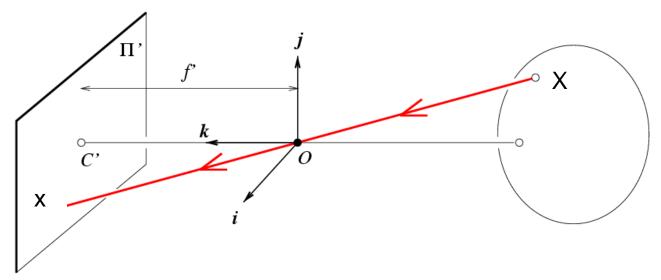
#### Previous classes

- Computer vision overview
- Mathematics of pinhole camera (Geometry)
- Sensors and light (Photometry)

## Recap: projection



$$x = K[R \ t]X$$



$$w\begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} \alpha & s & u_0 \\ 0 & \beta & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

## Relating multiple views

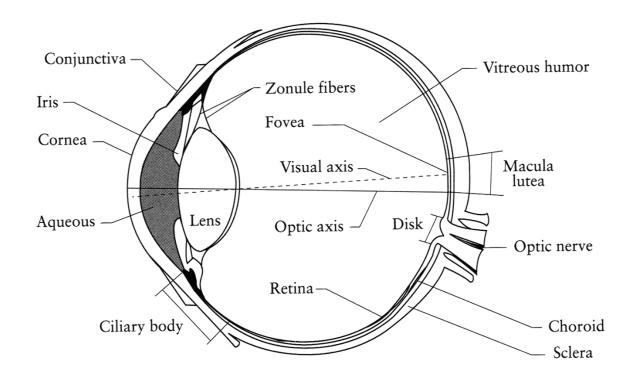


Why use lenses?

### Today's class

- Biological vision and color
- Image filtering

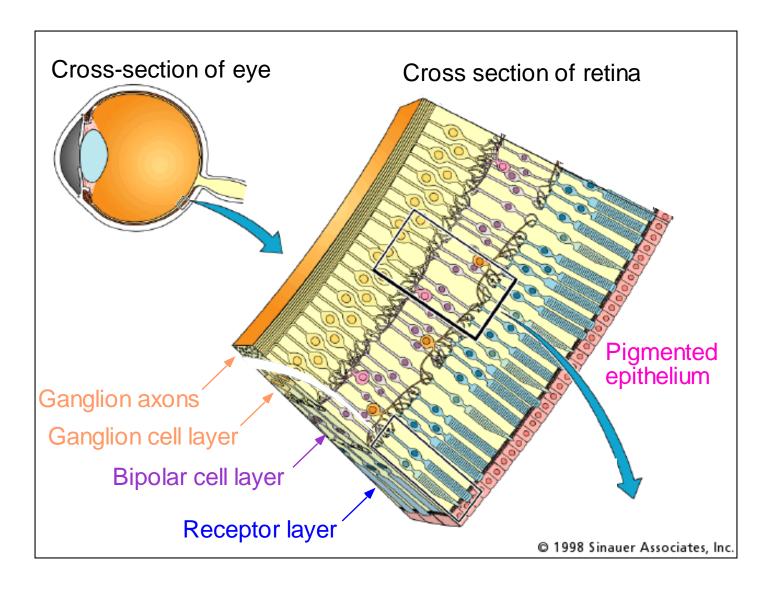
## The Eye



#### The human eye is a camera!

- Iris colored annulus with radial muscles
- Pupil the hole (aperture) whose size is controlled by the iris
- What's the "film"?
  - photoreceptor cells (rods and cones) in the retina

#### The Retina



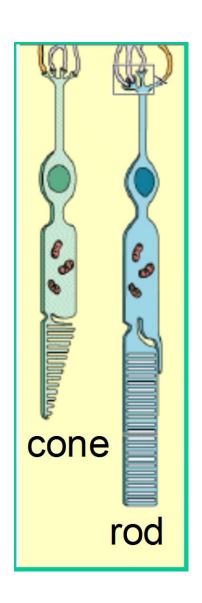
### Two types of light-sensitive receptors

#### Cones

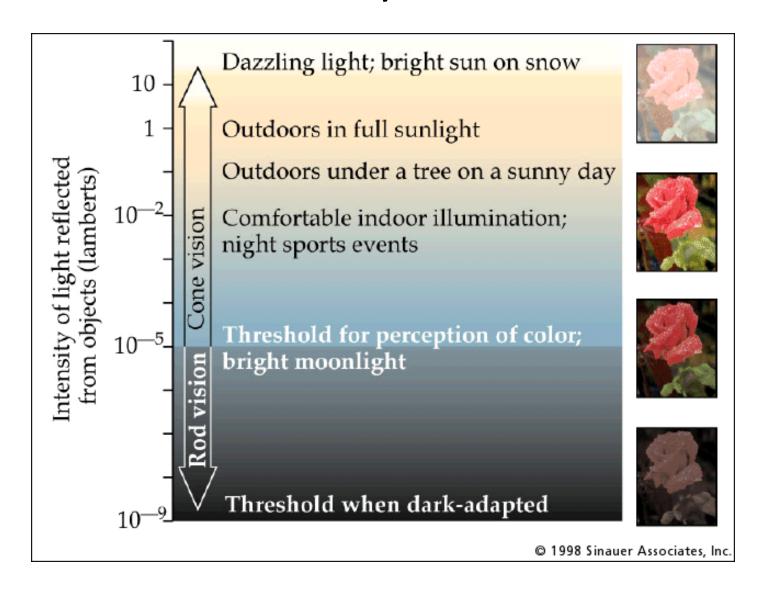
cone-shaped less sensitive operate in high light color vision

#### Rods

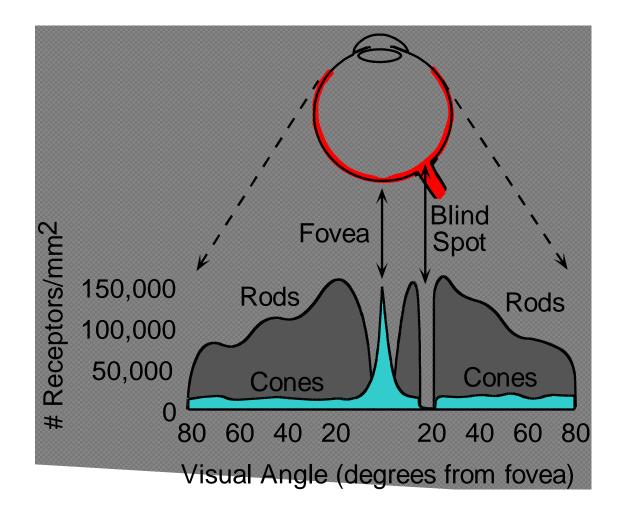
rod-shaped highly sensitive operate at night gray-scale vision



