so far will return 7.
The subarray that gives largest sum is
 $[+4, -1, -2, 1, 5] = 7$

Stack & Queue

"IMPLEMENT STACK USING DEQUE"

Before learning how to implement stack using deque, let us understand what is stack & deque.

Stack:

A stack is a linear data structure that follows LIFO rules (Last In First Out). This means the element inserted last will be removed first.

Deque (double-ended queue):

A deque (pronounced as "deck") is a double-ended queue where elements can be inserted or deleted from both the ends. (front & rear end).

Implementation of stack using deque:

We can implement a stack using deque (double-ended queue) from Python's collections module, as it provides efficient O(1) time complexity for both insertion & deletion at the end.

Steps to implement a stack using deque.

Step 1: Initialize the stack

- create a class Stack
- inside the constructor (`__init__`) define empty deque to store stack elements.

Step 2: Push operation

- use `deque.append(x)` to insert an element at the right end.

Step 3: pop operation

- use `deque.pop()` to remove the last inserted element

Step 4: peek operation

- use `deque[-1]` to retrieve the top element without removing it.

Step 5: check if stack is empty

- check if the deque has zero elements (`len(self.stack) == 0`)

Step 6: Get stack size

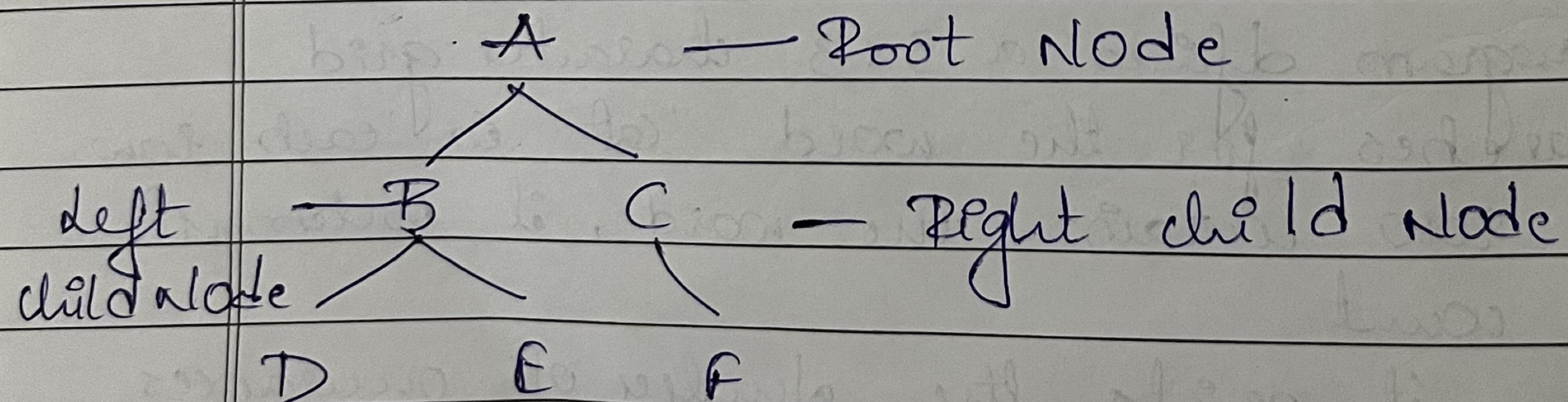
- return the no of elements using `len(self.stack)`

* Tree : — A tree is a hierarchical data structure that consists of nodes where each node has a value and may have child nodes. It is widely used in computer science for organizing data efficiently.

Characteristics of a Tree

1. Root Node : the topmost node in the tree
2. Parent child Relationship : Each node has a parent and may have multiple children
3. Leaf nodes : nodes without children
4. Height of Tree : the longest path from the root of a leaf node.
5. Subtree : a small tree within a large tree.

