Text As Data HW 1

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```
library(tidyverse)
library(quanteda)
library(quanteda.corpora)
library(quanteda.textstats)
library(quanteda.textplots)
```

Q1

```
speeches <- corpus_subset(data_corpus_inaugural, President == "Reagan")
tokenized <- tokens(speeches, remove_punct = TRUE)</pre>
```

(a)

```
TTR_calculator <- function(tokens_item) {
  corpused <- sapply(tokens_item, paste, collapse=" ") %>% corpus()
  corpus_info <- summary(corpused)
  corpus_info %>%
    mutate(TTR = Types / Tokens) %>%
    select(Text, TTR)
}
TTR_calculator(tokenized)
```

```
## Text TTR
## 1 1981-Reagan 0.3680099
## 2 1985-Reagan 0.3568643
```

(b)

```
reagan_dfm <- dfm(tokenized, tolower = FALSE)
textstat_simil(reagan_dfm, margin = "documents", method = "cosine")</pre>
```

```
## textstat_simil object; method = "cosine"
## 1981-Reagan 1985-Reagan
## 1981-Reagan 1.000 0.956
## 1985-Reagan 0.956 1.000
```

The cosine similarity between the two documents is 0.956.

$\mathbf{Q2}$

(a) I believe the TTR will decrease a little bit, but not much. This is because words with the same stems will now be grouped into the same types, while the number of tokens remains unchanged. The similarity between the two documents should also be relatively unaffected, because stemming the words simply groups more tokens together, and doesn't really create new words.

```
stemmed_token <- tokens_wordstem(tokenized)</pre>
TTR_calculator(stemmed_token)
##
            Text
                        TTR.
## 1 1981-Reagan 0.3322368
## 2 1985-Reagan 0.3178627
stemmed_dfm <- dfm(stemmed_token, tolower = FALSE)</pre>
textstat_simil(stemmed_dfm, margin = "documents", method = "cosine")
## textstat_simil object; method = "cosine"
##
                1981-Reagan 1985-Reagan
                      1.000
                                   0.957
## 1981-Reagan
## 1985-Reagan
                      0.957
                                   1.000
```

(b) I believe the TTR would increase drastically. This is because by removing the stop words, we are removing a large number of tokens (assuming Reagan speaks with lots of stop words like a normal person would) that are grouped into a few types. The similarity between the two documents should greatly decrease, because he likely used similar stop words in both of his speeches, and by removing these a major part of the similarities are discarded.

```
nostop_token <- tokens_remove(tokenized, pattern = stopwords("en"))</pre>
TTR_calculator(nostop_token)
##
            Text
                        TTR
## 1 1981-Reagan 0.6608544
## 2 1985-Reagan 0.6059908
nostop_dfm <- dfm(nostop_token, tolower = FALSE)</pre>
textstat_simil(nostop_dfm, margin = "documents", method = "cosine")
## textstat_simil object; method = "cosine"
               1981-Reagan 1985-Reagan
                      1.000
                                   0.668
## 1981-Reagan
## 1985-Reagan
                      0.668
                                   1.000
```

(c) I believe the TTR would decrease, but only very little. By converting all words to lowercase, the number of tokens remain unchanged, and the only words that are affected and grouped into the same type are likely just words that happen to be the start of sentences and certain proper nouns. The similarity between the two documents would also be largely unaffected, because the words are basically still the same, and in rare occasion a word after being lowercased becomes another word.