### Rod / Cone sensitivity



#### Distribution of Rods and Cones

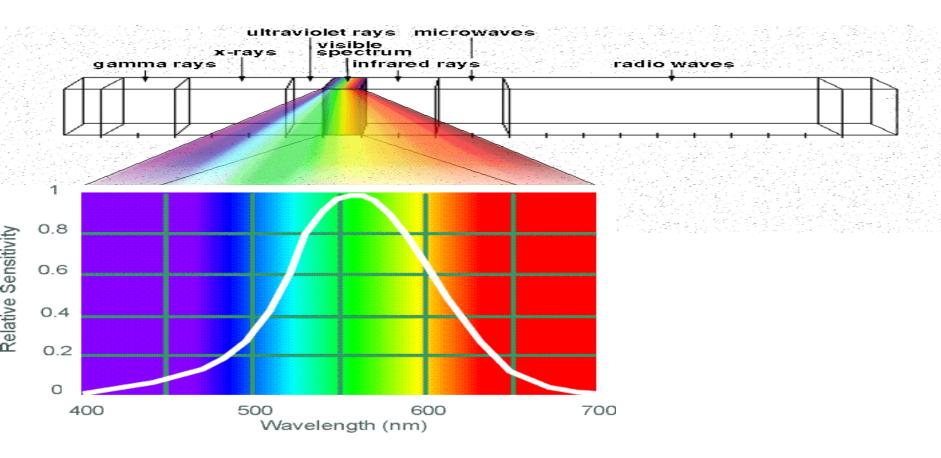


Night Sky: why are there more stars off-center? Averted vision: http://en.wikipedia.org/wiki/Averted\_vision

### **Eye Movements**

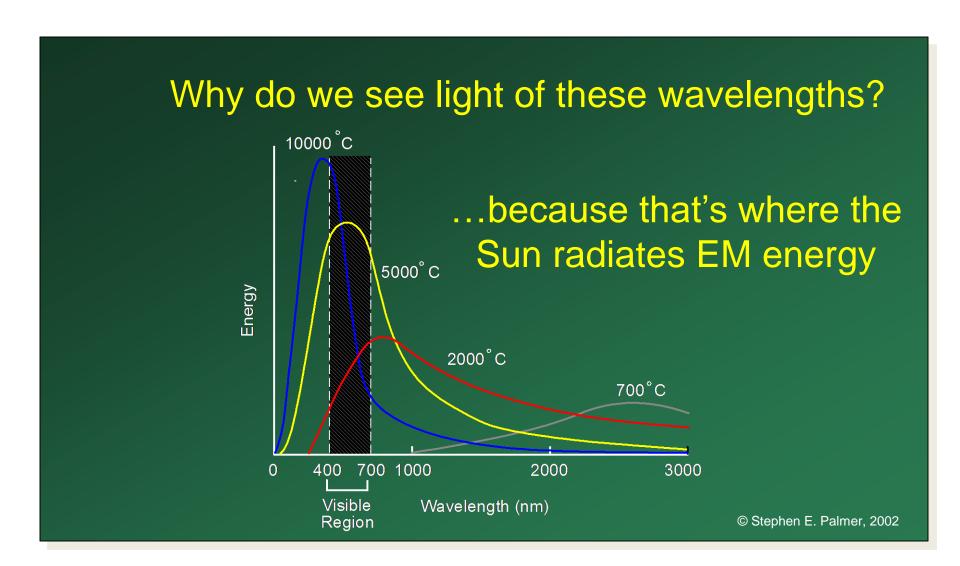
- Saccades
- Can be consciously controlled. Related to perceptual attention.
- 200ms to initiation, 20 to 200ms to carry out. Large amplitude.
- Microsaccades
- Involuntary. Smaller amplitude. Especially evident during prolonged fixation. Function debated.
- Ocular microtremor (OMT)
- involuntary. high frequency (up to 80Hz), small amplitude.
- Smooth pursuit tracking an object

### Electromagnetic Spectrum



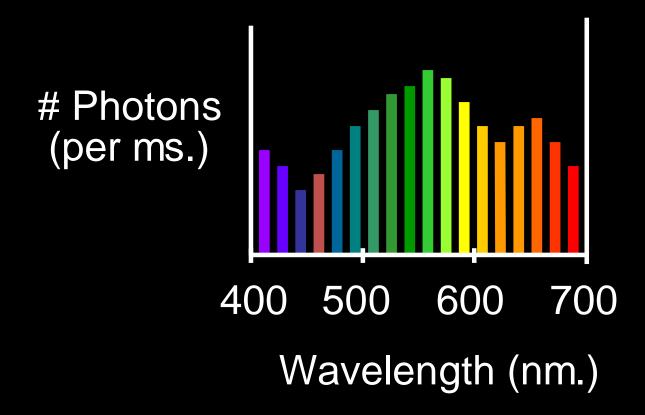
**Human Luminance Sensitivity Function** 

### Visible Light



### The Physics of Light

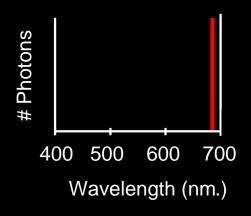
Any patch of light can be completely described physically by its spectrum: the number of photons (per time unit) at each wavelength 400 - 700 nm.



