## Forier spectroscopy of a tunable spin-orbit coupled Bose gas

Ana Valdés-Curiel

Joint Quantum Institute, University of Maryland and National Institute of Standards and Technology, College Park, Maryland, 20742, USA (Dated: March 1, 2016)

The coupling between an electron's spin and motion . The high degree of control in cold atoms systems makes them ideal candidates for studying new phases of matter and simulating quantum systems. Here generate spin-orbit coupling in a spin-1 Bose-Einstein condensate using Raman transitions. We are able to measure the system's spin and momentum dependent energy spectrum by looking at the time evolution of the three spin states. We drive transitions at different detunings from Raman resonance and extract the Fourier components of the time dependent evolution to reconstruct the spectrum. We also add a periodic modulation to one Raman field which allows us to have a fully tunable spin-orbit coupling dispersion that we can directly measure using our spectroscopy technique.

Empezar con porque nos interesa soc (tal tez hacer enfasis en edge states, topological stuff, hofstadter). Describir el Hamiltoniano para un sistema de spin uno. Aadir la modulacin y explicar que modulacin es equivalente a tres frequencias (citar spin one paper) espectralmente como en ciertos lmites puedes tener acoplamiento cclico. Por que quiero medir directamente las bandas? Mencionar que hay otras tecnicas como spin injection, pero que esta tecnica ofrece la ventaja de que no necesitas hardware adicional o "reservoir states" que solo ciertos elementos tienen. Motivar eso. De ah voy a Fourier spectroscopy, funciona para un sistema conocido. Hamiltoniano modulato, comparar el gap de Molmer-Sorensen (acoplamiento entre -1 y +1) con la transicin de dos fotones. Pensar en Mariposas de Hofstater, fin.

## I. METHODS

## A. Modulated Raman Coupling

Think transfer functions and spectroscopy. Spectroscopy is a vertical cut, it looks at response of the system when driven with frequencies within the Fourier limited bandwith of the pulse.

Point to sell: modulations are cool. Maybe talk about pulsed optical lattices? Previous studies have shown that strong modulation in the Raman coupling strength for an effective spin 1/2 system lead to tunable spin-orbit coupling strength. In addition to this, the use of two Raman couplings with different frequencies in a spin one system which is equivalent to a single frequency amplitude modulated coupling leads to new magnetic phases. Here we extend the study of the effects of amplitude modulation of the Raman coupling strength. We will show that for a spin one system, we can independently tune the spin orbit-coupling strength, and in addition we can engineer a cyclic coupling between the three hyperfine sublevels. In analogy to solid state stuff we introduce a new Fourier based spectroscopy technique that we use to measure the energy-momentum dispersion bands of the system. This work opens the ground for measurements of the Hofstadter butterfly.

Aqui un poco mas sobre por que me importa tunear y porque me importa la mariposa. O en la introduccion? I should also mention that I'm going to be looking at an effective spin 1/2 system.

We consider an ultra-cold spin one system in a uniform applied magnetic field  $B\hat{e}_z$  that Zeeman splits the energy levels by  $\hbar\omega_Z=g_f\mu_BB=12MHz$ . A quadratic Zeeman shift  $\epsilon$  breaks the  $m_f=\pm 1 \leftrightarrow m_f=0$  degeneracy. We generate spin-orbit coupling between the magnetic sub levels by using a pair of cross-polarized Raman beams, propagating at a 90° as shown in Fig 1a. The system can be fully described by the Hamiltonian

$$\hat{H} = \frac{\hbar^2 \hat{k}^2}{2m} + \alpha_0 \hat{k} \hat{F}_z + 4E_L \mathbb{I} + \frac{\Omega_R}{2} \hat{F}_x + (\epsilon + 4E_L)(\hat{F}_z^2 - \mathbb{I}) + \Delta \hat{F}_z$$
(1)

where  $\alpha_0 = \frac{\hbar^2 k_L}{m}$  is the spin-orbit coupling strength and  $\Omega_R$  is the Raman coupling strength. By periodically modulating the Raman field amplitude, or equiavalently, by adding three frequencies to one of the Raman fields, the coupling strength takes the form

$$\Omega_R(t) = \Omega_0 + \Omega \cos(\delta \omega t),\tag{2}$$

which will be the key term in our Hamiltonian that will lead to tunable spin-orbit coupling.