```
##
             Text
                         TTR.
## 1 1981-Reagan 0.3466283
## 2 1985-Reagan 0.3377535
lower_dfm <- dfm(lower_token, tolower = TRUE)</pre>
textstat_simil(lower_dfm, margin = "documents", method = "cosine")
## textstat_simil object; method = "cosine"
##
                1981-Reagan 1985-Reagan
## 1981-Reagan
                      1.000
                                    0.959
                                    1.000
## 1985-Reagan
                      0.959
 (d) I think tf-idf makes some sense, but might not be as useful given that our corpus only has two docu-
     ments. This means that every word Reagan used in both speeches would have a weight of zero, because
     idf = 0; while every word he used in one speech but not another has idf = 0.69. Therefore, the tf-idf
     is essentially solely dependent on the tf, and not the idf.
topfeatures(dfm_tfidf(reagan_dfm))
##
     weapons
                nuclear ourselves
                                       reduce
                                                      То
                                                             beyond
                                                                        means
                                                                                   price
##
     1.80618
                1.80618
                           1.50515
                                      1.50515
                                                 1.20412
                                                           1.20412
                                                                      1.20412
                                                                                 1.20412
##
     special
                  these
##
     1.20412
                1.20412
topfeatures(dfm_tfidf(stemmed_dfm))
##
    nuclear children
                                                          To maintain
                                                                          beyond
                           mean
                                 ourselv
                                              turn
##
    1.80618 1.50515
                       1.50515 1.50515
                                          1.50515
                                                     1.20412
                                                             1.20412
                                                                        1.20412
##
      price
             special
##
    1.20412
             1.20412
topfeatures(dfm_tfidf(nostop_dfm))
    weapons
             nuclear
                         reduce
                                  beyond
                                             means
                                                       price
##
    1.80618
             1.80618
                       1.50515
                                 1.20412
                                          1.20412
                                                     1.20412
                                                              1.20412
                                                                        1.20412
##
     better increase
    1.20412 1.20412
topfeatures(dfm_tfidf(lower_dfm))
##
     weapons
                nuclear ourselves
                                        union
                                                 reduce
                                                                                 special
                                                             means
                                                                        price
##
                           1.50515
                                                                                 1.20412
     1.80618
                1.80618
                                      1.50515
                                                 1.50515
                                                           1.20412
                                                                      1.20412
                 better
##
         ago
##
     1.20412
                1.20412
```

lower_token <- tokens_tolower(tokenized)</pre>

TTR_calculator(lower_token)

We can see that the terms "nuclear" and "weapons" have the highest weights, which suggest Reagan likely mentioned nuclear weapons many times in one speech and not at all in the other. Interestingly, when stemmed, "weapons" is no longer one of the top features. My guess is that he used "weapons" many times in one speech and mentioned "weapon" (but not "weapons") in the other speech, and once "weapons" is stemmed it becomes the same as "weapon" and received a weight of zero.

$\mathbf{Q3}$

In the preprocessing, I chose to remove punctuation and convert all words to lower case. This is because punctuation and capitalization in headlines often times simply reflects the style of editing, rather than provide any useful information.

(a) Euclidean Distance

```
sqrt(sum((head_dfm[1,] - head_dfm[2,])^2))
```

[1] 3

(b) Manhattan Distance

```
sum(abs(head_dfm[1,] - head_dfm[2,]))
```

[1] 9

(c) Cosine Similarity

```
product <- sum(head_dfm[1,] * head_dfm[2,])
norm_1 <- sqrt(sum(head_dfm[1,]^2))
norm_2 <- sqrt(sum(head_dfm[2,]^2))
product / (norm_1 * norm_2)</pre>
```

[1] 0.4780914

(d) Levenshtein Distance

The Levenshtein distance is 3. To go from robot to rover, we have to replace b with r, replace o with e, and replace t with r. That is a total of three operations.

$\mathbf{Q4}$

