### Positive and Negative Relationships

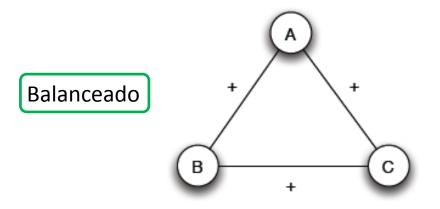
Ana Paula Fabrício Benevenuto Virgílio Almeida



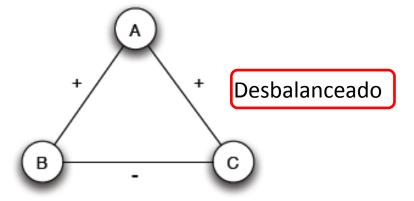
#### Redes com sinais

- Redes com relações positivas e negativas
- Considere um grafo completo não direcionado
- Cada aresta é rotulada como
  - Positiva: amigo, confiança, sentimento positivo
  - Negativa: inimigo, desconfiança, sentimento negativo
- Examine trios de nodos conectados

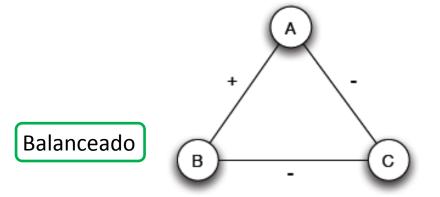
### Structural Balance



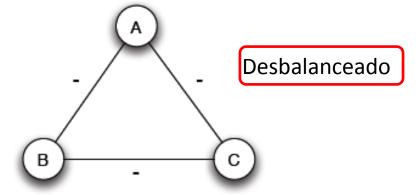
(a) A, B, and C are mutual friends: balanced.



(b) A is friends with B and C, but they don't get along with each other: not balanced.



(c) A and B are friends with C as a mutual enemy: balanced.

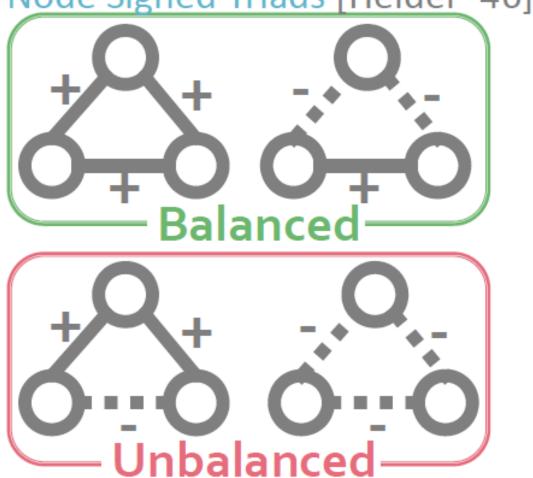


(d) A, B, and C are mutual enemies: not balanced.

Figure 5.1: Structural balance: Each labeled triangle must have 1 or 3 positive edges.

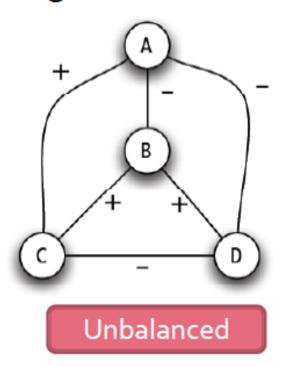
# Theory of Structural Balance

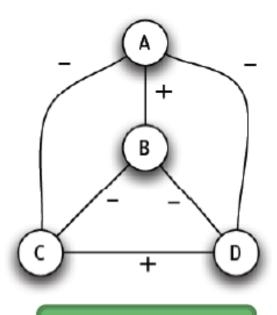
Three-Node Signed Triads [Heider '46]



### Balanced/unbalanced networks

 Graph is balanced if every connected triple of nodes has all 3 edges labeled +, or else exactly 1 edge is labeled +.