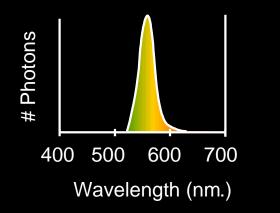
### The Physics of Light

#### Some examples of the spectra of light sources

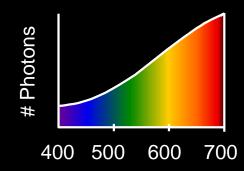
A. Ruby Laser



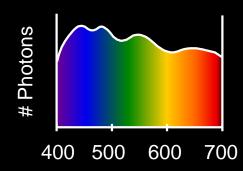
B. Gallium Phosphide Crystal



C. Tungsten Lightbulb

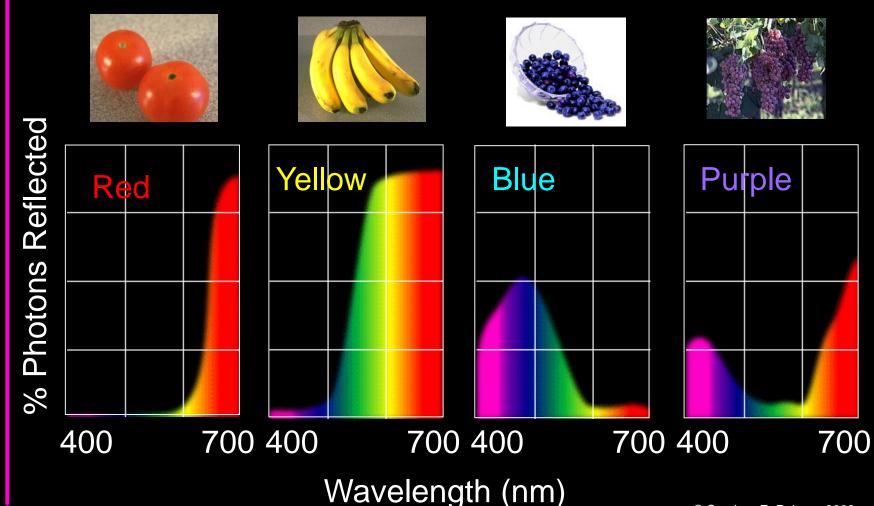


D. Normal Daylight



### The Physics of Light

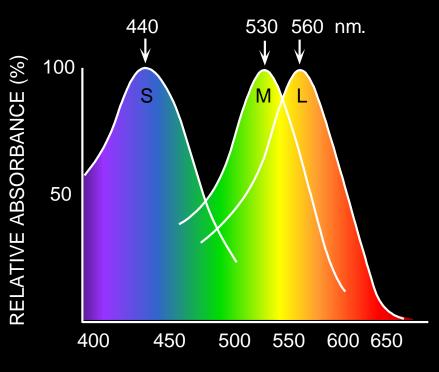
#### Some examples of the <u>reflectance</u> spectra of <u>surfaces</u>

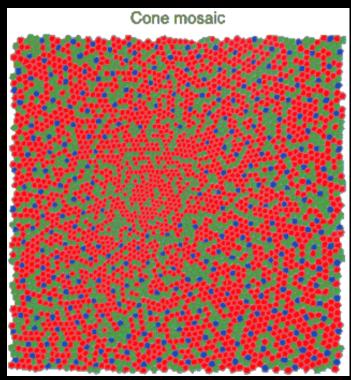


© Stephen E. Palmer, 2002

### **Physiology of Color Vision**

#### Three kinds of cones:

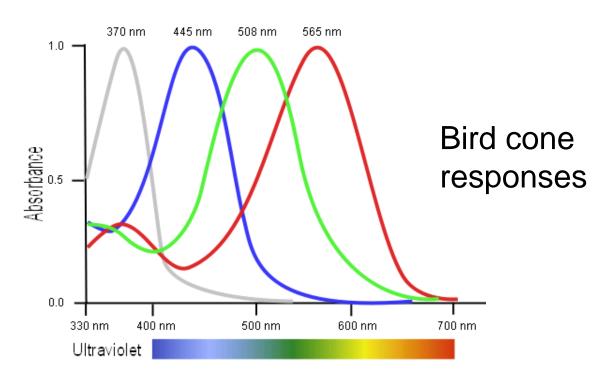




WAVELENGTH (nm.)

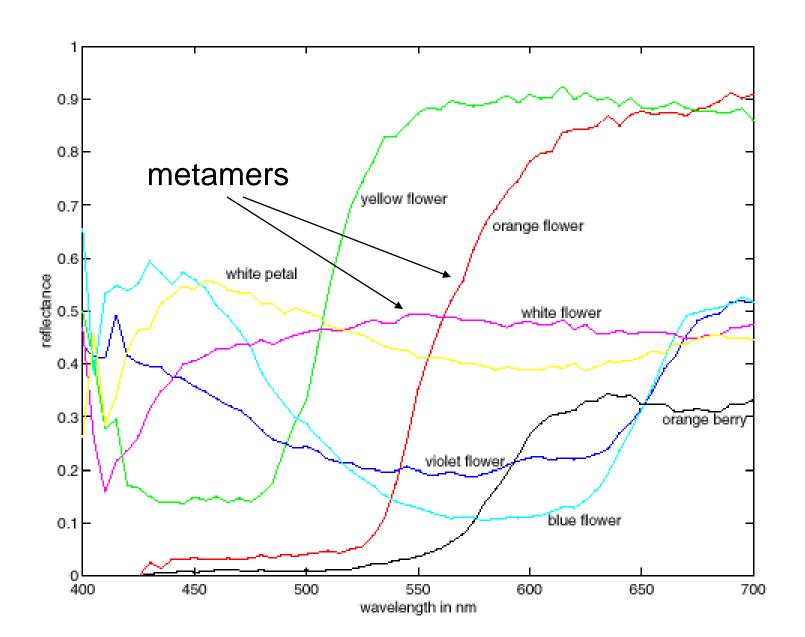
- Why are M and L cones so close?
- Why are there 3?

#### **Tetrachromatism**

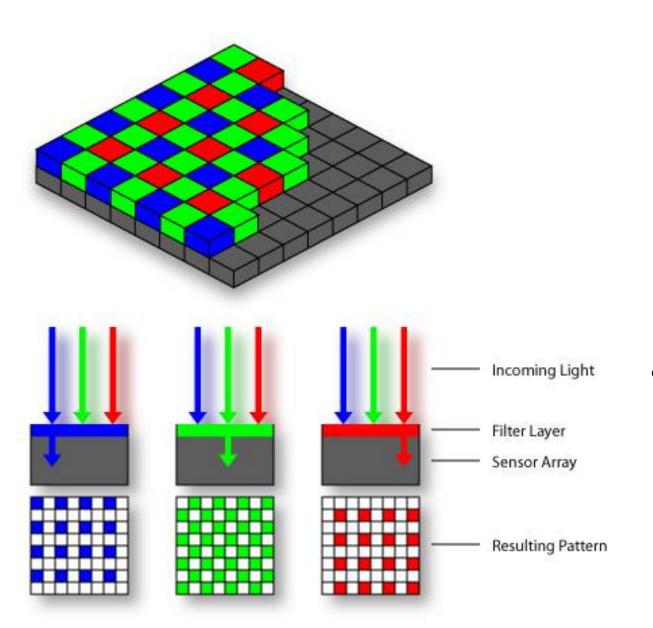


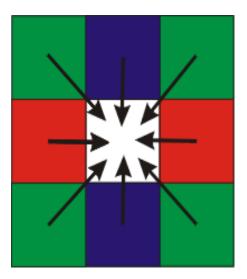
- Most birds, and many other animals, have cones for ultraviolet light.
- Some humans, mostly female, seem to have slight tetrachromatism.