By calculating the quasi-energies of the system using Floquet theory one can readily see the effect of this modulation in the dispersion relation. As can be seen in Fig1 (here goes an image of bands) location of the minima is shifted as well and the size of the spin-orbit gap is changed for different choices of  $\Omega_0$ ,  $\Omega$ , and  $\delta\omega$ .

We can alternatively try to find an effective Hamiltonian using a time dependent rotation. If the driving frequency is chosen so that  $\delta\omega\gg\epsilon$  and  $\delta\omega\gg4E_L$  the Hamiltonian retains the form of 1 with renormalized coefficients and quadratic Zeeman shift and an additional term that explicitly couples the  $m_f=-1$  and  $m_f=+1$  states. (cite Dalibards paper on modulations)

$$\hat{H} = \frac{\hbar^2 \hat{k}^2}{2m} + \alpha \hat{k} \hat{F}_z + 4E_L \mathbb{I} + \frac{\Omega_0}{2} \hat{F}_x + \frac{\tilde{\Omega}}{2} \hat{F}_{xz} + (\tilde{\epsilon} + 4E_L)(\hat{F}_z^2 - \mathbb{I}) + \Delta \hat{F}_z$$

$$(3)$$

with  $\alpha = J_0(\Omega/2\delta\omega)$ ,  $\tilde{\Omega} = 1/4(\epsilon + 4E_L)(J_0(\Omega/\delta\omega) - 1)$ , and  $\tilde{\epsilon} = 1/4(4E_L - \epsilon) - 1/4(4E_L + 3\epsilon)J_0(\Omega/\delta\omega)$ 

Two limiting cases of this effective Hamiltonian 3 are of interest: (1) for large quadratic Zeeman shift the system can be described as an effective spin 1/2 system where the spin orbit coupling strength and the Raman coupling can be independently tuned and (2) for small quadratic Zeeman shift we can tune the  $m_f = +1 \leftrightarrow m_f = -1$  and  $m_f = 0 \leftrightarrow m_f = \pm 1$  coupling strength as well as the spin-orbit coupling strength and the quadratic Zeeman shift, which with the addition of an optical lattice can lead to measurements of Hofstadter butterfly (cite synthetic dimensions). We will focus in the first case.

In the high field regime, when  $\epsilon > 4E_R$ , the  $m_f = -1 \leftrightarrow m_f = 0$  and  $m_f = 0 \leftrightarrow m_f = +1$  transition cannot be resonantly addressed with the same frequency. By adiabatically eliminating the  $m_f = 0$  state we can describe the system in terms of an effective spin 1/2 (cite lindsay's paper here) with an effective Hamiltonian

$$\hat{H}_{eff} = \frac{\hbar^2}{2m} (\hat{k} + 2k_R \hat{\sigma}_z)^2 + \frac{\hbar \Omega'}{2} \hat{\sigma}_x + \Delta \hat{\sigma}_z$$
(4)

where we have defined an effective coupling between the  $m_f = -1$  and  $m_f = +1$  states  $\Omega' = \tilde{\Omega} + \hbar\Omega_0^2/2(\tilde{\epsilon})$ . Here technical stuff