Example of a tree :



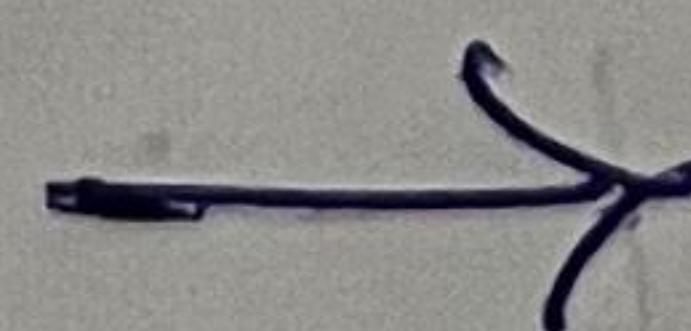
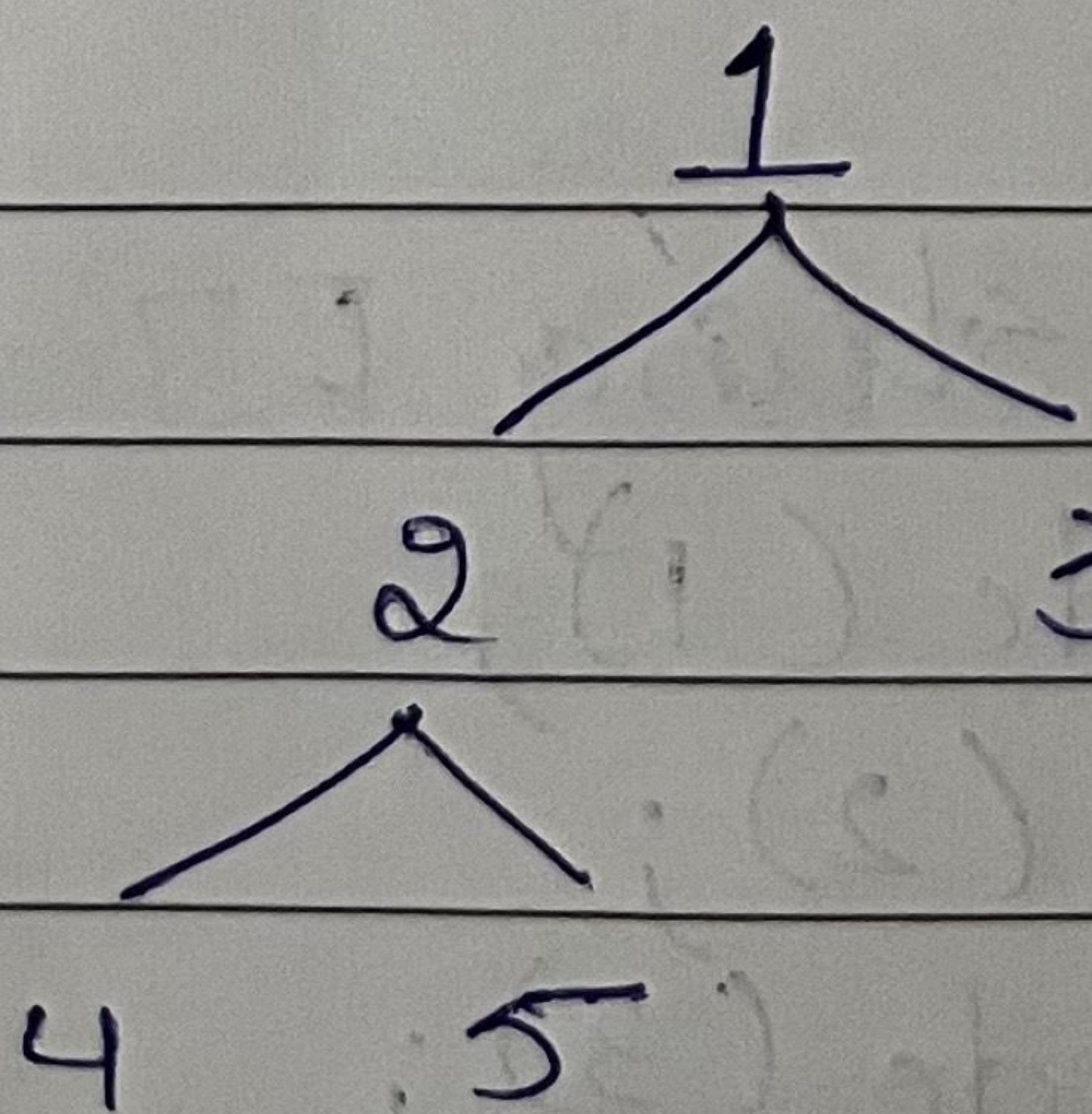
Leaf nodes.

