# Universitat Politècnica de València Master in Artificial Intelligence, Pattern Recognition and Digital Imaging 2022-2023

## **MACHINE TRANSLATION**

## 3. Neural Machine Translation

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December 20, 2022

## Index

- 1 Introduction ▷ 2
- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
- 4 Neural machine translation ≥ 23
- 5 Attention models and recurrent neural networks ≥ 31
- 6 Attention models for all ≥ 41
- 7 Training and Decoding with NMT ▷ 66
- 8 Translation results with neural machine translation > 72
- 9 Other issues of NMT ⊳ 77
- 10 Bibliography ▷ 89

## Index

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- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
- 4 Neural machine translation ≥ 23
- 5 Attention models and recurrent neural networks ≥ 31
- 6 Attention models for all ≥ 41
- 7 Training and Decoding with NMT ▷ 66
- 8 Translation results with neural machine translation > 72
- 9 Other issues of NMT ⊳ 77
- 10 Bibliography ⊳ 89

## Introduction

- Traditional approach to MT: Discrete representation of words and sentences.
- Most techniques of machine learning are developped in continuous spaces (i.e. vector spaces)
- In machine learning, (deep) neural networks are good models for many aplications.

- Can words and sentences be represented in a continuous space? Word and sentence embeddings.
- Can neural networks deal with sequences? Dynamic feed-forward networks and recurrent neural networks.

## Learned word embeddings

Problem: From words to vectors.

- Local (one-hot) coding and distributed coding.
- Neural language model (Bengio 2003)
- Bag-of-words neural networks (Mikolov 2013)
- Continuous skip-grams (Mikolov 2013)
- Pre-trained neural networks: BERT (Devlin 2019)

• ...

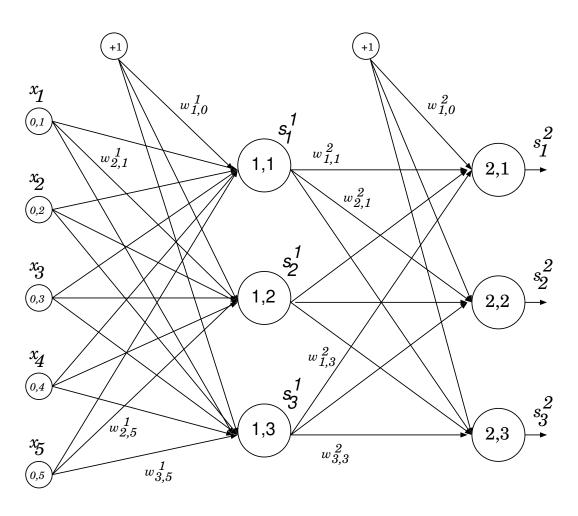
• Extension to sentence embeddings: SentenceBERT, Universal Sentence Encoder, ...

## Byte-Pair Encoding (BPE) (Sennrich 2015)

- Problem: Word embedding of unseen words.
- Solution: The use of subword units learned from a training set.
- Byte Pair Encoding (BPE) is a data compression technique that iteratively replaces the most frequent pair of bytes in a sequence with a single, unused byte.
- Toolkit: https://github.com/rsennrich/subword-nmt
- Other related techniques: SentencePiece, ...
- Character based units: convolutational networks.

Neural machine translation **Machine Translation** 

## A multilayer perceptron



Hidden layer Output layer

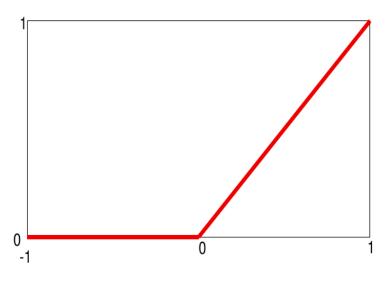
$$\mathbf{s}^1 = \mathbf{f}(\mathbf{W}^1 \mathbf{x}) \qquad \mathbf{s}^2 = \mathbf{f}(\mathbf{W}^2 \mathbf{s}^1)$$

#### **Activation functions**

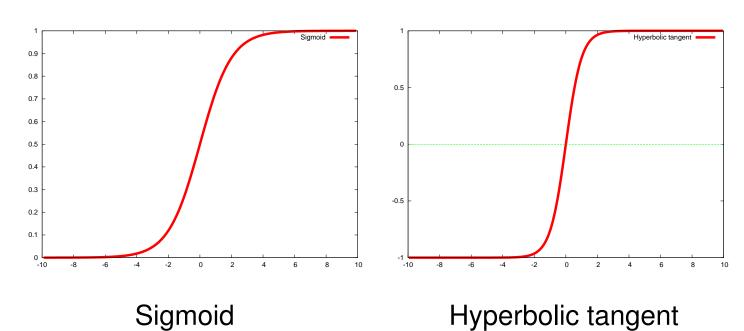
$$\mathbf{f}(\mathbf{z}) = (f(z_1), \dots, f(z_d))^t \text{ for } \mathbf{z} \equiv (z_1, \dots, z_d)^t \in \mathbb{R}^d$$

- **ReLU** (rectified linear unit):  $f_R(z_j) = \max(0, z_j)$
- Sigmoid:  $f_S(z_j) = \frac{1}{1 + \exp(-z_j)}$
- Hyperbolic tangent:  $f_T(z_j) = \frac{\exp(z_j) \exp(-z_j)}{\exp(z_j) + \exp(-z_j)}$   $(f_T(z_j) = 2 f_S(2 z_j) 1)$
- Softmax:  $f_{SM}(z_j) = \frac{\exp(z_j)}{\sum_{j'} \exp(z_{j'})}$   $\left(f_{SM}(z_j) = f_S(z_j \ln(\sum_{j' \neq j} \exp(z_{j'}))\right)$
- PReLU, ELU, Maxout, ...

## **Activation functions**



ReLu



#### The softmax activation function

A problem with the use of softmax in training

$$f_{sm}(z_w) = \frac{\exp(z_w)}{\sum_{w'} \exp(z_{w'})}$$

The sum in the normalization factor is extended on all the vocabulary |V|.

#### Solutions:

- Hierarchical softmax: using a binary tree representation of the output layer (Huffman coding)
- Negative sampling: each training sample only modify a subset of the weights (the weights of a small subset of "negative" words).
- Subsampling of frequent words.

# **Training neural networks**

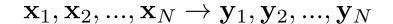
- A neural network defines  $\mathbf{f}: \mathbb{R}^{D_X} \to \mathbb{R}^{D_Y}$ :  $\mathbf{f}(\mathbf{x}_n; \mathbf{W}) = \mathbf{y}_n$  for  $1 \leq n \leq N$ .
- A training sequence  $T=(\mathbf{x}_1,\mathbf{t}_1),\ldots,(\mathbf{x}_N,\mathbf{t}_N):\mathbf{x}_n\in\mathbb{R}^{D_X}$  ,  $\mathbf{t}_n\in\mathbb{R}^{D_Y}$
- *Total error* (regression) is:  $\mathcal{F}_T(\mathbf{W}) = \sum_{n=1}^N \frac{1}{2} \sum_{i=1}^{D_Y} \left(t_{n,i} y_{n,i}\right)^2$
- Cross-entropy loss (classification) ( $\mathbf{t}_n \in \{0,1\}^{D_Y}$ ):  $\mathcal{F}_T(\mathbf{W}) = -\sum_{n=1}^N \sum_{i=1}^{D_Y} t_{n,i} \log y_{n,i}$
- ullet Training goal:  $\widehat{\mathbf{W}} = \mathop{\mathrm{argmin}}_{\mathbf{W}} \ \mathcal{F}_T(\mathbf{W})$
- Computing a local minimum of  $\mathcal{F}$ : GRADIENT DESCENT

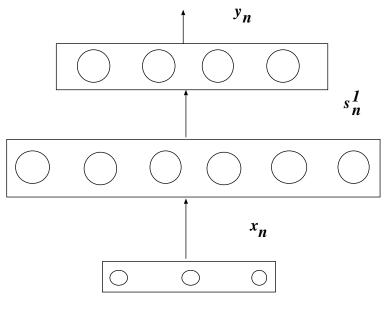
$$\Delta \mathbf{W} = -\rho \nabla_{\mathbf{W}} \mathcal{F}_T(\mathbf{W})$$

#### Index

- 1 Introduction ▷ 2
- 2 Syncronized feedforward neural networks ▷ 11
  - 3 Syncronized recurrent neural networks ▷ 14
  - 4 Neural machine translation ≥ 23
  - 5 Attention models and recurrent neural networks > 31
  - 6 Attention models for all ≥ 41
  - 7 Training and Decoding with NMT ▷ 66
  - 8 Translation results with neural machine translation ▶ 72
  - 9 Other issues of NMT ⊳ 77
  - 10 Bibliography ⊳ 89

# Sequence processing with dynamic feedforward networks

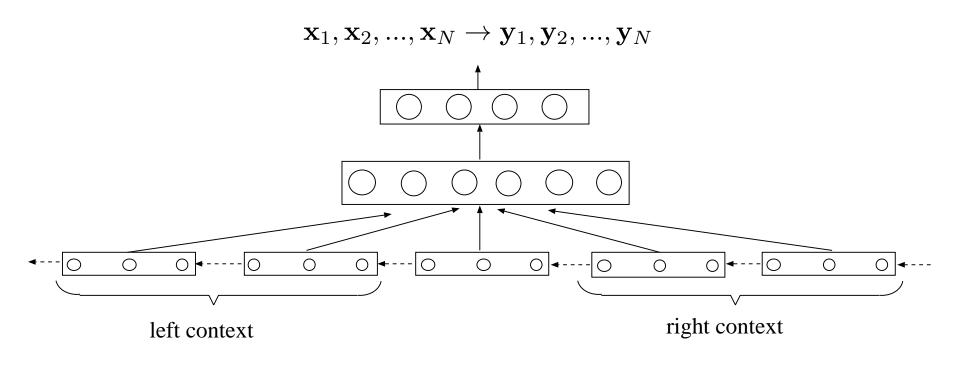




$$1 \le n \le N$$

t	input layer		hidden layer		output layer
1	$\mathbf{x}_1$	$\Rightarrow$	$\mathbf{s}_1^1$	$\Rightarrow$	$\mathbf{y}_1$
2	$\mathbf{x}_2$	$\Rightarrow$	$\mathbf{s}_2^1$	$\Rightarrow$	$\mathbf{y}_2$
			•••		
N	$\mathbf{x}_N$	$\Rightarrow$	$\mathbf{s}_N^1$	$\Rightarrow$	$\mathbf{y}_N$

# Sequence processing with dynamic feedforward networks



$$1 \le n \le N$$

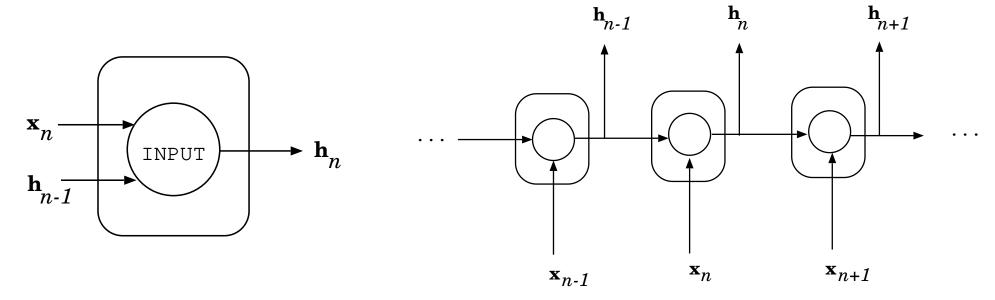
t	input layer		hidden layer		output layer
1	$\mathbf{x}_0,\mathbf{x}_1,\mathbf{x}_2$	$\Rightarrow$	$\mathbf{s}_1^1$	$\Rightarrow$	$\mathbf{y}_1$
2	$\mathbf{x}_1,\mathbf{x}_2,\mathbf{x}_3$	$\Rightarrow$	$\mathbf{s}_2^1$	$\Rightarrow$	$\mathbf{y}_2$
			•••		
N	$\mid \mathbf{x}_{N-1}, \mathbf{x}_N, \mathbf{x}_{N+1} \mid$	$\Rightarrow$	$\mathbf{s}_N^1$	$\Rightarrow$	$\mathbf{y}_N$

