

Instruction Graph Dynamics

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1 Configuration

To describe a state midway through execution, we define

Configuration $cfg ::= (n, vs, I, O)$ configurations

where $n \in \mathbb{Z}$, the integers, $vs \in \mathbf{Vertices}$, I is a *bool* list, representing the input used to satisfy a **Condition** cnd , and O is an **Action** list, representing the ordered (but reversed) list of actions that are executed.

cfg **cfgvalid** means that the configuration cfg is a valid configuration.

$$\frac{\mathbf{P}(v, vs) \text{ valid} \quad \mathbf{V}(n, c) \in v :: vs}{(n, v :: vs, I, O) \text{ cfgvalid}}$$

2 Terminated

(n, vs, I, O) **terminated** means that the state with vertex represented by n in vertices vs with remaining input I and current output O is in a finished state for the program execution context.

$$\frac{\mathbf{V}(n, \mathbf{end}) \in vs}{(n, vs, I, O) \text{ terminated}}$$

3 Waiting

(n, vs, I, O) **waiting** means that the state with vertex represented by n in vertices vs with remaining input I and current output O cannot proceed, as it requires more input to continue.

$$\frac{\mathbf{V}(n, \text{do } a \text{ until } cnd \text{ then } n') \in vs}{(n, vs, [], O) \text{ waiting}}$$

$$\frac{\mathbf{V}(n, \text{if } cnd \text{ then } n' \text{ else } n'') \in vs}{(n, vs, [], O) \text{ waiting}}$$

4 Steps

$(n, vs, I, O) \mapsto (n', vs, I', O')$ means that the state with vertex represented by n in vertices vs with remaining input I and current output O continues to the state with vertex represented by n' in vertices vs with remaining input I' and current output O' .

$$\frac{\mathbf{V}(n, \text{do } a \text{ then } n') \in vs}{(n, vs, I, O) \mapsto (n', vs, I, a :: O)}$$

$$\frac{\mathbf{V}(n, \text{do } a \text{ until } cnd \text{ then } n') \in vs}{(n, vs, true :: I, O) \mapsto (n', vs, I, a :: O)}$$

$$\frac{\mathbf{V}(n, \text{do } a \text{ until } cnd \text{ then } n') \in vs}{(n, vs, false :: I, O) \mapsto (n, vs, I, a :: O)}$$

$$\frac{\mathbf{V}(n, \text{if } cnd \text{ then } n' \text{ else } n'') \in vs}{(n, vs, true :: I, O) \mapsto (n', vs, I, O)}$$

$$\frac{\mathbf{V}(n, \text{if } cnd \text{ then } n' \text{ else } n'') \in vs}{(n, vs, false :: I, O) \mapsto (n'', vs, I, O)}$$

$$\frac{\mathbf{V}(n, \text{goto } n') \in vs}{(n, vs, I, O) \mapsto (n', vs, I, O)}$$