## More Spectra



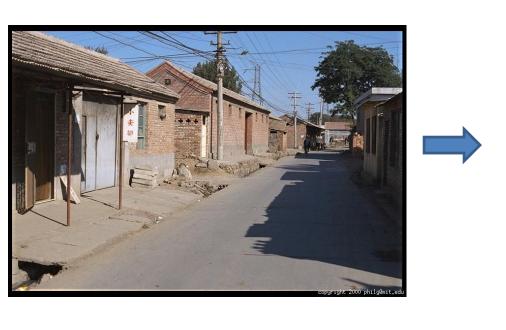
#### Practical Color Sensing: Bayer Grid





Estimate RGB
 at 'G' cells from
 neighboring
 values

# Color Image





## Images in Matlab

- Images represented as a matrix
- Suppose we have a NxM RGB image called "im"
  - im(1,1,1) = top-left pixel value in R-channel
  - im(y, x, b) = y pixels down, x pixels to right in the b<sup>th</sup> channel
  - im(N, M, 3) = bottom-right pixel in B-channel

	col	um	n -									$\Rightarrow$				
row	0.92	0.93	0.94	0.97	0.62	0.37	0.85	0.97	0.93	0.92	0.99	R				
	0.95	0.89	0.82	0.89	0.56	0.31	0.75	0.92	0.81	0.95	0.91					
	0.89	0.72	0.51	0.55	0.51	0.42	0.57	0.41	0.49	0.91	0.92	0.92	0.99	ı G		
	0.96	0.95	0.88	0.94	0.56	0.46	0.91	0.87	0.90	0.97	0.95	0.95	0.91			
	0.71	0.81	0.81	0.87	0.57	0.37	0.80	0.88	0.89	0.79	0.85	0.91	0.92	<u> </u>		В
	0.49	0.62	0.60	0.58	0.50	0.60	0.58	0.50	0.61	0.45	0.33	0.97	0.95	0.92	0.99	
	0.86	0.84	0.74	0.58	0.51	0.39	0.73	0.92	0.91	0.49	0.74	0.79	0.85	0.95	0.91	
	0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93	0.45	0.33	0.91	0.92	
	0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99	0.49	0.74	0.97	0.95	
	0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	0.43	0.74	0.79	0.85	
V	0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.82	0.99	0.45	0.33	
			0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.71	0.90	0.93	0.49	0.74	
					1		<u> </u>				0.73			0.82	0.93	
			0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.90	0.99	
					0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	
					0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	

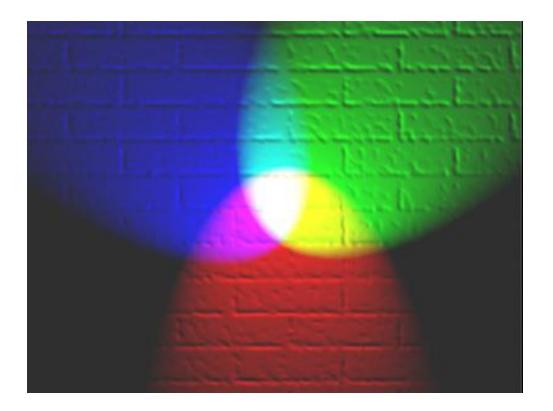
## Images in Matlab Python

- Images represented as a matrix
- Suppose we have a NxM RGB image called "im"
  - im(0,0,0) = top-left pixel value in R-channel
  - im(y, x, b) = y pixels down, x pixels to right in the b<sup>th</sup> channel
  - im(N-1, M-1, 2) = bottom-right pixel in B-channel

	col	um	n -									$\Rightarrow$				
row	0.92	0.93	0.94	0.97	0.62	0.37	0.85	0.97	0.93	0.92	0.99	R				
	0.95	0.89	0.82	0.89	0.56	0.31	0.75	0.92	0.81	0.95	0.91					
	0.89	0.72	0.51	0.55	0.51	0.42	0.57	0.41	0.49	0.91	0.92	0.92	0.99	ı G		
	0.96	0.95	0.88	0.94	0.56	0.46	0.91	0.87	0.90	0.97	0.95	0.95	0.91			_
	0.71	0.81	0.81	0.87	0.57	0.37	0.80	0.88	0.89	0.79	0.85	0.91	0.92			В
	0.49	0.62	0.60	0.58	0.50	0.60	0.58	0.50	0.61	0.45	0.33	0.97	0.95	0.92	0.99	
	0.86	0.84	0.74	0.58	0.51	0.39	0.73	0.92	0.91	0.49	0.74	0.79	0.85	0.95	0.91	
	0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93	0.45	0.33	0.91	0.92	
	0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99	0.49	0.74	0.97	0.95	
	0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	0.43	0.93	0.79	0.85	
V	0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.90	0.99	0.45	0.33	
			0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	0.49	0.74	
			0.91	0.73	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.82	0.93	
			0.91	0.54	0.83	0.49	0.41	0.78	0.78	0.77	0.83	0.33	0.93	0.90	0.99	
				l.	0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	
					0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	

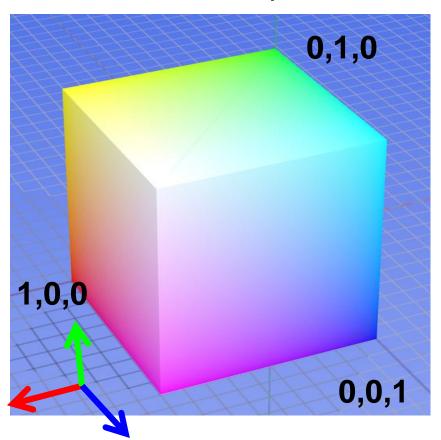
## Color spaces

How can we represent color?



## Color spaces: RGB

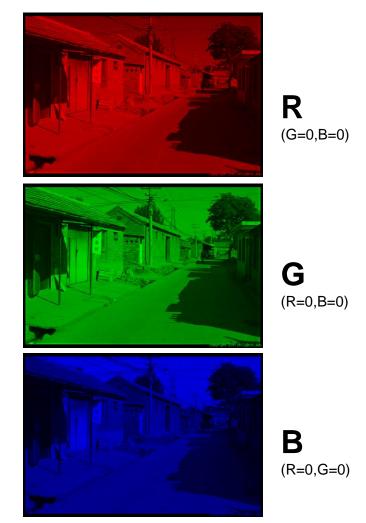
#### Default color space



#### Some drawbacks

- Strongly correlated channels
- Non-perceptual

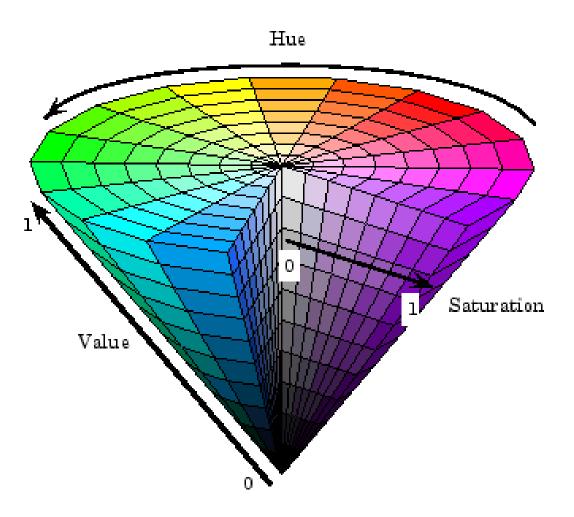


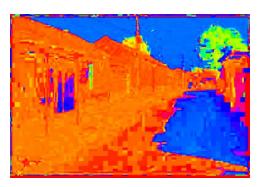


## Color spaces: HSV



#### Intuitive color space





**H** (S=1,V=1)



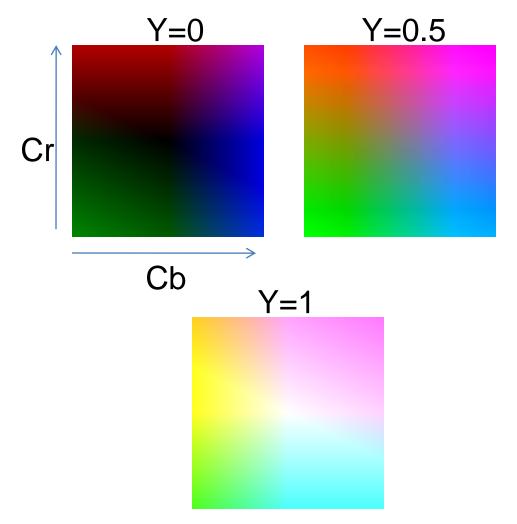
**S** (H=1,V=1)