#### Index

- 1 Introduction ▷ 2
- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
  - 4 Neural machine translation ≥ 23
  - 5 Attention models and recurrent neural networks ≥ 31
  - 6 Attention models for all ≥ 41
  - 7 Training and Decoding with NMT ▷ 66
  - 8 Translation results with neural machine translation > 72
  - 9 Other issues of NMT ⊳ 77
  - 10 Bibliography ⊳ 89

## Simple recurrent networks

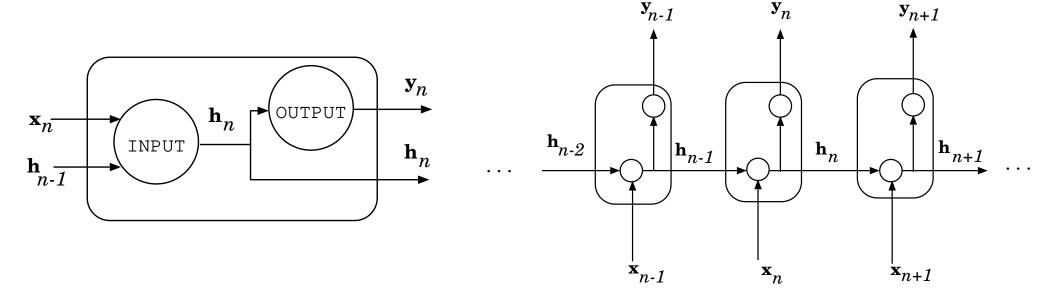
- A set H of  $D_H$  units and a set X of  $D_X$  inputs.
- Input:  $\mathbf{x}_n \in \mathbb{R}^{D_X}$  and output:  $\mathbf{h}_n \in \mathbb{R}^{D_H}$ ,  $n=1,2,\ldots$
- $\mathbf{y}_n = \mathbf{h}_n = \mathbf{f}(\mathbf{W}_X \mathbf{x}_n + \mathbf{W}_H \mathbf{h}_{n-1}) = \mathbf{F}(\mathbf{x}_n, \mathbf{h}_{n-1})$  with  $\mathbf{h}_0 = \mathbf{0}$



Unfolding a simple recurrent network

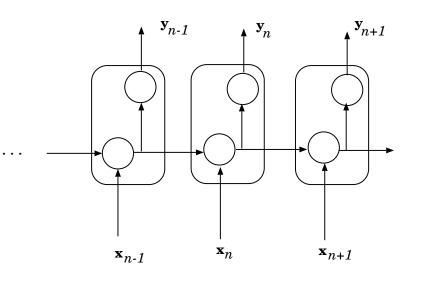
#### Elman recurrent neural networks

- A set Y of  $D_Y$  units, a set X of  $D_X$  inputs and a set H of  $D_H$  hidden units
- Input:  $\mathbf{x}_n \in \mathbb{R}^{D_X}$ , output:  $\mathbf{y}_n \in \mathbb{R}^{D_Y}$ , and hidden states:  $\mathbf{h}_n \in \mathbb{R}^{D_H}$ ,  $n = 1, 2, \dots$
- $\mathbf{y}_n = \mathbf{f}(\mathbf{W}_Y \mathbf{h}_n)$  and  $\mathbf{h}_n = \mathbf{f}(\mathbf{W}_H \mathbf{h}_{n-1} + \mathbf{W}_X \mathbf{x}_n)$  with  $\mathbf{h}_0 = \mathbf{0}$

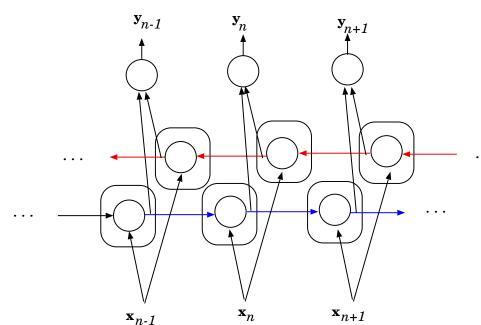


# Bidirectional recurrent neural networks (Schuster & Paliwal 1997)

Dependencies with the past inputs, but with the future?



Standard dynamics



Bidirectional dynamics

#### Bidirectional recurrent neural networks

- A set of  $D_H$  forward units, a set of  $D_H$  backward units, a set of  $D_Y$  output units and a set of  $D_X$  inputs.
- Input:  $\mathbf{x}_n \in \mathbb{R}^{D_X}$  and output:  $\mathbf{y}_n \in \mathbb{R}^{D_Y}$ .,
- Forward:  $\mathbf{h}_n^f = \mathbf{f}(\mathbf{W}_H^f \mathbf{h}_{n-1}^f + \mathbf{W}_X^f \mathbf{x}_n)$  n = 1, 2, ..., N with  $\mathbf{h}_0 = \mathbf{0}$
- Backward:  $\mathbf{h}_n^b = \mathbf{f}(\mathbf{W}_H^b \ \mathbf{h}_{n+1}^b + \mathbf{W}_X^b \ \mathbf{x}_n)$   $n = N, N-1, \dots, 1$  with  $\mathbf{h}_{N+1} = \mathbf{0}$
- Output:  $\mathbf{y}_n = \mathbf{f}(\mathbf{W}_Y^f \mathbf{h}_n^f + \mathbf{W}_Y^b \mathbf{h}_n^b)$   $n = 1, 2, \dots, N$
- *Output* (alternative):  $\mathbf{y}_n = \mathbf{f}(\mathbf{W}_Y[\mathbf{h}_n^f, \mathbf{h}_n^b])$   $n = 1, 2, \dots, N$

# **Training recurrent neural networks**

- Back-propagation through time algorithm (BPTT)
- Back-propagation through time algorithm with momentum.
- Truncate gradiente with momentum.

## Text translation using Elman networks

(Castaño et al. Eurospeech 1997)

 Problem: translate a source sentence from a source language to a sentence from a target language in a hotel-desk scenario:

/¿Tiene habitaciones libres?/  $\Rightarrow$  /Do you have any room available?/

#### Topology

- Elman network
- Distributed coding:
  - \* 61 input units (132 words)
  - \* 52 output units (87 words)
  - \* 160 hidden units
- windows of 6 words

#### Training

- Truncate gradiente with momentum and pattern-based training
- Training corpus: 5000 labeled pairs
- Number of iterations: 100.

#### Test

- 1000 pairs (12.6 words / source sentence and 11.8 words / output sentence).
- Percentage of right translated sentences: 49.5%
  Percentage of right translated words: 93.1%

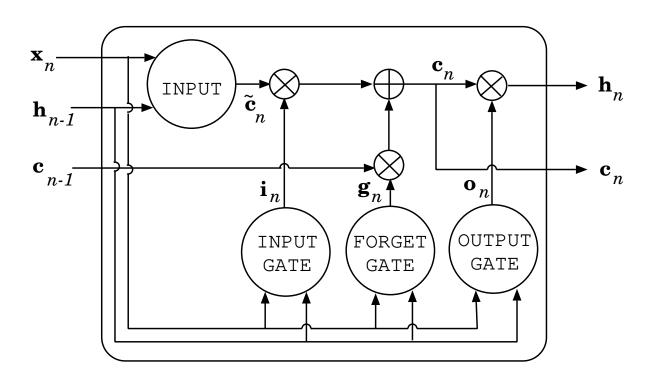
## Long Short-Term Memory (LSTM) [Hochreiter 1997]

Problems with recurrent neural networks:

- The output depends on the complete past information and sometimes only recent information is needed and sometimes more far context is needed
- In back-propagation through time algorithm and exact gradient or real-time recurrent learning algorithms the errors that propagated backwards in time tend to vanish or to oscillate.

A solution: Long Short-Term Memory (LSTM) or Gated Recurrent Units (GRU)

## **Long Short-Term Memory (LSTM)**



• 
$$\mathbf{i}_n = \mathbf{f}_s(\mathbf{W}_Y^I \mathbf{h}_{n-1} + \mathbf{W}_X^I \mathbf{x}_n)$$

$$\bullet \mathbf{h}_n \bullet \mathbf{g}_n = \mathbf{f}_s(\mathbf{W}_Y^F \mathbf{h}_{n-1} + \mathbf{W}_X^F \mathbf{x}_n)$$

• 
$$\mathbf{o}_n = \mathbf{f}_s(\mathbf{W}_Y^O \mathbf{h}_{n-1} + \mathbf{W}_X^O \mathbf{x}_n)$$

• 
$$\tilde{\mathbf{c}}_n = \mathbf{f}_{th}(\mathbf{W}_Y^C \mathbf{h}_{n-1} + \mathbf{W}_X^C \mathbf{x}_n)$$

• 
$$\mathbf{c}_n = \mathbf{g}_n \times \mathbf{c}_{n-1} + \mathbf{i}_n \times \tilde{\mathbf{c}}_n$$

• 
$$\mathbf{h}_n = \mathbf{o}_n \times \mathbf{f}_{th}(\mathbf{c}_n)$$

$$\mathbf{h}_n = \mathbf{F}(\mathbf{x}_n, \mathbf{h}_{n-1})$$

#### Index

- 1 Introduction ▷ 2
- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
- 4 Neural machine translation > 23
  - 5 Attention models and recurrent neural networks > 31
  - 6 Attention models for all ≥ 41
  - 7 Training and Decoding with NMT ▷ 66
  - 8 Translation results with neural machine translation > 72
  - 9 Other issues of NMT ⊳ 77
  - 10 Bibliography ⊳ 89

#### **Neural Machine Translation**

- Early proposals with syncronized recurrent neural networks (Castaño 1997)
- For a source sentence  $x_1^J$  search for a target sentence  $\hat{y}_1^{\hat{I}}$ ,

$$\begin{array}{lll} \hat{y}_{1}^{\hat{I}} & = & \underset{I,y_{1}^{I}}{\operatorname{argmax}} \, p(y_{1}^{I} \mid x_{1}^{J}) \\ & = & \underset{I,y_{1}^{I}}{\operatorname{argmax}} \prod_{i=1}^{I} p(y_{i} \mid y_{1}^{i-1}, x_{1}^{J}) \\ & = & \underset{I,y_{1}^{I}}{\operatorname{argmax}} \prod_{i=1}^{I} p(y_{i} \mid y_{1}^{i-1}, u(x_{1}^{J})) \end{array}$$

where  $u(x_1^J)$  is a representation of  $x_1^J$ .

#### **Neural Machine Translation**

- Non syncronized neural networks (many available tool-kits): The encoderdecoder approach (+ attention models) based on
  - LSTMs or GRUs + cross-attention model.
  - Transformer (attention models for everything).
  - Convolutional neural networks and/or recurrent neural networks (hybrid).
- MT applications:
  - Text and speech translation.
  - Interactive MT, multimodal MT, automatic post-editing, modernization of old text transcriptions, ...
- Other applications:
  - Automatic summarization.
  - Image description, video description, multilingual image description, visual question answering, image generation,

<del>-</del> ...

## **Encoder-decoder approach to NMT** (Peris 2018)

- Project source words to a sequence of continuous vectors → Source word embeddings.
- 2. Generate a contextual representation of the source sentence  $\rightarrow$  Encoder NN.
- 3. Generate an a-posteriori probabilistic distributions of succesive target words using the contextual representation of the source words  $\rightarrow$  Decoder NN.
- 4. Encode target words → Target word embeddings.

