Instruction Graph Dynamics

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1 Terminated

$$\frac{\mathbf{V}(n, \ \mathbf{end}) \in vs}{(n, \ vs, \ I, \ O) \ \mathsf{terminated}}$$

2 Stuck

$$\frac{\mathbf{V}(n, \ \mathbf{do} \ a \ \mathbf{until} \ cnd \ \mathbf{then} \ n') \in \mathit{vs}}{(n, \ \mathit{vs}, \ [\], \ \mathit{O}) \ \mathtt{stuck}}$$

$$\frac{\mathbf{V}(n, \ \mathbf{if} \ cnd \ \mathbf{then} \ n' \ \mathbf{else} \ n'') \in \mathit{vs}}{(n, \ \mathit{vs}, \ [\], \ \mathit{O}) \ \mathtt{stuck}}$$

3 Steps

$$\begin{array}{c} \mathbf{V}(n, \ \mathbf{do} \ a \ \mathbf{then} \ n') \in vs \\ \hline (n, \ vs, \ I, \ O) \longmapsto (n', \ vs, \ I, \ a :: \ O) \\ \hline \\ \mathbf{V}(n, \ \mathbf{do} \ a \ \mathbf{until} \ cnd \ \mathbf{then} \ n') \in vs \\ \hline (n, \ vs, \ true :: \ I, \ O) \longmapsto (n', \ vs, \ I, \ a :: \ O) \\ \hline \\ \mathbf{V}(n, \ \mathbf{do} \ a \ \mathbf{until} \ cnd \ \mathbf{then} \ n') \in vs \\ \hline (n, \ vs, \ false :: \ I, \ O) \longmapsto (n, \ vs, \ I, \ a :: \ O) \\ \hline \\ \mathbf{V}(n, \ \mathbf{if} \ cnd \ \mathbf{then} \ n' \ \mathbf{else} \ n'') \in vs \\ \hline (n, \ vs, \ true :: \ I, \ O) \longmapsto (n', \ vs, \ I, \ O) \\ \hline \\ \mathbf{V}(n, \ \mathbf{goto} \ n') \in vs \\ \hline \hline (n, \ vs, \ I, \ O) \longmapsto (n'', \ vs, \ I, \ O) \\ \hline \\ \hline \\ \mathbf{V}(n, \ \mathbf{goto} \ n') \in vs \\ \hline \hline (n, \ vs, \ I, \ O) \longmapsto (n', \ vs, \ I, \ O) \\ \hline \end{array}$$