

# Minimal L<sup>A</sup>T<sub>E</sub>Xexample

Eugen Croitoru

April 28, 2020

## 1 Introduction

### 1.1 Motivation

## 2 Method

We'll probably use Rastrigin's Function[2]:

$$f(x) = A \cdot n + \sum_{i=1}^n [x_i^2 - A \cdot \cos(2\pi x_i)], A = 10, x_i \in [-5.12, 5.15]$$

## 3 Experiments

Some of the experiments we have tried as part of the optimization problem.

### 1. Genetic algorithm

#### (a) Low crossover probability:

- crossover probability: 0.1
- bit mutation probability: 0.01
- chromosome mutation probability: 0.1
- selection: roulette

#### (b) High crossover probability:

- crossover probability: 0.6
- bit mutation probability: 0.01
- chromosome mutation probability: 0.1
- selection: roulette

### 2. Hill Climbing

#### (a) best selection

#### (b) first selection

### 3. Hybrid Hill Climbing

#### (a) 1a with 2a

## 4 Results

### 4.1 Griewangk

Experiment	Min	Max	Mean
1a	11.26	28.92	17.30
1b	12.33	29.62	19.89
2a	2.56-09	2.56-09	2.56-09
2b	0.03	2.56-09	0.40
3a	0.001	2.56-09	0.04