```
library(gutenbergr)
library(stylest)
set.seed(1984L)
```

```
(a)
author_list <- c("Poe, Edgar Allan", "Twain, Mark",</pre>
                 "Shelley, Mary Wollstonecraft", "Doyle, Arthur Conan")
book_list <- c(932,1064,1065,32037,74,76,86,91,84,6447,15238,18247,108,126,139,244)
prepare_dt <- function(book_list, num_lines, removePunct = TRUE){</pre>
     meta <- gutenberg_works(gutenberg_id == book_list)</pre>
     meta <- meta %>% mutate(author = unlist(str_split(author, ","))[1]
     %>% tolower(.))
     texts <- lapply(book_list, function(x) gutenberg_download(x,</pre>
     mirror="http://mirrors.xmission.com/gutenberg/") %>%
                        #select(text) %>%
                        sample n(500, replace=TRUE) %>%
                        unlist() %>%
                        paste(., collapse = " ") %>%
                        str_replace_all(., "^ +| +$|( ) +", "\\1"))
     # remove apostrophes
     texts <- lapply(texts, function(x) gsub("'', "", x))</pre>
     if(removePunct) texts <- lapply(texts, function(x)</pre>
     gsub("[^[:alpha:]]", " ", x))
     # remove all non-alpha characters
     output <- tibble(title = meta$title, author = meta$author, text =</pre>
     unlist(texts, recursive = FALSE))
texts_dt <- lapply(book_list, prepare_dt, num_lines = 500, removePunct = TRUE)
```

```
(b)
texts_dt <- do.call(rbind, texts_dt)
str(texts_dt)</pre>
```

```
## tibble [16 x 3] (S3: tbl_df/tbl/data.frame)
## $ title : chr [1:16] "The Fall of the House of Usher" "The Masque of the Red Death" "The Raven" "Eu
## $ author: chr [1:16] "poe" "poe" "poe" "poe" ...
## $ text : chr [1:16] "
```

(c)

```
stopwords_en <- stopwords("en")</pre>
filter <- corpus::text_filter(drop_punct = TRUE, drop_number = TRUE, drop = stopwords_en)
vocab_terms <- stylest_select_vocab(texts_dt$text, texts_dt$author,</pre>
                                     filter = filter, smooth = 1, nfold = 5,
                                     cutoff_pcts = c(25, 50, 75, 99))
vocab_terms$cutoff_pct_best
## [1] 75
vocab_terms$miss_pct
                      [,2]
                               [,3]
##
            [,1]
                                         [,4]
## [1,] 33.33333 33.33333 33.33333
## [2,] 33.3333 33.3333 0.00000 33.33333
## [3,] 25.00000 25.00000 25.00000 25.00000
## [4,] 50.00000 50.00000 50.00000 0.00000
## [5,] 25.00000 25.00000 25.00000 50.00000
(d)
vocab_subset <- stylest_terms(texts_dt$text, texts_dt$author,</pre>
                               vocab_terms$cutoff_pct_best , filter = filter)
style_model <- stylest_fit(texts_dt$text, texts_dt$author,</pre>
                            terms = vocab_subset, filter = filter)
authors <- unique(texts_dt$author)</pre>
term_usage <- style_model$rate</pre>
lapply(authors, function(x) head(term_usage[x,][order(-term_usage[x,])], 5)) %%
  setNames(authors)
```

```
## $poe
##
          upon
                       door
                                    one
                                             chamber
                                                              now
## 0.010938874 0.006981091 0.006871152 0.006761214 0.006431398
##
## $twain
##
                                    tom
                                                 got
## 0.024639678 0.013830013 0.008213226 0.008001272 0.007895295
##
##
   $shelley
##
                                    now
## 0.006079845 0.005326590 0.004788551 0.004465727 0.004142903
##
## $doyle
##
          said
                       upon
                                    one
                                                   s
                                                               us
## 0.010603680 0.010267056 0.008920557 0.006564183 0.005778725
```

It's hard for me to judge if these terms make sense or not, because I haven't read many of these selected books. However, I know that having the term "tom" in the top-5 for Mark Twain when we included the book *The Adventures of Tom Sawyer* and *Tom Sawyer Abroad* certainly makes sense.

(e)

```
test <- data.frame(term_usage) %>%
  filter(rownames(term_usage) %in% c('twain','doyle'))
rate_ratio <- term_usage['twain',] / term_usage['doyle',]
head(rate_ratio[order(-rate_ratio)], 5)</pre>
```

```
## says jim ain tom en
## 74.61297 72.72404 59.50148 48.79751 42.50106
```

I would interpret this ordering as "Mark Twain used the term 'says' 74 times more than Arthur Conan Doyle; this is the largest ratio for Twain over Doyle." and so on. We also see the terms 'jim' and 'tom', which make sense, because Jim is one of the main characters in *Adventures of Huckleberry Finn*, while Tom is the main character in the two Tom Sawyer books mentioned before.

(f)