* Mirror of a Tree: A mirror is a tree where the left and right subtrees of every node are swapped. The mirror image of a tree is obtained by recursively swapping the left and right children of all nodes.

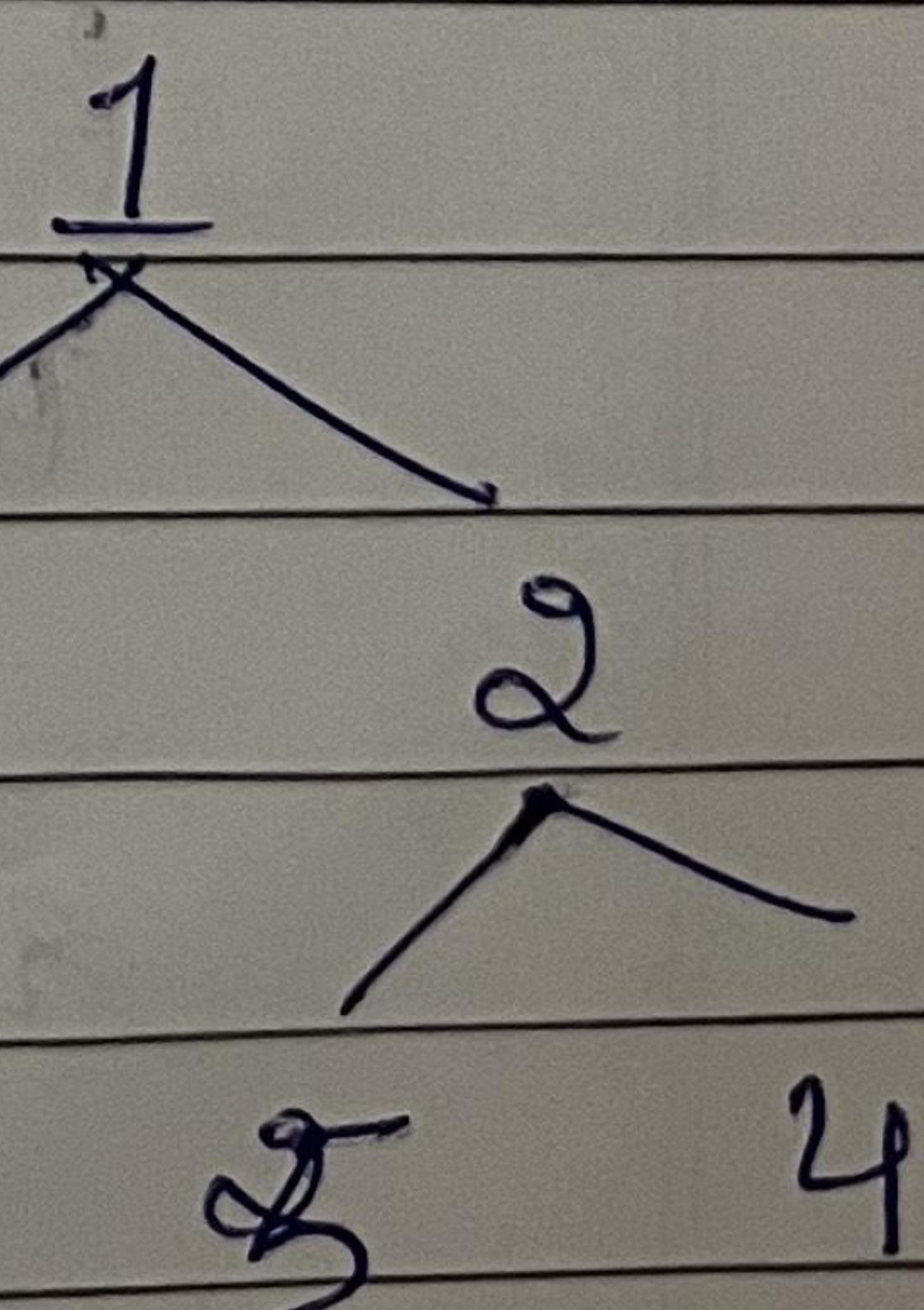
* Characteristics of a Mirror Tree:

