

**VISVESVARAYA TECHNOLOGICAL  
UNIVERSITY**

“JnanaSangama”, Belgaum -590014, Karnataka.



**LAB REPORT**

**on**

**Artificial Intelligence (23CS5PCAIN)**

*Submitted by*

**ANANYA N GOWDA (1BM23CS034)**

*in partial fulfillment for the award of the degree of*

**BACHELOR OF ENGINEERING**

*in*

**COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING**

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Bull Temple Road, Bangalore 560019**  
(Affiliated To Visvesvaraya Technological University, Belgaum)  
**Department of Computer Science and Engineering**



**CERTIFICATE**

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **ANANYA N GOWDA (1BM23CS034)**, who is a bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

Dr. K R Mamatha Assistant Professor Department of CSE, BMSCE	Dr. Kavitha Sooda Professor & HOD Department of CSE, BMSCE
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# Index

<b>Sl. No.</b>	<b>Experiment Title</b>	<b>Page No.</b>
1	Implement Tic –Tac –Toe Game Implement vacuum cleaner agent	6-15
2	Solve 8 puzzle problems Implement Iterative deepening search algorithm	16-24
3	Implement A* search algorithm	25-33
4	Implement Hill Climbing search algorithm to solve N-Queens problem	34-36
5	Simulated Annealing to Solve 8-Queens problem	37-38
6	Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.	39-41
7	Implement unification in first order logic	42-44ss
8	Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.	45-46
9	Create a knowledge base consisting of first order logic statements and prove the given query using Resolution	47-53
10	Implement Alpha-Beta Pruning.	54-55

**Github Link:**

<https://github.com/ananyarex/AI-Lab>

Artificial Intelligence Foundation Course Certificates:



## CERTIFICATE OF ACHIEVEMENT

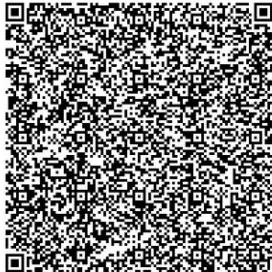
The certificate is awarded to

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## Program 1

Implement Tic - Tac - Toe Game

### Algorithm:

\* TIC TAC TOE

mini max algorithm

- mini : opponent trying to minimize your score (comp)
- max : you trying to maximize your score.

Scoring system:  
+1 if comp wins  
-1 if you win  
0 if its a tie.

maximise player  
best score = - $\infty$   
for each empty spot, make the best move  
update score if min possibility is true  
return best score

minimise score  
best score = + $\infty$   
make move for empty spot  
update score if win possibilities  
return best score

If game is won  
return +1 if comp wins  
-1 if we win  
if game tied,  
return 0.

output:

enter pos(0-8) : 4	
X	0

enter pos(0-8) : 8	
X	0   X
	0

enter pos(0-8) : 1	
X	0
0	X
	0

enter pos(0-8) : 2	
X	0   0
0	X
X	0

enter pos(0-8) : 6	
X	0   0
0	X
0	X   0

Its a draw.

### Code:

```
def print_board(board):
    print("\nCurrent Board:")
    for row in board:
        print(row)
    print()

def check_winner(board, player):
    for i in range(3):
        if all(cell == player for cell in board[i]):
            return True
```

```

if all(board[j][i] == player for j in range(3)):
    return True

if all(board[i][i] == player for i in range(3)):
    return True
if all(board[i][2 - i] == player for i in range(3)):
    return True

return False

def is_full(board):
    return all(cell != " " for row in board for cell in row)

def tic_tac_toe():
    board = [[" " for _ in range(3)] for _ in range(3)]
    current_player = "X"
    move_count = 0

    print("Tic-Tac-Toe Game (3x3 Matrix Format)\n")
    print_board(board)

    while True:
        try:
            row = int(input(f"Player {current_player}, enter row (0-2): "))
            col = int(input(f"Player {current_player}, enter col (0-2): "))
        except ValueError:
            print("Please enter integers between 0 and 2.")
            continue

        if not (0 <= row <= 2 and 0 <= col <= 2):
            print("Invalid position. Try again.")
            continue
        if board[row][col] != " ":
            print("Cell already filled. Choose another.")
            continue

        board[row][col] = current_player
        move_count += 1
        print_board(board)

        if check_winner(board, current_player):
            print(f"Player {current_player} wins!")

```

```

break

if is_full(board):
    print("Game is a draw.")
    break

current_player = "O" if current_player == "X" else "X"

print(f"Total moves (cost): {move_count}")

tic_tac_toe()

```

### **Output case1:**

Tic-Tac-Toe Game (3x3 Matrix Format)

Current Board:

```
[ ' ', ' ', ' ']
[ ' ', ' ', ' ']
[ ' ', ' ', ' ']
```

Player X, enter row (0-2): 1  
 Player X, enter col (0-2): 1

Current Board:

```
[ ' ', ' ', ' ']
[ ' ', 'X', ' ']
[ ' ', ' ', ' ']
```

Player O, enter row (0-2): 0  
 Player O, enter col (0-2): 2

Current Board:

```
[ ' ', ' ', 'O']
[ ' ', 'X', ' ']
[ ' ', ' ', ' ']
```

Player X, enter row (0-2): 1  
 Player X, enter col (0-2): 0

Current Board:

```
[ ' ', ' ', 'O']
[X, 'X', ' ']
[ ' ', ' ', ' ']
```

Player O, enter row (0-2): 2  
 Player O, enter col (0-2): 1

Current Board:

```
[ ' ', ' ', 'O']
[X, 'X', ' ']
[ ' ', 'O', ' ']
```

Player X, enter row (0-2): 2

```
Player X, enter col (0-2): 2
```

```
Current Board:
```

```
[ ' ', ' ', 'O' ]  
[ 'X', 'X', ' ' ]  
[ ' ', 'O', 'X' ]
```

```
Player O, enter row (0-2): 2
```

```
Player O, enter col (0-2): 0
```

```
Current Board:
```

```
[ ' ', ' ', 'O' ]  
[ 'X', 'X', ' ' ]  
[ 'O', 'O', 'X' ]
```

```
Player X, enter row (0-2): 0
```

```
Player X, enter col (0-2): 1
```

```
Current Board:
```

```
[ ' ', 'X', 'O' ]  
[ 'X', 'X', ' ' ]  
[ 'O', 'O', 'X' ]
```

```
Player O, enter row (0-2): 1
```

```
Player O, enter col (0-2): 2
```

```
Current Board:
```

```
[ ' ', 'X', 'O' ]  
[ 'X', 'X', 'O' ]  
[ 'O', 'O', 'X' ]
```

```
Player X, enter row (0-2): 0
```

```
Player X, enter col (0-2): 0
```

```
Current Board:
```

```
[ 'X', 'X', 'O' ]  
[ 'X', 'X', 'O' ]  
[ 'O', 'O', 'X' ]
```

```
Player X wins!
```

```
Total moves (cost): 9
```

---

### Output case2:

```
Tic-Tac-Toe Game (3x3 Matrix Format)
```

```
Current Board:
```

```
[ ' ', ' ', ' ' ]  
[ ' ', ' ', ' ' ]  
[ ' ', ' ', ' ' ]
```

```
Player X, enter row (0-2): 0
```

```
Player X, enter col (0-2): 2
```

```
Current Board:
```

```
[ ' ', ' ', 'X' ]
```

```
[ ' ', ' ', ' ']  
[ ' ', ' ', ' ']
```

```
Player O, enter row (0-2): 2  
Player O, enter col (0-2): 1
```

Current Board:

```
[ ' ', ' ', 'X'][ ' ', ' ', ' ']  
[ ' ', 'O', ' ']
```

```
Player X, enter row (0-2): 0  
Player X, enter col (0-2): 0
```

Current Board:

```
[ 'X', ' ', 'X'][ ' ', ' ', ' ']  
[ ' ', 'O', ' ']
```

```
Player O, enter row (0-2): 0  
Player O, enter col (0-2): 1
```

Current Board:

```
[ 'X', 'O', 'X'][ ' ', ' ', ' ']  
[ ' ', 'O', ' ']
```

```
Player X, enter row (0-2): 2  
Player X, enter col (0-2): 0
```

Current Board:

```
[ 'X', 'O', 'X'][ ' ', ' ', ' ']  
[ 'X', 'O', ' ']
```

```
Player O, enter row (0-2): 1  
Player O, enter col (0-2): 1
```

Current Board:

```
[ 'X', 'O', 'X'][ ' ', 'O', ' ']  
[ 'X', 'O', ' ']
```

```
Player O wins!  
Total moves (cost): 6
```

---

### Output case3:

Tic-Tac-Toe Game (3x3 Matrix Format):