```
mys_file <- "mystery_excerpt.rds"
mystery_excerpt <- readRDS(mys_file)
pred <- stylest_predict(style_model, mystery_excerpt)
pred$predicted</pre>
```

```
## [1] twain
## Levels: doyle poe shelley twain
```

Based on the prediction of the model, Mark Twain is the most likely author of this excerpt.

(g)

```
texts_tokens <- tokens(texts_dt$text) %>% setNames(texts_dt$title)

texts_lambda <- textstat_collocations(texts_tokens, min_count = 5) %>%
    arrange(desc(lambda))
head(texts_lambda, 10)
```

```
##
               collocation count count_nested length
                                                          lambda
                                                                         z
## 667
               edgar allan
                                7
                                              0
                                                      2 14.64330 7.202582
## 685
           denser perfumed
                                6
                                              0
                                                      2 14.50022 7.114569
## 686
           whispering vows
                                6
                                              0
                                                      2 14.50022 7.114569
## 709 syllable expressing
                                5
                                              0
                                                      2 14.33318 7.009050
## 548
          candelabrum amid
                                6
                                              0
                                                      2 13.40159 7.979787
## 549
             unseen censer
                                6
                                              0
                                                      2 13.40159 7.979787
## 524
                  allan poe
                                7
                                              0
                                                      2 13.03384 8.188891
## 557
         arabesque figures
                                5
                                              0
                                                      2 12.72371 7.918627
## 558
           densely crowded
                                5
                                              0
                                                      2 12.72371 7.918627
## 559
            unsuited limbs
                                5
                                                      2 12.72371 7.918627
```

```
texts_count <- textstat_collocations(texts_tokens, min_count = 5) %>%
  arrange(desc(count))
head(texts_count, 10)
##
        collocation count count nested length
                                                  lambda
## 1
                                             2 1.9096885 40.162016
             of the
                      692
                                      0
## 6
             in the
                      320
                                      0
                                             2 1.7353212 26.037857
## 1093
                      244
                                      0
                                             2 0.3679152 5.362239
            and the
## 175
                      228
                                      0
                                             2 0.8517698 11.743742
             to the
## 2
             it was
                      208
                                      0
                                             2 3.1108918 36.624131
## 18
                      130
                                      0
                                             2 2.1815977 19.780368
             on the
## 408
               of a
                                      0
                                             2 0.8819775 9.099416
                      120
                                      0
## 26
           from the
                      115
                                             2 1.9740319 17.432193
## 8
                                      0
                                             2 3.0204174 25.893505
              to be
                      112
## 1155
           that the
                      101
                                             2 0.5357825 5.071165
```

I don't think any of these sets of bi-grams are multi-word expressions. Most of the ones with a high lambda value are pairs of adverb-verbs or adjective-nouns. All of the ones with a high count are just conjunctions.

```
Q_5
library("sophistication")
data(data_corpus_ungd2017, package = "quanteda.corpora")
(a)
snippetData <- snippets_make(data_corpus_ungd2017, nsentence = 1, minchar = 150, maxchar = 350)</pre>
snippetData <- snippets_clean(snippetData)</pre>
head(snippetData, 10)
##
            docID snippetID
## 1 Afghanistan
                     100001
## 2 Afghanistan
                     100002
## 3
     Afghanistan
                     100003
## 4 Afghanistan
                     100009
## 5 Afghanistan
                     100011
## 6 Afghanistan
                     100012
## 7 Afghanistan
                     100015
## 8 Afghanistan
                     100016
      Afghanistan
                     100017
## 9
## 10 Afghanistan
                     100020
##
## 1
                                                          As I stand here before the General Assembly to
## 2
                                  Shaped by the Great Depression and tempered by the carnage of the Second
## 3
                     The United Nations, the International Monetary Fund, the World Bank and other orga
## 4
                                                                   There is an emerging consensus that ad
```

Driven by transnational terrorist networks, criminal organizations, cybercrime and State spon

Lastly, despite the incorporation of tenets of the Universal Declaration

Terrorism is not only an attack on human life and basic freedoms, but an attack on the compact of

Sixteen years after the tragedy of 11

We must confront the threat of

I welcome the chance for Af

5

6

7 ## 8

9

10

(b)

