Instruction Graph Dynamics

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1 continuesto

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Vertex(n', vcontent) \in V
tion Next(n')) with (V inputs output)
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 $\label{eq:Vertex} Vertex(n,\ Do(action,\ Next(n')))\ with\ (V,\ inputs,\ outputs)\\ continues to\ Vertex(n',\ vcontent)\ with\ (V,\ inputs,\ action::output)$

$$Vertex(n', vcontent) \in V$$

 $\label{eq:Vertex} {\tt Vertex}(n,\ {\tt DoUntil}({\tt action},\ {\tt cond},\ {\tt Next}(n')))\ {\tt with}\ ({\tt V},\ {\tt true}:: {\tt inputs},\ {\tt outputs}) \\ {\tt continuesto}\ {\tt Vertex}(n',\ {\tt vcontent})\ {\tt with}\ ({\tt V},\ {\tt inputs},\ {\tt action}:: {\tt output}) \\$

Vertex(n, DoUntil(action, cond, vnext)) with (V, inputs, action :: output)

$$Vertex(n', vcontent) \in V$$

 $\label{eq:Vertex} {\tt Vertex}(n, \ {\tt Conditional}({\tt cond}, \ {\tt Next}(n'), \ {\tt falsecase})) \ {\tt with} \ ({\tt V}, \ {\tt true} :: {\tt inputs}, \ {\tt outputs}) \\ {\tt continuesto} \ {\tt Vertex}(n', \ {\tt vcontent}) \ {\tt with} \ ({\tt V}, \ {\tt inputs}, \ {\tt output}) \\$

$$Vertex(n', vcontent) \in V$$

$Vertex(n', vcontent) \in V$

 $\label{eq:Vertex} Vertex(n, \; GoTo(Next(n'))) \; with \; (V, \; inputs, \; outputs) \\ continues to \; Vertex(n', \; vcontent) \; with \; (V, \; inputs, \; output) \\$

2 more continuesto (End cases)

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Vertex(n, Do(action, End)) with (V, inputs, outputs)
continuesto End with (V, inputs, action :: outputs)
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\label{eq:vertex} {\tt Vertex}(n,\ {\tt DoUntil}({\tt action},\ {\tt cond},\ {\tt End}))\ {\tt with}\ ({\tt V},\ {\tt true}:: {\tt inputs},\ {\tt outputs}) \\ {\tt continuesto}\ {\tt End}\ {\tt with}\ ({\tt V},\ {\tt inputs},\ {\tt action}:: {\tt outputs})
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 $\label{eq:conditional} {\tt Vertex}(n, \; {\tt Conditional}({\tt cond}, \; {\tt truecase}, \; {\tt End})) \; {\tt with} \; ({\tt V}, \; {\tt false} :: {\tt inputs}, \; {\tt outputs}) \\ {\tt continuesto} \; {\tt End} \; {\tt with} \; ({\tt V}, \; {\tt inputs}, \; {\tt outputs})$

 $\label{eq:Vertex} {\tt Vertex}(n, \; {\tt Conditional}({\tt cond}, \; {\tt End}, \; {\tt falsecase})) \; {\tt with} \; ({\tt V}, \; {\tt true} :: {\tt inputs}, \; {\tt outputs}) \\ {\tt continuesto} \; {\tt End} \; {\tt with} \; ({\tt V}, \; {\tt inputs}, \; {\tt outputs})$

Vertex(n, GoTo(End)) with (V, inputs, outputs)
 continues to End with (V, inputs, outputs)

3 terminates

 $\frac{\text{vertexwithstate continuesto End with (V, inputs, outputs)}}{\text{vertexwithstate terminates doing outputs}}$

vertexwithstate1 continuesto vertexwithstate2

vertexwithstate2 terminates doing outputs

vertexwithstate1 terminates doing outputs

4 dynamics

 $\frac{\texttt{vdecls definesvertices V} \quad \texttt{Vertex}(\texttt{n}, \, \texttt{vcontent}) \in \texttt{V}}{\texttt{Program}(\texttt{vdecls}, \, \texttt{Start}(\texttt{n})) \, \, \texttt{startsat Vertex}(\texttt{n}, \, \, \texttt{vcontent}) \, \, \texttt{in V}}$

 $\frac{\text{program startsat svertex in V}}{\text{svertex with (V, inputs, []) terminates doing outputs}}$