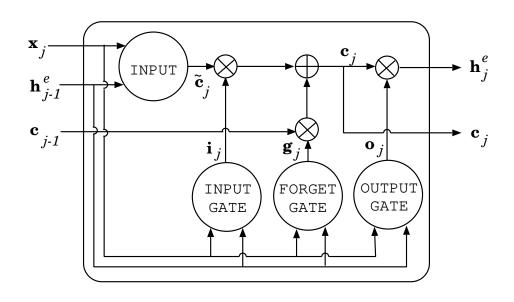
# **Encoder-decoder with LSTMs only**

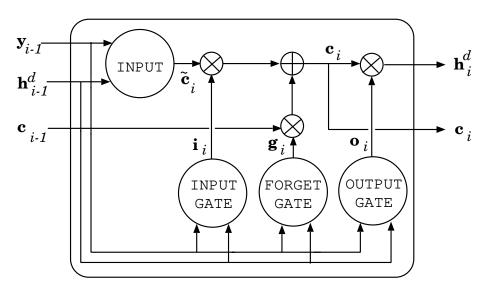
• Goal: Given a source sentence  $x_1^J$  and a target sentence  $y_1^I$ , compute:

$$p(y_1^I \mid x_1^J) = \prod_{i=1}^I p(y_i \mid y_1^{i-1}, u(x_1^J))$$

Neural networks: LSTMs or GRUs

## Long Short-Term Memory (LSTM) (Hochreiter & Schmidhuber, 1997)





$$\mathbf{h}_{j}^{e} = \mathbf{F}(\mathbf{x}_{j}, \mathbf{h}_{j-1}^{e}) \quad 1 \leq j \leq J$$

$$\mathbf{h}_i^d = \mathbf{F}(\mathbf{y}_{i-1}, \mathbf{h}_{i-1}^d) \quad 1 \le i \le I$$

MIARFID-UPV December 20, 2022 MT-4: 28

## Encoder-decoder approach to NMT (Bahdanau et al. 2015)

• The RNN-based encoder ( $\mathbf{F}_e$ ) converts a source word sequence  $x_1, \dots, x_J \equiv x_1^J$  into a vector  $\mathbf{u} = \mathbf{u}(x_1^J)$ ,

$$\mathbf{h}_0^e = \mathbf{0}$$

$$\mathbf{h}_{j}^{e} = \mathbf{F}_{e}(\mathbf{W}_{E}(x_{j}), \mathbf{h}_{j-1}^{e}) = \mathbf{F}_{e}(\mathbf{x}_{j}, \mathbf{h}_{j-1}^{e}) \quad 1 \leq j \leq J$$
$$u(x_{1}^{J}) \equiv \mathbf{u}(\mathbf{h}_{1}^{e}, \dots, \mathbf{h}_{J}^{e}) = \mathbf{u}$$

where  $\mathbf{h}_j^e$  is the states of a RNN-encoder and  $\mathbf{u}$  could be  $\mathbf{h}_J^e$  (sentence embedding)

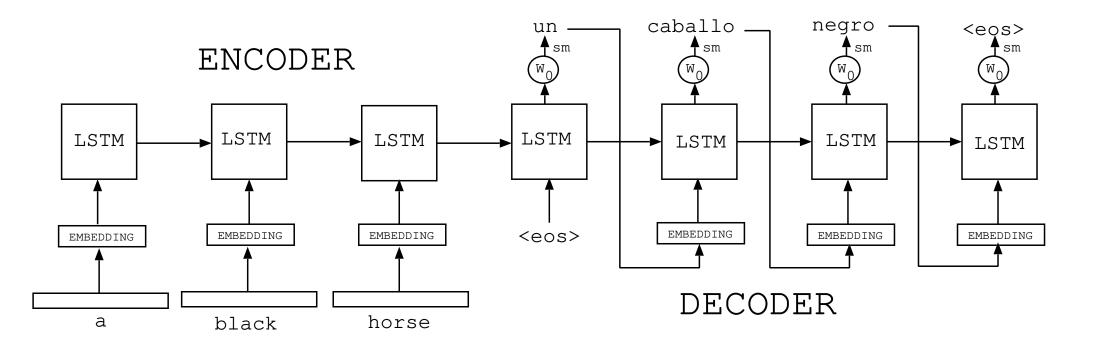
• The RNN-based decoder ( $\mathbf{F}_d$ ) is a kind of target language model

$$\mathbf{h}_0^d = \mathbf{u} \equiv \mathbf{h}_J^e$$

$$\mathbf{h}_i^d = \mathbf{F}_d(\mathbf{W}_E(y_{j-1}), \mathbf{h}_{i-1}^d) = \mathbf{F}_d(\mathbf{y}_{j-1}, \mathbf{h}_{i-1}^d) \quad 1 \le i \le I$$

$$p(y_1^I \mid x_1^J) = \prod_{i=1}^I p(y_i \mid y_1^{i-1}, u(x_1^J)) = \prod_{i=1}^I \mathbf{f}_{sm}(\mathbf{W}_O \mathbf{h}_i^d)_{i(y_i)}$$

# Text translation using LSTM (Sutskever 2014)



Experiments: WMT14 English-to-French

Systems	BLEU
Baseline (PB+Neural LM)	33.3
Ensemble of 5 LSTMs	34.8
Reescoring 1000-best with ensemble of 5 LSTMs	36.5
Moses for WMT14	37.0

## Index

- 1 Introduction ▷ 2
- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
- 4 Neural machine translation ≥ 23
- 5 Attention models and recurrent neural networks > 31
  - 6 Attention models for all ≥ 41
  - 7 Training and Decoding with NMT ▷ 66
  - 8 Translation results with neural machine translation > 72
  - 9 Other issues of NMT ⊳ 77
  - 10 Bibliography ⊳ 89

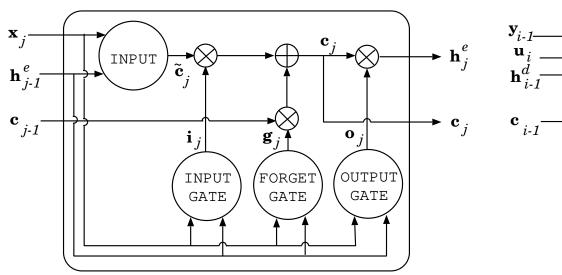
## Encoder-decoder with LSTMs (Vaswani 2017)(Ney 2018)

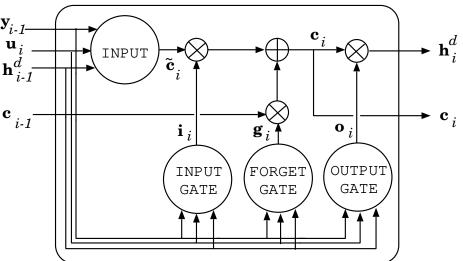
• Goal: Given a source sentence  $x_1^J$  and a target sentence  $y_1^I$ , compute:

$$p(y_1^I \mid x_1^J) = \prod_{i=1}^I p(y_i \mid y_1^{i-1}, u(x_1^J))$$

- Neural networks: LSTMs or GRUs.
- Intra-sentence attention (i,j): For each  $i, 1 \le i \le I$  a probabilistic contribution of  $j, 1 \le j \le J$ .

# **Long Short-Term Memory (LSTM)**





$$\mathbf{h}_{j}^{e} = \mathbf{F}(\mathbf{x}_{j}, \mathbf{h}_{j-1}^{e}) \quad 1 \leq j \leq J$$

$$\mathbf{h}_{j}^{e} = \mathbf{F}(\mathbf{x}_{j}, \mathbf{h}_{j-1}^{e}) \quad 1 \leq j \leq J$$

$$\mathbf{h}_{i}^{d} = \mathbf{F}(\mathbf{y}_{i-1}, \mathbf{h}_{i-1}^{d}, \mathbf{u}_{i}) \quad 1 \leq i \leq I$$

## Attention model (Vaswani 2018)

Given a sequence of encoder states  $\mathbf{h}_{j}^{e}$  for  $1 \leq j \leq J$  and a decoder state  $\mathbf{h}_{i-1}^{d}$  for  $1 \leq i \leq I$  an attention model for the decoder state  $\mathbf{h}_{i}^{d}$  is a function:

$$\mathbf{u}_i = \mathbf{a}(\mathbf{h}_1^e, \dots, \mathbf{h}_J^e, \mathbf{h}_{i-1}^d)$$

where a is:

$$\mathbf{u}_i = \sum_{j=1}^{J} s(\mathbf{h}_j^e, \mathbf{h}_{i-1}^d) \; \mathbf{h}_j^e$$

 $s(\mathbf{h}_{i-1}^d, \mathbf{h}_{j}^e)$  is similarity measure between  $\mathbf{h}_{i-1}^d$  and  $\mathbf{h}_{j}^e$ , as for example:

$$\mathbf{u}_i = \sum_{j=1}^J f_j(\mathbf{h}_1^e, \dots, \mathbf{h}_J^e, \mathbf{h}_{i-1}^d) \mathbf{h}_j^e$$

 $f_i$  is a softmax applied to position j:

$$f_{j}(\mathbf{h}_{1}^{e}, \dots, \mathbf{h}_{J}^{e}, \mathbf{h}_{i-1}^{d}) = \frac{\exp(\mathbf{h}_{i-1}^{d} \cdot \mathbf{h}_{j}^{e})}{\sum_{j'=1}^{J} \exp(\mathbf{h}_{i-1}^{d} \cdot \mathbf{h}_{j'}^{e})} = p(j \mid i) \qquad 1 \leq j \leq J$$

## Complete attention model (Vaswani 2018)

Given a sequence of encoder states  $\mathbf{h}_{j}^{e}$  for  $1 \leq j \leq J$  and a decoder state  $\mathbf{h}_{i-1}^{d}$  for  $1 \leq i \leq I$  an attention model for the decoder state  $\mathbf{h}_{i}^{d}$  is a function (V, Q) and K stand for "value", "query" and "key", respectively):

$$\mathbf{u}_i = \mathbf{a}(\mathbf{h}_1^e, \dots, \mathbf{h}_J^e, \mathbf{h}_{i-1}^d)$$

where a is:

$$\mathbf{u}_i = \sum_{j=1}^J f_j(\mathbf{h}_1^e, \dots, \mathbf{h}_J^e, \mathbf{h}_{i-1}^d) \; \mathbf{W}_V \mathbf{h}_j^e$$

 $f_i$  is a softmax:

$$f_{j}(\mathbf{h}_{1}^{e}, \dots, \mathbf{h}_{J}^{e}, \mathbf{h}_{i-1}^{d}) = \frac{\exp(\mathbf{W}_{Q}\mathbf{h}_{i-1}^{d} \cdot \mathbf{W}_{K}\mathbf{h}_{j}^{e})}{\sum_{j'=1}^{J} \exp(\mathbf{W}_{Q}\mathbf{h}_{i-1}^{d} \cdot \mathbf{W}_{K}\mathbf{h}_{j'}^{e})} \qquad 1 \leq j \leq J$$

#### NMT with attention model (Bahdanau et al. 2015) (Luong et al. 2015)

The RNN-based encoder:

$$\mathbf{h}_{j}^{e} = \mathbf{F}_{e}(\mathbf{W}_{E}(x_{j}), \mathbf{h}_{j-1}^{e}) = \mathbf{F}_{e}(\mathbf{x}_{j}, \mathbf{h}_{j-1}^{e}) \quad 1 \leq j \leq J \text{ and } \mathbf{h}_{0}^{e} = \mathbf{0}$$

The RNN-based decoder with attention model:

$$\mathbf{u}_i = \mathbf{a}(\mathbf{h}_1^e, \dots, \mathbf{h}_J^e, \mathbf{h}_{i-1}^d) \quad 1 \le i \le I$$

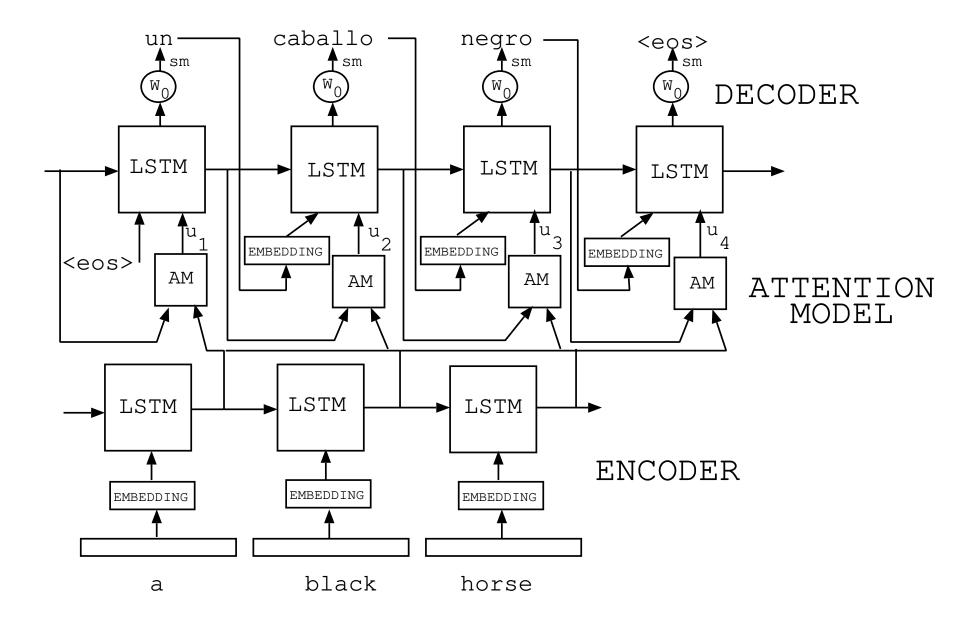
$$\mathbf{h}_{i}^{d} = \mathbf{F}_{d}(\mathbf{W}_{E}(y_{i-1}), \mathbf{h}_{i-1}^{d}, \mathbf{u}_{i}) = \mathbf{F}_{d}(\mathbf{y}_{i-1}, \mathbf{h}_{i-1}^{d}, \mathbf{u}_{i}) \quad 1 \leq i \leq I \text{ and } \mathbf{h}_{0}^{d} = \mathbf{0}$$

