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Please, solve this problem and also show the steps to solve it.

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1)

- a) What is the surface temperature of Betelgeuse, a red giant star in the constellation of Orion, which radiates with a peak wavelength of about 970 nm?
  - b) Rigel, a bluish-white star in Orion, radiates with a peak wavelength of 145 nm. Find the temperature of Rigel's surface?

**<u>Hint:</u>** Use Wien's displacement law

2) Let f be a positive differentiable function defined on  $(0, \infty)$ . Then

$$\lim_{n \to \infty} \left( \frac{f\left(x + \frac{1}{n}\right)}{f\left(x\right)} \right)^{n} \tag{1}$$

- a) equals 1; b) equals  $\frac{f'(x)}{f(x)}$ ; c) equals  $e^{\frac{f'(x)}{f(x)}}$  d) may not exist for some f(x).
- **3)** A monatomic gas obeys the van der Waals equation  $P = \frac{N \cdot R \cdot T}{V N \cdot b} \frac{N^2 \cdot a}{V^2}$ , where N is the total number of particles, parameter a measure of the attraction between the particles and the parameter b is the volume of the molecules per mole. This gas has a heat capacity  $C_V = \frac{3N \cdot k_B}{2}$  in the limit  $V \to \infty$  ( $k_B$  is the Boltzmann constant).
  - a) Prove, using the equation of state, that  $\left. \frac{\partial C_V}{\partial V} \right|_T = 0$ .
  - b) Use the preceding result to determine the entropy of the van der Waals gas, S(T,V) to within an additive constant.

- c) Calculate the internal energy  $\varepsilon(T,V)$  to within an additive constant.
- d) What is the final temperature when the gas is adiabatically compressed from  $\left(T_1,V_1\right)$  to final volume  $V_2$  .
  - e) How much work is done in this compression?
- **4)** Suppose a spacecraft of mass  $m_0$  and cross-sectional area A is coasting with velocity  $v_0$  when it encounters a stationary dust cloud of density  $\rho$ . Solve for the subsequent motion of the spacecraft assuming that the dust sticks its surface and that A is constant over time.