```
testData <- sample_n(snippetData, 1000)
snippetPairsMST <- pairs_regular_make(testData)
gold_questions <- pairs_gold_make(snippetPairsMST, n.pairs = 10)
print(gold_questions$text1)</pre>
```

[1] "Peacekeeping reform in particular requires a carefully tailored approach, without abrupt shift
[2] "If that endeavour is successful, we will be honoured to work even harder for the advancement o
[3] "Bulgaria categorically condemns the repeated nuclear tests and missile launches by the Democra
[4] "We contemplate how we can best find grand solutions, when all we really need is to translate to
[5] "Ghana will also continue to be active in the multilateral organizations to which we belong, su
[6] "For those who question the veracity of that science, the cluster of extreme weather events ove
[7] "Once again, Cameroon, as it did from this very rostrum on 10 September 2000, urges the world to
[8] "Eliminating radicalism and religious fundamentalism should also be a major priority for our St
[9] "Practical approaches could allow us to work through existing controversies in order to achieve
[10] "On behalf of the people and the Government of the Republic of Paraguay, I wish to express to to

print(gold_questions\$text2)

[1] "Others are economic migrants prepared to risk everything on perilous sea crossings in the desp
[2] "Above and beyond those urgent humanitarian actions, Monaco's cooperation system implements a p
[3] "Let me end by reciting a verse that is a synthesis of our thought: \"May all be happy; may all
[4] "Accordingly, this year has witnessed numerous initiatives for fruitful cooperation, notably th
[5] "We all want to be a part of the EU, but sometimes people in the Balkans and people in Serbia a
[6] "The Holy See therefore appreciates the Secretary-General's explicit and strong emphasis on pre
[7] "Protracted conflicts require a holistic United Nations response, encompassing preventive diplo
[8] "No country has the right to make the world an unsafe place to live in, and we owe it to our pe
[9] "We are also committed to supporting efforts to make the Council more transparent and promote to

[10] "We have disbursed \$500 million for the Syria crisis since 2016, which means that we are on tra

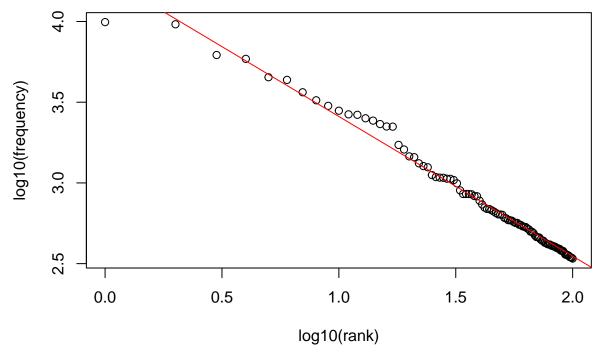
My selections (in order): 2 1 2 1 2 2 2 2 2

```
print(gold_questions$easier_gold)
```

[1] 2 1 2 1 2 1 1 2 2 2

I was in agreement with the automated classification in nine of the ten gold pairs; the lone disagreement occurred on pair number 6. The difference in judgement likely comes from the fact that text 2 in pair 6 used some proper nouns and was also a longer text, so the classification treated it as harder to read, but I felt like some vocabularies in text 1 in pair 6 was slightly harder to interpret its true meaning.

Top 100 Words in Little Women & The Great Gatsby



The only preprocessing decision I made is to remove punctuation. I chose not to remove stopwords because I believe stopwords have a smaller impact on texts such as novels, compared to texts such as speeches. Many of the unnecessary stopwords are likely removed in the editing process.

$\mathbf{Q7}$

```
num_tokens <- sum(lengths(little_women), lengths(great_gatsby))
M <- nfeat(combined_dfm)
k <- 44
b <- 0.4645909
k * (num_tokens)^b