Balanced

# Um grafo balanceado pode ser dividido em dois grupos antagônicos

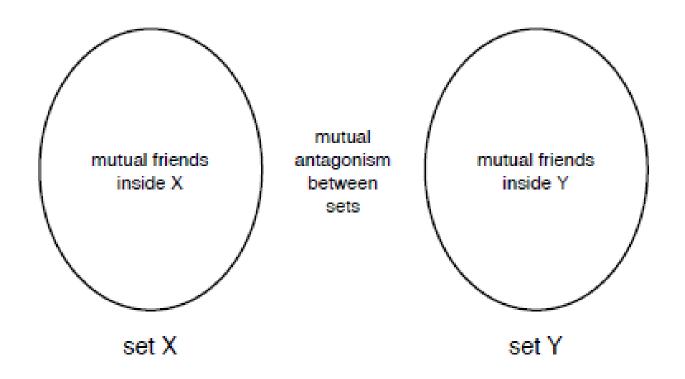
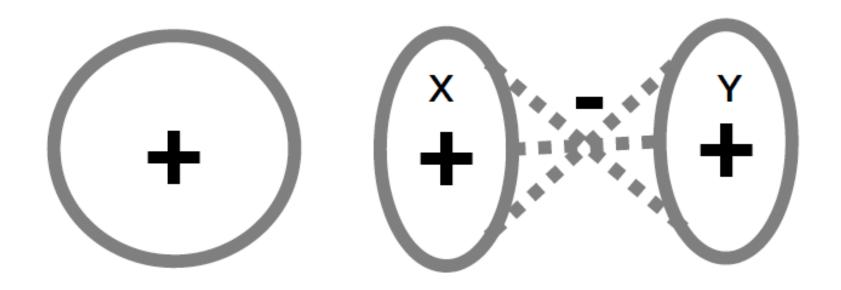


Figure 5.3: If a complete graph can be divided into two sets of mutual friends, with complete mutual antagonism between the two sets, then it is balanced. Furthermore, this is the only way for a complete graph to be balanced.

### Local balance → Global factions

- Balance implies global coalitions [Cartwright-Harary]
  - If all triangles are balanced, then either:
    - The network contains only positive edges, or
    - Nodes can be split into 2 factions linked by negative edges



#### The Balance Theorem

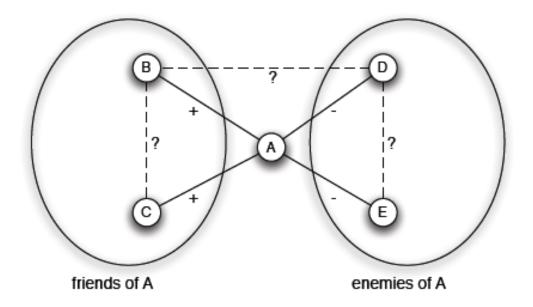
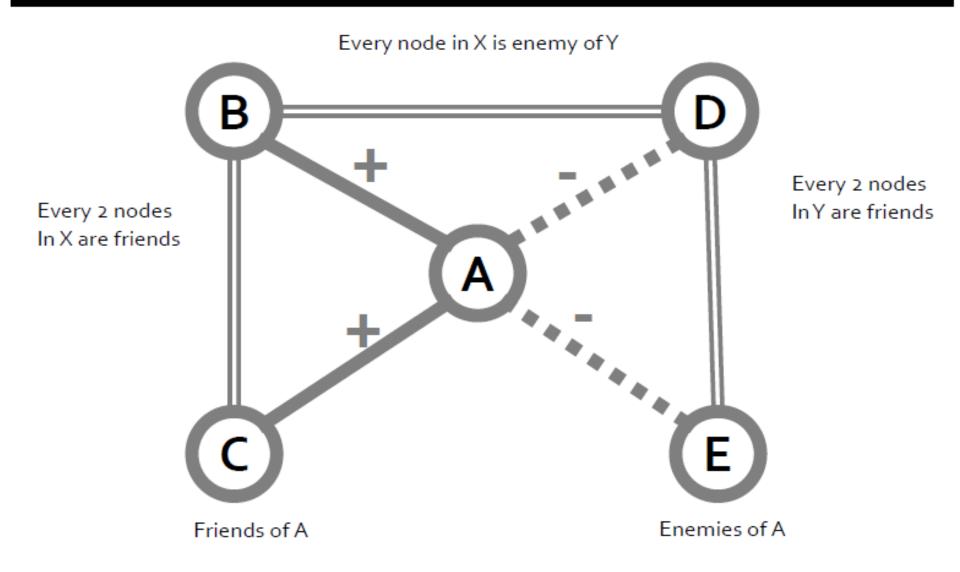
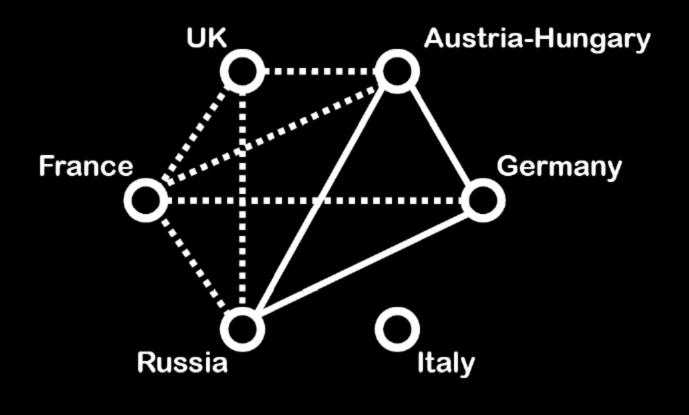