**V** (H=1,S=0)

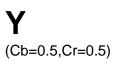
## Color spaces: YCbCr

Fast to compute, good for compression, used by TV











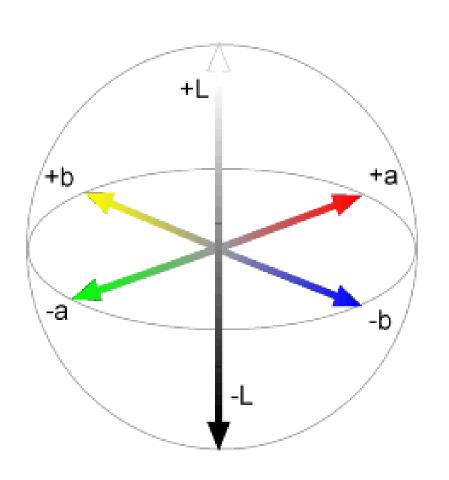
**Cb** (Y=0.5,Cr=0.5)



**Cr** (Y=0.5,Cb=05)

## Color spaces: L\*a\*b\*

"Perceptually uniform" color space





(a=0,b=0)

a

(L=65,b=0)





If you had to choose, would you rather go without luminance or chrominance?

If you had to choose, would you rather go without luminance or chrominance?

## Most information in intensity



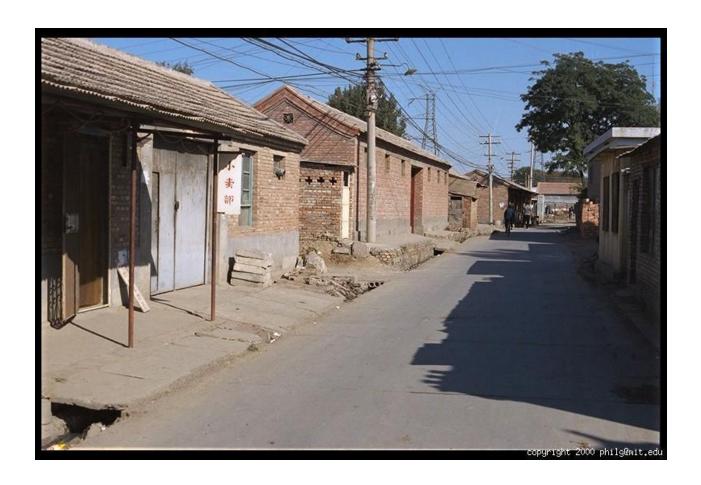
Only color shown – constant intensity

## Most information in intensity



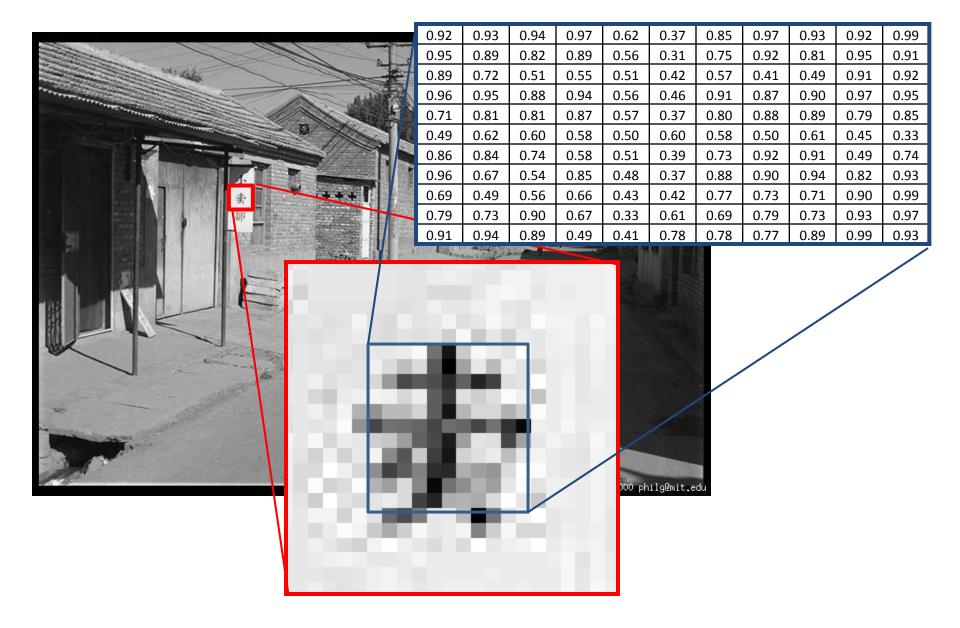
Only intensity shown – constant color

## Most information in intensity



Original image

## Back to grayscale intensity



# Image Filtering

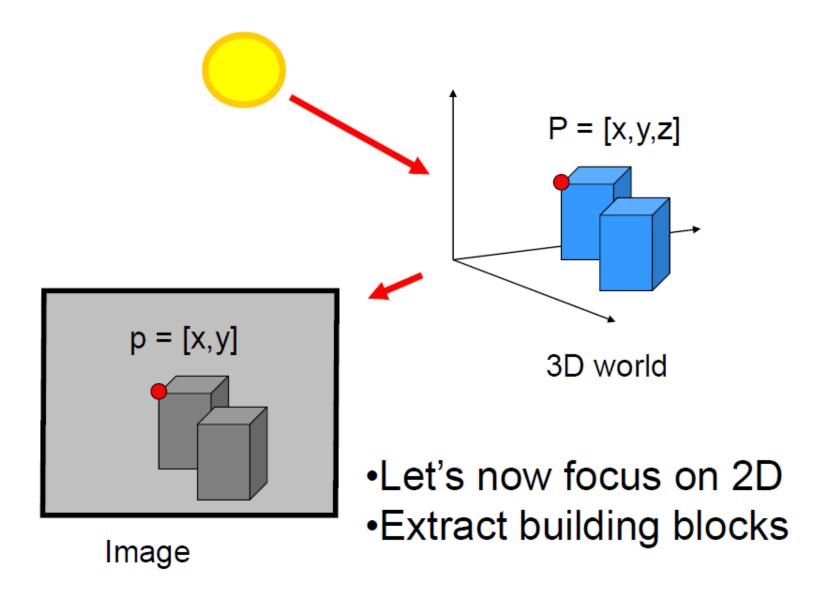


Computer Vision
James Hays

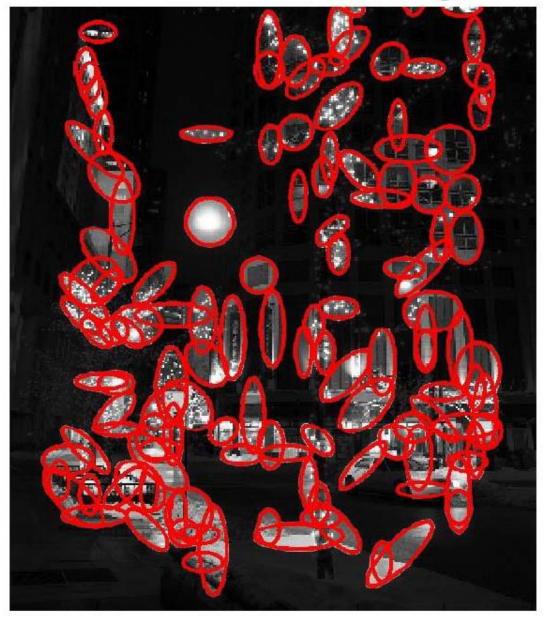
# Project 1



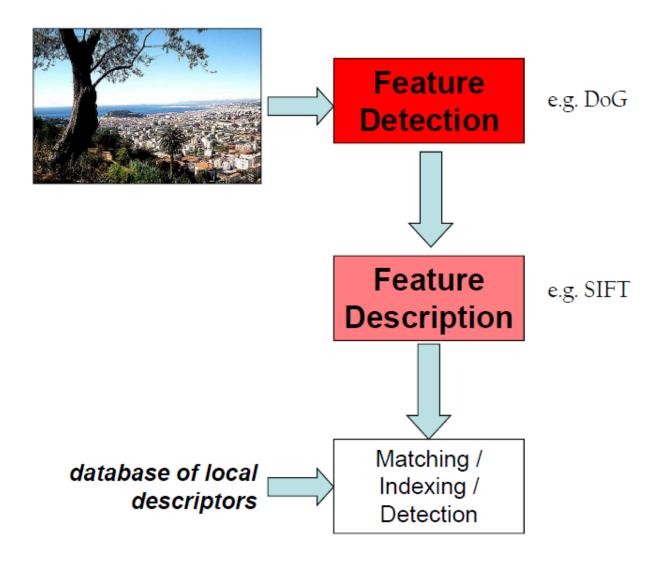
#### From the 3D to 2D



### Extract useful building blocks



# The big picture...



### Upcoming classes: three views of filtering

- Image filters in spatial domain
  - Filter is a mathematical operation of a grid of numbers
