Lil' Trie Adventure

(alternative node definitions for smaller memory footprints)

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Abstract

We have studied *tries*, a specialized tree designed for the quick search of sequenced data such as words or IP addresses. Our lecture and 3P version of lowercase word tries allocated 26 pointers (208 bytes!) to store the .children[] of each node.

This project has you consider more specialized node structures designed to reduce the overall memory footprint of the 3P word trie and investigates the run-time trade-off in doing so.

Part 1

Clone the LilTrieAdventure repo according to the Canvas assignment instructions. Drop in your header and source file from the Trie programming project and follow the README.md instructions to make sure you can build run-main.

Take Note 1: The CMakeLists.txt expects your header and source to be trie.h and trie.cpp, but you can change these names if you choose.

Additionally, this write-up assumes you've used a singular class (trie_node) as opposed to a nested two-class structure, like trie::node. You aren't required to use the former but you'll need to make some mental translations and perhaps some "wrapper" functions in your top level (trie) class. You're permitted to change any of the functions provided in liltrie.h — we are interested in your results, not so much the code gymnastics to get them.^a

 a This would be a wonderful project to learn about C++ polymorphism, user-defined iterators and virtual base class design — but these are beyond the scope of this course and assignment. It makes me sad :/

The first thing we will do is add some statistics collecting member functions to your trie_node class. We'll refer to the base 3P trie node structure as trie_node, you may have called it something else. That's not a big deal.

- void trie_node::finalize() {}: for now this function can do nothing, you may choose to use it in Part 4 of this analysis. (But it needs to be implemented for compilations.)
- size_t trie_node::node_children() reports the number of children a node has. For the 3P Trie code, you'll need to iterate through .children[] and return the count of non-nullptr's in the array.
- size_t trie_node::descendants() reports the total number of child edges at and below the current node. The calculation of this is the sum of ::descendants() for all of the calling object's children plus node_children() of the calling object.
- void trie_node::children_histogram(vector<size_t>& histo) should increment the
 node_children() valued index in histo by one:

histo[this->node_children()]++;

and recursively call child_histogram on its children with the same histo parameter.

Once you have the node member functions implemented and compiling cleanly, change the zero in main-lta.cpp's #if line to a 1 and rebuild. The test_node_functions<Y> parameterized function in main() will make sure your implementations compile cleanly. You will probably want to populate the string of vectors with data from the wordlists files for a more thorough test.

Expected values for the various word dictionaries used in this project are in the test_node_functions directory of the repo.

Take Note 2: If test_node_functions<Y> is called with a dictionary less than 2000 words or with sample=false, it will put all the dictionary vector's words into the trie. If the dictionary has more than 2000 words and sample=true, it will put a random number of words into the trie and test .contains() for both included and un-included words. The default value for the function is sample=false.

test_node_functions<Y> always randomizes the order in which words go into your trie and the order in which they are tested for appropriate .contains() results.

Now we want to collect some statistics about the structure of our uncompressed trie after it has stored a dictionary of words. We will build a count histogram of the node_children() results in our trie. This is best done with a helper function, which has been provided to you in liltrie.h.

Provide collect_child_histogram<Y> an empty trie of your creation, a vector of strings read from one of the project dictionaries (you've done similar word reading in 2A) and the size_t vector for the histogram.

collect_child_histogram<Y> has two optional parameters, if sample_size=COLLECT_CH_FULLSIZE
then all the dictionary vector words are used, if sample_size=COLLECT_CH_RANDOMSIZE a random
number of words are sampled, and if sample_size>1) a precise number of words are sampled. The
default for collect_child_histogram<Y> is to sample a random number of words from the dictionary
vector.

If the Boolean parameter show=true, collect_child_histogram<Y> will display to the console the histogram result as both counts and population fractions.

Expected values for the smaller word dictionaries (size < 2000) are in the project's child_histogram directory of the repo. If your implementation results from calling collect_child_histogram() don't match up, the issue is likely in your descendants() or node_children() member functions. Of course, you can always inspect liltrie.h for collect_child_histogram() implementation details.

The value at child_histogram[i] is the number of nodes in the trie that have i children (or the fraction of nodes in the trie with i children, if you are looking at the frequency histogram results).

