Introduction to Linear Algebra (Week 3)

Fall, 2019

- 1. (3D Graphics in MATLAB)
 - (a) Referring to the followings, draw a graph of helix curve given by the vector equation

$$\mathbf{c}(t) = (t\cos(20\pi t), t\sin(20\pi t), \tanh t),$$

where the parameter t varies from -1 to 1.

- i. Construct a vector \mathbf{t} which consist of equally-spaced points in [-1, 1]. [If you do not know what to do, go back to 'week2'.]
- ii. Use the MATLAB built-in command plot3 to plot the curve in 3D space.
- (b) Referring to the followings, plot the surface (or mesh graph) of the graph given by

$$z = xe^{-x^2 - y^2},$$

over the region in the xy-plane defined by $\mathcal{D} = \{(x,y) : -2 \le x \le 2, -2 \le y \le 2\}.$

- i. Using the MATLAB built-in command meshgrid, construct two matrices, each of which consist of the x coordinates and y coordinates of the \mathcal{D} , respectively.
- ii. Using the MATLAB built-in commands surf or mesh, create a 3D surface plot.

Submission guide

- Download the guide code(assignment3_1a.m) in the KLMS and fill out missing parts to plot a 3D graph of the curve given by (a).
- Download the guide code(assignment3_1b.m) in the KLMS and fill out missing parts to plot a graph of the surface given by (b).
- Upload the completed code files, assignment3_1a.m and assignment3_1b.m, to 'Homework box for MATLAB assignment 3' in the KLMS

Due date: Oct 04 (Fri) 10:55 a.m. Late submission will not be allowed.

- 2. (Supplement problem)
 - (a) Plot the graph of the curve $\mathbf{M}(t)$ given by the parametric equations,

$$\mathbf{M}(t) = (x(t), y(t), z(t)), \qquad t \in [-1, 1]$$

where the x(t), y(t), z(t) are defined as

$$x(t) = R\cos\phi + r\cos\theta\cos\eta,$$

$$y(t) = R\sin\phi + r\sin\theta,$$

$$z(t) = r\cos\theta\sin\eta,$$

with appropriate values R, r, η and functions $\phi(t) = 2\pi t$, $\theta(t) = 2\pi t p$ with appropriate p. (You can choose R, r, η , p by your self)

[Note that if you choose the values such as $R\approx 1.5\times 10^9, r\approx 4\times 10^5, \eta=5.14^\circ$ and $p\approx 365.24$, then the curve represents the orbit of the Moon around the Earth.]

3. Read the attachment "MATLAB_Week3.pdf" and practice by yourself.