## [1] 13758

M

## [1] 0.4645909</pre>
```

No additional preprocessing were done for this question.

```
head(kwic(little women, pattern = "poor*"))
## Keyword-in-context with 6 matches.
      [text74, 6]
##
                  It's so dreadful to be | poor | sighed Meg looking down at
##
     [text188, 1]
                                          | Poor | Jo It's too bad but
     [text575, 5] Goodness only knows Some | poor | creeter came a-beggin and your
##
                     away from here lies a | poor | woman with a little newborn
##
     [text639, 8]
## [text649, 11] carry the things to the | poor | little children asked
     [text666, 2]
                                         A | poor | bare miserable room it was
head(kwic(great_gatsby, pattern = "poor*"))
## Keyword-in-context with 6 matches.
##
      [text700, 6] It's a libel I'm too | poor |
##
     [text1848, 5]
                       Well if you're a | poor | driver you oughtn't to try
     [text1947, 8] and felt it in others | poor | young clerks who
##
##
     [text3277, 1]
                                         | poor | get children In the meantime
## [text4315, 13] he had just got some | poor |
                          because I was | poor | and she was tired of
     [text4574, 4]
head(kwic(little_women, pattern = "rich*", window = 4))
## Keyword-in-context with 6 matches.
      [text132, 5]
##
                         father if he isn't | rich | and insult you when
##
     [text724, 12]
                        the theater and not | rich | enough to
     [text875, 10]
##
                         because he is not | rich | They shout and
##
    [text1583, 10] nursery governess and felt | rich | with her
                                         how | rich | she was in the
##
     [text1597, 2]
##
     [text1603, 9]
                     being remembered in the | rich | old lady's will but
head(kwic(great_gatsby, pattern = "rich*", window = 4))
## Keyword-in-context with 6 matches.
                   played polo and were | rich | together This was a
##
      [text192, 7]
##
      [text713, 1]
                                           | rich | nevertheless I was confused
##
    [text2131, 11]
                              it It was a | rich | cream colour bright
##
     [text2630, 2]
                                       and | rich | and wild but she
##
     [text3162, 1]
                                          | rich | heap mounted higher shirts
     [text3276, 8] and nothing's surer The | rich | get richer and the
##
head(kwic(little_women, pattern = "wealth*", window = 4))
## Keyword-in-context with 6 matches.
      [text879, 8] that she bequeaths untold | wealth | to the young pair
## [text4390, 10] ancient name and boundless | wealth | in return for
##
   [text7983, 2]
                                      talent | wealth | or beauty And Amy
## [text11549, 1]
                                              | Wealth | is certainly a most
## [text12663, 4]
                                or women of | wealth | and position we might
## [text18993, 3]
                                  the better | wealth | of love confidence and
```

```
head(kwic(great_gatsby, pattern = "wealth*", window = 3))
## Keyword-in-context with 4 matches.
##
      [text183, 6] family were enormously | wealthy | even in college
##
      [text188, 1]
                                           | wealthy | enough to do
                              son of some | wealthy | people in the
##
    [text2163, 11]
     [text5272, 3]
                             mystery that | wealth | imprisons and preserves
head(kwic(little_women, pattern = "money*", window = 4))
## Keyword-in-context with 6 matches.
##
      [text93, 5]
                      ought not to spend | money | for pleasure when our
##
     [text110, 7] say anything about our | money | and she won't wish
##
    [text141, 13]
                         wish we had the | money |
                          spite of their | money |
##
     [text147, 4]
##
     [text618, 4]
                             gave all my | money | to get it and
     [text881, 8] several quarts of tin | money | shower down upon the
##
head(kwic(great_gatsby, pattern = "money*", window = 4))
## Keyword-in-context with 6 matches.
##
     [text132, 11]
                            and gold like new | money | from the mint
##
      [text184, 3]
                                 freedom with | money | was a matter for
##
      [text927, 9] Tom decisively Here's your | money | Go and buy
##
    [text1017, 13]
                             they think of is | money | I
                                where all his | money | comes from
##
     [text1086, 4]
##
     [text1382, 2]
                                          easy | money | in the vicinity and
```

Based on the Key Words in Context chosen, it seems like *Little Women* discusses the concept of poverty in a more positive way, while *The Great Gatsby* promotes the ideas of being rich and wealthy. It seems like perhaps the two books regard the topic of class from different perspectives, and therefore have different conclusions.

$\mathbf{Q9}$