A probabilistic distribution over the target dictionary:  $\mathbf{f}_{sm}(\mathbf{W}_O \ \mathbf{h}_i^d)$ 

Output generation:

$$p(y_1^I \mid x_1^J) = \prod_{i=1}^I p(y_i \mid y_1^{i-1}, u(x_1^J)) = \prod_{i=1}^I \mathbf{f}_{sm}(\mathbf{W}_O \ \mathbf{h}_i^d)_{i(y_i)}$$

## **Text translation with attention mechanism** (Luong 2015)



### Bidirectional RNN for neural machine translation (Bahdanau et al. 2015)

The RNN-based encoder:

$$\mathbf{h}_{j}^{e,f} = \mathbf{F}_{e}(\mathbf{x}_{j}, \mathbf{h}_{j-1}^{e,f}) \quad 1 \leq j \leq J \qquad \mathbf{h}_{0}^{e,f} = \mathbf{0}$$

$$\mathbf{h}_{j}^{e,b} = \mathbf{F}_{e}(\mathbf{x}_{j}, \mathbf{h}_{j+1}^{e,b}) \quad J \geq j \geq 1 \qquad \mathbf{h}_{J+1}^{e,b} = \mathbf{0}$$

$$\mathbf{h}_{j}^{e} = [\mathbf{h}_{j}^{e,f}; \mathbf{h}_{j}^{e,b}] \quad 1 \leq j \leq J$$

The RNN-based decoder with attention model:

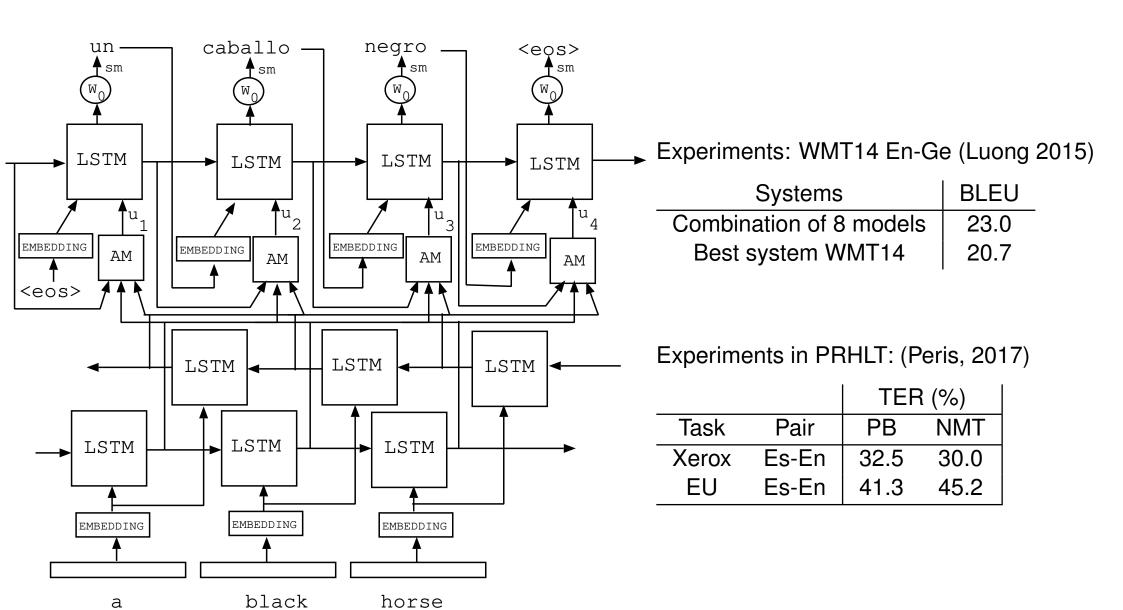
$$\mathbf{u}_i = \mathbf{a}(\mathbf{h}_1^e, \dots, \mathbf{h}_j^e, \mathbf{h}_{i-1}^d) \quad 1 \le i \le I$$
$$\mathbf{h}_i^d = \mathbf{F}_d(\mathbf{y}_{i-1}, \mathbf{h}_{i-1}^d, \mathbf{u}_i) \quad 1 \le i \le I \qquad \mathbf{h}_0^d = \mathbf{0}$$

A probabilistic distribution over the target dictionary:  $\mathbf{f}_{sm}(\mathbf{W}_O \ \mathbf{h}_i^d)$ 

Output generation:

$$p(y_1^I \mid x_1^J) = \prod_{i=1}^I p(y_i \mid y_1^{i-1}, u(x_1^J)) = \prod_{i=1}^I \mathbf{f}_{sm}(\mathbf{W}_O \mathbf{h}_i^d)_{i(y_i)}$$

### **Text translation with attention mechanism** (Luong 2015)



#### Other encoder-decoder architectures

- Multilayer encoder / multilayer decoder
- Conditional recurrent units (RNN blocks with attention models in between)
- GRUs

#### Index

- 1 Introduction ▷ 2
- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
- 4 Neural machine translation ≥ 23
- 5 Attention models and recurrent neural networks > 31
- 6 Attention models for all > 41
  - 7 Training and Decoding with NMT ▷ 66
  - 8 Translation results with neural machine translation > 72
  - 9 Other issues of NMT ⊳ 77
  - 10 Bibliography ⊳ 89

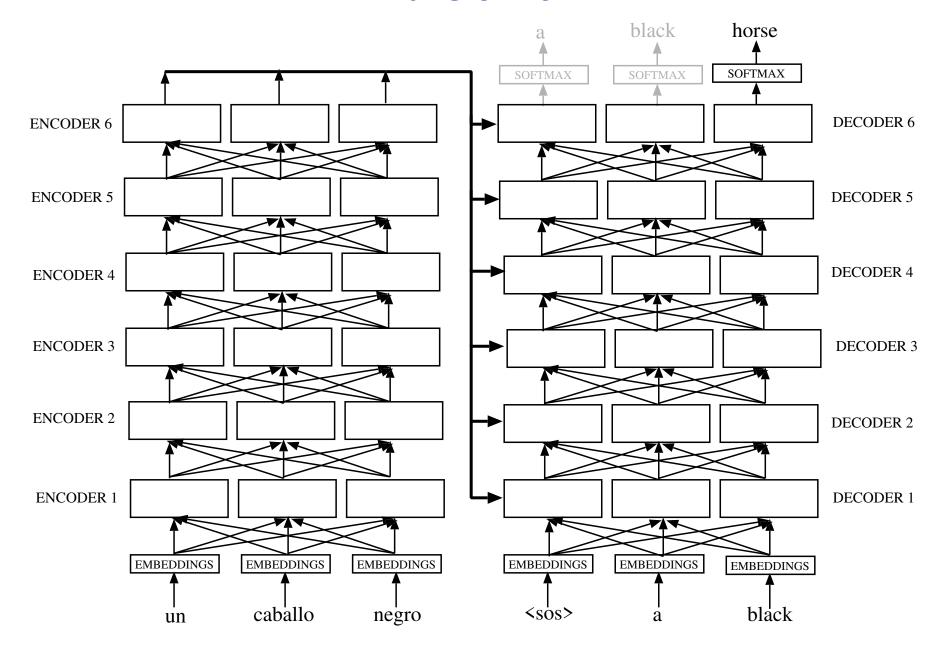
### **Transformer** (Vaswani 2017)(Ney 2018)

• Goal: Given a source sentence  $x_1^J$  and a target sentence  $y_1^I$ , compute:

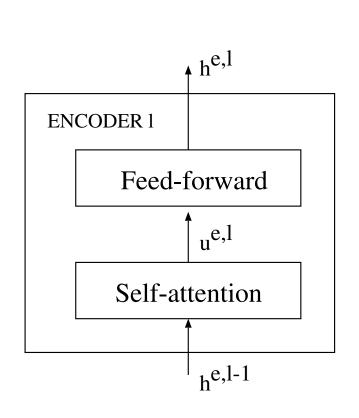
$$p(y_1^I \mid x_1^J) = \prod_{i=1}^I p(y_i \mid y_1^{i-1}, u(x_1^J))$$

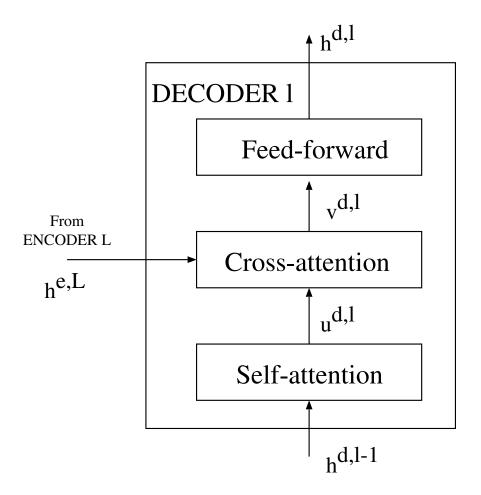
- Feed-forward networks.
- Self-attention or intra-sentence attention: (j, j') & (i, i') in addition to the cross-attention (i, j).
- Position encoding.
- Multi-head attention.
- Faster than RNN.

### **Transformer**

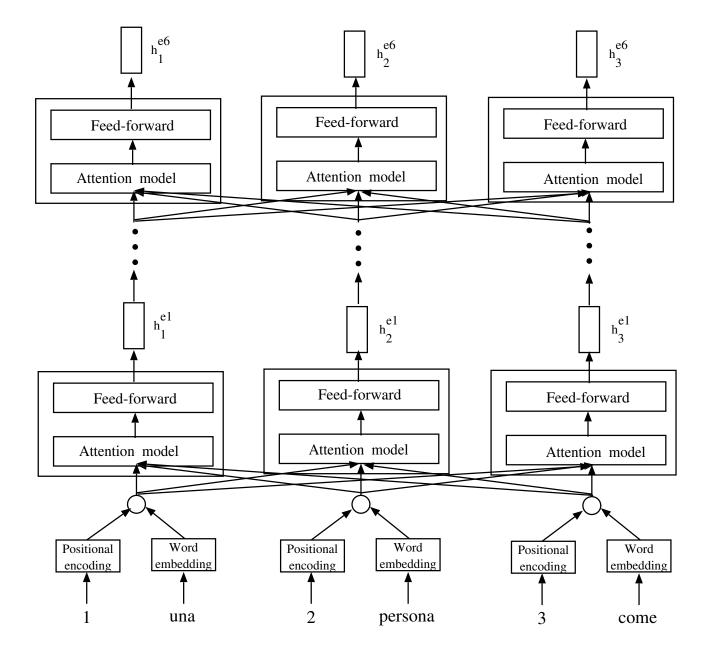


### **Transformer**





# A simplified view of the encoder in the Transformer



## Positional and word encodings

- A word x from a ordered vocabulary  $V_X$  with index i(x)
- Word embeddings:  $\mathbf{W_E}(x) \equiv [\mathbf{W_E}]_{i(x)} = \mathbf{x} \in \mathbb{R}^{D_W}$ : a row of  $\mathbf{W_E}$  is the word embedding of x
- Positional embeddings: Given a sentence  $x_1^J$  the positional embedding of position  $j, 1 \le j \le J$  is  $\mathbf{p}_j \in \mathbb{R}^{D_P}$ :

$$p_{j,2k} = \sin(j/10000^{2k/D_P})$$
  
 $p_{j,2k+1} = \cos(j/10000^{2k/D_P})$ 

- Relative positional embeddings.
- Learned positional embeddings.