Current Board:

```
[ ' ', ' ', ' '][ ' ', ' ', ' ']  
[ ' ', ' ', ' ']
```

```
Player X, enter row (0-2): 1  
Player X, enter col (0-2): 0
```

```
Current Board:
```

```
[ ' ', ' ', ' ']  
[ 'X', ' ', ' ']  
[ ' ', ' ', ' ']
```

```
Player O, enter row (0-2): 0  
Player O, enter col (0-2): 2
```

```
Current Board:
```

```
[ ' ', ' ', 'O ']  
[ 'X', ' ', ' ']  
[ ' ', ' ', ' ']
```

```
Player X, enter row (0-2): 2  
Player X, enter col (0-2): 0
```

```
Current Board:
```

```
[ ' ', ' ', 'O ']  
[ 'X', ' ', ' ']  
[ 'X', ' ', ' ']
```

```
Player O, enter row (0-2): 0  
Player O, enter col (0-2): 0
```

```
Current Board:
```

```
[ 'O', ' ', 'O ']  
[ 'X', ' ', ' ']  
[ 'X', ' ', ' ']
```

```
Player X, enter row (0-2): 0  
Player X, enter col (0-2): 1
```

```
Current Board:
```

```
[ 'O', 'X', 'O ']  
[ 'X', ' ', ' ']  
[ 'X', ' ', ' ']
```

```
Player O, enter row (0-2): 2  
Player O, enter col (0-2): 1
```

```
Current Board:
```

```
[ 'O', 'X', 'O ']  
[ 'X', ' ', ' ']  
[ 'X', 'O', ' ' ]
```

```
Player X, enter row (0-2): 2  
Player X, enter col (0-2): 2
```

```
Current Board:
```

```
[ 'O', 'X', 'O ']  
[ 'X', ' ', ' ']  
[ 'X', 'O', 'X' ]
```

```
Player O, enter row (0-2): 1  
Player O, enter col (0-2): 1
```

```
Current Board:
```

```
['O', 'X', 'O']  
['X', 'O', ' ']  
['X', 'O', 'X']
```

```
Player X, enter row (0-2): 1  
Player X, enter col (0-2): 2
```

```
Current Board:
```

```
['O', 'X', 'O']  
['X', 'O', 'X']  
['X', 'O', 'X']
```

```
Game is a draw.
```

```
Total moves (cost): 9
```

## Implement vacuum cleaner agent

### Algorithm:

LAB - 1	Date <u>20/8/25</u>	Page _____
* Robot vacuum cleaner algorithm		
→ 2 dimensional array $n \times m$ initial pos $(0,0)$		
→ visited array: to store coordinates of every cell it has cleaned		
→ recursive dfs() if the current cell is visited, mark it clean() explore all 4 directions (up, down, left, right)		
→ After the recursive dfs() ends, we need to get the robot back to initial position. Fix the change direction() to right or left only, to ensure uniformity.		
* FIGURE		
* Output :		
Robot starts at room 0 move to 1 and clean move to 2 and clean move to 3 and clean move to 0 and clean stay at 0 and finish cleaning		

**Code:**

```
def vacuum_cleaner()
    A = int(input("Enter state of A (0 for clean, 1 for dirty): "))
    B = int(input("Enter state of B (0 for clean, 1 for dirty): "))
    location = input("Enter location (A or B): ").upper()

    cost = 0
    state = {'A': A, 'B': B}

    if location == 'A':
        if state['A'] == 1: # If A is dirty
            print("Cleaned A.")
            state['A'] = 0
            cost += 1
        else:
            print("A is clean")

        if state['B'] == 1: # If B is dirty
            print("Moving vacuum right")
            print("Cleaned B.")
            state['B'] = 0
            cost += 1
            print("Is B clean now? (0 if clean, 1 if dirty):", state['B'])
            print("Is A dirty? (0 if clean, 1 if dirty):", state['A'])
            print("B is clean")
            print("Moving vacuum left")
        else:
            print("Turning vacuum off")

    elif location == 'B':
        if state['B'] == 1: # If B is dirty
            print("Cleaned B.")
            state['B'] = 0
            cost += 1
        else:
            print("B is clean")

        if state['A'] == 1: # If A is dirty
            print("Moving vacuum left")
            print("Cleaned A.")
            state['A'] = 0
            cost += 1
            print("Is A clean now? (0 if clean, 1 if dirty):", state['A'])
            print("Is B dirty? (0 if clean, 1 if dirty):", state['B'])
            print("A is clean")
```

```

        print("Moving vacuum right")
else:
    print("Turning vacuum off")

print("Cost:", cost)
print(state)

vacuum_cleaner()

```

### **OUTPUT Case1:**

```

Enter state of A (0 for clean, 1 for dirty): 1
Enter state of B (0 for clean, 1 for dirty): 1
Enter location (A or B): A
Cleaned A.
Moving vacuum right
Cleaned B.
Is B clean now? (0 if clean, 1 if dirty): 0
Is A dirty? (0 if clean, 1 if dirty): 0
B is clean
Moving vacuum left
Cost: 2
{'A': 0, 'B': 0}

```

### **OUTPUT Case2:**

```

Enter state of A (0 for clean, 1 for dirty): 0
Enter state of B (0 for clean, 1 for dirty): 1
Enter location (A or B): A
A is clean
Moving vacuum right
Cleaned B.
Is B clean now? (0 if clean, 1 if dirty): 0
Is A dirty? (0 if clean, 1 if dirty): 0
B is clean
Moving vacuum left
Cost: 1
{'A': 0, 'B': 0}

```

### **OUTPUT Case3:**

```

Enter state of A (0 for clean, 1 for dirty): 0
Enter state of B (0 for clean, 1 for dirty): 0
Enter location (A or B): A
A is clean
Turning vacuum off
Cost: 0
{'A': 0, 'B': 0}

```

## Program2

Implement Iterative deepening search algorithm

### Algorithm:

<p>LAB-2 Date _____ Page 3/9/25</p> <p>8-puzzle using misplaced tiles and Manhattan distance and IDDFS.</p> <p>Perform iterative deepening search (IDDFS)</p> <pre> graph TD     A((A)) --&gt; B((B))     A --&gt; C((C))     B --&gt; D((D))     B --&gt; E((E))     C --&gt; F((F))     C --&gt; G((G))     D --&gt; H((H))     D --&gt; I((I))     E --&gt; J((J))     F --&gt; K((K))     K --&gt; Goal((Goal))   </pre> <p>soln</p> <table border="1" style="margin-left: 20px; border-collapse: collapse;"> <thead> <tr> <th>depth</th> <th>IDDFS</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>A</td> </tr> <tr> <td>1</td> <td>ABC</td> </tr> <tr> <td>2</td> <td>ABDECFG</td> </tr> <tr> <td>3</td> <td>ABDHIEJCFKG</td> </tr> </tbody> </table>	depth	IDDFS	0	A	1	ABC	2	ABDECFG	3	ABDHIEJCFKG	<p>8-puzzle problem.</p> <p>operation: The 8 puzzle problem has a 3x3 grid with numbering 1-8 and a blank space. The end goal is to solve the jumbled arrangement and find/get the end result.</p> <p>Possible move : up, down, left, right.</p> <p>example</p> <pre> graph TD     846 --&gt; 57     846 --&gt; 231     846 --&gt; 86     846 --&gt; 547     57 --&gt; 123     57 --&gt; 48-     231 --&gt; 123     231 --&gt; 485     86 --&gt; 75     86 --&gt; 76     547 --&gt; 75     547 --&gt; 76     123 --&gt; 123     123 --&gt; 485     123 --&gt; 485     48- --&gt; 76     48- --&gt; 786     75 --&gt; 123     75 --&gt; 485     76 --&gt; 123     76 --&gt; 485     76 --&gt; 786   </pre> <p>(PTO)</p>
depth	IDDFS										
0	A										
1	ABC										
2	ABDECFG										
3	ABDHIEJCFKG										

### Code:

```
def get_neighbors(state):
    neighbors = []
    idx = state.index("0")
    moves = [(-1, 0), (1, 0), (0, -1), (0, 1)]
    x, y = divmod(idx, 3)
```

for dx, dy in moves:

    nx, ny = x + dx, y + dy

```

if 0 <= nx < 3 and 0 <= ny < 3:
    new_idx = nx * 3 + ny
    state_list = list(state)
    state_list[idx], state_list[new_idx] = state_list[new_idx], state_list[idx]
    neighbors.append("".join(state_list))
return neighbors

def dfs_limit(start_state, goal_state, limit):
    stack = [(start_state, 0)]
    visited = set()
    parent = {start_state: None}
    path = []

    while stack:
        current_state, depth = stack.pop()

        if current_state == goal_state:
            while current_state:
                path.append(current_state)
                current_state = parent[current_state]
            return path[::-1]

        if depth < limit and current_state not in visited:
            visited.add(current_state)
            neighbors = get_neighbors(current_state)
            neighbors.reverse() # Maintain consistent exploration order
            for neighbor in neighbors:
                if neighbor not in visited:
                    parent[neighbor] = current_state
                    stack.append((neighbor, depth + 1))

    return None

def iddfs(start_state, goal_state, max_depth):
    for limit in range(max_depth + 1):
        print(f"Searching with depth limit: {limit}")
        solution = dfs_limit(start_state, goal_state, limit)
        if solution:
            return solution
    return None

print("Enter the initial state (enter 3 digits per row, separated by spaces, 0 for empty):")
initial_state_rows = []
for i in range(3):
    row = input(f"Row {i+1}: ").split()
    initial_state_rows.extend(row)
initial_state = "".join(initial_state_rows)

print("\nEnter the goal state (enter 3 digits per row, separated by spaces, 0 for empty):")
goal_state_rows = []
for i in range(3):
    row = input(f"Row {i+1}: ").split()
    goal_state_rows.extend(row)

```

```

goal_state = "".join(goal_state_rows)

max_depth = 50

solution = iddfs(initial_state, goal_state, max_depth)

if solution:
    print("\nIDDFS solution path:")
    for s in solution:
        print(s[:3])
        print(s[3:6])
        print(s[6:])
        print()
else:
    print(f"\nNo solution found within the maximum depth of {max_depth}.")