1. Left and Right subtrees are swapped
 - Every node's left child becomes the right child and vice versa.
 2. Recursive structure
 - The mirroring process is applied recursively to all subtrees.
 3. Inorder Traversal of original and mirrored trees are opposite.
 - If we perform an inorder traversal on the original and mirrored tree, the results will be reversed
- * Example of a Mirror Tree:

Original Tree



Mirrored tree



- Here the original tree is converted to mirror tree
- The left and right children of every node are swapped.

Program

```

class Node { - represents a tree node
    int data; the value of a node
    Node left, right; - Pointers to child nodes
    Node (int data) { this.data = data; }
}

class MirrorTree {
    static void main (Node node) {
        if (node == null) return;
        Node temp = node.left; swap operations
        node.left = node.right;
        node.right = temp;
        mirror (node.left);
        mirror (node.right);
    }

    static void inorder (Node node) {
        if (node == null) return; In-order traversal
        inorder (node.left); left → root → right Print tree
        System.out.print (node.data + " ");
        inorder (node.right); in sorted order.
    }
}

main - Public static void main (String [] args)
method
    Node root = new Node (1);
    root.left = new Node (2);
    root.right = new Node (3);

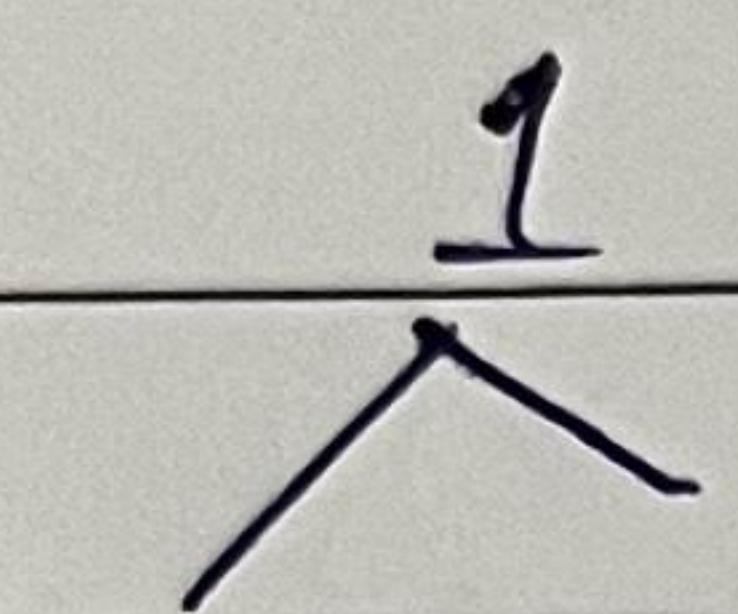
```

```

    inorder (root); Print original tree
    mirror (root); convert to mirror image
    System.out.println();
    inorder (root); Print mirrored tree
}
}

```

Output :- * Given the Binary Tree values.
like 1, 2, 3.