#### The encoder of Transformer

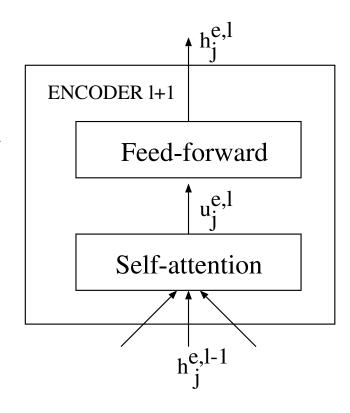
Given a source sentence  $x_1^J$ ,

- Initialization:  $\mathbf{h}_{j}^{e,0} = \mathbf{x}_{j} = \mathcal{E}(x_{j}) \quad 1 \leq j \leq J$
- In layer l of the encoder  $(1 \le l \le L)$ 
  - Self-attention model:

$$\mathbf{u}_{j}^{e,l} = \mathbf{a}(\mathbf{h}_{1}^{e,l-1}, \dots, \mathbf{h}_{J}^{e,l-1}, \mathbf{h}_{j}^{e,l-1}) \quad 1 \le i \le J$$

– Feed-forward network:

$$\mathbf{h}_{j}^{e,l} = \mathbf{F}_{f}(\mathbf{u}_{j}^{e,l}) \quad 1 \le j \le J$$



#### Self-attention models for the encoder

Given a sequence of encoder states  $\mathbf{h}_{j}^{e,l-1}$  for  $1 \leq j \leq J$  in layer  $1 \leq l \leq L$ , a self-attention model for a position j in a layer l is a function:

$$\mathbf{u}_{j}^{e,l} = \mathbf{a}(\mathbf{h}_{1}^{e,l-1}, \dots, \mathbf{h}_{J}^{e,l-1}, \mathbf{h}_{j}^{e,l-1}) \quad 1 \le i \le J$$

where a is:

$$\mathbf{u}_{j}^{e,l} = \sum_{j'=1}^{J} f_{j'}(\mathbf{h}_{1}^{e,l-1}, \dots, \mathbf{h}_{J}^{e,l-1}, \mathbf{h}_{j}^{e,l-1}) \; \mathbf{h}_{j'}^{e,l-1} \quad 1 \leq i \leq J$$

$$f_{j'}(\mathbf{h}_{1}^{e,l-1}, \dots, \mathbf{h}_{J}^{e,l-1}, \mathbf{h}_{j}^{e,l-1}) = \frac{\exp(\mathbf{h}_{j}^{e,l-1} \cdot \mathbf{h}_{j'}^{e,l-1})}{\sum_{j''=1}^{J} \exp(\mathbf{h}_{j}^{e,l-1} \cdot \mathbf{h}_{j''}^{e,l-1})} = p(j' \mid j) \quad 1 \leq j, j' \leq J$$

## Complete self-attention models for the encoder

Given a sequence of encoder states  $\mathbf{h}_{j}^{e,l-1}$  for  $1 \leq j \leq J$  in layer  $1 \leq l \leq L$ , a self-attention model for a position j in a layer l is a function:

$$\mathbf{u}_{j}^{e,l} = \mathbf{a}(\mathbf{h}_{1}^{e,l-1}, \dots, \mathbf{h}_{J}^{e,l-1}, \mathbf{h}_{j}^{e,l-1}) \quad 1 \le i \le J$$

where a is:

$$\mathbf{u}_{j}^{e,l} = \sum_{j'=1}^{J} f_{j'}(\mathbf{h}_{1}^{e,l-1}, \dots, \mathbf{h}_{J}^{e,l-1}, \mathbf{h}_{j}^{e,l-1}) \; \mathbf{W}_{V}^{e,l} \mathbf{h}_{j'}^{e,l-1} \quad 1 \leq i \leq J$$

$$f_{j'}(\mathbf{h}_{1}^{e,l-1}, \dots, \mathbf{h}_{J}^{e,l-1}, \mathbf{h}_{j}^{e,l-1}) = \frac{\exp(\mathbf{W}_{Q}^{e,l}\mathbf{h}_{j}^{e,l-1} \cdot \mathbf{W}_{K}^{e,l}\mathbf{h}_{j'}^{e,l-1})}{\sum_{j''=1}^{J} \exp(\mathbf{W}_{Q}^{e,l}\mathbf{h}_{j}^{e,l-1} \cdot \mathbf{W}_{K}^{e,l}\mathbf{h}_{j''}^{e,l-1})} \quad 1 \leq j, j' \leq J$$

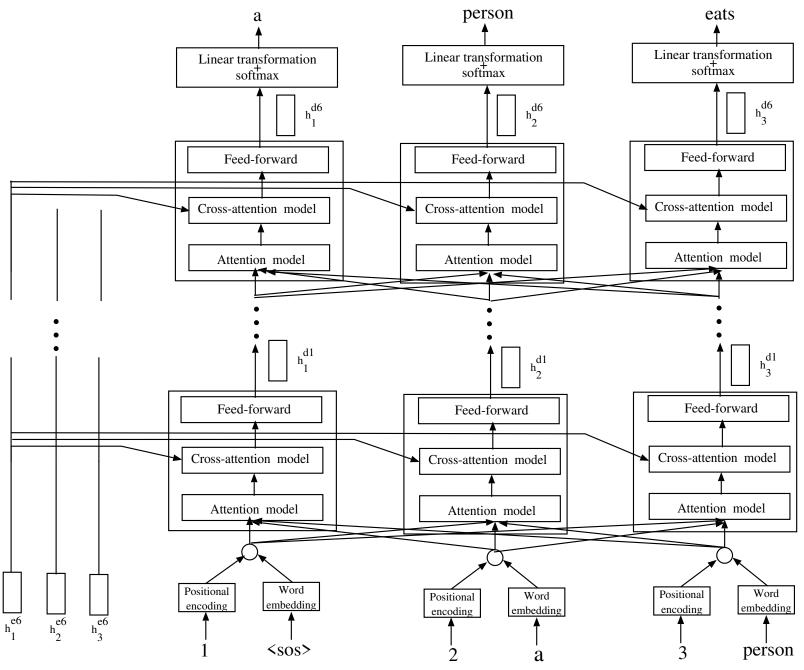
#### **Feed-forward network**

• Feed-forward networks,  $\mathbf{F}_f$  for layer l

$$\mathbf{F}_f(\mathbf{u}_j^{e,l}) \ = \ \mathbf{W}_2^{e,l} \ \mathbf{f}_{ReLU}(\mathbf{W}_1^{e,l} \ \mathbf{u}_j^{e,l} + \mathbf{b}_1^{e,l}) + \mathbf{b}_2^{e,l}$$

where  $\mathbf{W}_{2}^{e,l}$ ,  $\mathbf{W}_{1}^{e,l}$  are the weights of the second and first layer of the feed-forward networks, and  $\mathbf{b}_{2}^{e,l}$  and  $\mathbf{b}_{1}^{e,l}$  the corresponding bias.

# A simplified view of the decoder in the Transformer



#### The decoder of Transformer

Given a sequence of states of the encoder  $\mathbf{h}_{j}^{e,L}$   $1 \leq j \leq J$ ,

- For  $1 \le i \le I$ 
  - Initialization:  $\mathbf{u}_{i-1}^{d,0} = \mathbf{y}_{i-1} = \mathcal{E}(y_{i-1})$ ,  $(y_0 = " < sos > ")$
  - In layer l of the decoder  $(1 \le l \le L)$ :
    - \* Self-attention model:

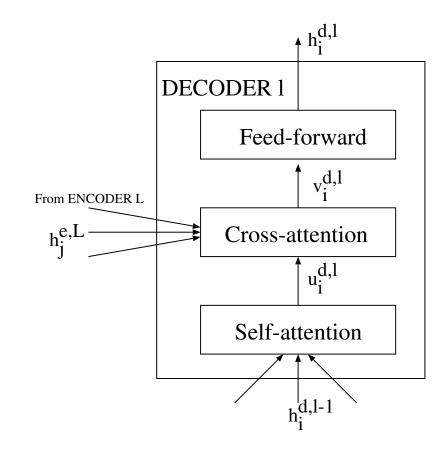
$$\mathbf{u}_i^{d,l} = \mathbf{a}(\mathbf{h}_1^{d,l-1}, \dots, \mathbf{h}_i^{d,l-1}, \mathbf{h}_i^{d,l-1})$$

\* Cross-attention model:

$$\mathbf{v}_i^{d,l} = \mathbf{a}(\mathbf{h}_1^{e,L},\dots,\mathbf{h}_J^{e,L},\mathbf{u}_i^{d,l})$$

\* Feed-forward network:

$$\mathbf{h}_i^{d,l} = \mathbf{F}_f(\mathbf{v}_i^{d,l})$$



#### Self-attention models for the decoder

Given a sequence of decoder states  $\mathbf{h}_i^{d,l-1}$  for  $1 \leq i \leq I$ , a self-attention model for a position i in a layer l is a function:

$$\mathbf{u}_i^{d,l} = \mathbf{a}(\mathbf{h}_1^{d,l-1}, \dots, \mathbf{h}_I^{d,l-1}, \mathbf{h}_i^{d,l-1}) \quad 1 \le i \le I$$

where a is:

$$\mathbf{u}_{i}^{d,l} = \sum_{i'=1}^{I} f_{i'}(\mathbf{h}_{1}^{d,l-1}, \dots, \mathbf{h}_{I}^{d,l-1}, \mathbf{h}_{i}^{d,l-1}) \; \mathbf{h}_{i'}^{d,l-1} \quad 1 \leq i \leq I$$

$$f_{i'}(\mathbf{h}_{1}^{d,l-1},\ldots,\mathbf{h}_{I}^{d,l-1},\mathbf{h}_{i}^{d,l-1}) = \frac{\exp(\mathbf{h}_{i}^{d,l-1} \cdot \mathbf{h}_{i'}^{d,l-1})}{\sum_{i''=1}^{I} \exp(\mathbf{h}_{i}^{d,l-1} \cdot \mathbf{h}_{i''}^{d,l-1})} = p(i' \mid i) \quad 1 \leq i, i' \leq I$$

MIARFID-UPV December 20, 2022 MT-4: 53

## Complete self-attention models for the decoder

Given a sequence of decoder states  $\mathbf{h}_i^{d,l-1}$  for  $1 \le i \le I$ , a self-attention model for a position i in a layer l is a function:

$$\mathbf{u}_i^{d,l} = \mathbf{a}(\mathbf{h}_1^{d,l-1}, \dots, \mathbf{h}_I^{d,l-1}, \mathbf{h}_i^{d,l-1}) \quad 1 \le i \le I$$

where a is:

$$\mathbf{u}_i^{d,l} = \sum_{i'=1}^I f_{i'}(\mathbf{h}_1^{d,l-1}, \dots, \mathbf{h}_I^{d,l-1}, \mathbf{h}_i^{d,l-1}) \; \mathbf{W}_V^{d,l} \mathbf{h}_{i'}^{d,l-1} \quad 1 \leq i \leq I$$

$$f_{i'}(\mathbf{h}_{1}^{d,l-1},\ldots,\mathbf{h}_{I}^{d,l-1},\mathbf{h}_{i}^{d,l-1}) = \frac{\exp(\mathbf{W}_{Q}^{d,l}\mathbf{h}_{i}^{d,l-1}\cdot\mathbf{W}_{K}^{d,l}\mathbf{h}_{i'}^{d,l-1})}{\sum_{i''=1}^{I}\exp(\mathbf{W}_{Q}^{d,l}\mathbf{h}_{i}^{d,l-1}\cdot\mathbf{W}_{K}^{d,l}\mathbf{h}_{i''}^{d,l-1})} \quad 1 \leq i,i' \leq I$$