```

## Output:

```

Enter the initial state (enter 3 digits per row, separated by spaces, 0 for empty):
Row 1: 283
Row 2: 164
Row 3: 765

Enter the goal state (enter 3 digits per row, separated by spaces, 0 for empty):
Row 1: 123
Row 2: 084
Row 3: 765

Searching with depth limit: 0
Searching with depth limit: 1
Searching with depth limit: 2
Searching with depth limit: 3
Searching with depth limit: 4
Searching with depth limit: 5

IDDFS solution path:
283
164
765

283
164
765

283
184
765

023
184
765

123
084
765

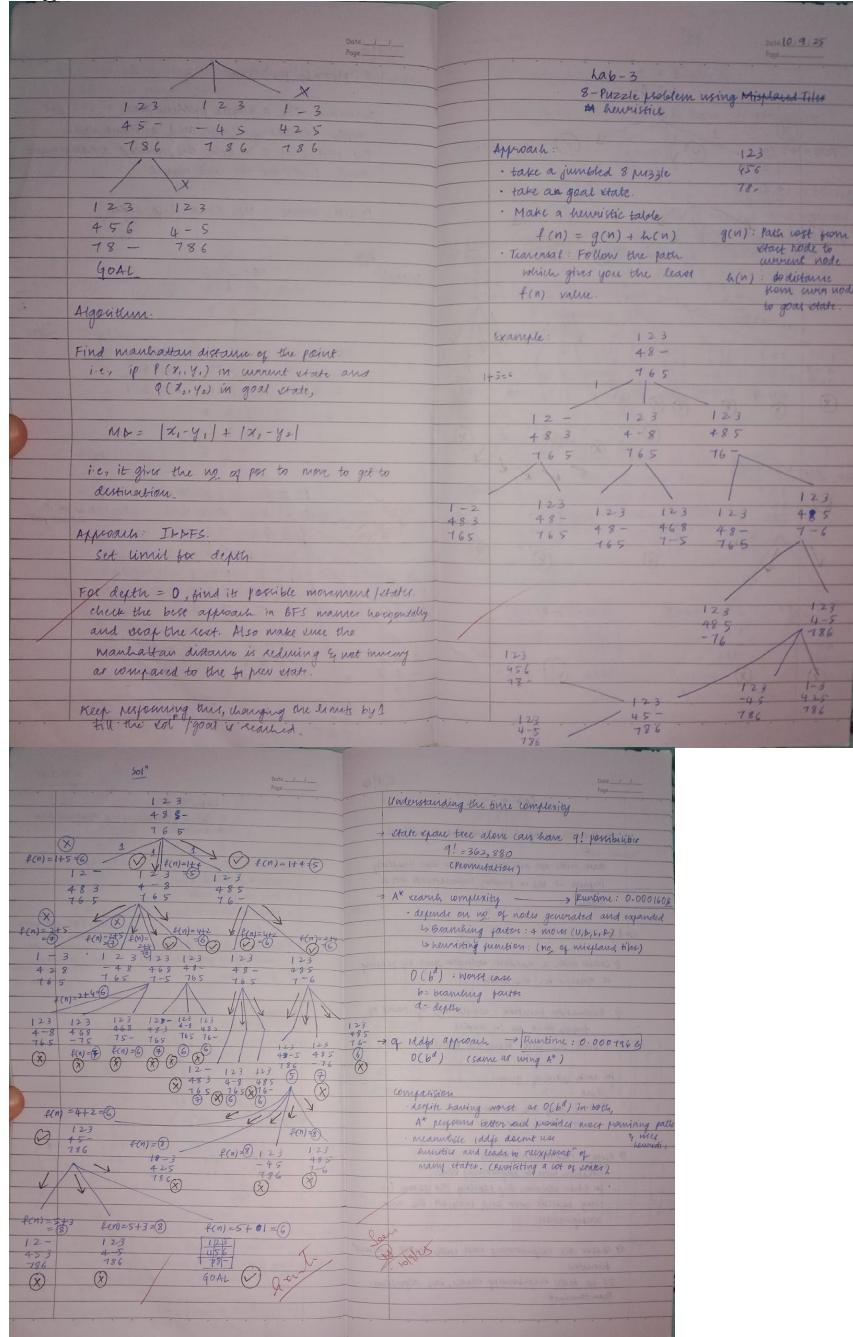
123
804
765

```

## Program3

Implement A\* search algorithm

### Algorithm:



**Code:**

```
#MISPLACED TILE
import heapq
from itertools import count

def misplaced_heuristic(board, goal):
    """h(n): number of tiles not in their goal position (excluding blank 0)."""
    n = len(board)
    misplaced = 0
    for i in range(n):
        for j in range(n):
            if board[i][j] != 0 and board[i][j] != goal[i][j]:
                misplaced += 1
    return misplaced

def find_blank(board):
    n = len(board)
    for i in range(n):
        for j in range(n):
            if board[i][j] == 0:
                return i, j
    raise ValueError("Board does not contain a blank tile (0)")

def neighbors(board):
    """Generate neighboring boards by sliding one tile into the blank."""
    n = len(board)
    x, y = find_blank(board)
    dirs = [(0,1),(0,-1),(1,0),(-1,0)]
    res = []
    for dx, dy in dirs:
        nx, ny = x + dx, y + dy
        if 0 <= nx < n and 0 <= ny < n:
            b = [list(row) for row in board]
            b[x][y], b[nx][ny] = b[nx][ny], b[x][y]
            res.append(tuple(tuple(row) for row in b))
    return res

def flatten(board):
    return [x for row in board for x in row]

def inversion_count(seq):
    arr = [x for x in seq if x != 0]
    inv = 0
    for i in range(len(arr)):
        for j in range(i+1, len(arr)):
            if arr[i] > arr[j]:
                inv += 1
    return inv

def blank_row_from_bottom(board):
    n = len(board)
    for i in range(n):
```

```

for j in range(n):
    if board[i][j] == 0:
        return n - i
raise ValueError("Board does not contain a blank tile (0)")

def is_solvable(start, goal):
    """General n-puzzle solvability test (odd/even width)."""
    n = len(start)
    start_flat = flatten(start)
    goal_flat = flatten(goal)

    pos = {val: idx for idx, val in enumerate(goal_flat)}
    start_perm = [pos[val] for val in start_flat]

    inv = inversion_count(start_perm)

    if n % 2 == 1:
        # odd grid: inversions parity must be even
        return inv % 2 == 0
    else:
        # even grid: blank row from bottom parity matters
        blank_row = blank_row_from_bottom(start)
        goal_blank_row = blank_row_from_bottom(goal)
        # When using relative permutation to goal, parity of blank rows must match
        return (inv + blank_row) % 2 == (0 + goal_blank_row) % 2

def reconstruct_path(came_from, current):
    path = [current]
    while current in came_from:
        current = came_from[current]
        path.append(current)
    path.reverse()
    return path

def a_star_misplaced(start, goal):
    start = tuple(tuple(row) for row in start)
    goal = tuple(tuple(row) for row in goal)

    if len(start) != len(start[0]) or len(goal) != len(goal[0]) or len(start) != len(goal):
        raise ValueError("Initial and goal must be square boards of the same size.")

    start_vals = sorted(flatten(start))
    goal_vals = sorted(flatten(goal))
    if start_vals != goal_vals:
        raise ValueError("Initial and goal must contain the same set of tiles.")

    if not is_solvable(start, goal):
        return None, None, 0, 0 # unsolvable

    counter = count() # tie-breaker

    h0 = misplaced_heuristic(start, goal)

```

```

g_score = {start: 0}
f0 = h0

open_heap = [(f0, next(counter), start)]
open_set = {start: f0}
closed = set()
came_from = {}

expansions = 0

while open_heap:
    _, _, current = heapq.heappop(open_heap)
    if current in closed:
        continue
    closed.add(current)

    if current == goal:
        path = reconstruct_path(came_from, current)
        return path, g_score[current], expansions, len(closed)

    expansions += 1

    for nb in neighbors(current):
        tentative_g = g_score[current] + 1
        if nb in closed:
            continue
        if nb not in g_score or tentative_g < g_score[nb]:
            came_from[nb] = current
            g_score[nb] = tentative_g
            h = misplaced_heuristic(nb, goal)
            f = tentative_g + h
            if nb not in open_set or f < open_set[nb]:
                heapq.heappush(open_heap, (f, next(counter), nb))
                open_set[nb] = f

return None, None, expansions, len(closed)

def read_board(n, prompt):
    print(prompt)
    board = []
    for i in range(n):
        row = list(map(int, input().split()))
        if len(row) != n:
            raise ValueError(f"Row {i+1} must contain exactly {n} integers.")
        board.append(row)
    return board

def print_board(board):
    for row in board:
        print(" ".join(f"{x}" for x in row))

def main():

```

```

try:
    n = int(input("Enter puzzle size n (e.g., 3 for 3x3): ").strip())
    initial = read_board(n, "Enter initial state row by row (use 0 for blank):")
    goal = read_board(n, "Enter goal state row by row (use 0 for blank):")

    result = a_star_misplaced(initial, goal)
    path, cost, expansions, explored = result

    if path is None:
        print("No solution (unsolvable with given start/goal).")
        return

    print("\nSolution path (each state shows g, h, f):\n")
    for idx, state in enumerate(path):
        g = idx # each step costs 1
        h = misplaced_heuristic(state, tuple(tuple(r) for r in goal))
        f = g + h
        print(f"Step {idx}: g={g}, h={h}, f={f}")
        print_board(state)
        print()

    print(f"Total cost (number of moves): {cost}")
    print(f"Nodes expanded: {expansions}")
    print(f"Nodes explored (unique): {explored}")

except Exception as e:
    print("Error:", e)

if __name__ == "__main__":
    main()

```

## Output:

```

Enter puzzle size n (e.g., 3 for 3x3): 3
Enter initial state row by row (use 0 for blank):
2 8 3
1 6 4
7 0 5
Enter goal state row by row (use 0 for blank):
1 2 3
8 0 4
7 6 5

Solution path (each state shows g, h, f):

Step 0: g=0, h=4, f=4
2 8 3
1 6 4
7 0 5

Step 1: g=1, h=3, f=4
2 8 3
1 6 4
7 0 5

Step 2: g=2, h=3, f=5
2 0 3
1 8 4
7 6 5

Step 3: g=3, h=2, f=5
0 2 3
1 8 4
7 6 5

Step 4: g=4, h=1, f=5
1 2 3
0 8 4
7 6 5

Step 5: g=5, h=0, f=5
1 2 3
8 0 4
7 6 5

Total cost (number of moves): 5
Nodes expanded: 6
Nodes explored (unique): 7