Part 2 – a smaller trie node

Our first alternative node structure to investigate stems from the observation that the majority of tree nodes have in fact a small number of children. Our new node structure takes advantage of this feature by using a fixed size smaller array to hold the children pointers for the majority of nodes. We'll call the size of this fixed child pointer array T. If a node has more than T children, an additional array of LETTERS-T pointers is allocated and maintained to hold the overflow (LETTERS is the size of the language alphabet, in our case 26).

```
struct trie_Tnode {
  bool is_terminal;
  char fixed_letters[T];
  struct trie_Tnode* fixed_children[T];
  typedef trie_Tnode* trie_Tnode_ptr;
  struct trie_Tnode_ptr* *overflow_children;
};
```

In this case, we have used a typedef for a trie_Tnode pointer, which should make reading and writing this code more straightforward for students. (It can be a more approachable way for students to think of "pointers to pointers.") The typedef is used only at compile time, so it does not increase the memory footprint of a trie_Tnode.

You may not have to implement trie_Tnode for this project, so hold off on writing code for it just now! But we do want to explain how it works so you can be convinced it is a valid structure for a compressed Trie.

We have included a fixed_letters[] array so we know which characters are associated the with edges stored in fixed_children. (In 3P, we knew this information implicitly by adding 'a' to the index of our children array.) When trying to find the edge associated with a character, we would follow these steps:

Access a trie_Tnode letter edge

a. First consider the T fixed_letters[] values. If any of these are for the edge we seek, we are done.

- b. If the overflow_children pointer is nullptr, then we don't have an edge for the letter we seek and we are done.
- c. Otherwise, we iterate through the LETTERS-T elements of overflow_children, associating 'a' with index 0, 'b' with index 1 and so forth. EXCEPT (and this is the tricky part) we skip over the T letters held in fixed_letters. So if T=2 and fixed_letters={'a', 'c'}, overflow_children[0] is associated with the 'b' edge, overflow_children[1] is associated with the 'd' edge.

The size of this alternative node in memory depends on T and the total number of child edges stored in the node (C).

```
nodeSize(C) = \begin{cases} sizeof(bool) + T \times sizeof(char) \\ + T \times sizeof(trie\_Tnode*) + sizeof(trie\_Tnode\_ptr*) & C \leq T \\ sizeof(bool) + T * sizeof(char) \\ + T \times sizeof(trie\_Tnode*) + sizeof(trie\_Tnode\_ptr*) & \text{otherwise} \\ + (LETTERS - T) \times sizeof(trie\_Tnode\_ptr) \end{cases}
```

data member	memory allocated	size in bytes
is_terminal	allocated with object	sizeof(bool)
<pre>fixed_letters[0] fixed_letters[1] : fixed_letters[T-1]</pre>	$\left\{ \begin{array}{ll} \text{allocated with object} \end{array} \right.$	T*sizeof(char)
<pre>fixed_children[0] fixed_children[1] : fixed_children[T-1]</pre>	$\left\{ egin{array}{l} { m allocated \ with \ object} \end{array} ight.$	T*sizeof(trie_Tnode*)
overflow_children	allocated with object, initialized to nullptr, valued with new in .insert() as needed	<pre>sizeof(trie_Tnode_ptr*)</pre>

How much space can be saved with this $trie_Tnode$ structure? It depends on T (of course) so the task is to determine the optimal T given the $child_histogram$ valued from $collect_child_histogram()$.

Let N = nodes in the trie, N=root.descendants(). Let s = number of nodes in the trie with $\leq T$ children (so N - s is the number of nodes in the trie with > T children). The memory footprint of a trie using trie_Tnode nodes is

$$footPrint = s \times nodeSize(T) + (N-s) \times nodeSize(T+1)$$

Clearly, we could use this equation to find the optimal T value for a particular dictionary, which is to say the T that produces the smallest trie footPrint.

Part 3 - empirical evidence

Include the struct trie_Tnode definition in your program source and write two functions: trie_node_footprint and trie_Tnode_footprint. All the *_footprint functions in this project will take the same parameter list, we show the details with trie_Tnode_footprint:

size_t trie_Tnode_footprint(size_t N, const vector<size_t>& child_histogram);
where N is the total number of nodes in a trie and child_histogram is the data determined from
collect_child_histogram().