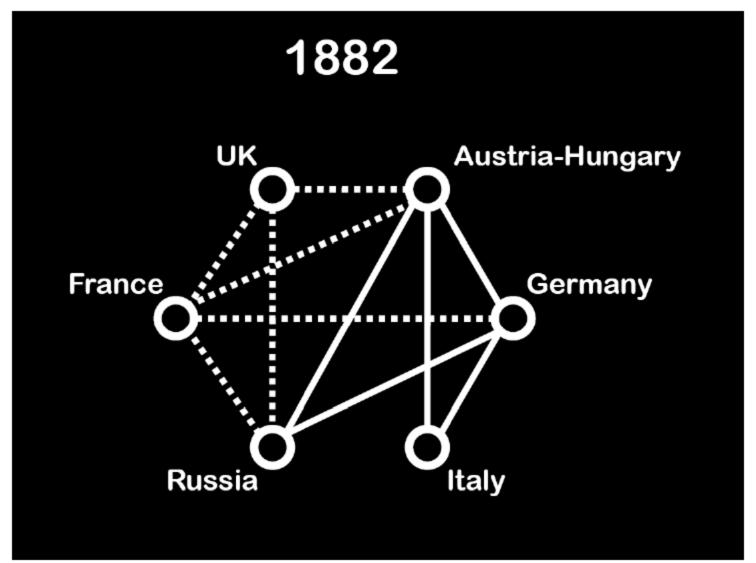
Figure 5.4: A schematic illustration of our analysis of balanced networks. (There may be other nodes not illustrated here.)