```

**Code:**

```
#MANHATTAN DISTANCE
import heapq
from itertools import count

def misplaced_heuristic(board, goal):
    misplaced = 0
    n = len(board)
    for i in range(n):
        for j in range(n):
            if board[i][j] != 0 and board[i][j] != goal[i][j]:
                misplaced += 1
    return misplaced

def manhattan_heuristic(board, goal):
    n = len(board)
    # Map goal positions for each tile
    goal_pos = {}
    for i in range(n):
        for j in range(n):
            goal_pos[goal[i][j]] = (i, j)

    dist = 0
    for i in range(n):
        for j in range(n):
            val = board[i][j]
            if val != 0:
                gi, gj = goal_pos[val]
                dist += abs(i - gi) + abs(j - gj)
    return dist

def find_blank(board):
    n = len(board)
    for i in range(n):
        for j in range(n):
            if board[i][j] == 0:
                return i, j
    raise ValueError("Board does not contain a blank tile (0)")

def neighbors(board):
    n = len(board)
    x, y = find_blank(board)
    dirs = [(0,1),(0,-1),(1,0),(-1,0)]
    res = []
    for dx, dy in dirs:
        nx, ny = x + dx, y + dy
        if 0 <= nx < n and 0 <= ny < n:
            b = [list(row) for row in board]
            b[x][y], b[nx][ny] = b[nx][ny], b[x][y]
            res.append(tuple(tuple(row) for row in b))
    return res
```

```

def flatten(board):
    return [x for row in board for x in row]

def inversion_count(seq):
    arr = [x for x in seq if x != 0]
    inv = 0
    for i in range(len(arr)):
        for j in range(i+1, len(arr)):
            if arr[i] > arr[j]:
                inv += 1
    return inv

def blank_row_from_bottom(board):
    n = len(board)
    for i in range(n):
        for j in range(n):
            if board[i][j] == 0:
                return n - i
    raise ValueError("Board does not contain a blank tile (0)")

def is_solvable(start, goal):
    n = len(start)
    start_flat = flatten(start)
    goal_flat = flatten(goal)

    pos = {val: idx for idx, val in enumerate(goal_flat)}
    start_perm = [pos[val] for val in start_flat]

    inv = inversion_count(start_perm)

    if n % 2 == 1:
        return inv % 2 == 0
    else:
        blank_row = blank_row_from_bottom(start)
        goal_blank_row = blank_row_from_bottom(goal)
        return (inv + blank_row) % 2 == (0 + goal_blank_row) % 2

def reconstruct_path(came_from, current):
    path = [current]
    while current in came_from:
        current = came_from[current]
        path.append(current)
    path.reverse()
    return path

def a_star_manhattan(start, goal):
    start = tuple(tuple(row) for row in start)
    goal = tuple(tuple(row) for row in goal)

    if len(start) != len(start[0]) or len(goal) != len(goal[0]) or len(start) != len(goal):
        raise ValueError("Initial and goal must be square boards of the same size.")

```

```

start_vals = sorted(flatten(start))
goal_vals = sorted(flatten(goal))
if start_vals != goal_vals:
    raise ValueError("Initial and goal must contain the same set of tiles.")

if not is_solvable(start, goal):
    return None, None, 0, 0

counter = count()
h0 = manhattan_heuristic(start, goal)
g_score = {start: 0}
f0 = h0

open_heap = [(f0, next(counter), start)]
open_set = {start: f0}
closed = set()
came_from = {}

expansions = 0

while open_heap:
    _, _, current = heapq.heappop(open_heap)
    if current in closed:
        continue
    closed.add(current)

    if current == goal:
        path = reconstruct_path(came_from, current)
        return path, g_score[current], expansions, len(closed)

    expansions += 1

    for nb in neighbors(current):
        tentative_g = g_score[current] + 1
        if nb in closed:
            continue
        if nb not in g_score or tentative_g < g_score[nb]:
            came_from[nb] = current
            g_score[nb] = tentative_g
            h = manhattan_heuristic(nb, goal)
            f = tentative_g + h
            if nb not in open_set or f < open_set[nb]:
                heapq.heappush(open_heap, (f, next(counter), nb))
                open_set[nb] = f

return None, None, expansions, len(closed)

```

```

def read_board(n, prompt):
    print(prompt)
    board = []
    for i in range(n):
        row = list(map(int, input().split()))

```

```

if len(row) != n:
    raise ValueError(f"Row {i+1} must contain exactly {n} integers.")
board.append(row)
return board

def print_board(board):
    for row in board:
        print(" ".join(f"{x}" for x in row))

def main():
    try:
        n = int(input("Enter puzzle size n (e.g., 3 for 3x3): ").strip())
        initial = read_board(n, "Enter initial state row by row (use 0 for blank):")
        goal = read_board(n, "Enter goal state row by row (use 0 for blank):")

        result = a_star_manhattan(initial, goal)
        path, cost, expansions, explored = result

        if path is None:
            print("No solution (unsolvable with given start/goal).")
            return

        print("\nSolution path (each state shows g, h, f):\n")
        for idx, state in enumerate(path):
            g = idx
            h = manhattan_heuristic(state, tuple(tuple(r) for r in goal))
            f = g + h
            print(f"Step {idx}: g={g}, h={h}, f={f}")
            print_board(state)
            print()

        print(f"Total cost (number of moves): {cost}")
        print(f"Nodes expanded: {expansions}")
        print(f"Nodes explored (unique): {explored}")

    except Exception as e:
        print("Error:", e)

if __name__ == "__main__":
    main()

```

## OUTPUT:

```
Enter puzzle size n (e.g., 3 for 3x3): 3
Enter initial state row by row (use 0 for blank):
2 8 3
1 6 4
7 0 5
Enter goal state row by row (use 0 for blank):
1 2 3
8 0 4
7 6 5
Solution path (each state shows g, h, f):
Step 0: g=0, h=5, f=5
2 8 3
1 6 4
7 0 5

Step 1: g=1, h=4, f=5
2 8 3
1 0 4
7 6 5

Step 2: g=2, h=3, f=5
2 0 3
1 8 4
7 6 5

Step 3: g=3, h=2, f=5
0 2 3
1 8 4
7 6 5

Step 4: g=4, h=1, f=5
1 2 3
0 8 4
7 6 5

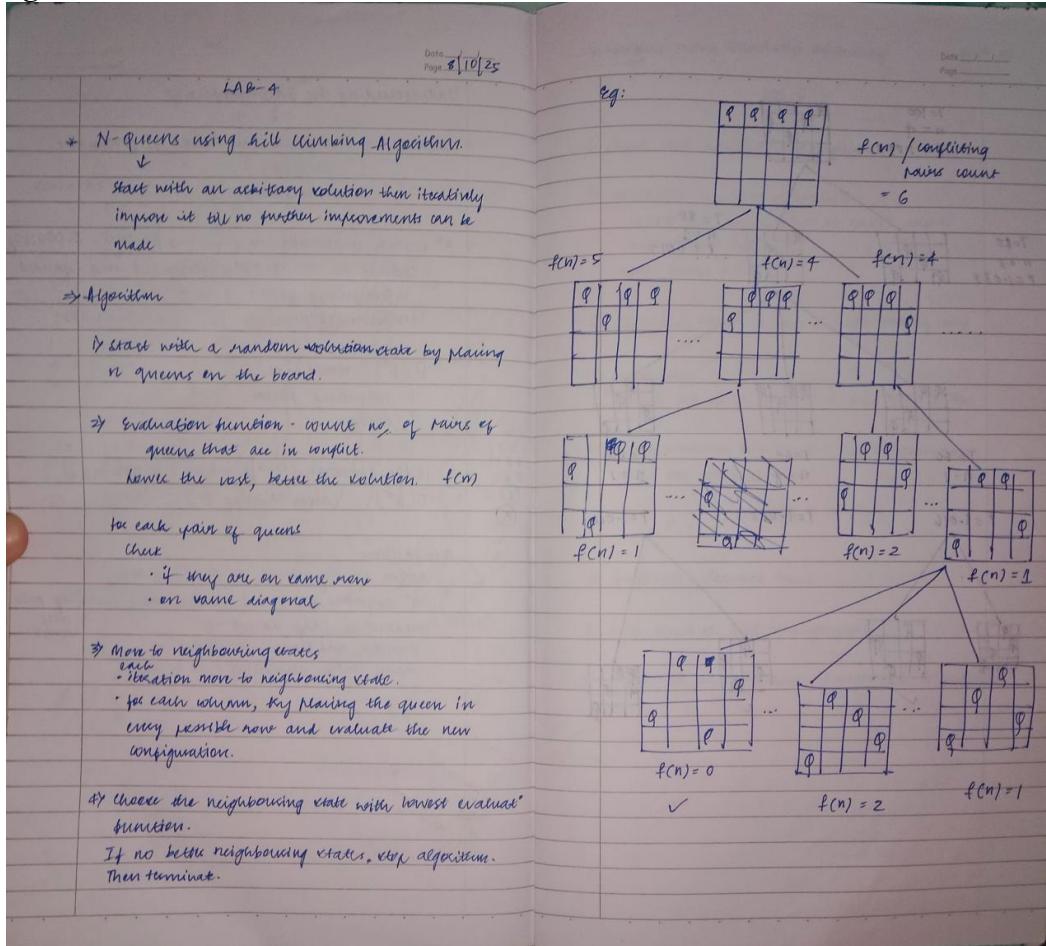
Step 5: g=5, h=0, f=5
1 2 3
8 0 4
7 6 5

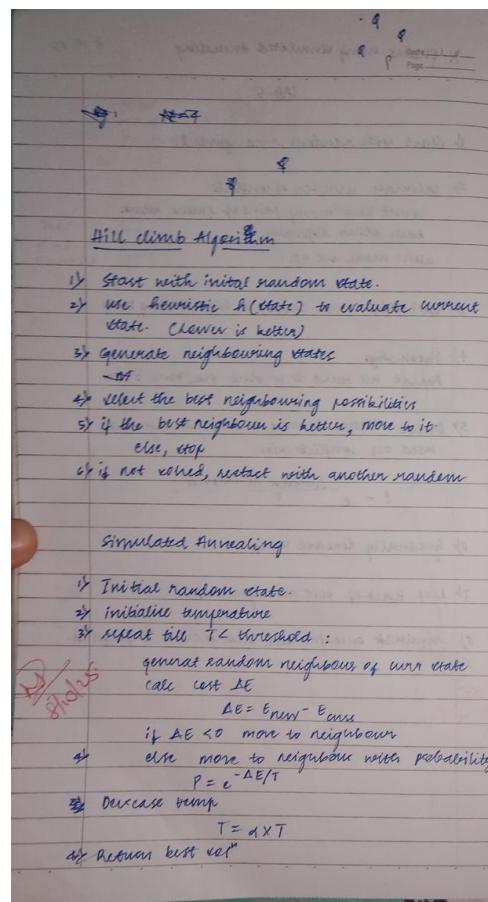
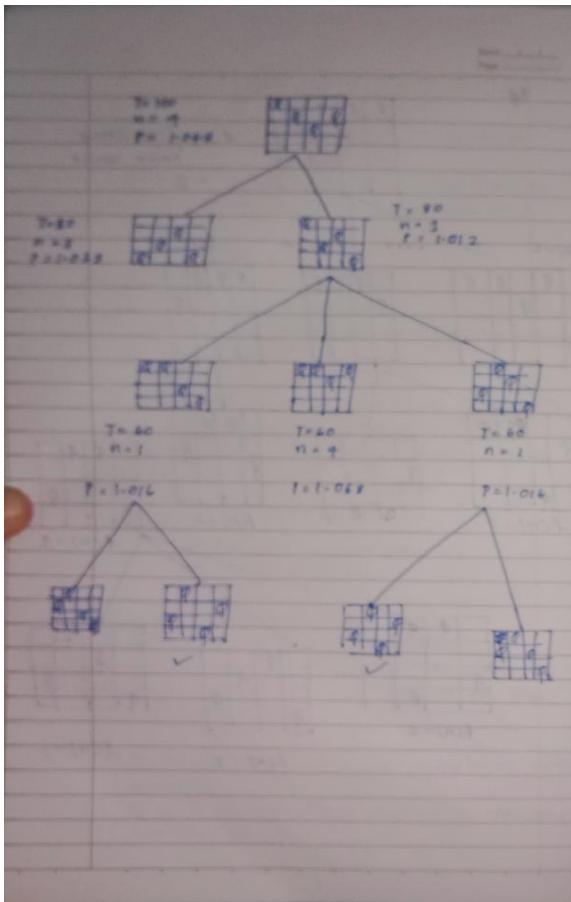
Total cost (number of moves): 5
Nodes expanded: 5
Nodes explored (unique): 6
```