 $trie_Tnode_footprint()$ should return the smallest footprint a trie would have using $trie_Tnode$ nodes — you don't have to report the optimal T, but you are welcome to print it to the console for debug or testing.

The trie_node_footprint() calculation is much simpler, it is based on the "3P" of a Trie and is simply:

```
return N*(sizeof(bool) + LETTERS*sizeof(trie_node*))
```

data member	memory allocated	size in bytes		
is_terminal	allocated with object	sizeof(bool)		
<pre>children[0]</pre>	(
children[1]				
:	allocated with object	LETTERS*sizeof(trie_node*)		
	1			
children[LETTERS-1]	(

Write a loop to run an experiment (tweak the following as you see fit):

- 1. Read the words from the project dictionary (dictionary.txt) into a vector.
- 2. For some reasonably large value of EXPERIMENTS:

```
vector<size_t> histogram_data[LETTERS+1];
while( EXPERIMENTS-- ) {
   trie = myTrie();
   collect_child_histogram( trie, words_vector, histogram_data);
   size_t N = trie.descendants();
   node_footprint = trie_node_footprint( N, histogram_data );
   Tnode_footprint = trie_Tnode_footprint( N, histogram_data );
   resultsFile << N << " " << node_footprint << " " << Tnode_footprint << endl;
}</pre>
```

A second, even smaller trie node

Both the 3P trie node definition and the $trie_Inode$ definition over-allocate space for children (the $trie_Inode$ does this only when the number of children is not exactly T). We can reduce the footprint of a trie node even more with some bit-twiddling and allocating a children[] array for only the number of children needed for each node.

We'll call this final node structure a trie_Mnode, where M stands for "mask" or more accurately "bitmask". A bitmask uses a standard integer data type but treats each bit as a Boolean value. Our LETTERS=26, so we can have a flag for each character, when that flag is on or "up", then our node has a valid pointer for the character edge in its children array. A four byte integer (int) has 32 bits, so we have more flags than needed for characters, let's use the last flag as our is_terminal Boolean.

The mask layout (labeling the bits with indices 0–31) would be

bit index	0	1	2	3	4	5	·	23	24	25		31
associated with	'a'	'b'	'c'	'd'	'e'	'f'		'x'	'y'	'z'	(unused)	is_terminal

(See the Helpful hints appendix to this write-up for bitwise manipulation of masks — but not before you've read through Part 4!)

The trie_Mnode data declaration would be:

```
struct trie_Mnode {
   int mask;
   typedef trie_Mnode* trie_Mnode_ptr;
   trie_Mnode_ptr* children;
};
```

The memory footprint of this data structure depends on the absolute number of children a node has, C. There is no flexible parameter like T in trie_Tnode. The memory footprint of trie_Mnode is simply: sizeof(int) + sizeof(trie_Mnode_ptr*) + C*sizeof(trie_Mnode*)

Deliverable 1

Incorporate a $trie_Mnode_footprint$ function into your application code and generate a scatterplot with N on the independent horizontal axis and the results of our three trie node memory footprints each in their own series. Provide this final three series scatterplot in your submission.

Deliverable 2

Summarize your scatterplot results by answering these questions.

- a. How much space savings would you expect to gain for storing a dictionary of 100,000 words?
- b. Is the percentage of expected savings consistent across a range of dictionary sizes?
- c. Which O(n) relationships that we've studied $(O(1), O(n), O(n \log n), \ldots)$ might this space savings belong to? We aren't asking you to derive this relationship! Just comment on which it might be.

Runtime considerations

While we have decreased the memory footprint of the trie, have we changed its runtime complexity? If so, to what extent? Consider this: with trie_node constructed tries (as in 3P) there is immediate access to the child pointer of a letter. It is simply .children[letter-'a'], that's $\mathcal{O}(1)$ for those of you who are counting:)

With trie_Tnode, things aren't as simple (recall the Access a trie_Tnode letter edge algorithm mentioned before). If n=LETTERS — what is the $\mathcal{O}(n)$ of this algorithm? What are its average (expected) and worst case? Hint: an overly simple solution is **not** $\mathcal{O}(1)$ — but you might do better...

On the other hand, we see substantial space savings with both trie_Tnode and trie_Mnode, which might translate to better cache performance and mitigate some of the worsened runtime complexity. It's "time" to let the our machines weigh in on this question!