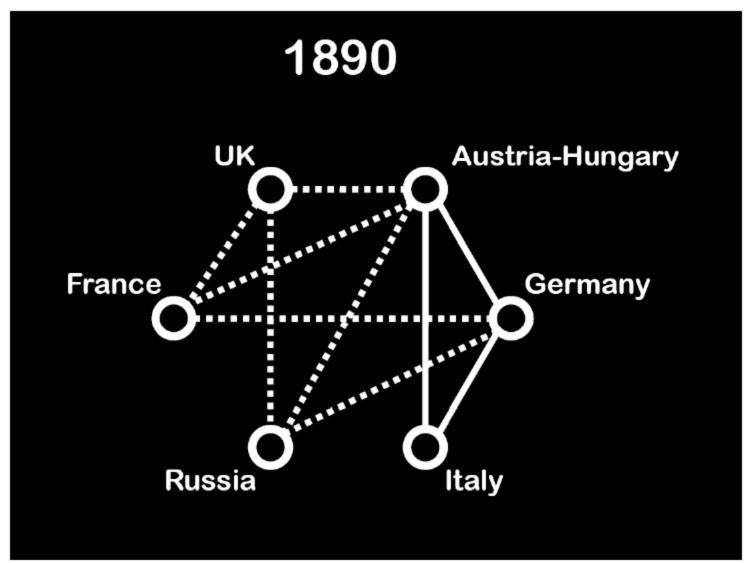
# **Analysis of balance**

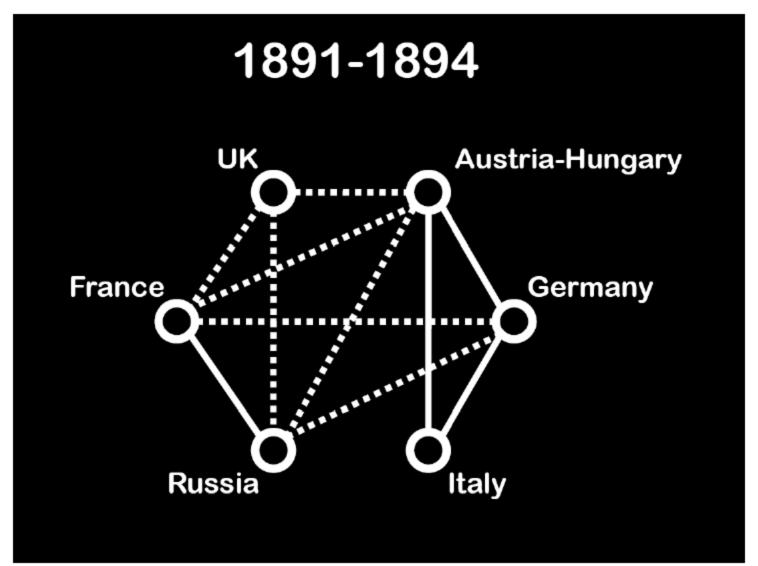


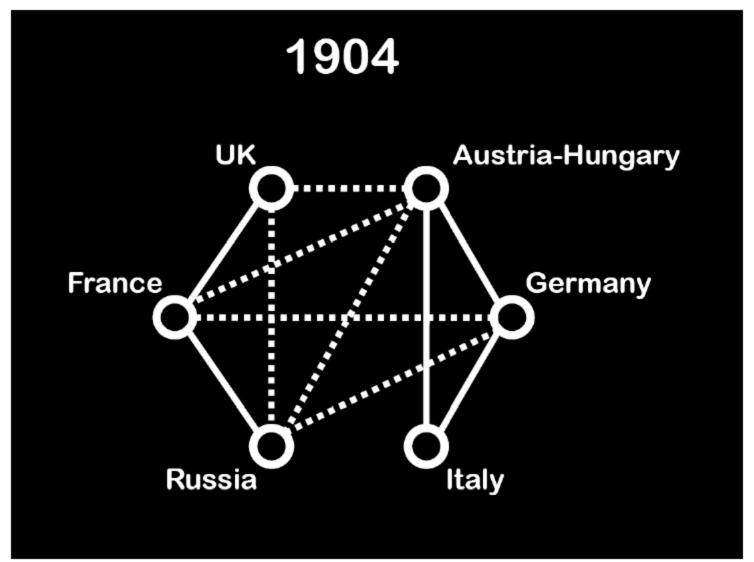
### 1872-1881

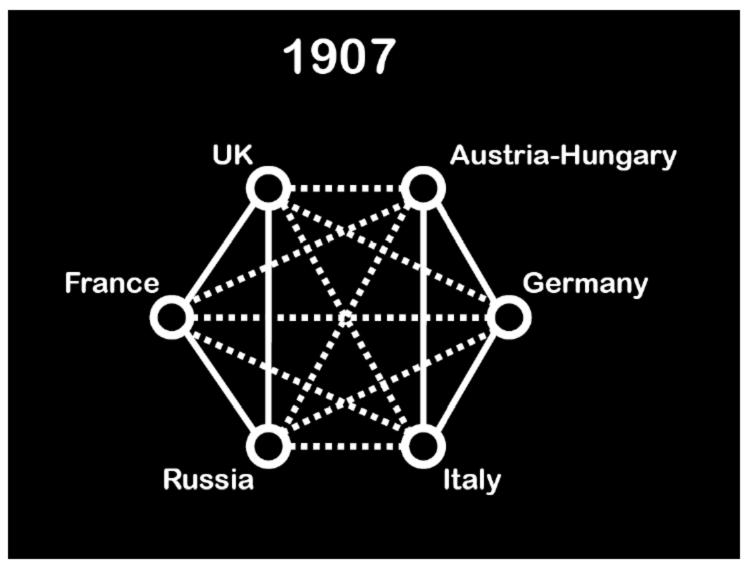




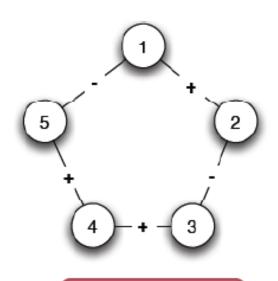






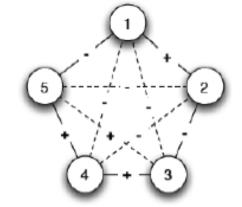