## Program4

Implement Hill Climbing search algorithm to solve N-Queens problem

### Algorithm:





### Code:

```

def calculate_cost(state):
    cost = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                cost += 1
    return cost

def generate_neighbors(state):
    neighbors = []
    n = len(state)
    for col in range(n):
        for row in range(n):
            if state[col] != row: # move queen
                new_state = list(state)
                new_state[col] = row
                neighbors.append(new_state)
    return neighbors

def hill_climbing(initial_state):
    current = initial_state

```

```

current_cost = calculate_cost(current)
step = 0

print(f"Step {step}: State = {current}, Cost = {current_cost}")

while True:
    neighbors = generate_neighbors(current)
    neighbor_costs = [(n, calculate_cost(n)) for n in neighbors]

    # Print state space for this step
    print("\nNeighbors and their costs:")
    for n, c in neighbor_costs:
        print(f"  {n} -> Cost = {c}")

    # Pick the best neighbor (lowest cost)
    best_neighbor, best_cost = min(neighbor_costs, key=lambda x: x[1])

    if best_cost >= current_cost:
        break

    step += 1
    current, current_cost = best_neighbor, best_cost
    print(f"\nStep {step}: Move to {current}, Cost = {current_cost}")

    if current_cost == 0:
        print("\nGoal reached! Solution found.")
        break

initial_state = [3, 1, 2, 0]

hill_climbing(initial_state)

```

### Output:

```

→ Week 7
Step 0: State = [3, 1, 2, 0], Cost = 2

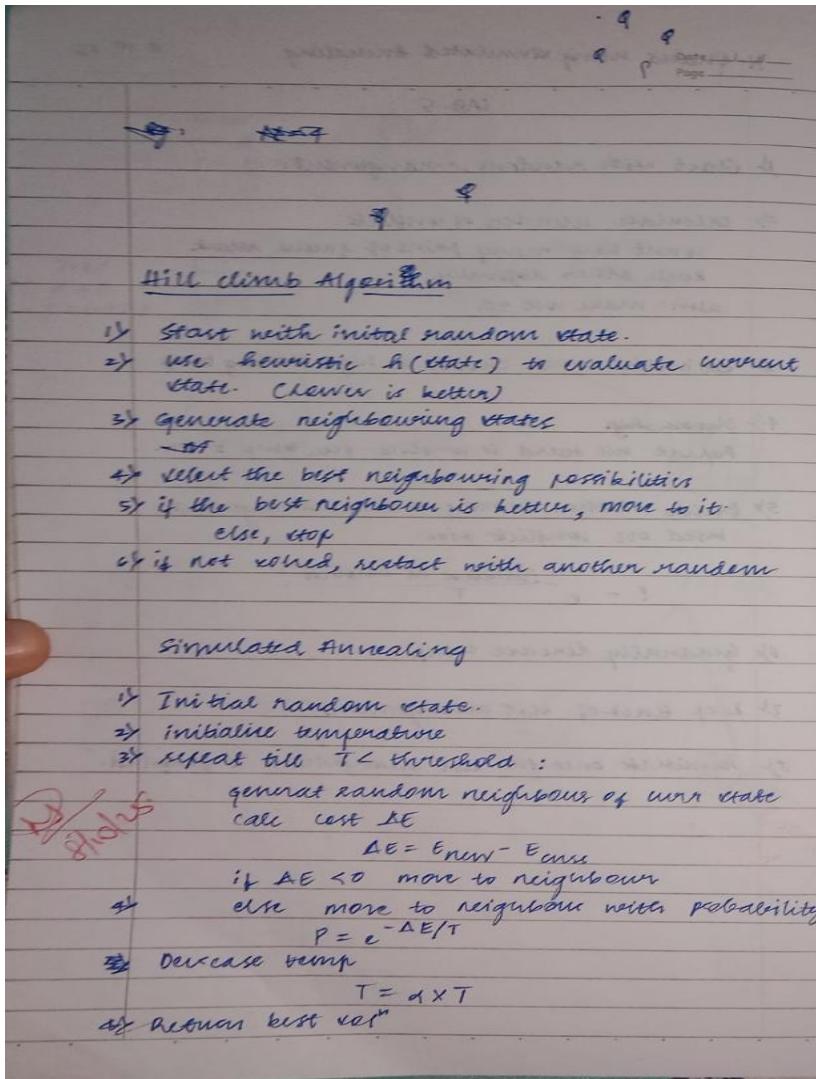
Neighbors and their costs:
  [0, 1, 2, 0] -> Cost = 4
  [1, 1, 2, 0] -> Cost = 2
  [2, 1, 2, 0] -> Cost = 3
  [3, 0, 2, 0] -> Cost = 2
  [3, 2, 2, 0] -> Cost = 4
  [3, 3, 2, 0] -> Cost = 3
  [3, 1, 0, 0] -> Cost = 3
  [3, 1, 1, 0] -> Cost = 4
  [3, 1, 3, 0] -> Cost = 2
  [3, 1, 2, 1] -> Cost = 3
  [3, 1, 2, 2] -> Cost = 2
  [3, 1, 2, 3] -> Cost = 4

```

## Program 5

Simulated Annealing to Solve 8-Queens problem

**Algorithm:**



**Code:**

```
import random
import math

def calculate_cost(state):
    cost = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                cost += 1
    return cost
```

```

def get_random_neighbor(state):
    n = len(state)
    new_state = list(state)
    col = random.randint(0, n - 1)
    row = random.randint(0, n - 1)
    new_state[col] = row
    return new_state

def simulated_annealing(n=8, max_iterations=10000, initial_temp=100.0, cooling_rate=0.99):

    current = [random.randint(0, n - 1) for _ in range(n)]
    current_cost = calculate_cost(current)
    best = current
    best_cost = current_cost
    temperature = initial_temp

    for _ in range(max_iterations):
        if current_cost == 0:
            break

        neighbor = get_random_neighbor(current)
        neighbor_cost = calculate_cost(neighbor)
        delta = neighbor_cost - current_cost

        if delta < 0 or random.random() < math.exp(-delta / temperature):
            current, current_cost = neighbor, neighbor_cost

            if current_cost < best_cost:
                best, best_cost = current, current_cost

        temperature *= cooling_rate
        if temperature < 1e-6:
            break

    return best, best_cost

best_state, best_cost = simulated_annealing()

print("The best position found:", best_state)
print("cost =", best_cost)

