

# Causal discovery

AI4ER MRes Workshop



# So far...

So far we have assumed we know the causal graph (the DAG)!

This may not always be true!!

The question is...can we discover it from data...?

This is a real leap...how are we going to do it?!!

# This is the world of causal discovery

- First thing to note - **some people think this is impossible and should never even be entertained.**
- There are a number of methods to do this which will be outlined here.
- I, for one, am undecided...

# Firstly, some assumptions we have to make

1. **Acyclicity** — causal structure can be represented by DAG,  $G$
2. **Markov Property** — all nodes are independent of their non-descendants when conditioned on their parents
3. **Faithfulness** — all conditional independencies in true underlying distribution  $p$  are represented in  $G$
4. **Sufficiency** — any pair of nodes in  $G$  has no common external cause

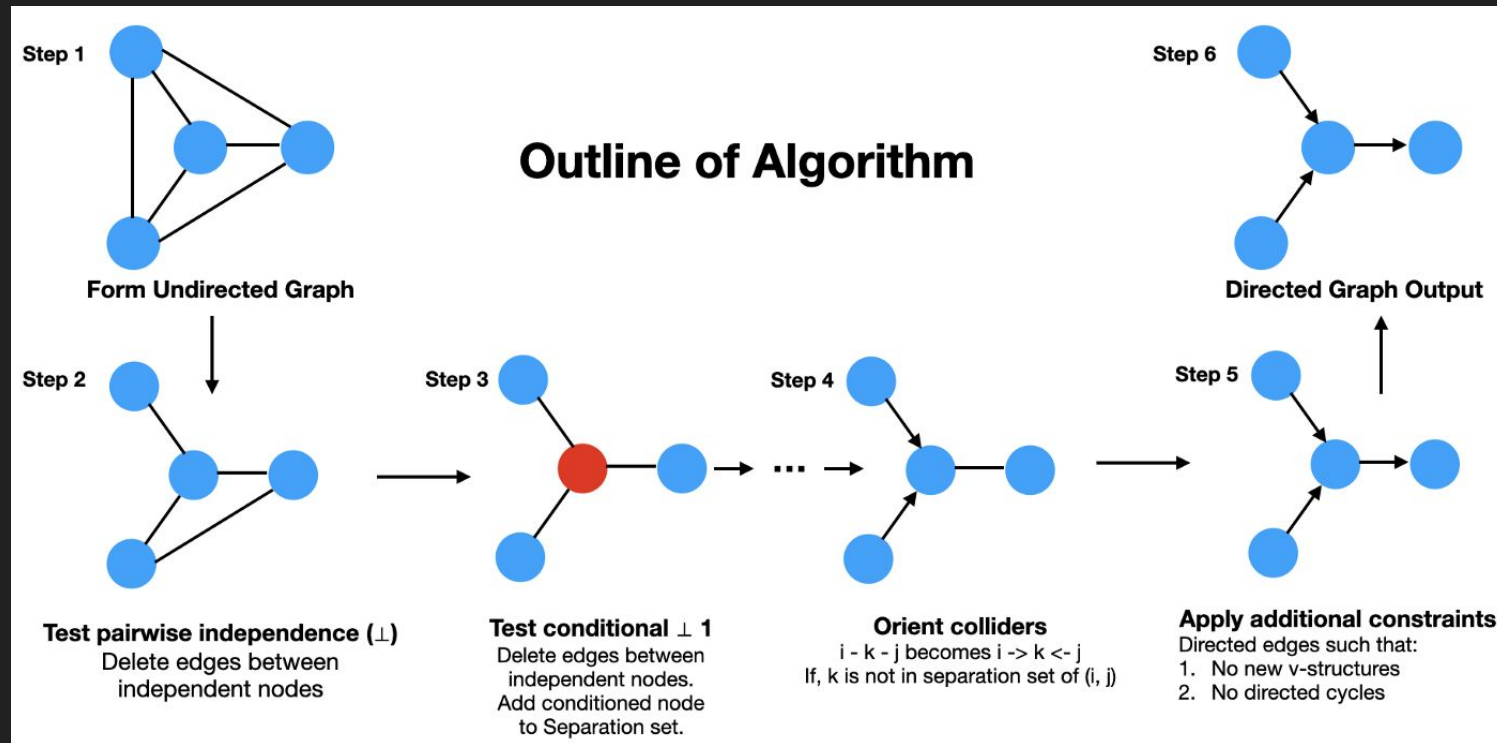
# Any ideas?