Part 4 — runtime performance

How do these two different compressed node trie implementations fair at runtime? Is it worth it to use substantially more memory for better performance? The last question depends on the application needs and its runtime environment (is it on a small embedded device with limited memory?). In a professional setting you would want to collect some performance measures to guide your decision — and this is precisely what you'll do in this last part of the project.

We ask you to implement **only one** of the two compressed node definitions and report your findings compared to your original trie definition (the 3P node structure). There are two ways you can go about this task. Regardless of your approach you will need to run your timing experiments on both your 3P **trie_node** structure and your compressed node trie.

On the fly

You can write a brand new trie class and manage the compressed node structure from start to finish. This means implementing the constructor, destructor, .insert() and .contains() (at least). There is more memory management required for this scheme, but it's not too much to ask from students in this course. We call this "on the fly" because you'll be allocating memory as needed in .insert().

Using .finalize()

You can also copy your current trie class definition (or, if you're into the whole class hierarchy approach, you could inherit from your original trie class) and implement or rework the .finalize(), .contains() and destructor functions for the class. The advantage to this approach is that it doesn't require any memory management and you won't have to debug .insert() and constructor logic for a brand new class.

The key to this solution is the .finalize() member function. This is called by all the routines in liltrie.h after all words have been .insert()'d into a trie. When .finalize() is called, you can morph the data stored in your 3P node structures into the member variables associated with your chosen compressed trie node. You may see how this would work in code right off the bat, if not see item V. in the Helpful hints appendix to this write-up.

Generating paired timed comparisons

When you have your compressed node compiling cleanly, test it with test_node_functions<Y> and varying sized dictionaries. Compare the results against your original trie implementation and make sure the reported metrics match up.

Finally, you're ready for the last bit of data generation in CSCI220!

Use the time_trials<Y,O> function defined in liltrie.h to generate a pair of std::chrono::duration<double> values. The returned pair's .first is the runtime for the Y trie class, it's .second is the runtime for the O trie class. The function should be provided with empty tries for comparison (the Y trie being your 3P equivalent, the O trie being your compressed node implementation), a dictionary of words and an optional Boolean finalize parameter. The default value for finalize is true. Your invocation might look like:

```
myTrie trie3P;
trie_Tnode trie0;
auto secs = time_trials( trie3P, trie0, dictionary )
size_t W = trie3P.size();
cout << W << " " << secs.first << " " << secs.second << endl;</pre>
```

If you have implemented an "on the fly" compressed node, you can provide finalize=false and the timing results will reflect the total load time as well (all the .insert() calls).

You will provide a scatterplot of these timing results for your submitted write-up to this project. Of course this could be a simple two series plot with W on the horizontal access and runtime on the vertical axis. However care has been taken in $time_trials<\Upsilon,0>$ to make sure that each trie sees the same order of words for both .insert()'ions and .contain()s tests — so it is legitimate to compare these values directly within one experiment.

Consider the following four styles of scatterplot graphs to show your results, if t_{3P} and t_{O} are the .first and .second values for one experiment:

a. You could plot the difference in time vs trie size:

$$(W, t_O - t_{3P})$$

b. The percentage increase in runtime by the compressed node:

$$(W,(t_O-t_{3P})/t_{3P})$$

c. The difference in time normalized by the number of words in the trie:

$$(W, (t_O - t_{3P})/W)$$

d. Or you could plot the coordinate pair (t_{3P}, t_O) along with the line of identity (y = x). If these points lie on or near the line of identity it means the runtime performance is nearly identical. If the points lie above y = x, then t_O is consistently $> t_{3P}$.

Deliverable 3

Choose your preferred graphic presentation(s), make sure the axis, title and labels are accurate and provide a plot of your runtime results. **Also**, be sure to state whether you have coded an "on-the-fly" or .finalize() solution.

Deliverable 4

Among the implementations you've provided runtime results for, which would prefer to use in a real world application? What development or runtime factors might influence your choice?

Deliverable 5

Finally, copy and paste a nicely formatted version of the .contains() logic of your compressed node implementation and any other functions it may call. Use a fixed width font, single line spacing and consistent block indentation for this in your report.

