$$\omega_x = \dot{\phi} \sin \theta \sin \psi + \dot{\theta} \cos \psi$$
$$\omega_y = \dot{\phi} \sin \theta \cos \psi - \dot{\theta} \sin \psi$$

 $\omega_z = \dot{\phi}\cos\theta + \dot{\psi}$