

Instruction Graph Statics

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1 Validity

$$\overline{\text{EmptyProgram valid}}$$
$$\frac{\text{vdecls definesvertices } V \quad s \text{ connectsto}_{\text{index}} V \text{ in } V}{\text{Program}(\text{vdecls}, \text{Start}(s)) \text{ valid}}$$

2 Defined Vertices

$$\overline{\text{Singleton}(\text{vdecl}) \text{ definesvertices } \{\text{vdecl}\}}$$
$$\frac{\text{vdecls definesvertices } U \quad \text{vdecl} \notin U}{\text{Cons}(\text{vdecl}, \text{vdecls}) \text{ definesvertices } U \cup \{\text{vdecl}\}}$$

3 Connected Vertices

$$\frac{\text{Vertex}(n, \text{vcontent}) \in V \quad \text{Vertex}(n, \text{vcontent}) \text{ connectsto } U \text{ in } V}{n \text{ connectsto}_{\text{index}} U \text{ in } V}$$

$$\frac{\text{vcontent accesses } U \text{ in } V}{\text{Vertex}(n, \text{vcontent}) \text{ connectsto } U \cup \{\text{Vertex}(n, \text{vcontent})\} \text{ in } V}$$

$$\frac{\text{Vertex}(n, \text{vcontent}) \in V \quad \text{Vertex}(n, \text{vcontent}) \text{ connectsto } U \text{ in } V}{\text{Do}(\text{action}, \text{Next}(n)) \text{ accesses } U \text{ in } V}$$

$$\frac{\text{Vertex}(n, \text{vcontent}) \in V \quad \text{Vertex}(n, \text{vcontent}) \text{ connectsto } U \text{ in } V}{\text{DoUntil}(\text{action}, \text{condition}, \text{Next}(n)) \text{ accesses } U \text{ in } V}$$

$$\frac{\text{Vertex}(n, \text{vcontent}) \in V \quad \text{Vertex}(m, \text{vcontent}) \in V \quad \text{Vertex}(n, \text{vcontent}) \text{ connectsto } U \text{ in } V}{\text{Conditional}(\text{condition}, \text{Next}(n), \text{Next}(m)) \text{ accesses } U \text{ in } V}$$

$$\frac{\text{Vertex}(n, \text{vcontent}) \in V \quad \text{Vertex}(n, \text{vcontent}) \text{ connectsto } U \text{ in } V}{\text{GoTo}(\text{Next}(n)) \text{ accesses } U \text{ in } V}$$