Helpful hints

I. For "on the fly" implementations, You want to avoid memory leaks and corrupted data, fortunately our runtime needs for a compressed trie node are simple: allocate memory as needed in .insert() and make sure our destructor frees all memory for a node. You really want to avoid the stray typo or synapse misfire and accidentally copy construct or assign a node, because without these procedures properly implemented you will likely have very hard to debug issues when testing large tries. Recall that C++ will provide default (aka, dumb, wrong) versions of

these "big 3" functions for you. You can prevent this by providing declarations for these in your class definition, and then not providing procedure definitions. So your trie_Mnode should have the following prototypes:

```
trie_Mnode( const trie_Mnode& trie );
trie_Mnode& operator=( const trie_Mnode& rhs );
```

Providing these will prevent C++ from using its default versions. Now when you would have introduced memory errors, you'll be greeted with linker errors when building. And hopefully you'll say to yourself: "Wait a minute — I shouldn't need an assignment operator!"

II. For "on the fly" implementations of trie_Mnode, you can use the following bitwise operators for turning bits on and testing their state:

```
// bit is 0 to 31
static inline bool bit_on( int mask, unsigned bit )
{ return mask & (1<<bit); }
static inline int set_bit_on( int mask, unsigned bit )
{ return mask | (1<<bit); }
```

III. For "on the fly" implementations, remember that

```
children = new trie_Xnode_ptr[Q];
```

does not initialize the elements to nullptr — you have to do that yourself.

IV. For the trie_Tnode compressed node, a small insight into the Access a trie_Tnode letter edge algorithm can make a substantial improvement in the node's runtime performance. We need to avoid a one-by-one search of .overflow_children[], which seems difficult because for each letter slot to consider, that letter might be in the .fixed_letters[] array and should be ignored. Here is a nice idea:

If this were a 3P trie node, we would know the slot in .overflow_children[] associated with a letter, it would be letter-'a'. And, in fact, this is slot we should inspect if all the values in .fixed_letters[] come after the query letter in the alphabet! Some examples:

- A. if .fixed_letters[] = {'s', 'b', 'q'} and we are looking for 'a', it is still in slot 0 of .overflow_children[] because s, b, and q are all after a in the alphabet.
- B. with the same .fixed_letters, if we are looking for 'r', it won't be at slot 'r'-'a', because b and q come before r and their edges are stored in .fixed_children[1] and .fixed_children[2] respectively. The r slot of .overflow_children[] is 'r'-'a'-2.
- C. one more: 'z' won't be at index 25 of .overflow_children[] because s, b, and q have their edges stored in .fixed_children[]. So the z edge is at .overflow_children[LETTERS-T-1] (or 'z'-'a'-3).

Do you see the pattern? If we are looking for an edge associated with the letter L

- a. first calculate the variable int L_in_overflow=L-'a';
- b. when inspecting each letter F in .fixed_letters, decrement L_in_overflow by one if F < L.
- c. now, if you have to consider .overflow_children[] (L is not in .fixed_letters, and .overflow_children != nullptr), the slot to inspect is .overflow_children[L_in_overflow].
- V. Here are more details for implementing the finalize() approach for runtime measurements. Recall from the initial description, the idea here is to leverage the code and structure already written (and working!) for 3P in order get runtime measurements with the least amount of code to write and debug.

The steps for implementing .finalize() "fake" compressed nodes are:

- (a) Copy your 3P trie class header and source files as starting points to your compressed node implementation.
- (b) Keep all the data members of your original class, augment the class' definition with the data members you'll need to "fake" your compressed node at runtime (details for trie_Tnode and trie Mnode below.
- (c) Implement finalize() for the node to convert the 3P stored data into the design used by your compressed node (again, an example for each are below).
- (d) Change your .contains() implementation to only use the information stored for your particular compressed node.
- (e) If you wrote a **destructor** for your original 3P class, change that as well to reflect your compressed node design.

The examples below show possible "fake" compressed node implementations the will permit accurate runtime measurements. In each case we try to reuse the object footprint of the 3P trie node defintion to the greatest extent.

Each compressed node example shows how data from an arbitrary node would be translated from the 3P structure to the "fake" compressed mode structures. In both cases we show the result of

.finalize() would be for a terminal node containing child edges associated with the letters a, c, h, q, t and v.