```

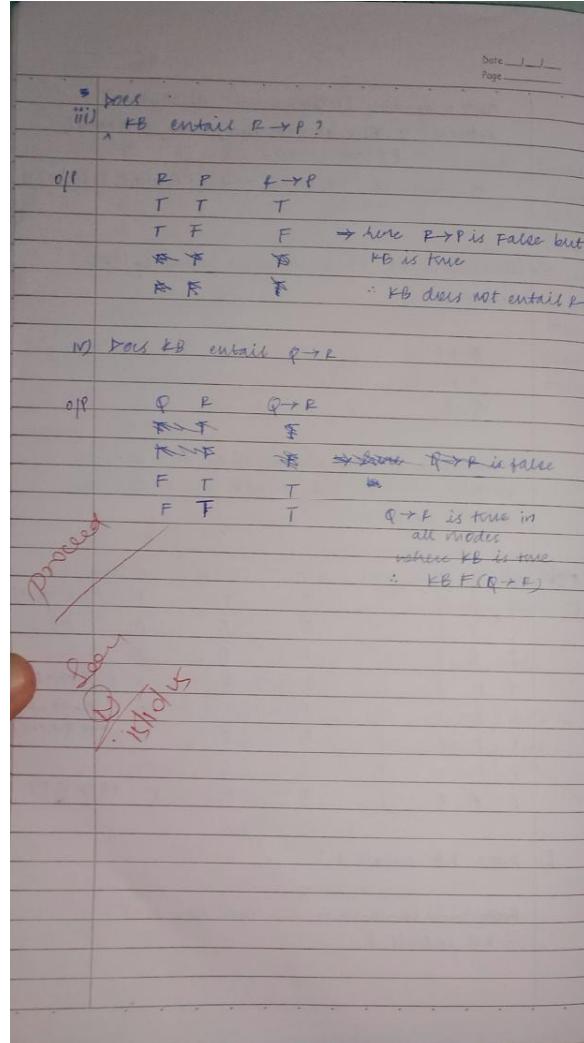
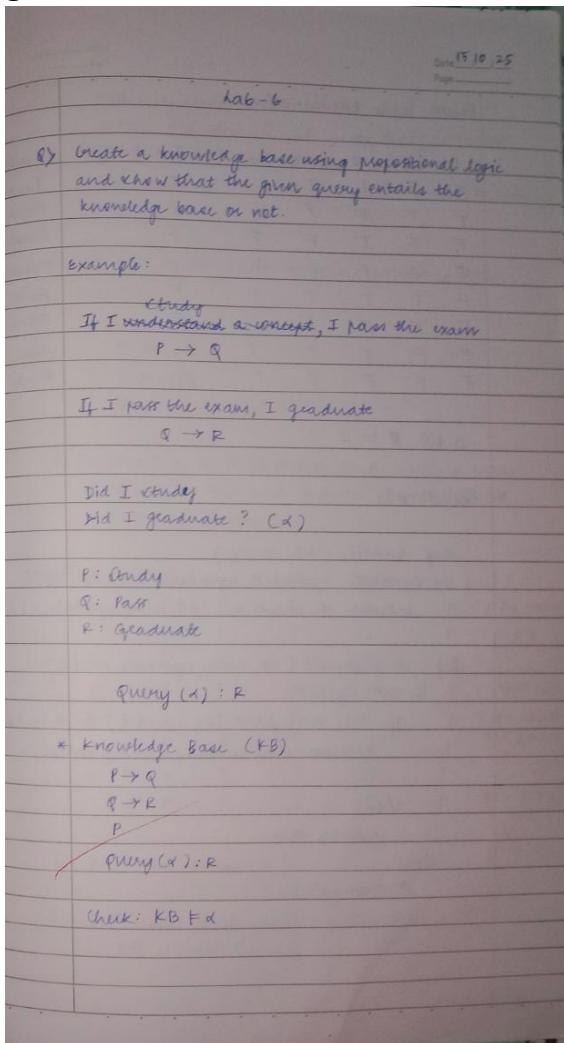
#### Output:

→ The best position found: [5, 2, 6, 1, 7, 4, 0, 3]  
cost = 0

## Program 6

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

### Algorithm:



Truth Table construction						
P	Q	R	$P \rightarrow Q$	$Q \rightarrow R$	$(P \rightarrow Q) \wedge (Q \rightarrow R)$	entails R?
T	T	T	T	T	T	True
T	T	F	T	F	F	False
T	F	T	F	T	F	False
T	F	F	T	F	F	False
F	T	T	T	F	F	False
F	T	F	T	F	F	False
F	F	T	T	F	F	False
F	F	F	T	F	F	False

rest = symbols[1:]  
return tt\_check\_all(KB, query, rest, f"model,  
P:@true}") and  
tt\_check\_all(KB, query, rest, f"model, P:@false"))

By consider a KB what contains following logic sentences

$P \rightarrow Q$   
 $P \wedge \neg P$   
 $Q \vee R$

i) Construct a TT that shows truth value of each sentence in KB and indicate the models in which KB is true.

\* Pseudocode

```

def entails(KB, query):
    symbols = extract_symbols(KB + query)
    return tt_check_all(KB, query, symbols, f"")
def tt_check_all(KB, query, symbols, model):
    if not symbols:
        if all(want_formula(i, model) for i in KB):
            return want_formula(query, model)
        else:
            return True
    else:
        p = symbols[0]
    
```

outpt

P	Q	R	$P \rightarrow Q$	$P \wedge Q$	$Q \vee R$	KB True?
T	T	T	T	T	T	F : $(P \rightarrow \neg Q)$
T	T	F	T	F	T	F : $(\neg Q \vee R)$
T	F	T	T	F	T	T
T	F	F	T	F	F	F : $(\neg Q \wedge \neg R)$
F	T	T	F	F	T	F : $(P \wedge \neg Q)$
F	T	F	F	F	T	F : $(\neg Q \wedge \neg R)$
F	F	T	T	T	T	T
F	F	F	T	T	F	F : $(Q \vee \neg R)$

ii) Does KB entail R?

Both rows where KB True has P:T  
 $\therefore$  KB entails P.

## Code:

```
import itertools
```

```

def eval_expr(expr, model):
    try:
        return eval(expr, {}, model)
    except:
        return False

def tt_entails(KB, query):
    symbols = sorted(set([ch for ch in KB + query if ch.isalpha()]))
    print("\nTruth Table:")
    print(" | ".join(symbols) + " | KB | Query")
    print("-" * (6 * len(symbols) + 20))

    entails = True
    for values in itertools.product([False, True], repeat=len(symbols)):
        model = dict(zip(symbols, values))
        kb_val = eval_expr(KB, model)
        query_val = eval_expr(query, model)

        row = " | ".join(["T" if model[s] else "F" for s in symbols])
        print(f"{{row}} | {{kb_val}} | {{query_val}}")

        if kb_val and not query_val:
            entails = False

    return entails

```

```

KB = input("Enter Knowledge Base (use &, |, ~ for AND, OR, NOT): ")
query = input("Enter Query: ")

result = tt_entails(KB, query)

print("\nResult:")
if result:
    print("KB entails Query (True in all cases).")
else:
    print("KB does NOT entail Query.")

```

## Output:

```

✉ Enter Knowledge Base (use &, |, ~ for AND, OR, NOT): (A|C)&(B|~C)
Enter Query: A|B

Truth Table:
A | B | C | KB | Query
-----
F | F | F | 0 | False
F | F | T | 0 | False
F | T | F | 0 | True
F | T | T | 1 | True
T | F | F | 1 | True
T | F | T | 0 | True
T | T | F | 1 | True
T | T | T | 1 | True

Result:
KB entails Query (True in all cases).

```

## Program 7

Implement unification in first order logic

### Algorithm:

Date \_\_\_\_\_  
Page 29 / 10 / 25

Lab - 7  
Unification in FOL

i)  $P(f(x), g(y), y)$   
 $P(f(g(z)), g(f(a)), f(a))$   
 find  $\theta$  (MGU)

ii)  $Q(x, f(x))$   
 $Q(f(y), y)$

iii)  $H(x, g(x))$   
 $H(g(y), g(g(z)))$

i)  $x = g(z), y = f(x)$  // possible

ii)  $x = f(y), y = f(x)$  // not possible

iii)  $x = g(y)$  // possible  
 $x = g(z)$   
 $\Rightarrow y = z$

i) compare  $f(x)$  and  $f(g(x))$   
 $\theta_1 = \{x/g(z)\}$   
 $\rightarrow g(y) \& g(f(a))$   
 $\theta_2 = \{y/f(a)\}$   
 $\rightarrow u \notin f(a)$   
 $\theta_3 = \{u/f(a)\}$

$\Rightarrow \theta = \{x/g(z), y/f(a), a/f(a)\}$   
 Apply  $\theta$  to both predicates  
 $P(f(x), g(y), u) \{ \theta \} =$   
 $P(f(g(z)), g(f(a))/f(a))$   
 $= P(f(g(z)), f(a), f(a), \{ \theta \})$   
 Both are identical

Date \_\_\_\_\_  
Page \_\_\_\_\_

2. Comparing  $x$  and  $f(y)$   
 $x = f(y)$   
 $f(x) \& y$   
 $f(x) = y$

Now  $x : f(f(y)) = y$   
 $\rightarrow$  cyclic not justifiable

3. Comparing  $x \& g(y)$   
 $x = g(y)$   
 comparing  $g(x)$  and  $g(g(z))$   
 $x = g(z)$   
 $g(x) = g(g(y))$   
 can be unified  
 when  $y = z$

$x = g(y)$   
 $y = z$   
 $z = g(z)$   
 $y = z$

Thus MGU is  
 $\theta = \{x/g(z), y/z\}$   
 Substitute

$H(x, g(x)) \{ x/g(z), y/z \} = H(g(z)), g(g(z))$   
 $H(g(y), g(g(z)) \{ y/z \} = H(g(z)) = g(g(z))$