```
data("data_corpus_ukmanifestos")
manifestos <- corpus_subset(data_corpus_ukmanifestos, Party == "Con")
sent_tokens <- unlist(tokens(manifestos, what = "sentence", include_docvars = TRUE))
yearnames <- list(unlist(names(sent_tokens)))
yearnames <- lapply(yearnames[[1]], function(x){strsplit(x, "_")[[1]][3]})
yearslist <- unlist(yearnames)
years <- unique(yearslist)
sentences_df <- tibble(text = sent_tokens, year = yearslist)
sentences_df <- sentences_df[grepl(("[\\.\?\\!]$"), sentences_df$text),]
sent_corp <- corpus(sentences_df$text)
docvars(sent_corp, field = "Year") <- sentences_df$year</pre>
```

(a)

```
library(pbapply)
iters <- 10
boot flesch <- function(grouping){</pre>
 N <- nrow(grouping)</pre>
  bootstrap_sample <- corpus_sample(corpus(c(grouping$text)), size = N, replace = TRUE)
  bootstrap_sample<- as.data.frame(as.matrix(bootstrap_sample))</pre>
  readability_results <- textstat_readability(bootstrap_sample$V1, measure = "Flesch")</pre>
  return(mean(readability_results$Flesch))
boot_flesch_year <- pblapply(years, function(x){</pre>
  sub_data <- sentences_df %>% filter(year == x)
  output_flesch <- lapply(1:iters, function(i) boot_flesch(sub_data))</pre>
 return(unlist(output flesch))})
year_means <- lapply(boot_flesch_year, mean) %>% unname() %>% unlist()
year_ses <- lapply(boot_flesch_year, sd) %>% unname() %>% unlist()
estimates <- data.frame(year = years,</pre>
                         mean = round(year_means, 2),
                         ses = round(year ses, 2))
estimates
```

```
##
     year mean ses
## 1 1945 49.22 1.61
## 2 1950 43.76 1.19
## 3 1951 52.36 2.28
## 4 1955 49.15 1.17
## 5 1959 49.33 0.98
## 6 1964 45.80 1.67
## 7 1966 46.06 1.47
## 8 1970 45.72 1.12
## 9 1974 42.12 0.43
## 10 1979 47.44 0.40
## 11 1983 47.23 0.85
## 12 1987 46.91 0.62
## 13 1992 46.10 0.60
## 14 1997 50.10 0.69
## 15 2001 48.91 0.94
## 16 2005 49.57 1.17
```

(b)

```
##
     year mean.boot mean.noboot diff
## 1
     1945
              49.22
                          48.97 0.25
## 2
     1950
              43.76
                           43.90 -0.14
## 3 1951
              52.36
                           52.01 0.35
## 4
     1955
              49.15
                           49.09 0.06
## 5
                          48.43 0.90
     1959
              49.33
## 6
     1964
              45.80
                           45.78 0.02
              46.06
                          46.27 -0.21
## 7 1966
## 8 1970
                           46.09 -0.37
              45.72
## 9
     1974
              42.12
                           42.31 -0.19
## 10 1979
              47.44
                           47.48 -0.04
                           47.68 -0.45
## 11 1983
              47.23
## 12 1987
              46.91
                           46.67 0.24
## 13 1992
                           46.40 -0.30
              46.10
## 14 1997
              50.10
                           49.91 0.19
## 15 2001
              48.91
                           48.09 0.82
## 16 2005
                           49.48 0.09
               49.57
```

It seems like the difference in mean FRE scores over time with and without bootstrapping estimation is rather similar. I suppose this suggests that the bootstrapping estimate is doing a good job in predicting the FRE scores.