MIARFID-UPV December 20, 2022 MT-4: 54

#### Cross-attention models for the decoder

Given a sequence of output of self-attentions in the decoder  $\mathbf{u}_{i'}^{d,l-1}$  for  $1 \leq i' \leq i$  and some i, a cross-attention model for a position  $i' \leq i$  in a layer i is a function:

$$\mathbf{v}_{i'}^{d,l} = \mathbf{a}(\mathbf{h}_1^{e,L}, \dots, \mathbf{h}_J^{1,L}, \mathbf{u}_{i'}^{d,l}) \quad 1 \le i' \le i$$

where  $\mathbf{a}_c$  is in:

$$\mathbf{v}_{i'}^{d,l} = \sum_{j=1}^J f_j(\mathbf{h}_1^{e,L},\ldots,\mathbf{h}_J^{e,L},\mathbf{u}_{i'}^{d,l}) \; \mathbf{h}_j^{e,L}$$

$$f_j(\mathbf{h}_1^{e,L}, \dots, \mathbf{h}_J^{e,L}, \mathbf{u}_{i'}^{d,l}) = \frac{\exp(\mathbf{u}_{i'}^{d,l} \cdot \mathbf{h}_j^{e,L})}{\sum_{j=1}^{J} \exp(\mathbf{u}_{i'}^{d,l} \cdot \mathbf{h}_j^{e,L})} = p(j \mid i'); 1 \leq i' \leq i, \quad 1 \leq j \leq J$$

## Complete cross-attention models for the decoder

Given a sequence of output of self-attentions in the decoder  $\mathbf{u}_{i'}^{d,l-1}$  for  $1 \leq i' \leq i$  and some i, a cross-attention model for a position  $i' \leq i$  in a layer l is a function:

$$\mathbf{v}_{i'}^{d,l} = \mathbf{a}(\mathbf{h}_1^{e,L}, \dots, \mathbf{h}_J^{1,L}, \mathbf{u}_{i'}^{d,l}) \quad 1 \le i' \le i$$

where  $\mathbf{a}_c$  is in:

$$\mathbf{v}_{i'}^{d,l} = \sum_{j=1}^J f_j(\mathbf{h}_1^{e,L},\ldots,\mathbf{h}_J^{e,L},\mathbf{u}_{i'}^{d,l}) \ \mathbf{W}_V^{c,l} \mathbf{h}_j^{e,L}$$

$$f_{j}(\mathbf{h}_{1}^{e,L},\ldots,\mathbf{h}_{J}^{e,L},\mathbf{u}_{i'}^{d,l}) = \frac{\exp(\mathbf{W}_{Q}^{c,l}\mathbf{u}_{i'}^{d,l}\cdot\mathbf{W}_{K}^{c,l}\mathbf{h}_{j}^{e,L})}{\sum_{i=1}^{J}\exp(\mathbf{W}_{Q}^{c,l}\mathbf{u}_{i'}^{d,l}\cdot\mathbf{W}_{K}^{c,l}\mathbf{h}_{j}^{e,L})} \quad 1 \leq i' \leq i, \quad 1 \leq j \leq J$$

#### **Feed-forward network**

• Feed-forward networks,  $\mathbf{F}_f$ : Given a  $\mathbf{v}_i^{d,l} \in \mathbb{R}^d$ .

$$\mathbf{F}_f(\mathbf{v}_i^{d,l}) \ = \ \mathbf{W}_2^{d.l} \ \mathbf{f}_{ReLU}(\mathbf{W}_1^{d.l} \ \mathbf{v}_i^{d,l} + \mathbf{b}_1^{d.l}) + \mathbf{b}_2^{d.l}$$

where  $\mathbf{W}_2^{d.l}$ ,  $\mathbf{W}_1^{d.l}$  are the weights of the second and first layer of the feed-forward networks, and  $\mathbf{b}_2^{d.l}$  and  $\mathbf{b}_1^{d.l}$  the corresponding bias.

### The decoder of Transformer (Vaswani 2017)

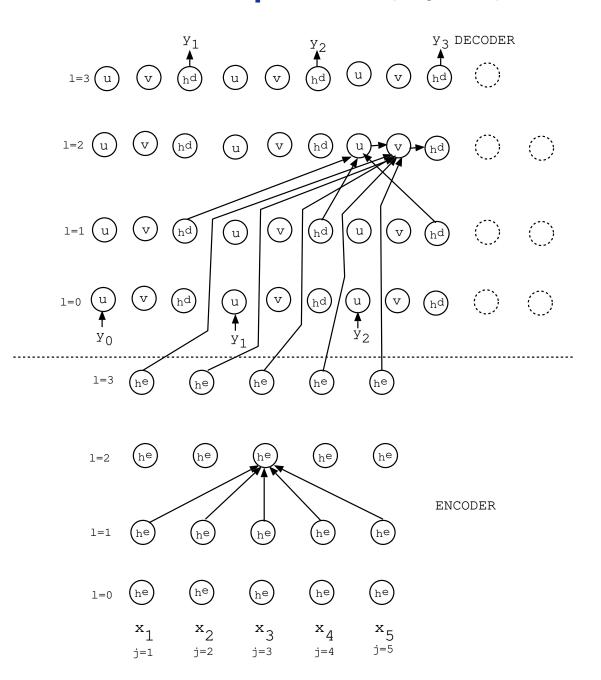
• For each the state of the decoder in the last layer  $\mathbf{h}_i^{d,L}$   $1 \leq i \leq I$ :

A probabilistic distribution over the target dictionary:  $\mathbf{f}_{sm}(\mathbf{W}_O \ \mathbf{h}_i^{d,L})$ 

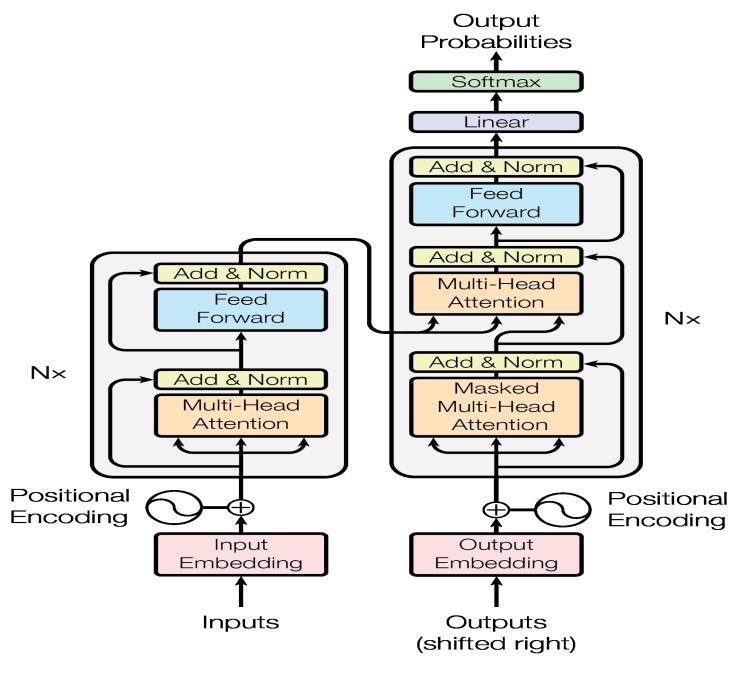
Output generation:

$$p(y_1^I \mid x_1^J) = \prod_{i=1}^I p(y_i \mid y_1^{i-1}, u(x_1^J)) = \prod_{i=1}^I \mathbf{f}_{sm}(\mathbf{W} \ \mathbf{h}_i^{d,L})_{i(y_i)}$$

## The whole process (Ney 2018)



## **Transformer** (Vaswani 2017)



### Some details and additional features of Transformer

- Residual networks
- Layer normalization
- Multi-head attention

MIARFID-UPV December 20, 2022 MT-4: 61

### Some details and additional features of Transformer (Xiong arXiv 2020)

• Given  $\mathbf{z} \in \mathbb{R}^d$  and a function  $\mathbf{f} : \mathbb{R}^d \to \mathbb{R}^d$ , a residual function  $\mathbf{R}$  is defined as:

$$\mathbf{R}(\mathbf{z}, \mathbf{f}(\mathbf{z})) = \mathbf{f}(\mathbf{z}) + \mathbf{z}$$

• Given a sequence of vectors  $\mathbf{z}_1, \dots, \mathbf{z}_K$  from a layer with  $\mathbf{z}_k \in \mathbb{R}^d$  for  $1 \le k \le K$ , a layer normalization  $\mathbf{N}$  is  $\mathbf{N}(\mathbf{z}_1, \dots, \mathbf{z}_K) = (\bar{\mathbf{z}}_1, \dots, \bar{\mathbf{z}}_K)$  such that:

$$\bar{z}_{k,i} = \gamma \, \frac{z_{k,i} - \mu_i}{\sigma_i} + \beta \quad 1 \le k \le K, \ 1 \le i \le d$$

where  $\gamma$  and  $\beta$  are hyper-parameters:

$$\mu_i = \frac{\sum_{k=1}^K z_{k,i}}{K} \quad \text{and} \quad \sigma_i^2 = \frac{\sum_{k=1}^K (z_{k,i} - \mu_i)^2}{K} \quad 1 \le i \le d$$

#### **Multi-head attention in Transformer**

For N heads and  $1 \le l \le L$ ,  $1 \le j \le J$  and  $1 \le i \le I$ :

Encoder self-attention:

$$\begin{aligned} \mathbf{u}_{j,n}^{e,l} &=& \mathbf{a}_{n}(\mathbf{h}_{1}^{e,l-1}, \dots, \mathbf{h}_{J}^{e,l-1}, \ \mathbf{h}_{j}^{e,l-1}) \quad 1 \leq j \leq J \text{ and } 1 \leq n \leq N \\ &=& \sum_{j'=1}^{J} \frac{\exp(\mathbf{W}_{Q}^{e,l,n} \mathbf{h}_{j}^{e,l-1} \cdot \mathbf{W}_{K}^{e,l,n} \mathbf{h}_{j'}^{e,l-1})}{\sum_{j''=1}^{J} \exp(\mathbf{W}_{Q}^{e,l,n} \mathbf{h}_{j}^{e,l-1} \cdot \mathbf{W}_{K}^{e,l,n} \mathbf{h}_{j''}^{e,l-1})} \mathbf{W}_{V}^{e,l,n} \mathbf{h}_{j'}^{e,l-1} \qquad 1 \leq j, j' \leq J \end{aligned}$$

 $\mathbf{W}_Q^{e,l,n}, \mathbf{W}_K^{e,l,n}, \mathbf{W}_V^{e,l,n}$  are matrix of  $D_W/N imes D_W$ 

$$\mathbf{u}_{j}^{e,l} = \begin{bmatrix} \mathbf{u}_{j,1}^{e,l}, \dots, \mathbf{u}_{j,N}^{e,l} \end{bmatrix}; \quad \mathbf{h}_{j}^{e,l} = \mathbf{F}_{f}(\mathbf{u}_{j}^{e,l}) \quad 1 \leq j \leq J$$

#### **Multi-head attention in Transformer**

For N heads and  $1 \le l \le L$ ,  $1 \le j \le J$  and  $1 \le i \le I$ :

Decoder self-attention:

$$\begin{aligned} \mathbf{u}_{i,n}^{d,l} &=& \mathbf{a}_{n}(\mathbf{h}_{1}^{d,l-1}, \dots, \mathbf{h}_{J}^{d,l-1}, \ \mathbf{h}_{i}^{d,l-1}) \quad 1 \leq i \leq I \ \text{and} \ 1 \leq n \leq N \\ &=& \sum_{i'=1}^{I} \frac{\exp(\mathbf{W}_{Q}^{d,l,n} \mathbf{h}_{i}^{d,l-1} \cdot \mathbf{W}_{K}^{d,l,n} \mathbf{h}_{i'}^{d,l-1})}{\sum_{i''=1} \exp(\mathbf{W}_{Q}^{d,l,n} \mathbf{h}_{i}^{d,l-1} \cdot \mathbf{W}_{K}^{d,l,n} \mathbf{h}_{i''}^{d,l-1})} \ \mathbf{W}_{V}^{d,l,n} \mathbf{h}_{i'}^{d,l-1} \qquad 1 \leq i,i' \leq I \end{aligned}$$