  - Smoothing, sharpening, measuring texture
- Image filters in the frequency domain
  - Filtering is a way to modify the frequencies of images
  - Denoising, sampling, image compression
- Templates and Image Pyramids
  - Filtering is a way to match a template to the image
  - Detection, coarse-to-fine registration

 Image filtering: compute function of local neighborhood at each position

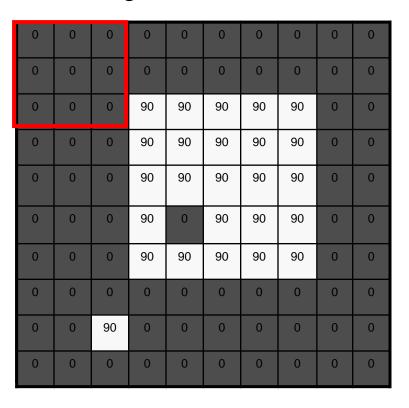
- Really important!
  - Enhance images
    - Denoise, resize, increase contrast, etc.
  - Extract information from images
    - Texture, edges, distinctive points, etc.
  - Detect patterns
    - Template matching
  - Deep Convolutional Networks

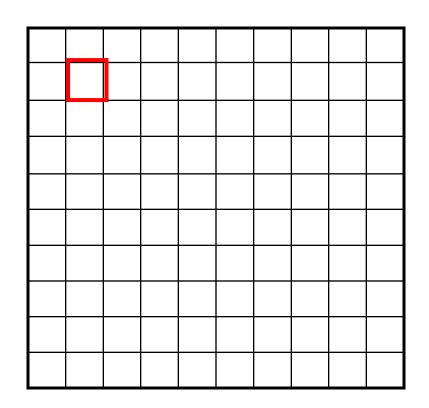
### Example: box filter

$$g[\cdot,\cdot]$$

$$\frac{1}{9}\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

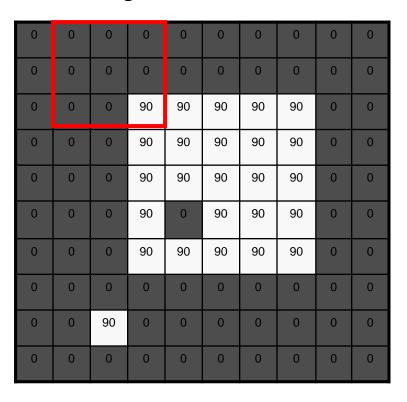
$$g[\cdot,\cdot]^{\frac{1}{9}}$$

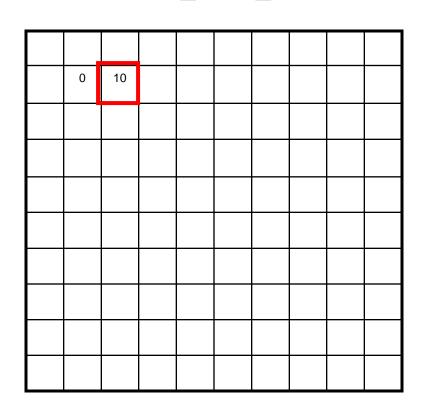




$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

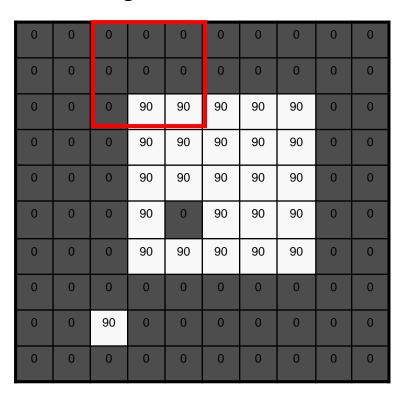
$$g[\cdot,\cdot]^{\frac{1}{9}}$$

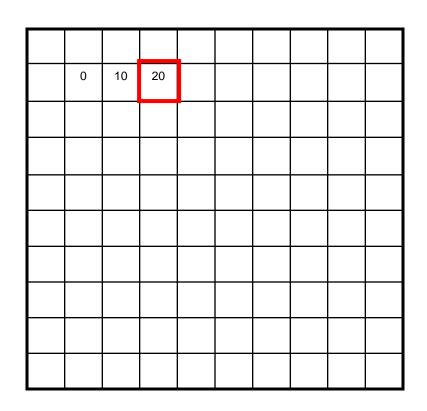




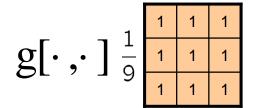
$$h[m,n] = \sum_{l=1}^{n} g[k,l] f[m+k,n+l]$$