F=1 ground state manifold of  $^87Rb$  atoms. A bias field  $\hat{e}_z$  breaks the degeneracy between the  $m_f$  magnetic sub levels. We generate spin-orbit coupling with a pair of Raman beams propagating along  $\hat{e}_x \pm \hat{e}_y$  and with frequencie

where  $\Omega_{ij} \propto \vec{E_i} \times \vec{E_j}^{\star}$  represents the coupling strength associated to each pair of Raman beams and  $\omega_{ij} = \omega_i - \omega_j$ . The frequencies are chosen so that  $\omega_{31} + \omega_{21}$  is at 4 photon resonance with the  $m_f = +1 \to m_f = -1$ . Under a rotation about the z axis  $\hat{U} = e^{i\omega t \hat{F}_z}$  at frequency  $\bar{\omega} = \frac{\omega_{21} + \omega_{31}}{2}$ , and after applying the rotating wave approximation (RWA), the Hamiltonian transforms to

## B. Fourier Spectroscopy

We present a new method to measure the spinful dispersion relations of the system as well as for the future measurement of the Hofstadter Butterfly spectrum, the Fourier Spectroscopy technique, which relies on the time evolution of an atomic state after a dressing field is suddenly turned. An initial bare state becomes a superposition of dressed states and it undergoes Rabi oscillations in time, with spectral components related to the relative energies of the dressed states.

For the case of a spin-orbit coupled atomic system, the dressed state energies are explicitly dependent on the particle's both spin and momentum. Therefore, in order to fully characterize the energy-momentum dispersion we must prepare an atomic state at a given spin and momentum  $|k_i, m_{f_i}\rangle$ , pulse on the Raman field, and measure the time dependent oscillations of the final states  $|k, m_f\rangle$ .

The measurement however can be simplified by noticing that a non-moving atom cloud in the laboratory reference frame dressed by a field with non-zero detuning is equivalent to a moving cloud with a resonant field in a suitable moving reference frame. This can be explicitly seen in the Hamiltonian (citarlo aqui) where the detuning term  $\delta/Er$  and the momentum term  $4k/k_R$  have the same effect in the energy differences up to a numerical pre factor.

It is important to emphasize that the method described above so far only allows us to measure relative energies. We must add a known energy reference if we want to recover In the case of spin-orbit coupled systems with a high quadratic Zeeman shift, the lowest branch of the dispersion curve is nearly quadratic and one can directly measure the effective mass. We can therefore convert to absolute energies by adding the dispersion of the lower branch.

The system is let to evolve for a finite time T and afterwards the field is snapped off. A Stern-Gerlach pulse applied at our 21 ms time of flight (TOF) allows us to project the state of the condensate back into the bare  $m_f$  basis.

We start our experimental sequence with a Bose Einstein condensate with  $40 \times 10^5$  <sup>87</sup>Rb atoms in the  $\dot{F}=1$  ground state manifold. We adiabatically transfer the atoms into the  $|F=1,m_f=0\rangle$  state using a combination of radio frequency and a bias magnetic fields (cite adiabatic rapid passage, etc). We then turn on our Raman lasers with some given detuning and let the system evolve for a time T. After we snap off the field we let the atoms expand in time of flight and apply a Stern-Gerlach pulse which allows us to resolve the different spin components and directly extract the spin dependent time evolution of the system. We repeat this procedure for different pulsing times and detunings between  $-12E_R$  and  $12E_R$ . The spacing and the total number of pulse times for a given detuning value were chosen so that the bandwith and resolution of the Fourier transform were appropriate given the energy scales of the system. The frequencies were extracted using the Lasso algorithm, which given n data points y and p basis functions x, seeks to minimize the quantity

$$\sum_{i=1}^{n} (y_i - \sum_{j=1}^{n} x_{ij}\beta_j)^2 + \lambda \sum_{j=1}^{p} |\beta|$$
 (5)

which is equivalent to a least square fit with a constraint on the L1 norm of the fit coefficients. Here we used the real part of the Fourier basis as our basis functions and the constraint constraint helped to reduce the spectral noise and allowed us to identify the main frequencies of the problem more easily.

(Tibshirani, 1995)

- II. RESULTS
- III. DISCUSSION
- IV. CONCLUSION