- Does anyone have any idea how we might construct our causal graph from data?

# Method 1: Conditional Independence Testing (constraints)

- This method relies on the idea that two statistically independent variables are not causally linked.

# Outline of how these algorithms work!

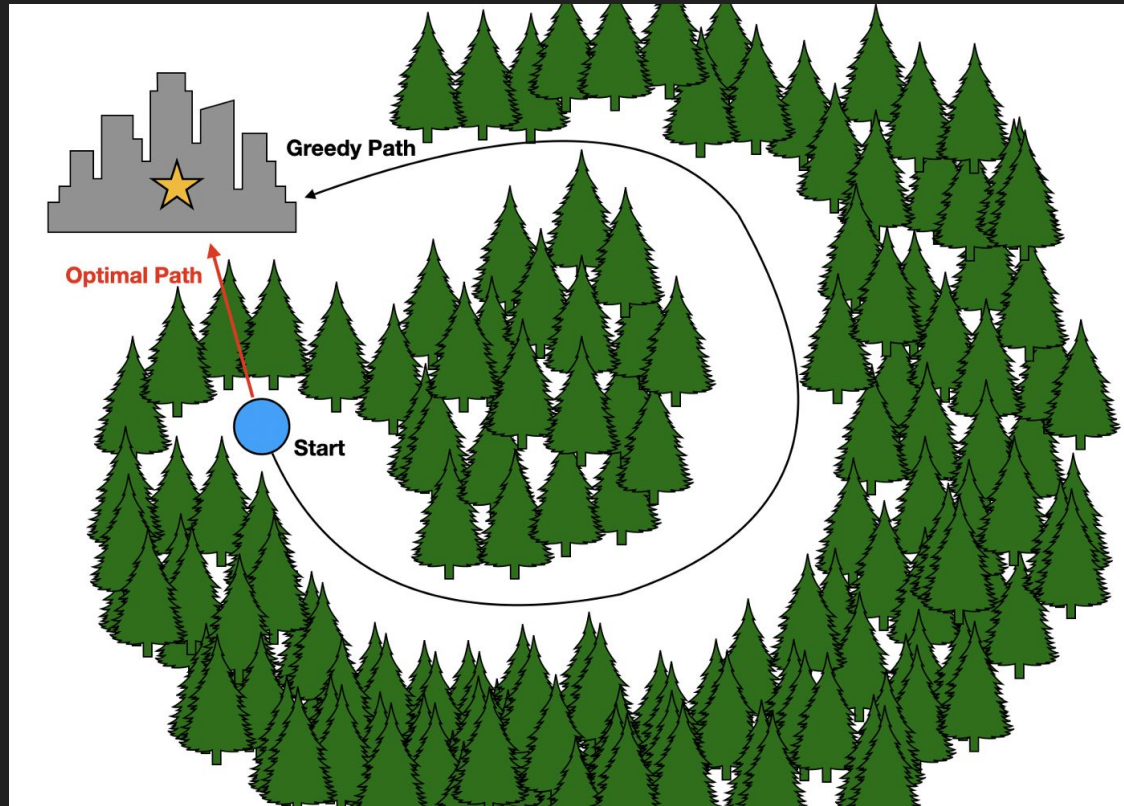


## Method 2: Greedy Search of Graph Space (score-based)

- There are three main elements to this method: a graph, a graph space, and a greedy search.
- A graph space is a collection of graphs. This is just a fancy way to formalize that there are many possible graphs for a given number of vertices and edges. For example, a DAG with 2 vertices and 1 edge could take the forms:  $A \rightarrow B$  or  $B \rightarrow A$ .
- Finally, a greedy search is a way to navigate a space such that you always move in a direction that seems most beneficial based on the local surroundings.