$$g[\cdot,\cdot]^{\frac{1}{9}}$$

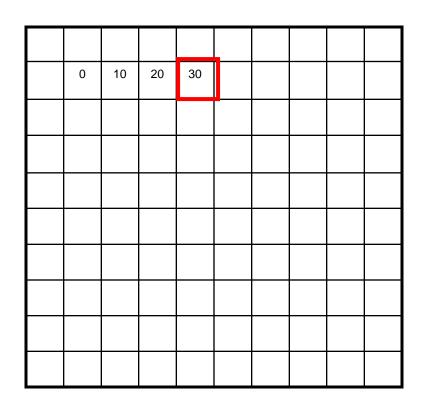




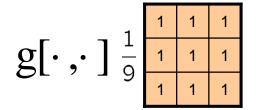
$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

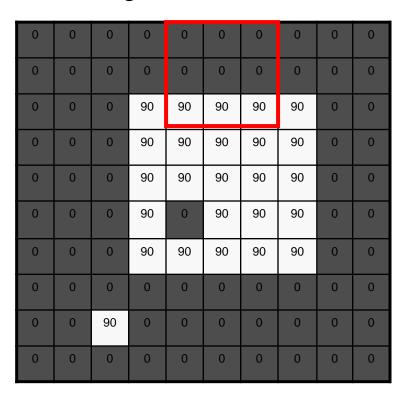


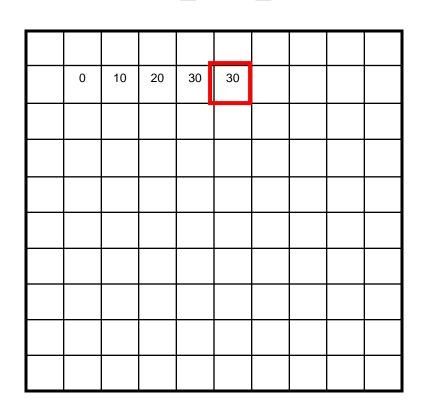
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



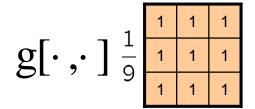
$$h[m,n] = \sum_{l=1}^{n} g[k,l] f[m+k,n+l]$$



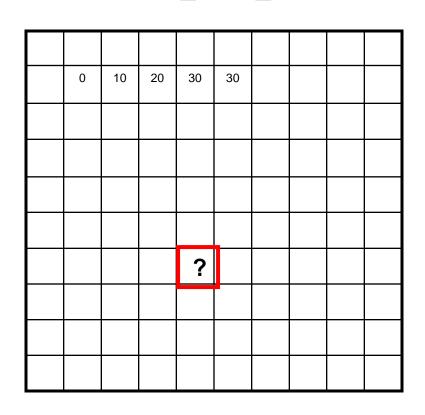




$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$



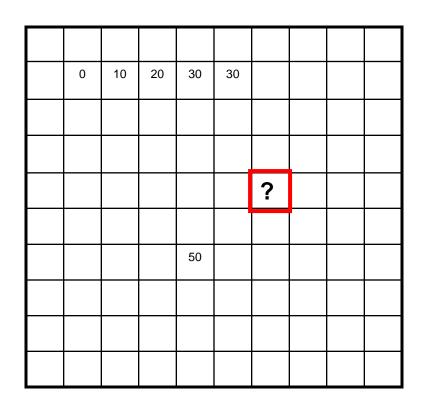
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



$$h[m,n] = \sum_{l=1}^{n} g[k,l] f[m+k,n+l]$$

$$g[\cdot,\cdot]^{\frac{1}{9}}$$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

$$g[\cdot,\cdot]_{\frac{1}{9}}$$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

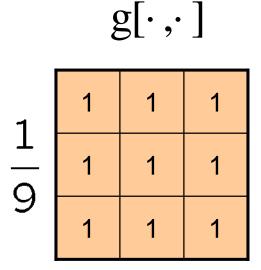
0	10	20	30	30	30	20	10	
0	20	40	60	60	60	40	20	
0	30	60	90	90	90	60	30	
0	30	50	80	80	90	60	30	
0	30	50	80	80	90	60	30	
0	20	30	50	50	60	40	20	
10	20	30	30	30	30	20	10	
10	10	10	0	0	0	0	0	

$$h[m,n] = \sum_{l=1}^{n} g[k,l] f[m+k,n+l]$$

#### **Box Filter**

#### What does it do?

- Replaces each pixel with an average of its neighborhood
- Achieve smoothing effect (remove sharp features)



# Smoothing with box filter





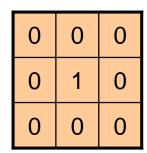
O	rię	gir	nal
	-	_	

0	0	0
0	1	0
0	0	0





Original





Filtered (no change)



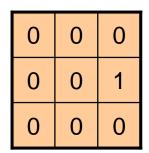
$\sim$	•	•	1
$O_1$	r19	711	าลไ
<u> </u>	٦- ٦	>**	101

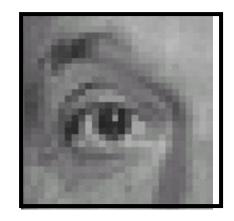
0	0	0
0	0	1
0	0	0





Original





Shifted left By 1 pixel



Original

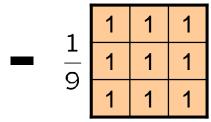
0	0	0	1	1	1	1
0	2	0	<u> </u>	1	1	1
0	0	0	9	1	1	1

(Note that filter sums to 1)

