



Faculty of Technology and Environment

Prince of Songkla University Phuket Campus

No.....

Exam 1 Semester 2/64

Date 17 February 2022

Course code 976-120 and 977-120

Time 09:00 – 11:00 am

Course Title Mathematics

Lecturer Dr. Pariyaporn Roop-o

Student Name นางสาว อัญชลี ปิยะรัตน์

Student ID 6130613056

Instructions:

1. This exam consists of **4 printed pages** (include cover and formula of derivatives).
2. The maximum score of this exam is 44 which is **20%** of this course.
3. Absolutely no books are allowed during the examination **except the handouts of this course**.
4. Be sure to show all the steps necessary for the calculation. Correct answers without necessary work will receive only minimal point.
5. Submit as pdf or picture files and please name all files as student ID.

No.	Full score	Student's scores
1	16	
2	4	
3	4	
4	5	
5	4	
6	6	
7	5	
Total	44	

1. Use the given graph of  $f$  to state the value of each quantity, if it exists. (16 scores)

1)  $\lim_{x \rightarrow -2^-} f(x) = 3$

2)  $\lim_{x \rightarrow -2^+} f(x) = 3$

3)  $\lim_{x \rightarrow -2} f(x) = 3$

4)  $f(-2) = 5$

5)  $\lim_{x \rightarrow 0} f(x) = -2$

6)  $f(0) = -2$

7)  $\lim_{x \rightarrow 4^-} f(x) = \text{หาค่าไม่ได้}$

8)  $\lim_{x \rightarrow 4^+} f(x) = \text{หาค่าไม่ได้}$

9)  $\lim_{x \rightarrow 4} f(x) = \text{หาค่าไม่ได้}$

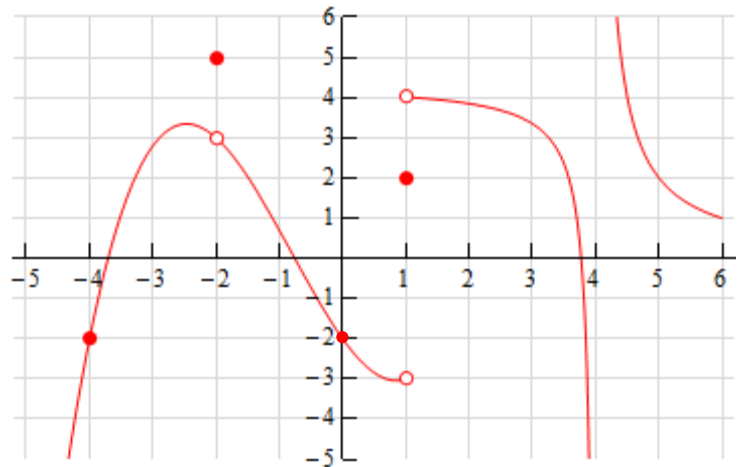
10) Domain of  $f$  is .....

11) Range of  $f$  is .....

12) The equation of the vertical asymptote is.....

13) Is  $f$  continuous at  $x = -2$ ? Why?

.....



2. Find the domain of  $f(x) = \frac{\sqrt{16-x^2}}{x-1}$ .

(4 scores)

3. Suppose  $\lim_{x \rightarrow 4} f(x) = 3$  and  $\lim_{x \rightarrow 4} g(x) = 6$ . Determine the following limits: (4 scores)

$$\begin{aligned} (a) \lim_{x \rightarrow 4} [f(x) + 2g(x)] &= \lim_{x \rightarrow 4} f(x) + \lim_{x \rightarrow 4} 2g(x) = 3 + 2(6) = 15 \\ (b) \lim_{x \rightarrow 4} 2[f(x)g(x)] &= 2 \cdot \lim_{x \rightarrow 4} f(x) \cdot \lim_{x \rightarrow 4} g(x) = 2(3)(6) = 36 \\ (c) \lim_{x \rightarrow 4} \frac{3f(x) - g(x)}{f(x) + g(x)} &= \frac{3(3) - 6}{3 + 6} = \frac{3}{9} = \frac{1}{3} \\ (d) \lim_{x \rightarrow 4} \sqrt{f(x) + 3g(x)} &= \sqrt{\lim_{x \rightarrow 4} f(x) + \lim_{x \rightarrow 4} 3g(x)} = \sqrt{3 + 3(6)} = \sqrt{21} \end{aligned}$$

4. Evaluate  $\lim_{x \rightarrow 0} \frac{\sin(5x)}{x^2 + 3x}$ . (Do not use L'Hopital's rule) (5 scores)

$$\begin{aligned} \lim_{x \rightarrow 0} \frac{\sin(5x)}{x^2 + 3x} &= \frac{1}{\lim_{x \rightarrow 0} \frac{x^2 + 3x}{\sin 5x}} \\ &= \frac{1}{\lim_{x \rightarrow 0} \frac{x^2}{\sin 5x} + 3 \lim_{x \rightarrow 0} \frac{x}{\sin 5x}} \\ &= \frac{1}{\frac{1}{\lim_{x \rightarrow 0} \frac{\sin 5x}{x^2}} + \frac{3}{\lim_{x \rightarrow 0} \frac{\sin 5x}{x}}} \\ &= \frac{1}{\frac{5}{\lim_{x \rightarrow 0} \frac{1}{x} \cdot \lim_{x \rightarrow 0} \frac{\sin 5x}{5}} + \frac{15}{\lim_{x \rightarrow 0} \frac{\sin 5x}{5x}}} \\ &= \frac{1}{\frac{5}{5} + 15} = \frac{1}{0 + 15} = \frac{1}{15} \end{aligned}$$

5. Evaluate  $\lim_{x \rightarrow -\infty} \frac{2x^3 - 5x + 9}{x^2 - 4x - 1}$ . (4 scores)

$$\begin{aligned} &= \lim_{x \rightarrow -\infty} \frac{x^3 (2 - \frac{5}{x^2} + \frac{9}{x^3})}{x^3 (\frac{1}{x} - \frac{4}{x^2} - \frac{1}{x^3})} \\ &= \lim_{x \rightarrow -\infty} \frac{(2 - \frac{5}{x^2} + \frac{9}{x^3})}{(\frac{1}{x} - \frac{4}{x^2} - \frac{1}{x^3})} \\ &= -\infty \end{aligned}$$

6. Evaluate  $\lim_{x \rightarrow \infty} \left( x - \sqrt{x^2 + 2x} \right)$ . (Do not use L'Hopital's rule) (6 scores)

$$\begin{aligned}
 &= \lim_{x \rightarrow \infty} x - \sqrt{x^2 + 2x} \cdot \frac{x + \sqrt{x^2 + 2x}}{x + \sqrt{x^2 + 2x}} \\
 &= \lim_{x \rightarrow \infty} \frac{x^2 - (x^2 + 2x)}{x + \sqrt{x^2 + 2x}} \\
 &= \lim_{x \rightarrow \infty} \frac{-2x}{x + \sqrt{x^2 + 2x}} \\
 &= \lim_{x \rightarrow \infty} \frac{-2}{1 + \sqrt{1 + \frac{2}{x}}} \\
 &= \frac{-2}{1 + \sqrt{1 + 0}} \\
 &= \frac{-2}{1 + 1} \\
 &= \frac{-2}{2} \\
 &= -1
 \end{aligned}$$

7. For what value of the constant  $k$  is the function  $f(x) = \begin{cases} \frac{x^2 - 5x + 6}{x - 2} & ; x \neq 2 \\ kx - 3 & ; x = 2 \end{cases}$

continuous on  $(-\infty, \infty)$

(5 scores)