Example: converting from trie_node to trie_Tnode

Our "trie_Tnode augmented" 3P trie_node structure would look like:

```
struct fake_trie_Tnode {
   static const int T=17;     // pick a better value guided by your histograms :)
   /** trie_node data members **/
   bool is_terminal;
   fake_trie_Tnode* children[LETTERS];
   /** need to know which letters are in the ``fixed'' block */
   char fixed_letters[T];
};
```

For the example, we'll suppose trie_Tnode::T=4. We pretend the first T slots of children are trie_Tnode::fixed_children, and indexes T through LETTERS-T of children are trie_Tnode::overflow_children — your .contains() should be re-written appriopriately!

trie_node:: data member	value	moved to fake_trie_Tnode:: data member(s)
is_terminal	true	is_terminal (same)
children[0]	0x40007780	fixed_letter[0]='a'; children[0] = $0x40007780$;
children[1]	nullptr	none
children[2]	0x40007880	fixed_letter[1]='c'; children[1] = $0x40007880$;
:		
children['h'-'a']	0x40007980	fixed_letter[2]='h'; children[2] = $0x40007980$;
children['q'-'a']	0x40007c80	fixed_letter[3]='q'; children[3] = $0x40007c80$;
:		
	0400071-90	ah i 3 da an [141 151 4] 0 - 40007h 90.
children['t'-'a']	0x40007b80	children['t'-'a'-4] = $0x40007b80;$
children['v'-'a']	0x40007a80	children['v'-'a'-4] = 0x40007a80;

Take Note 3: The special case of children[0] being unchanged in this example is because this node has an 'a' edge. This is certainly *not* gauranteed for every node in a trie

Example: converting from trie_node to trie_Mnode

A "trie_Mnode augmented" 3P trie_node structure might look like:

```
struct fake_trie_Mnode {
   /** trie_node data members **/
bool is_terminal;
   fake_trie_Mnode* children[LETTERS];
   /** need a mask for trie_Mnode::contains() and destructor logic */
   int mask;
};
```

For trie_Mnode, we simply need to

- a. "Crunch" the pointers spread out in children down to the first 6 slots that would have been allocated for trie_Mnode::children,
- b. and store which letter edges exist as well as the value of is_terminal into mask.

trie_node:: data member	value	moved to fake_trie_Mnode:: data member(s)
is_terminal	true	<pre>set_bit_on(mask,31);</pre>
children[0]	0x40007780	$set_bit_on(mask,0)$; $children[0] = 0x40007780$;
children[1]	nullptr	none
children[2]	0x40007880	$set_bit_on(mask,2); children[1] = 0x40007880;$
:		
:		
children['h'-'a']	0x40007980	$set_bit_on(mask, 'h'-'a'); children[2] = 0x40007980;$
children['q'-'a']	0x40007c80	$set_bit_on(mask, 'q'-'a'); children[3] = 0x40007c80;$
:		
children['t'-'a']	0x40007b80	$set_bit_on(mask, 't'-'a'); children[4] = 0x40007b80;$
children['v'-'a']	0x40007a80	$set_bit_on(mask, 'v'-'a'); children[5] = 0x40007a80;$

Part V. wrap-up!

Take Note 4: Note that in both cases, we have "overloaded" the .children array of edge pointers to avoid the need to manage memory with new's and delete[]'s. After .finalized() is finished, we must access .children[] as if it were both .fixed_children[] and .overflow_children[] of the trie_Tnode or .children[] of trie_Mnode; in either case the first array location may or may not be an edge for the letter a!

Take Note 5: For both fake_trie_Tnode and fake_trie_Mnode .finalize() implementations, you are moving pointer values around in the your .children[] array. Be sure to nullify the pointer's old location when doing so! For instance, when finalizing the q node in the previous example, you would want to write:

```
children[3] = children['q'-'a']
children['q'-'a'] = nullptr;
```

Or course, the 'q' and 3 would probably be stored in looping variables of your logic. Nullify the old pointer locations correctly and *mostly likely*, the code you wrote for collect_child_histogram<yourTrie> will still work correctly (since you likely just traversed .children[] looking for non-null pointers....). Checking that you get identical histogram data from your original Trie object and your new .finalize()'d version is a reassuring sanity test before generating runtime results.