Thus successful unification

### Code:

```
def occurs_check(var, term, subst):
    if var == term:
        return True
    elif isinstance(term, tuple):
        return any(occurs_check(var, t, subst) for t in term)
    elif term in subst:
        return occurs_check(var, subst[term], subst)
    return False
```

```

def unify(x, y, subst):
    if subst is None:
        return None
    elif x == y:
        return subst
    elif isinstance(x, str) and x.isupper():
        return unify_var(x, y, subst)
    elif isinstance(y, str) and y.isupper():
        return unify_var(y, x, subst)
    elif isinstance(x, tuple) and isinstance(y, tuple):
        if x[0] != y[0] or len(x) != len(y):
            return None
        for a, b in zip(x[1:], y[1:]):
            subst = unify(a, b, subst)
        if subst is None:
            return None
        return subst
    else:
        return None

def unify_var(var, x, subst):
    if var in subst:
        return unify(subst[var], x, subst)
    elif x in subst:
        return unify(var, subst[x], subst)
    elif occurs_check(var, x, subst):
        return None
    else:
        subst[var] = x
        return subst

def parse_expr(s):
    s = s.replace(" ", "")
    if '(' not in s:
        return s
    name_end = s.index('(')
    name = s[:name_end]
    args = []
    depth = 0
    current = ""
    for c in s[name_end+1:-1]:
        if c == ',' and depth == 0:
            args.append(parse_expr(current))
            current = ""
        else:
            if c == '(':
                depth += 1
            elif c == ')':
                depth -= 1
                current += c
    if current:
        args.append(parse_expr(current))

```

```

return tuple([name] + args)

def expr_to_str(expr):
    if isinstance(expr, tuple):
        return expr[0] + "(" + ",".join(expr_to_str(e) for e in expr[1:]) + ")"
    else:
        return expr

expr1_input = input("Enter first expression: ")
expr2_input = input("Enter second expression: ")

expr1 = parse_expr(expr1_input)
expr2 = parse_expr(expr2_input)

subst = unify(expr1, expr2, {})

if subst:
    formatted_subst = {var: expr_to_str(val) for var, val in subst.items()}
else:
    formatted_subst = None

print("Most General Unifier (MGU):", formatted_subst)

```

**Output:**

```

→ Enter first expression: p(b,X,f(g(Z)))
Enter second expression: p(Z,f(Y),f(Y))
Most General Unifier (MGU): {'Z': 'b', 'X': 'f(Y)', 'Y': 'g(Z)'}

```

## Program 8

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

### **Algorithm:**

Date: 29/10/25  
Page: 29

Lab - 8  
Forward Reasoning

function FOL-FC-ASK(KB, x) returns true or false.

inputs : KB, the knowledge base  
x, the query

local variable : new

repeat until new is empty  
new = {}

for each rule in KB, do

(p<sub>1</sub> ∧ p<sub>2</sub> ... ∧ p<sub>n</sub> → q) STANDARD VARIABLE  
(A<sub>1</sub>, A<sub>2</sub>, ..., A<sub>m</sub>)

for each θ such that SUBST(θ, p<sub>1</sub>, ..., p<sub>n</sub>)  
= SUBST(θ, p<sub>1</sub>, ..., p<sub>n</sub>)

q' ← SUBST(θ, q)

if q' does not unify with some sentence already  
in KB or new then add q' to new

φ ∈ UNIFY(q', x)

if φ not fail then return φ

add new to KB

return false

### **Code:**

```
facts = {  
    'American(Robert)': True,  
    'Hostile(A)': True,  
    'Sells_Weapons(Robert, A)': True  
}
```

If American(X) and Hostile(Y) and Sells\_Weapons(X, Y), then Crime(X)  
def forward\_reasoning(facts):

If American(X) and Hostile(Y) and Sells\_Weapons(X, Y), then Crime(X)

```
if facts.get('American(Robert)', False) and facts.get('Hostile(A)', False) and facts.get('Sells_Weapons(Robert,  
A)', False):  
    facts['Crime(Robert)'] = True  
  
forward_reasoning(facts)  
  
if facts.get('Crime(Robert)', False):  
    print("Robert is a criminal.")  
else:  
    print("Robert is not a criminal.")
```

**Output:**

Robert is a criminal.

## Program 9

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

### Algorithm:

Handwritten notes from a notebook page titled "Lab - 9 FOL to CNF". The page contains several sections of text and formulas related to the conversion of First-Order Logic (FOL) to Conjunctive Normal Form (CNF).

- Algorithm:**
  - Eliminate biconditionals and implications
    - Replace  $\alpha \leftrightarrow \beta$  with  $(\alpha \rightarrow \beta) \wedge (\beta \rightarrow \alpha)$
    - Replace  $\neg \alpha \rightarrow \beta$  with  $\neg \alpha \vee \beta$
  - Move  $\neg$  inwards
    - $\neg(\forall x P) = \exists x \neg P$
    - $\neg(\exists x P) = \forall x \neg P$
    - $\neg(\alpha \vee \beta) = \neg \alpha \wedge \neg \beta$
    - $\neg(\alpha \wedge \beta) = \neg \alpha \vee \neg \beta$
    - $\neg \neg \alpha = \alpha$
  - Standardise variables apart by renaming them
  - Skolemization
    - $\exists y: \exists x \text{ Rich}(x) \text{ becomes } \text{Rich}(g_1)$   
 $g_1 \rightarrow \text{variable constant}$
    - $\forall x \text{ Person}(x) \text{ becomes } \text{Person}(x)$
  - Dispose universal quantifiers
  - Substitute  $\wedge$  over  $\vee$ 

$$(\alpha \wedge \beta) \vee \gamma \equiv (\alpha \vee \gamma) \wedge (\beta \vee \gamma)$$
- Example:**

Given formula:  $\forall x (P(x) \rightarrow \exists y Q(y, x))$

formula = f  
 'op': FORALL, 'var': 'x',  
 'body':  
 'op': IMPLITS,  
 'left': q, 'op': ATOM, 'mid': 'P', 'args': [x]  
 'right': q  
 'op': EXISTS, 'var': 'y',  
 'body': f, 'op': ATOM, 'mid': 'Q', 'args': [ $y$ , x]

### Code:

```
import copy
```

```
# -----
# Predicate Structure
# -----
class Predicate:
    def __init__(self, name, args, negated=False):
        self.name = name
        self.args = args if isinstance(args, tuple) else tuple(args)
```

```

self.negated = negated

def __eq__(self, other):
    return (self.name == other.name and
            self.args == other.args and
            self.negated == other.negated)

def __hash__(self):
    return hash((self.name, self.args, self.negated))

def __repr__(self):
    neg = "~" if self.negated else ""
    args_str = ",".join(str(a) for a in self.args)
    return f'{neg} {self.name}({args_str})'

def negate(self):
    return Predicate(self.name, self.args, not self.negated)

def substitute(self, theta):
    """Apply substitution theta to this predicate"""
    new_args = tuple(substitute_term(arg, theta) for arg in self.args)
    return Predicate(self.name, new_args, self.negated)

def substitute_term(term, theta):
    """Apply substitution to a term"""
    if isinstance(term, str) and term.islower(): # variable
        if term in theta:
            return substitute_term(theta[term], theta)
        return term
    elif isinstance(term, tuple):
        return tuple(substitute_term(t, theta) for t in term)
    return term

# -----
# Unification Algorithm
# -----

def unify(x, y, theta=None):
    if theta is None:
        theta = {}
    if theta == "FAIL":
        return "FAIL"
    elif x == y:
        return theta
    elif isinstance(x, str) and x.islower(): # variable
        return unify_var(x, y, theta)
    elif isinstance(y, str) and y.islower(): # variable
        return unify_var(y, x, theta)

```

```

        elif isinstance(x, tuple) and isinstance(y, tuple):
            if len(x) != len(y):
                return "FAIL"
            theta = unify(x[0], y[0], theta)
            if theta == "FAIL":
                return "FAIL"
            return unify(x[1:], y[1:], theta)
        else:
            return "FAIL"

def unify_var(var, x, theta):
    if var in theta:
        return unify(theta[var], x, theta)
    elif isinstance(x, str) and x.islower() and x in theta:
        return unify(var, theta[x], theta)
    elif occurs_check(var, x, theta):
        return "FAIL"
    else:
        new_theta = copy.deepcopy(theta)
        new_theta[var] = x
        return new_theta

def occurs_check(var, x, theta):
    if var == x:
        return True
    elif isinstance(x, str) and x.islower() and x in theta:
        return occurs_check(var, theta[x], theta)
    elif isinstance(x, tuple):
        return any(occurs_check(var, xi, theta) for xi in x)
    return False

# -----
# Variable Standardization
# -----
var_counter = 0

def standardize_variables(clause):
    """Rename all variables in a clause to unique names"""
    global var_counter
    mapping = {}
    new_clause = []

    for pred in clause:
        new_args = []
        for arg in pred.args:
            if isinstance(arg, str) and arg.islower(): # variable
                if arg not in mapping:

```

```

        mapping[arg] = f"{{arg}} {{var_counter}}"
        var_counter += 1
        new_args.append(mapping[arg])
    else:
        new_args.append(arg)
new_clause.append(Predicate(pred.name, new_args, pred.negated))

return new_clause

# -----
# Resolution Algorithm
# -----
def resolve(ci, cj):
    """Resolve two clauses using FOL resolution"""
    ci = standardize_variables(ci)
    cj = standardize_variables(cj)

    resolvents = []

    for i, pi in enumerate(ci):
        for j, pj in enumerate(cj):
            # Check if predicates can be resolved (opposite signs, same name)
            if pi.negated != pj.negated and pi.name == pj.name:
                # Try to unify the arguments
                theta = unify(pi.args, pj.args)

                if theta != "FAIL":
                    # Create resolvent by removing resolved predicates and applying substitution
                    new_clause = []

                    # Add literals from ci except pi
                    for k, pred in enumerate(ci):
                        if k != i:
                            new_clause.append(pred.substitute(theta))

                    # Add literals from cj except pj
                    for k, pred in enumerate(cj):
                        if k != j:
                            new_clause.append(pred.substitute(theta))

                    # Remove duplicates
                    new_clause = list(set(new_clause))
                    resolvents.append(new_clause)

    return resolvents

def fol_resolution(kb, query):

