

1. The velocity at the first cross section is

$$v_1 = \frac{Q}{7.854 \cdot 10^{-3} \text{ m}^2}.$$

The velocity at the second cross section is

$$v_2 = \frac{4Q}{\pi d^2}.$$

Due to Bernoulli's law,

$$v_1^2 - v_2^2 = 2g\Delta h = 3.92 \text{ m}^2/\text{s}^2.$$

By substituting the velocities, we get

$$Q^2 \left(10^4 \text{ m}^{-4} + \frac{1}{d^4} \right) = 2.418 \text{ m}^2/\text{s}^2,$$

which implies

$$Q = \sqrt{2.418 \text{ m}^2/\text{s}^2 \cdot \left(10^4 \text{ m}^{-4} + \frac{1}{d^4} \right)^{-1}}.$$

2. The potential energy of a mass m on such a planet on a height h is

$$W(h) = mh \left(g_0 - \frac{\alpha h}{2} \right).$$

The the Bernoulli equation looks like

$$p + \frac{\rho v^2}{2} + \rho h \left(g_0 - \frac{\alpha h}{2} \right).$$

3. The air masses move circumferentially under the influence of the pressure gradient. If the velocity pattern is $v(r)$, then the Newton's law states

$$\frac{\rho v^2}{r} = \frac{dp}{dr}.$$

It's natural to assume that the Bernoulli's law works for all the range of r , although it's a controversial issue. If it's true then

$$p + \frac{\rho v^2}{2} = \text{const.}$$

Differentiation yields

$$\frac{dp}{dr} + \rho v \frac{dv}{dr} = 0.$$

Comparing this equation with the Newton's, we get

$$\frac{dv}{v} = -\frac{dr}{r},$$

which solution is

$$v(r) \propto r^{-1},$$

or

$$v(r) = v_0 \frac{r_0}{r},$$

where v_0 and r_0 are some constants. As it can be seen, this solution is absurd in the range of small r , that happens because Bernoulli's law works bad for big velocities (actually, it works bad everywhere, the truth is that it's *never* true). Maybe, a better solution would be obtained from the Navier-Stokes equation.