 $\mathbf{W}_Q^{d,l,n}, \mathbf{W}_K^{d,l,n}, \mathbf{W}_V^{d,l,n}$  are matrix of  $D_W/N imes D_W$ 

$$\mathbf{u}_i^{d,l} = \begin{bmatrix} \mathbf{u}_{i,1}^{d,l}, \dots, \mathbf{u}_{i,N}^{d,l} \end{bmatrix}; \quad \mathbf{h}_i^{d,l} = \mathbf{F}_f(\mathbf{u}_i^{d,l}) \quad 1 \leq i \leq I$$

#### **Multi-head attention in Transformer**

For N heads and  $1 \le l \le L$ ,  $1 \le j \le J$  and  $1 \le i \le I$ :

Decoder cross-attention:

$$\begin{aligned} \mathbf{v}_{i,n}^{d,l} &= & \mathbf{a}_n(\mathbf{h}_1^{e,L}, \dots, \mathbf{h}_J^{e,L}, \ \mathbf{u}_i^{d,l}) \quad 1 \leq i \leq I \ \text{and} \ 1 \leq n \leq N \\ &= & \sum_{j=1}^J \frac{\exp(\mathbf{W}_Q^{c,l,n} \mathbf{u}_i^{d,l} \cdot \mathbf{W}_K^{c,l,n} \mathbf{h}_j^{e,L})}{\sum_{j=1}^J \exp(\mathbf{W}_Q^{c,l,n} \mathbf{u}_i^{d,l} \cdot \mathbf{W}_K^{c,l,n} \mathbf{h}_j^{e,L})} \ \mathbf{W}_V^{c,n} \mathbf{h}_j^{e,L} \qquad 1 \leq i \leq I \end{aligned}$$

 $\mathbf{W}_Q^{c,l,n}, \mathbf{W}_K^{c,l,n}, \mathbf{W}_V^{c,l,n}$  are matrix of  $D_W/N \times D_W$ 

$$\mathbf{v}_i^{d,l} = \begin{bmatrix} \mathbf{v}_{i,1}^{d,l}, \dots, \mathbf{v}_{i,N}^{d,l} \end{bmatrix}; \quad \mathbf{h}_i^{d,l} = \mathbf{F}_f(\mathbf{v}_i^{d,l}) \quad 1 \leq i \leq I$$

#### Index

- 1 Introduction ▷ 2
- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
- 4 Neural machine translation ≥ 23
- 5 Attention models and recurrent neural networks > 31
- 6 Attention models for all ≥ 41
- 7 Training and Decoding with NMT > 66
  - 8 Translation results with neural machine translation > 72
  - 9 Other issues of NMT ⊳ 77
  - 10 Bibliography ⊳ 89

### Training with NMT (Koehn, 2017)

• Given a training set of bilingual pairs T, maximize the log-likelihood:

$$\begin{split} \widehat{\mathbf{W}} &= \underset{\mathbf{W}}{\operatorname{argmax}} \, \mathcal{F}_T(\mathbf{W}) &\equiv \underset{\mathbf{W}}{\operatorname{argmax}} \, \sum_{(x_1^J, y_1^I) \in T} \log p(y_1^I \mid x_1^J; \mathbf{W}) \\ &= \underset{\mathbf{W}}{\operatorname{argmax}} \, \sum_{(x_1^J, y_1^I) \in T} \sum_{i=1}^I \log p(y_i \mid y_1^{i-1}, x_1^J; \mathbf{W}) \\ &= \underset{\mathbf{W}}{\operatorname{argmax}} \, \sum_{(x_1^J, y_1^I) \in T} \sum_{i=1}^I \log \mathbf{f}_{sm}(\mathbf{W}_O \, \mathbf{h}_i^d(x_1^J))_{i(y_i)} \end{split}$$

- Optimization algorithms: Based on backpropagation through time using stochastic gradient descent.
  - Shuffle the training corpus.
  - Break up the corpus into maxi-batches.
  - Break up each maxi-batch into mini-batches.
  - Compute gradients for each mini-batches.
  - Update all the parameters (weights and word embeddings) at the end of a maxibatch.

## Gradient descent optimization algorithms (Ruder 2016)

- SDG (stochastic gradient descent).
- SGD with momentum
- Adagrad (Adaptive Gradient)
- Adadelta (an extension of Adagrad)
- Adam (Adaptive Moment Estimation)
- NAG, RMSProp, AdaMax, Nadam, ...

 Implementation through computational graphs in TensorFlow, PyTorch, JAX.

## **Training issues**

- Early stopping.
- Batch and layer normalization.
- Data augmentation.
- Hyperparameters
  - Dimension of source word embeddings.
  - Dimension of target word embeddings.
  - Number of LSTM/GRUs in encoder.
  - Number of LSTM/GRUs in decoder.
  - Number of layers in encoder of Transformer.
  - Number of layers in decoder of Transformer.
  - Initial learning rate.
  - Patience.
  - Dropout parameter.
  - Weight decay.
  - Noisy injection (to inputs, outputs, ...)

**–** ...

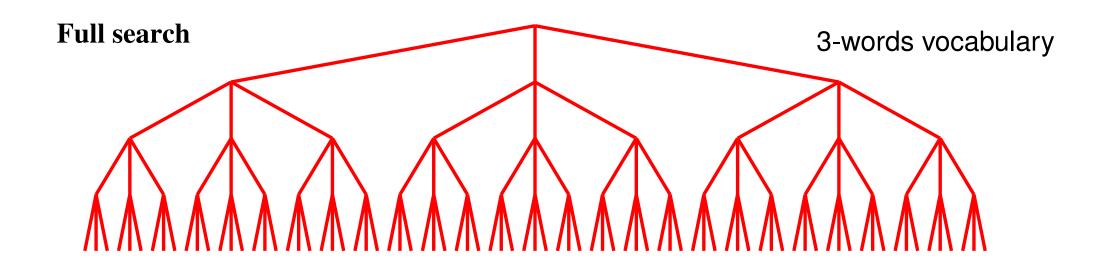
### Inference (decoding) with NMT (Koehn, 2017)

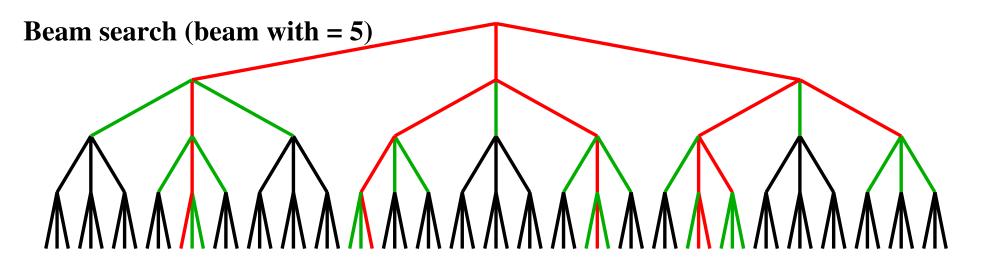
• For a source sentence  $x_1^J$  search for a target sentence  $\hat{y}_1^{\hat{I}}$ ,

$$\begin{split} \hat{y}_1^{\hat{I}} &= \underset{I,y_1^I}{\operatorname{argmax}} \, p(y_1^I \mid x_1^J; \mathbf{W}) \\ &= \underset{I,y_1^I}{\operatorname{argmax}} \prod_{i=1}^I p(y_i \mid y_1^{i-1}, u(x_1^J); \mathbf{W}) \\ &= \underset{I,y_1^I}{\operatorname{argmax}} \prod_{i=1}^I \mathbf{f}_{sm}(\mathbf{W}_O \; \mathbf{h}_i^d(x_1^J))_{i(y_i)} \\ &= \underset{I,y_1^I}{\operatorname{argmax}} \prod_{i=1}^I \mathbf{f}_{sm}(\mathbf{W}_O \; \mathbf{h}_i^d(x_1^J))_{i(y_i)} \end{aligned}$$

- Translation:
  - Greedy approach: for each i the maximum from the softmax output.
  - Smart tree search with beam search (suboptimal search)
    - \* At the begining of the process there is a empty list of target hypotheses.
    - \* At each target position there is a bounded prefix tree of K target prefixes. For each prefix, a bounded set of extended prefixes is generated by appending the most promising words.
    - \* The process ends when a "eof" is generated.

# **Decoding with NMT** (Ney, 2018)





black=possible arcs

green = extended & discarded

red = extended & preserved

#### Index

- 1 Introduction ▷ 2
- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
- 4 Neural machine translation ≥ 23
- 5 Attention models and recurrent neural networks > 31
- 6 Attention models for all ≥ 41
- 7 Training and Decoding with NMT ▷ 66
- 8 Translation results with neural machine translation > 72
  - 9 Other issues of NMT ⊳ 77
  - 10 Bibliography ▷ 89

### **Corpus for text translation**

- XRCE: Printer manuals.
- TED: Transcription of videos from expert speakers on education, business, science, tech and creativity.

```
https://www.ted.com/talks
```

• UFAL: Medical texts.

```
https://ufal.mff.cuni.cz/ufal_medical_corpus
```

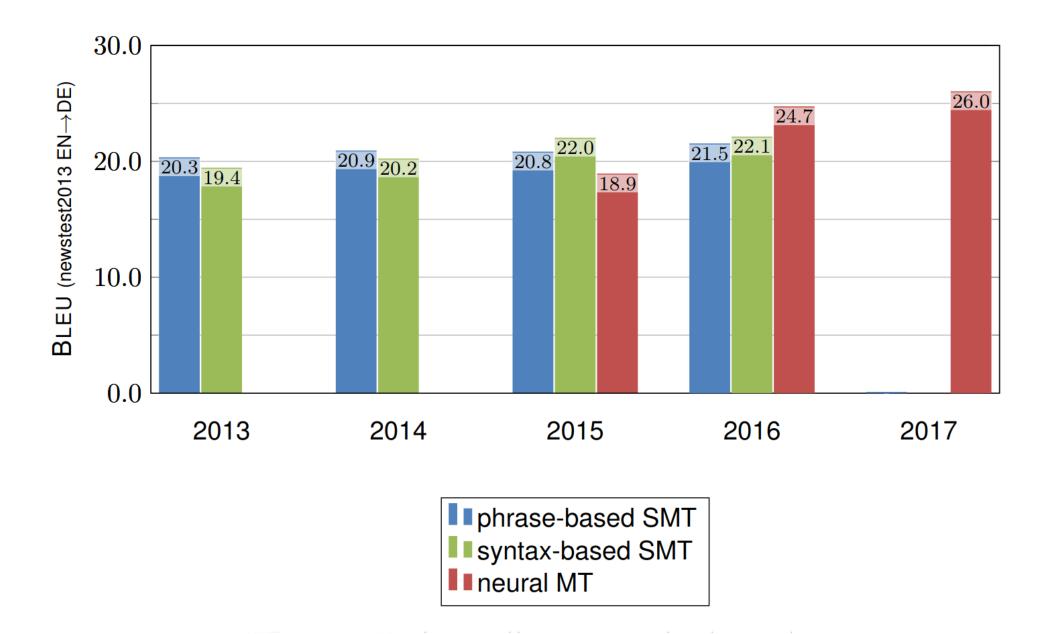
• EUROPARL: Proceedings of the European Parliament

```
https://www.statmt.org/europarl/
```

# **Text translation results** (Peris 2019)

Task	Languages	Recurrent		Transformer		PB-SMT	
		BLEU	TER	BLEU	TER	BLEU	TER
XRCE	EN-FR	38.0	51.9	32.0	57.2	37.9	50.2
XRCE	GE-EN	36.2	51.1	31.3	54.9	36.8	50.1
TED	FR-EN	32.4	46.6	30.1	49.5	29.9	50.5
TED	ZH-EN	13.7	75.7	11.5	76.7	11.0	77.5
UFAL	EN-FR	37.2	46.1	37.8	45.9	35.0	47.9
UFAL	ES-EN	44.4	35.4	43.1	36.4	38.7	40.4
<b>EUROPARL</b>	EN-ES	25.0	58.6	26.1	55.4	24.6	56.8
EUROPARL	GE-EN	21.2	62.9	22.3	60.7	20.4	60.9