```

```

"""FOL resolution algorithm"""
# Negate query and add to KB
clauses = [clause[:] for clause in kb] # deep copy
clauses.append([query.negate()])

print(f"\nKnowledge Base + Negated Query:")
for i, clause in enumerate(clauses):
    print(f" {i+1}. {clause}")
print()

iteration = 0
while True:
    iteration += 1
    n = len(clauses)
    pairs = [(clauses[i], clauses[j]) for i in range(n) for j in range(i + 1, n)]

    new_clauses = []
    for (ci, cj) in pairs:
        resolvents = resolve(ci, cj)

        for resolvent in resolvents:
            if len(resolvent) == 0:
                print(f"Iteration {iteration}: Derived empty clause from:")
                print(f" {ci}")
                print(f" {cj}")
                print(" → [] (Contradiction found!)")
                return True

    # Check if this is a new clause
    if resolvent not in clauses and resolvent not in new_clauses:
        new_clauses.append(resolvent)

    if not new_clauses:
        print(f"Iteration {iteration}: No new clauses derived. Query cannot be proved.")
        return False

    print(f"Iteration {iteration}: Generated {len(new_clauses)} new clause(s)")
    for clause in new_clauses:
        clauses.append(clause)

# -----
# Example Usage
# -----
if __name__ == "__main__":
    # Define knowledge base
    kb = [
        # John likes all food: Food(x) => Likes(John, x)

```

```

[Predicate("Food", ("x",), negated=True), Predicate("Likes", ("John", "x"))],
# Food(Apple)
[Predicate("Food", ("Apple",))],  

# Food(Vegetables)
[Predicate("Food", ("Vegetables",))],  

# Eats(Anil, Peanuts)
[Predicate("Eats", ("Anil", "Peanuts"))],  

# Alive(Anil)
[Predicate("Alive", ("Anil",))],  

# If alive and eats something, that thing is food: Alive(x) ∧ Eats(x,y) => Food(y)  

[Predicate("Alive", ("x",), negated=True),
 Predicate("Eats", ("x", "y"), negated=True),
 Predicate("Food", ("y",))],  

# Harry eats everything Anil eats: Eats(Anil,y) => Eats(Harry,y)
[Predicate("Eats", ("Anil", "y"), negated=True),
 Predicate("Eats", ("Harry", "y"))]
]  

# Query: Does John like Peanuts?
query = Predicate("Likes", ("John", "Peanuts"))

print("=" * 60)
print("FIRST-ORDER LOGIC RESOLUTION THEOREM PROVER")
print("=" * 60)
print(f"\nQuery: {query}")
print("-" * 60)

result = fol_resolution(kb, query)

print("\n" + "=" * 60)
if result:
    print("Query is PROVED using resolution!")
else:
    print("Query CANNOT be proved.")
print("=" * 60)

```

## Output:

Query: Likes(John,Peanuts)

Knowledge Base + Negated Query:

1. [~Food(x), Likes(John,x)]
2. [Food(Apple)]
3. [Food(Vegetables)]
4. [Eats(Anil,Peanuts)]
5. [Alive(Anil)]
6. [~Alive(x), ~Eats(x,y), Food(y)]
7. [~Eats(Anil,y), Eats(Harry,y)]
8. [~Likes(John,Peanuts)]

Iteration 1: Generated 8 new clause(s)

Iteration 2: Generated 16 new clause(s)

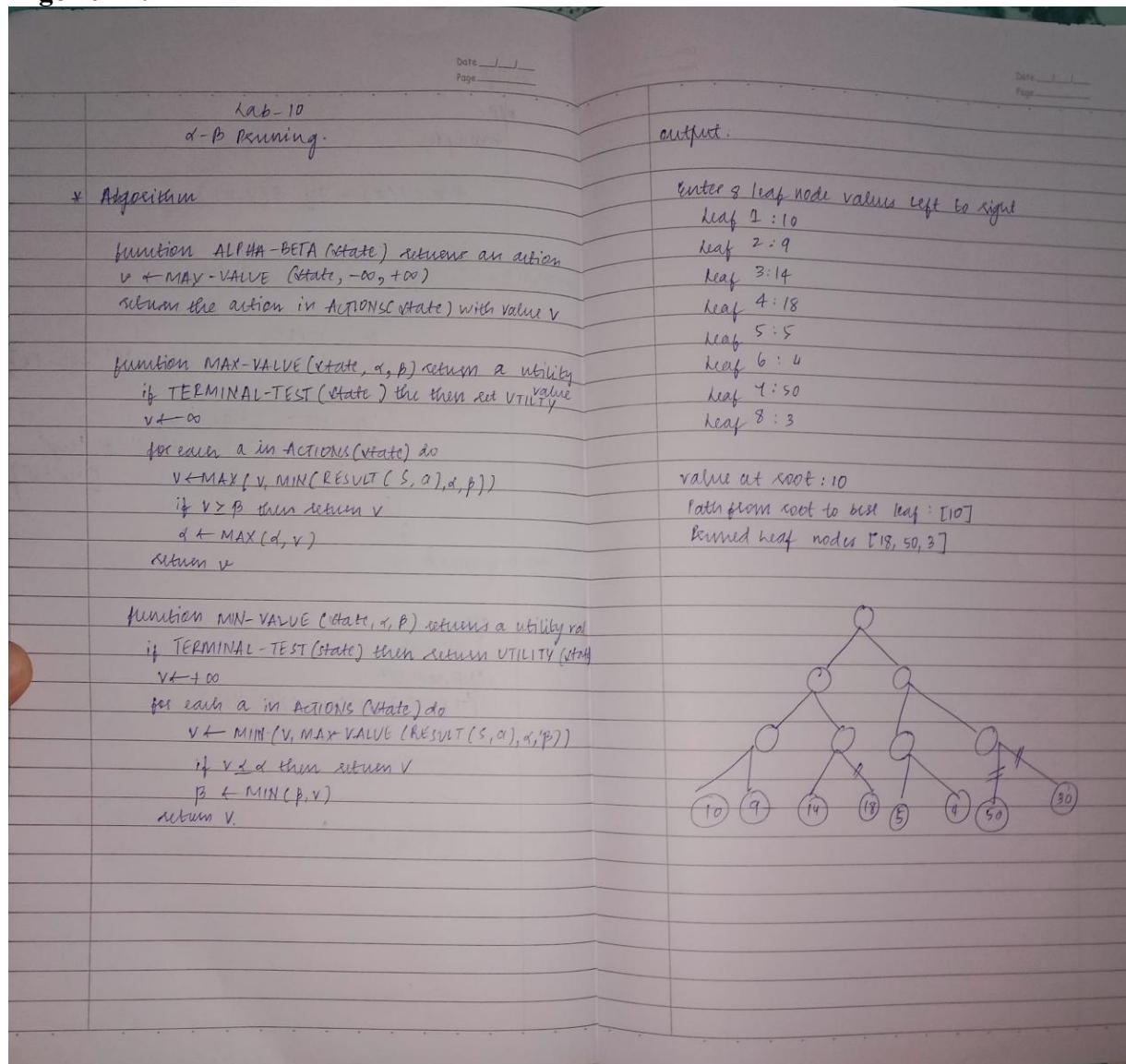
Iteration 3: Derived empty clause from:

- [Eats(Anil,Peanuts)]
- [~Eats(Anil,Peanuts)]
- [] (Contradiction found!)

## Program 10

Implement Alpha-Beta Pruning.

### Algorithm:



### Code:

```
import math
```

```
# Alpha-Beta Pruning Algorithm
```

```
def alpha_beta(depth, node_index, maximizing_player, values, alpha, beta, max_depth, path, pruned):
```

```
    # Base case: leaf node
```

```
    if depth == max_depth:
```

```
        return values[node_index], [node_index]
```

```
    if maximizing_player:
```

```
        best = -math.inf
```

```
        best_path = []
```

```
        for i in range(2): # two children per node
```

```
            val, child_path = alpha_beta(depth + 1, node_index * 2 + i, False, values, alpha, beta, max_depth, path, pruned)
```

```

if val > best:
    best = val
    best_path = [node_index] + child_path
alpha = max(alpha, best)
if beta <= alpha:
    pruned.append((node_index, "Right" if i == 0 else "Left"))
    break
return best, best_path
else:
    best = math.inf
    best_path = []
    for i in range(2):
        val, child_path = alpha_beta(depth + 1, node_index * 2 + i, True, values, alpha, beta, max_depth, path, pruned)
        if val < best:
            best = val
            best_path = [node_index] + child_path
        beta = min(beta, best)
        if beta <= alpha:
            pruned.append((node_index, "Right" if i == 0 else "Left"))
            break
    return best, best_path

```

```

# Example usage
if __name__ == "__main__":
    # Example game tree (leaf node values)
    values = [3, 5, 6, 9, 1, 2, 0, -1]

    print("Leaf Node Values:", values)
    path = []
    pruned = []

    max_depth = 3
    result, best_path = alpha_beta(0, 0, True, values, -math.inf, math.inf, max_depth, path, pruned)

    print("\nOptimal Value at Root Node:", result)
    print("Best Path (Node Indices):", best_path)
    print("Pruned Nodes:", pruned)

```

### Output:

```

*** Leaf Node Values: [3, 5, 6, 9, 1, 2, 0, -1]

Optimal Value at Root Node: 5
Best Path (Node Indices): [0, 0, 0, 1]
Pruned Nodes: [(1, 'Right'), (1, 'Right')]

```