

How find p-value from the table for appropriate test?

TABLE C (t test statistic)

Find confidence interval for two-sample problems

Confidence interval for $\mu_1 - \mu_2$ is

$$(\bar{x}_1 - \bar{x}_2) \pm t^* \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

find t^* in the body of table C if you know df and level of confidence (95%, 90%, 99%, etc).

To find a confidence interval you need find t^* from table C

- calculate df (degrees of freedom): df is the smaller of $n_1 - 1$ and $n_2 - 1$. If you cannot find calculated df in table C, just round down to the nearest df in this table
- select the column for appropriate level of confidence.

How find t from table C?

- 1) suppose your df = 4 and level of confidence is 95%:

| DEGREES OF FREEDOM | 50% | 60% | 70% | 80% | 90% | 95% |
|--------------------|-------|-------|-------|-------|-------|-------|
| 1 | 1.000 | 1.376 | 1.963 | 3.078 | 6.314 | 12.71 |
| 2 | 0.816 | 1.061 | 1.386 | 1.886 | 2.920 | 4.303 |
| 3 | 0.765 | 0.978 | 1.250 | 1.638 | 2.353 | 3.182 |
| 4 | 0.741 | 0.941 | 1.190 | 1.533 | 2.132 | 2.776 |
| 5 | 0.727 | 0.920 | 1.156 | 1.476 | 2.015 | 2.571 |

From the table C $\rightarrow t^* = 2.776$.

Similarly, df = 4 and level of confidence is 90%: from the table C $\rightarrow t^* = 2.132$.

- 2) suppose your df = 47 and level of confidence is 95%:

| | | | | | | |
|------|-------|-------|-------|-------|-------|-------|
| 40 | 0.681 | 0.851 | 1.050 | 1.303 | 1.684 | 2.021 |
| 50 | 0.679 | 0.849 | 1.047 | 1.299 | 1.676 | 2.009 |
| 60 | 0.679 | 0.848 | 1.045 | 1.296 | 1.671 | 2.000 |
| 80 | 0.678 | 0.846 | 1.043 | 1.292 | 1.664 | 1.990 |
| 100 | 0.677 | 0.845 | 1.042 | 1.290 | 1.660 | 1.984 |
| 1000 | 0.675 | 0.842 | 1.037 | 1.282 | 1.646 | 1.962 |

df=47 isn't in table, so round down df to 40. From the table C $\rightarrow t = 2.021$.

Similarly, df = 46 and level of confidence is 90%: from the table C $\rightarrow t^* = 1.684$.

Similarly, df = 53 and level of confidence is 90%: from the table C $\rightarrow t^* = 1.676$.

TABLE C (find sample size given margin of error and level of confidence)

$$n = \left(\frac{z^*}{m}\right)^2 p^*(1 - p^*)$$

For 90% confidence level $z^* = 1.645$

For 95% confidence level $z^* = 1.960$

For 99% confidence level $z^* = 2.576$

Find p-value for t statistic: $t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$ with $df = n - 1$

Suppose you calculate t – statistic and $df = n - 1$. Also suppose your alternative hypothesis is one-sided (has sign > or <)

How find p-value from table C?

- 1) suppose your $df = 80$ and $t = 1.664$

| | | | | | |
|-------------|-------|-------|-------|-------|-------|
| 80 | 0.678 | 0.846 | 1.043 | 1.292 | 1.664 |
| 100 | 0.677 | 0.845 | 1.042 | 1.290 | 1.660 |
| 1000 | 0.675 | 0.842 | 1.037 | 1.282 | 1.646 |
| z^* | 0.674 | 0.841 | 1.036 | 1.282 | 1.645 |
| One-sided P | .25 | .20 | .15 | .10 | .05 |

Select column which contains t for appropriate df, p-value will be in the same column (row for One-sided P):
 $p = 0.05$

- 2) suppose your $df = 86$ and $t = -1.353$

| | | | | | |
|-------------|-------|-------|-------|-------|-------|
| 80 | 0.678 | 0.846 | 1.043 | 1.292 | 1.664 |
| 100 | 0.677 | 0.845 | 1.042 | 1.290 | 1.660 |
| 1000 | 0.675 | 0.842 | 1.037 | 1.282 | 1.646 |
| z^* | 0.674 | 0.841 | 1.036 | 1.282 | 1.645 |
| One-sided P | .25 | .20 | .15 | .10 | .05 |
| Two-sided P | .50 | .40 | .30 | .20 | .10 |

t value is negative, so take absolute value $t = |-1.353| = 1.353$

$df = 86$ isn't in table, so round down $df = 86$ to 80. Select columns which contains t for appropriate df, p-value also will be between these columns (row for One-sided P): $0.05 < p < 0.10$

TABLE C (one-sample proportion test)

| | | | | | | | | | | | | |
|-------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| z^* | 0.674 | 0.841 | 1.036 | 1.282 | 1.645 | 1.960 | 2.054 | 2.326 | 2.576 | 2.807 | 3.091 | 3.291 |
| One-sided P | .25 | .20 | .15 | .10 | .05 | .025 | .02 | .01 | .005 | .0025 | .001 | .0005 |
| Two-sided P | .50 | .40 | .30 | .20 | .10 | .05 | .04 | .02 | .01 | .005 | .002 | .001 |

- 1) Suppose your alternative hypothesis is one-sided, and you calculate $z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}} = 2.521$. Find p-value.

$z = 2.521$ is between $z^* = 2.326$ and $z^* = 2.576$, so p-value also will be between these columns (row for One-sided P): $0.005 < p - \text{value} < 0.01$

- 2) Suppose your alternative hypothesis is two-sided, and you calculate $z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}} = -2.13$. Find p-value.

$|z| = 2.13$ is between $z^* = 2.054$ and $z^* = 2.326$, so p-value also will be between these columns (row for Two-sided P): $0.02 < p - \text{value} < 0.04$

TABLE D (chi-square test)

Suppose your $\chi^2 = 8.32$ and $df = (r - 1)(c - 1) = 2$. Select columns which contains χ^2 for appropriate df, p-value also will be between these columns (top row): $0.01 < p < 0.02$

| df | .25 | .20 | .15 | .10 | .05 | .025 | .02 | .01 | .005 | .0025 | .001 | .0005 |
|----|------|------|------|------|------|------|------|-------|-------|-------|-------|-------|
| 1 | 1.32 | 1.64 | 2.07 | 2.71 | 3.84 | 5.02 | 5.41 | 6.63 | 7.88 | 9.14 | 10.83 | 12.12 |
| 2 | 2.77 | 3.22 | 3.79 | 4.61 | 5.99 | 7.38 | 7.82 | 9.21 | 10.60 | 11.98 | 13.82 | 15.20 |
| 3 | 4.11 | 4.64 | 5.32 | 6.25 | 7.81 | 9.35 | 9.84 | 11.34 | 12.84 | 14.32 | 16.27 | 17.73 |