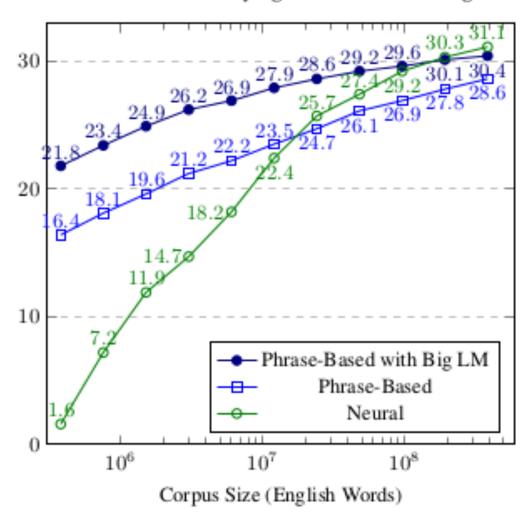
# Edinburgh's WMT results over the years (Sennrich et al. 2017)



### PBMT vs NMT and the size of training data (Koehn & Knowles. 2017)

### **English-Spanish**

#### **BLEU Scores with Varying Amounts of Training Data**



### Index

- 1 Introduction ≥ 2
- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
- 4 Neural machine translation ≥ 23
- 5 Attention models and recurrent neural networks > 31
- 6 Attention models for all ≥ 41
- 7 Training and Decoding with NMT ▷ 66
- 8 Translation results with neural machine translation ▶ 72
- 9 Other issues of NMT ▷ 77
  - 10 Bibliography ⊳ 89

### Character based text translation (Larriba 2018)

#### • Pros:

- Smaller vocabularies.
- Reduce out-of-vocabulary words.
- Profit from in-word lexical information

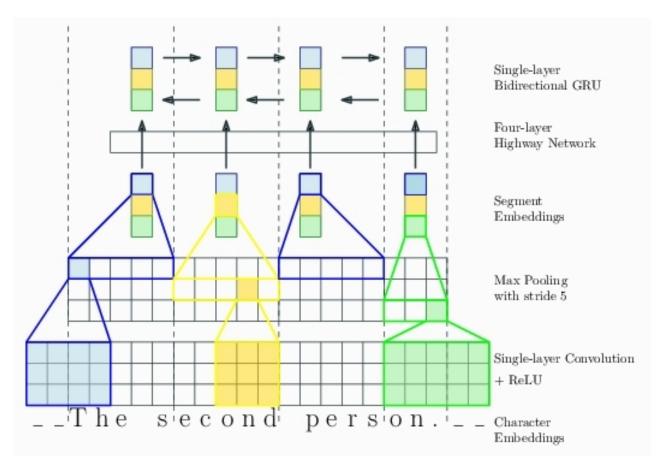
#### • Cons:

- Longer input sequences.
- References at word level.

#### Approaches:

- Fully character based NMT
- Encoder based on convolutional character NN
- Word embedding from character embedding

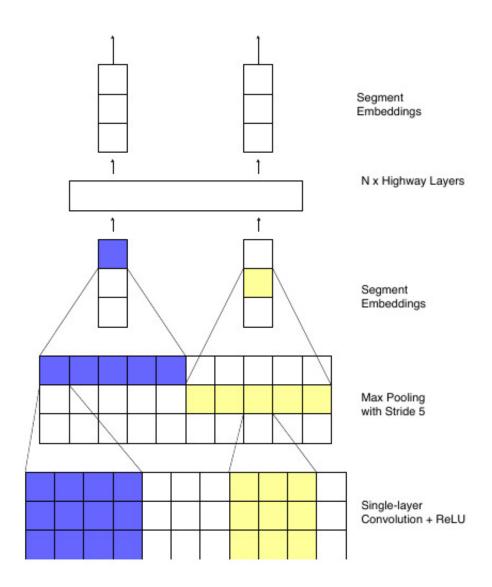
## **Convolutional character NMT** (Lee 2017)



### WMT'15 (Ge-En)

System	BLEU
BPE(s)+BPE(t) NN	24.0
BPE(s)+char(t) NN	25.3
char(s)+char(t) NN	25.8

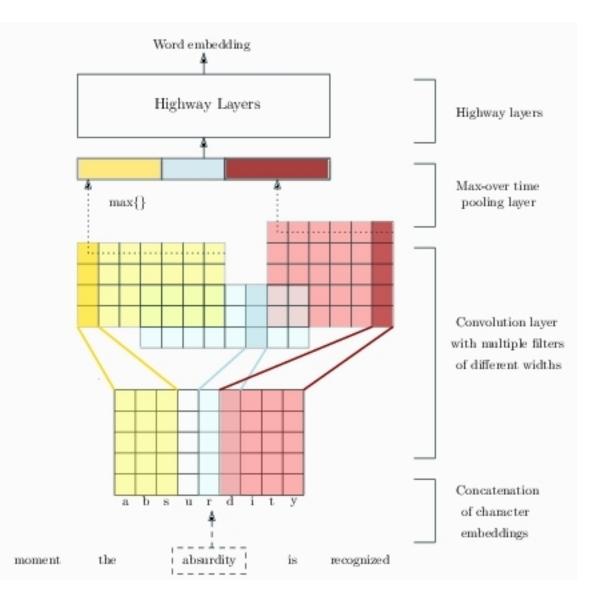
# Convolutional character encoder for Transformer (Banar 2020)



WMT'15 (Ru-En)

System	Unit	BLEU
CharRNN	char	22.73
Transformer	char	26.99
CharTransformer	char	26.19
Transformer	bpe	28.01

# Convolutional character encoder (Costa-Jussà & Fenollosa 2016)



	BLEU		
System	Ge-En	En-Ge	
PBM	21.0	17.0	
Word-based NN	20.6	17.2	
Character-based NN	22.1	20.2	

### Refinements (Koehn, 2017)

- Ensemble decoding.
- Reranking n-best output list with a target language decoding.
- Large vocabularies and out-of-vocabulary words: BPE, categories, character-based translation, ...
- Adding monolingual data:
  - Back translation.
  - Adding a language model.
- Combining statistical alignment models and attention models.
- Adaptation.
- Adding linguistic annotation in the target.

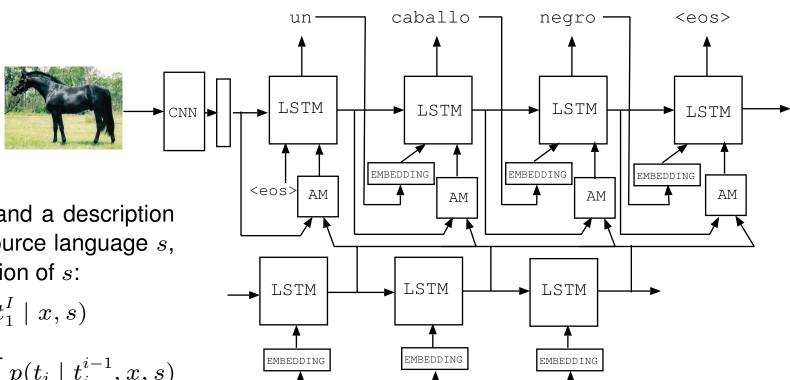
#### Other issues in the course

- Multimodal machine translation (in this section)
- Speech machine translation (in this section)
- Computer-assisted translation (topic 4)
- In topic 5:
  - Context-aware or document machine translation.
  - Multilingual machine translation.
  - Training NMT systems from monolingual corpora.
  - Syntax in NMT.
  - Reinforcement Learning in NMT.
  - Pre-trained models.

### Other topics in the NMT

- Translation with low-resource languages.
- Data selection (this is a general topic)
- The use of specific glossaries (place holders)
- LegoNN: building encoder-decoder architectures with decoder modules that can be reused across various MT tasks [Damnia arXiv 2022]
- Reduction of inference time: CTranslate 2.0 from openNMT.
- Other computational issues: computational graphs, parallelism, the use of GPUs, ...

## Multimodal machine translation (Huang 2016)



black

horse

Given an image x and a description of the image in a source language s, search for a translation of s:

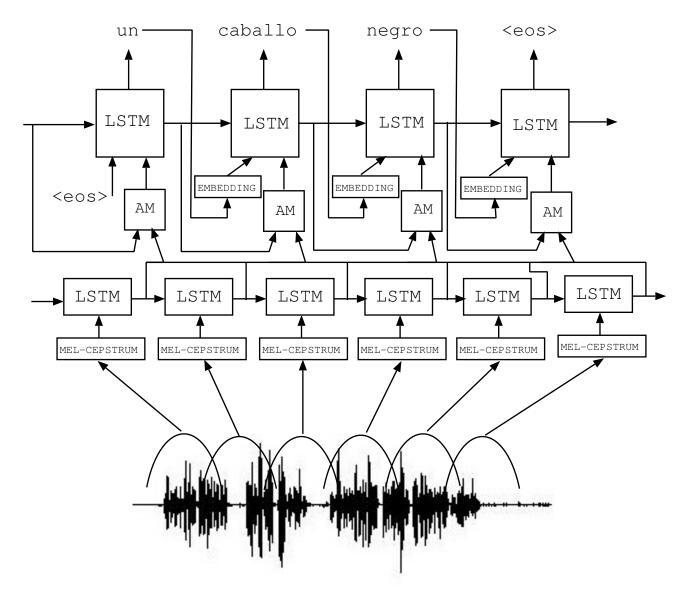
$$egin{array}{lll} \hat{t}_1^{\hat{I}} &=& rgmax \, p(t_1^I \mid x,s) \ &=& rgmax \prod_{I,t}^I p(t_i \mid t_i^{i-1},x,s) \end{array}$$

Experiments: WMT16 Multimodal machine translation English-to-German

Systems	METEOR
Our model (without optimization)	41.1
Best system WMT16 (without Moses)	51.5
Best system WMT16 (using Moses)	53.2

а

### Speech machine translation (Weiss et al. 2017)



Given an utterance x, search for a translation of s:

$$egin{array}{lll} \hat{t}_1^{\hat{I}} &=& rgmax \, p(t_1^I \mid x) \ &=& rgmax \prod_{I,t}^I p(t_i \mid t_i^{i-1}, x) \end{array}$$

Spanish-English Fisher task

Systems	BLEU
End-to-end	47.3
Supervised source	48.7
Cascade ASR+NMT	45.5

#### Toolkits for neural machine translation

- Fairseq https://github.com/pytorch/fairseq Facebook, Google Brain (Ott+ arXiv 2019)
- MarianNMT
   https://github.com/marian-nmt/marian/

   Microsoft, Adam Mickiewicz U., U. of Edinburgh, (Junczys-Dowmunt+ ACL 2018)
- modernNMT https://github.com/modernmt/modernmt Facebook, FBK. Translated ()
- Nematus
   U. of Edinburgh, Middle East U., New York U., Heidelberg U., U. of Zurich (Sennrich+ arXiv 2017)
- NMT-Keras https://github.com/lvapeab/nmt-keras UPV (Peris+ PBML 2018)
- OpenNMT SYSTRAN, Harward U., Ubiqus (Klein+ arXiv 2018)
- RETURNN

  https://github.com/rwth-i6/returnn

  RWTH Aachen, AppTek, NNAISENSE (Zeyer+ arXiv 2018)
- Sockeye
  Amazon (Hieber+ arXiv 2017)

  https://github.com/awslabs/sockeye
- T2T https://github.com/tensorflow/tensor2tensor Google, DeepMind (Wasvani+ arXiv 2018)
- XNMT

  CMU, KIT, Limsi, NIST, Inria, Pennsylvania U., Illinois U. (Neubig+ arXiv 2018)

MIARFID-UPV December 20, 2022 MT-4: 87

# **Neural machine translation systems**

• DeepL https://www.deepl.com/en/translator

Google translate

https://translate.google.com/

Pure Neural Machine Translation

https://translate.systran.net/translationTools/text

UPV Neural Machine Translation

http://casmacat.prhlt.upv.es/inmt/

#### Index

- 1 Introduction ▷ 2
- 2 Syncronized feedforward neural networks ▶ 11
- 3 Syncronized recurrent neural networks ▷ 14
- 4 Neural machine translation ≥ 23
- 5 Attention models and recurrent neural networks ≥ 31
- 6 Attention models for all ≥ 41
- 7 Training and Decoding with NMT ▷ 66
- 8 Translation results with neural machine translation > 72
- 9 Other issues of NMT ⊳ 77
- 10 Bibliography ▷ 89

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