

Given the polynomial $P(x) = x^4 + x + 1$ and the message represented by the polynomial $M(x) = x^{10} + x^7 + x^4 + x^3 + x + 1$, we perform the CRC encoding by multiplying $M(x)$ by x^4 and dividing by $P(x)$. The remainder from this division is the CRC.

The division process is as follows:

$$\begin{array}{r}
 P(x) = x^4 + x + 1 \quad \frac{x^{10} + x^6 + x^4 + x^2}{x^{14} + x^{11} + x^8 + x^7 + x^5 + x^4} = x^4 \cdot M(x) \\
 \underline{x^{14} + x^{11} + x^{10}} \\
 x^{10} + x^8 + x^7 \\
 \underline{x^{10} + x^6 + x^5 + x^4} \\
 x^6 \\
 \underline{x^6} \\
 x^3 + x^2 = R(x)
 \end{array}$$

The remainder $R(x) = x^3 + x^2$ corresponds to the binary sequence 1100 when translated from polynomial form.