# Balance in general networks

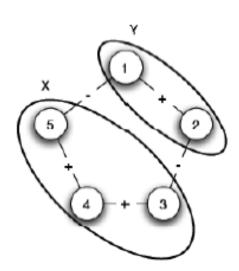


Balanced?

- Def 1: Local view
  - Fill in the missing edges to achieve balance



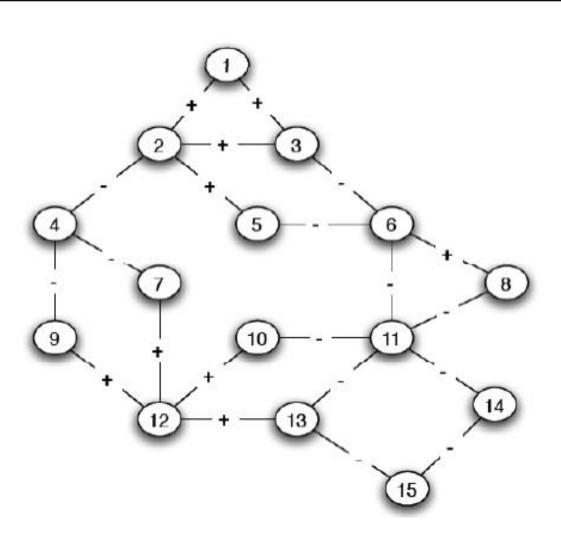
- Def 2: Global view
  - Divide the graph into two coalitions
- Defs are equivalent!



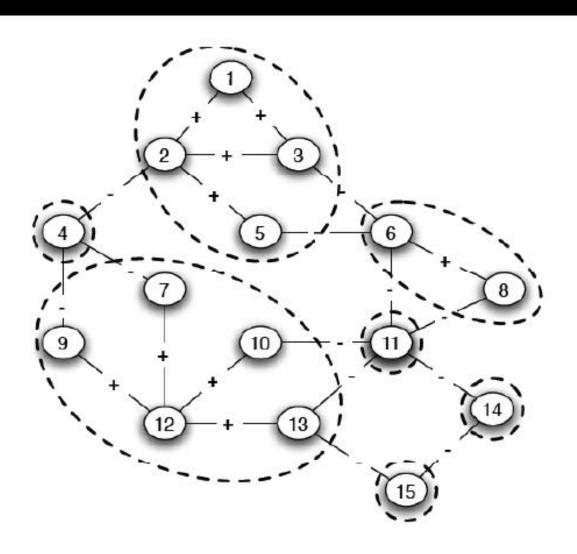
## Is a signed network balanced?