# Greedy Search



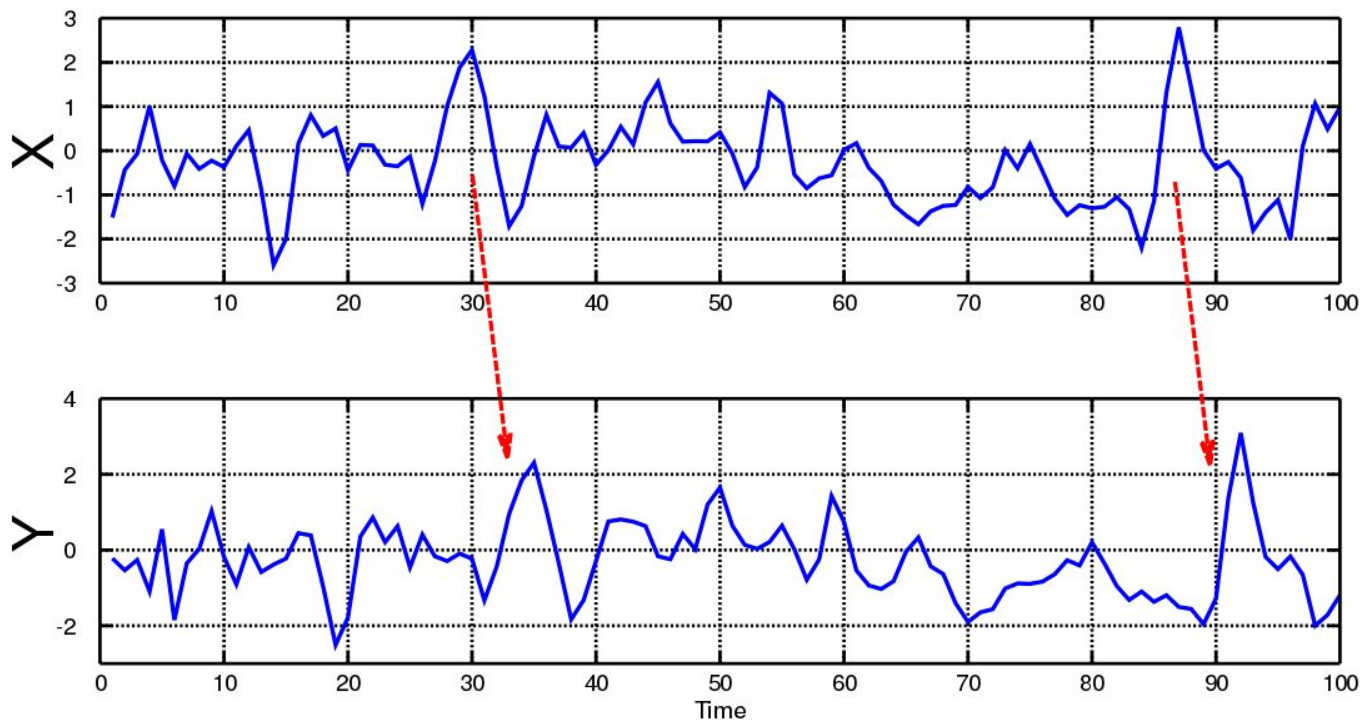
# Greedy Equivalence Search

- The Greedy Equivalence Search (GES) algorithm uses this trick. GES starts with an empty graph and iteratively adds directed edges such that the improvement in a model fitness measure (i.e. score) is maximized. An example score is the Bayesian Information Criterion (BIC).

## Method 3: Exploiting Asymmetries

- A fundamental property of causality is asymmetry. A could cause B, but B may not cause A. There is a large space of algorithms that leverage this idea to select between causal model candidates.
- One possible asymmetry is **time**. A cause must precede the effect!
- This sits at the core of **Granger causality**. Although Granger causality is not sufficient to claim causality, it leverages the idea that causes precede effects.
- It does this in the two variable case (e.g. X and Y), by quantifying the gain in predicting Y given past information of Y and X, as opposed to past information of Y alone.

# Example of Granger Causality



# Causal discovery for time series!

- Granger causality points at causal discovery for time series.
- This is highly relevant for environmental problems, and as such we will explore in more depth in code.