Source: D. Lowe



0	0	0
0	2	0
0	0	0



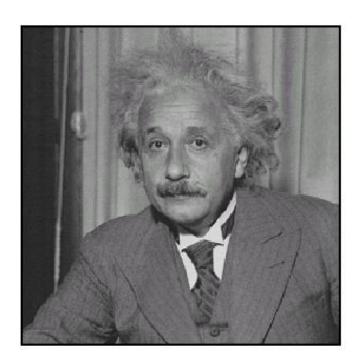


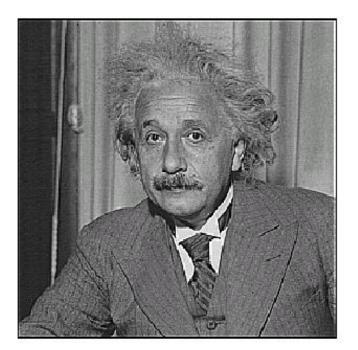
Original

#### **Sharpening filter**

- Accentuates differences with local average

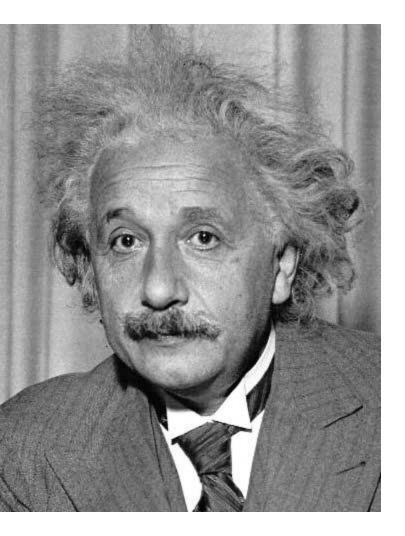
# Sharpening





before after

### Other filters



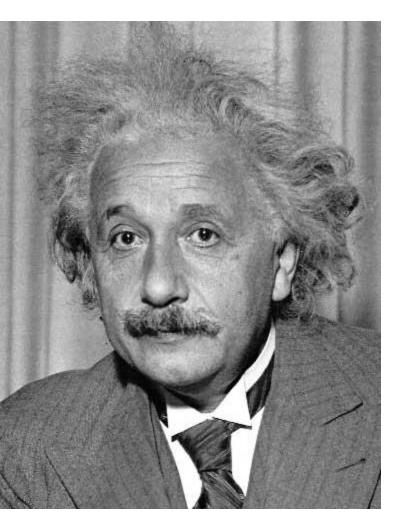
1	0	-1
2	0	-2
1	0	-1

Sobel



Vertical Edge (absolute value)

### Other filters



1	2	1
0	0	0
-1	-2	-1

Sobel



Horizontal Edge (absolute value)

### Filtering vs. Convolution

• 2d filtering f=filter I=image -h=filter2(f,I); or h=imfilter(I,f);  $h[m,n] = \sum_{k,l} f[k,l] I[m+k,n+l]$ 

#### 2d convolution

-h=conv2(f, I); 
$$h[m,n] = \sum_{k,l} f[k,l] I[m-k,n-l]$$

### Key properties of linear filters

#### **Linearity:**

```
imfilter(I, f_1 + f_2) =
imfilter(I, f_1) + imfilter(I, f_2)
```

# **Shift invariance:** same behavior regardless of pixel location

```
imfilter(I, shift(f)) = shift(imfilter(I, f))
```

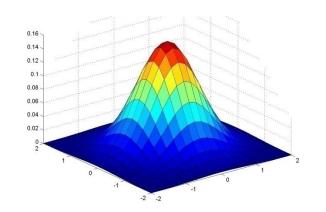
Any linear, shift-invariant operator can be represented as a convolution

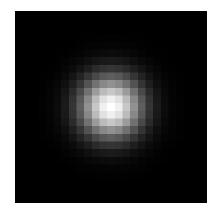
### More properties

- Commutative: *a* \* *b* = *b* \* *a* 
  - Conceptually no difference between filter and signal
  - But particular filtering implementations might break this equality
- Associative: a \* (b \* c) = (a \* b) \* c
  - Often apply several filters one after another:  $(((a * b_1) * b_2) * b_3)$
  - This is equivalent to applying one filter: a \*  $(b_1 * b_2 * b_3)$
- Distributes over addition: a \* (b + c) = (a \* b) + (a \* c)
- Scalars factor out: ka \* b = a \* kb = k (a \* b)
- Identity: unit impulse e = [0, 0, 1, 0, 0],
   a \* e = a

### Important filter: Gaussian

Weight contributions of neighboring pixels by nearness





0.003	0.013	0.022	0.013	0.003
0.013	0.059	0.097	0.059	0.013
0.022	0.097	0.159	0.097	0.022
0.013	0.059	0.097	0.059	0.013
0.003	0.013	0.022	0.013	0.003

$$5 \times 5$$
,  $\sigma = 1$ 

$$G_{\sigma} = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

# Smoothing with Gaussian filter



# Smoothing with box filter



#### Gaussian filters

- Remove "high-frequency" components from the image (low-pass filter)
  - Images become more smooth
- Convolution with self is another Gaussian
  - So can smooth with small-width kernel, repeat, and get same result as larger-width kernel would have
  - Convolving two times with Gaussian kernel of width  $\sigma$  is same as convolving once with kernel of width  $\sigma$ V2
- Separable kernel
  - Factors into product of two 1D Gaussians

### Separability of the Gaussian filter

$$G_{\sigma}(x,y) = \frac{1}{2\pi\sigma^2} \exp^{-\frac{x^2 + y^2}{2\sigma^2}}$$

$$= \left(\frac{1}{\sqrt{2\pi}\sigma} \exp^{-\frac{x^2}{2\sigma^2}}\right) \left(\frac{1}{\sqrt{2\pi}\sigma} \exp^{-\frac{y^2}{2\sigma^2}}\right)$$

The 2D Gaussian can be expressed as the product of two functions, one a function of x and the other a function of y

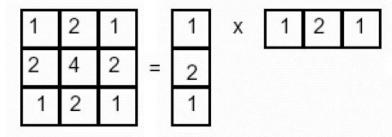
In this case, the two functions are the (identical) 1D Gaussian

### Separability example

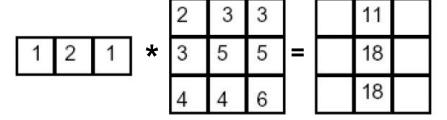
2D convolution (center location only)

1	2	1		2	3	3
2	4	2	*	3	5	5
1	2	1		4	4	6

The filter factors into a product of 1D filters:



Perform convolution along rows:



Followed by convolution along the remaining column:

# Separability

Why is separability useful in practice?

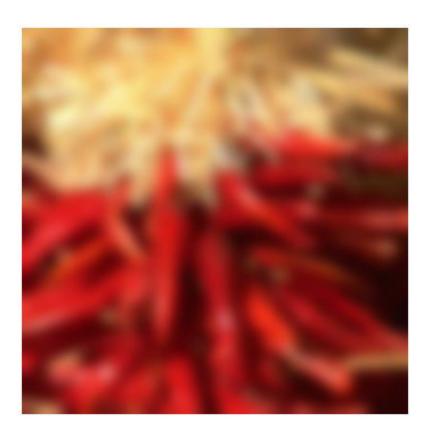
# Some practical matters

# Practical matters How big should the filter be?

- Values at edges should be near zero
- Rule of thumb for Gaussian: set filter half-width to about 3  $\sigma$

#### Practical matters

- What about near the edge?
  - the filter window falls off the edge of the image
  - need to extrapolate
  - methods:
    - clip filter (black)
    - wrap around
    - copy edge
    - reflect across edge



To be continued...

### Next class: Thinking in Frequency