- A graph is balanced if and only if it contains no cycle with an odd number of negative edges.
- How to compute this?
  - Find connected components on + edges
  - For each component create a super-node
  - Connect components A and B if there is a negative edge between the members
  - Assign super-nodes to sides using BFS

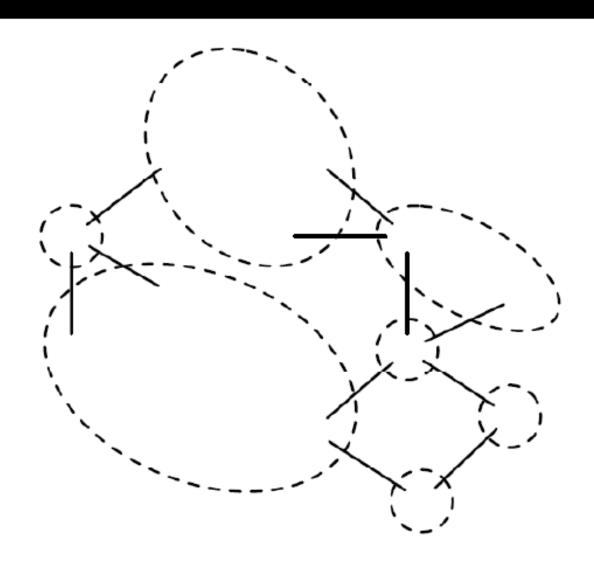
# Signed Graph



# Positive connected components

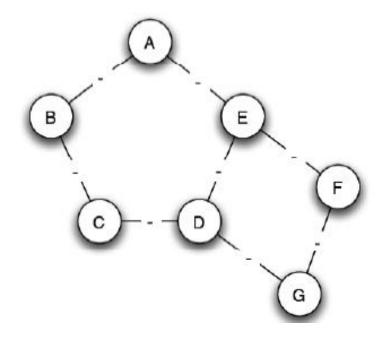


# Reduced graph on super nodes



# BFS on reduced graph

- Using BFS assign each node a side
- Graph is unbalanced if any two supernodes are assigned the same side



# Real Large Signed Networks

- Each edge has a sign (+ or –)
- Meaning of signs can be:
  - Support/Oppose (Wikipedia)
  - Trust/Distrust (Epinions)
  - Friend/Foe (Slashdot)

	Epinions	Slashdot	Wikipedia
Nodes	119,217	82,144	7,118
Edges	841,200	549,202	103,747
+ edges	85.0%	77.4%	78.7%
<ul><li>edges</li></ul>	15.0%	22.6%	21.2%

#### • Questions:

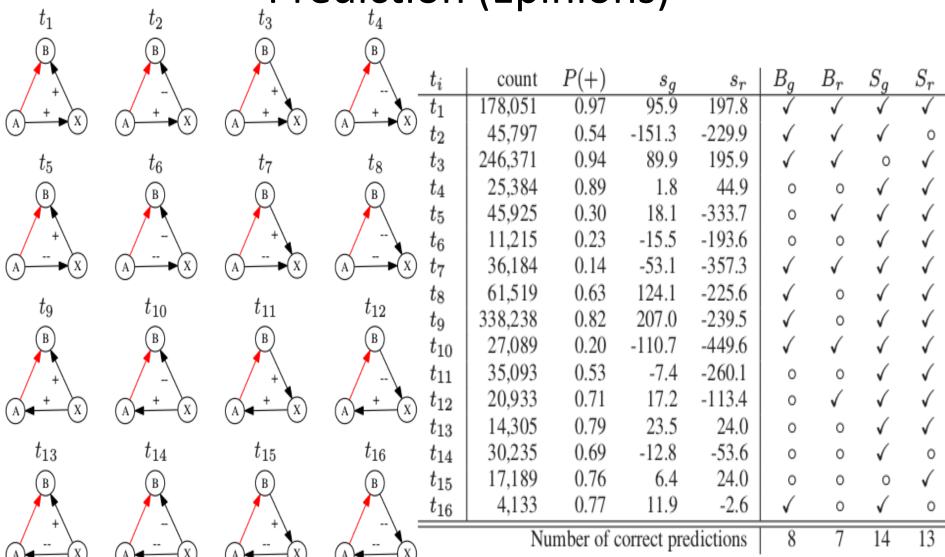
- How do edge signs and network structure interact?
- What theories explain signs of edges?
- Can we accurately predict signs of edges?