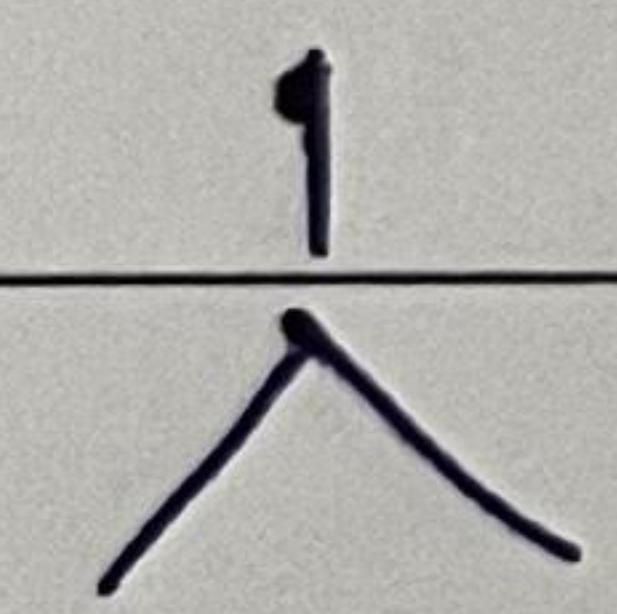


- inorder Traversal (left \rightarrow Root \rightarrow right)
- Traverse left subtree \rightarrow 2
- visit root \rightarrow 1
- Traverse right subtree \rightarrow 3

- output Before mirroring :

2, 1, 3.

* Mirrored Binary Tree after Mirroring



After swapping the left and right subtrees at each node.

3 2

- Inorder Traversal (left \rightarrow root \rightarrow right)
- Traverse left subtree \rightarrow 3
- Visit root \rightarrow 1
- Traverse right subtree \rightarrow 2

- output after mirroring

3, 1, 2

Final Program Output :-

2 1 3

3 1 2

(* Count of number of given string in 2D character array.)

→ Counting the number of times a given string appears in a 2D-character array by checking in all 8 possible directions horizontally, vertically, and diagonally.)

- ① Horizontally - left to right, right to left
- ② Vertically - top to bottom, bottom to top
- ③ Diagonally - four possible diagonal directions

For Example,

consider this 3×3 grid:

c a t
a t c
t c a.

- If we search for "cat", we can find it in different locations and directions.

like;

- ① (0,0) → Right (c → a → t).
- ② (0,0) → Diagonal Down (c → t → a).
- ③ (0,2) → Left (t → a → c).
- ④ (2,0) → Diagonal up (a → t → c).

* Program

```

public class SimpleWordSearch {
    public static void main (String [] args) {
        char [][] grid = {
            {'c', 'a', 't'}, These 3x3 character grid represents
            {'a', 'c', 't'}, letters arranged in rows
            {'t', 'a', 't'} , the goal is to search for word
        }; 'cat' in these rows

        String word = "cat"; it is looking for word cat
        int count = 0;

        for (int i = 0; i < grid.length; i++) { it converts the
            String rowString = new String (grid [i]); row from a
            if (rowString.contains (word)) { character array
                count++; to string (
            }
        }

        System.out.println ("Occurrences of '" + word + "' : "
            + count); it will finally display - the
        word cat.
    }
}

```

Here :

- This Program defines a 3×3 character grid
- It searches for the word "cat" in each row.
- If the row contains the word, it increments the count
- Finally, it prints the number of occurrences

Output :-

Occurrences of 'cat' : 1

Sorting on Array based on set bits

1) What is a set bit?

→ It is a bit that has a value of 1 in the binary representation of a number.

ex: → Binary of 5 = 101 (2 set bits)

.. " 7 = 111 (3 set bits)

2) Problem statement

" Given an array of integers, we need to sort them in descending order based on the number of set bits in their binary representation.

2) Example to illustrate

arr = [5, 3, 7]

number	binary representation	setbit count
5	101	2
3	11	2
7	111	3

sorting based on set bits

1. The number with most bits come first.
2. Same no. of set bits numbers retain original order

- 7 has the highest no. of set bits, so it comes first

3) How to count set bit

1. basic method - normal count
2. Mathematical function - Brian Kernighan's Algo
3. Python provides built-in function $\text{bin}(n).\text{count}(i)$

4) Real life applications

- Cryptography
- Hardware optimization
- Data compression
- Computer networks

5) Time complexity and space complexity

Time complexity

- counting set bits takes $O(\log N)$ (because a number N has $\log_2 N$ bits)
- sorting takes $O(N \log N)$
- Total: $O(N \log N)$

Space complexity

- If sorting is done in place, requires $O(1)$ space extra
- If creates a new list, takes $O(N)$ extra space