#### **Dataset - Statistics**

Triad $T_i$	$ T_i $	$p(T_i)$	$p_0(T_i)$	$s(T_i)$		
Epinions						
$T_3 \mid ++++$	11,640,257	0.870	0.621	1881.1		
$T_1 \mid +$	947,855	0.071	0.055	249.4		
$T_2 \mid ++-$	698,023	0.052	0.321	-2104.8		
$T_0 \mid$	89,272	0.007	0.003	227.5		
Slashdot						
$T_3$ +++	1,266,646	0.840	0.464	926.5		
$T_1 \mid +$	109,303	0.072	0.119	-175.2		
$T_2 \mid ++-$	115,884	0.077	0.406	-823.5		
$T_0 \mid$	16,272	0.011	0.012	-8.7		
Wikipedia						
$T_3$   +++	555,300	0.702	0.489	379.6		
$T_1 \mid +$	163,328	0.207	0.106	289.1		
$T_2 \mid ++-$	63,425	0.080	0.395	-572.6		
$T_0 \mid$	8,479	0.011	0.010	10.8		

Table 3. Number of balanced and unbalanced undirected triads.

### Prediction (Epinions)



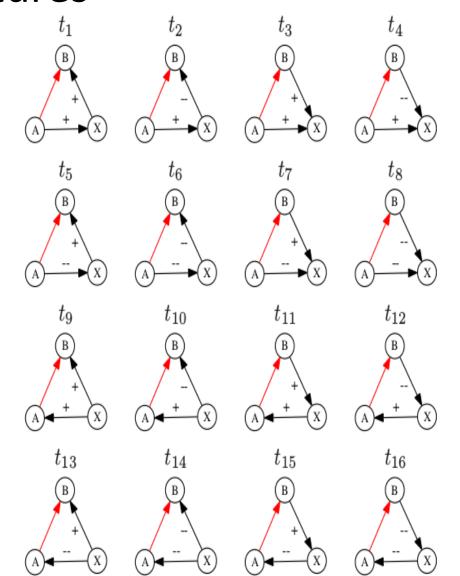
Paper: Predicting Positive and Negative Links in Online Social Networks

#### **Features**

- predicting the sign of the edge from u to v
  - outgoing edge from  $u : d^+_{out}(u), d^-_{out}(u)$
  - incoming edge to  $v : d^+_{in}(v), d^-_{in}(v)$
  - embeddedness : C(u, v)
  - total out-degree of  $u : d^+_{out}(u) + d^-_{out}(u)$
  - total in-degree of  $v : d_{in}^+(v) + d_{in}^-(v)$

#### **Features**

- Triads involving (u,v)



### Result

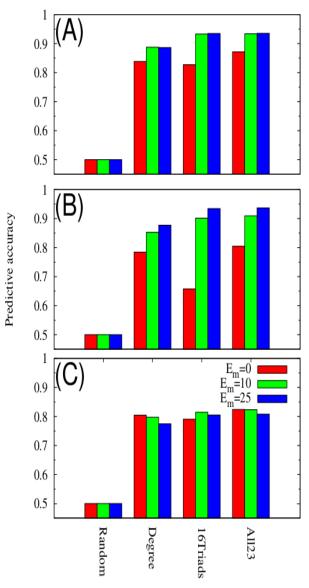


Figure 1: Accuracy of predicting a sign of edge (u,v) given signs of all other edges in the network. (a) Epinions, (b) Slashdot, (c) Wikipedia.

#### Generalization

All23	Epinions	Slashdot	Wikipedia
Epinions	0.9342	0.9289	0.7722
Slashdot	0.9249	0.9351	0.7717
Wikipedia	0.9272	0.9260	0.8021

Table 6: Predictive accuracy when training on the "row" dataset and evaluating the prediction on the "column" dataset.