Figure 1: minimum, maximum and the mean values for each experiment

#### 4.1.1 Genetic Algorithm

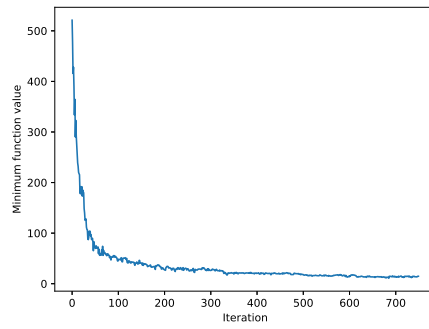


Figure 2: Function value

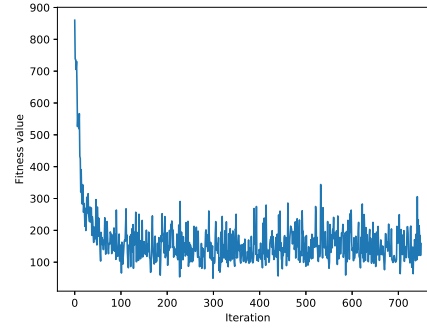


Figure 3: Fitness value

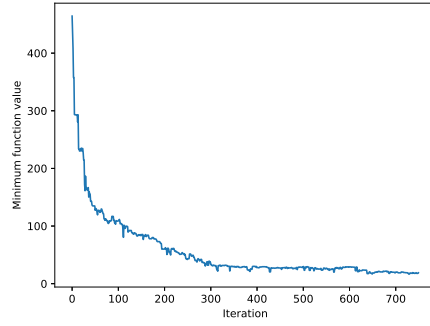


Figure 4: Function value

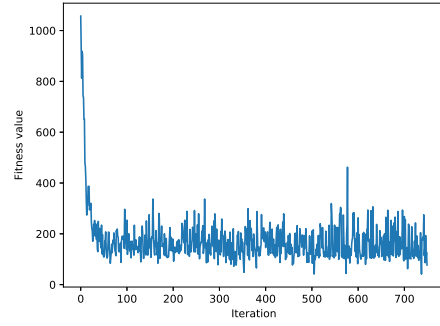


Figure 5: Fitness value

#### 4.1.2 Hill Climbing

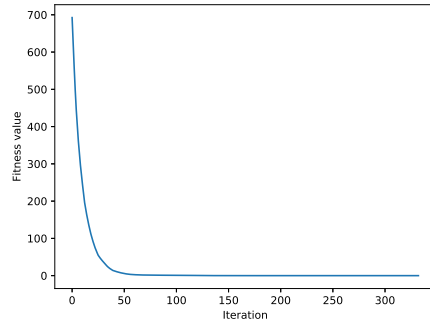


Figure 6: Best improvement

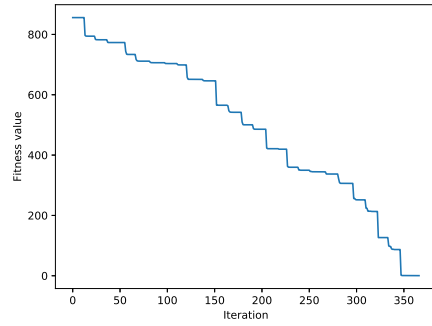


Figure 7: First improvement

#### 4.1.3 Hybrid

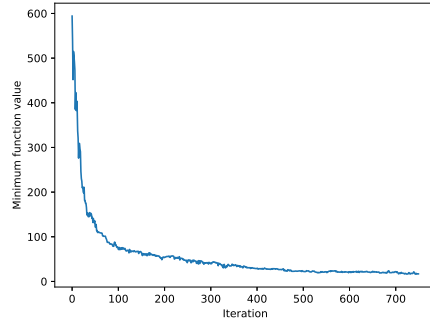


Figure 8: Genetic algorithm

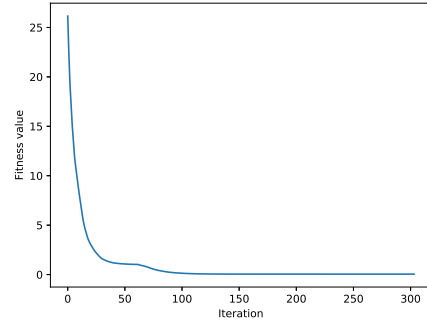


Figure 9: Hill Climbing

#### 4.1.4 Interpretation

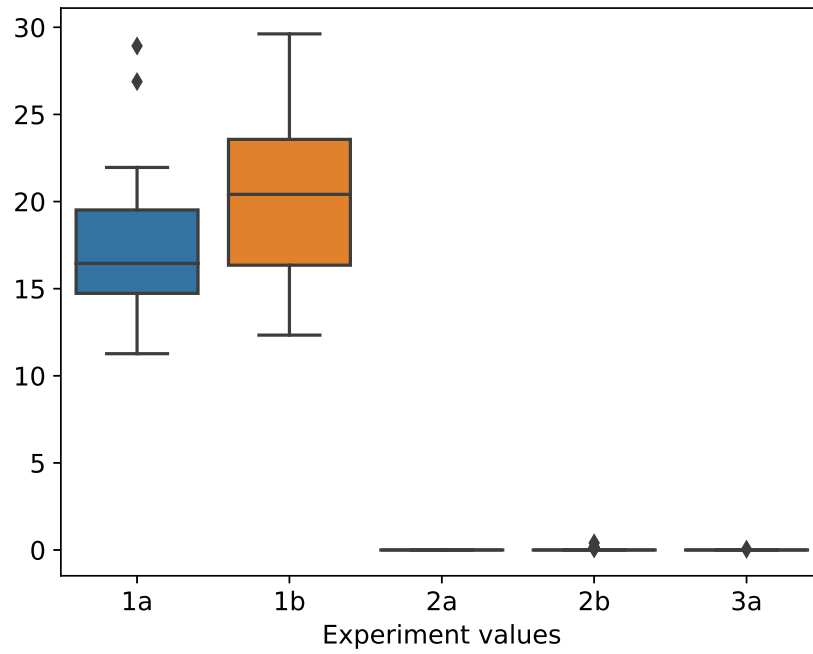


Figure 10: Griewangk experiments boxplot

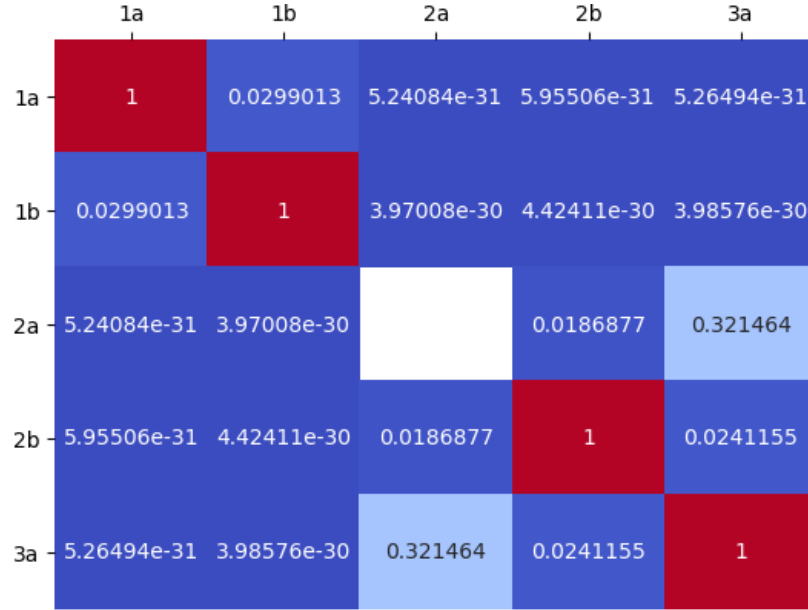


Figure 11: Griewangk experiments t test matrix

**Observations** We can observe in Fig. 10 that the experiments 1a and 1b have the worst results but we can't really say which of the other three is the best. The t test does not give a significant p value to affirm that the experiments means differ.

## 4.2 Rastrigin

Experiment	Min	Max	Mean
1a	44.09	85.05	64.57
1b	50.77	107.90	76.33
2a	26.78	59.28	44.77
2b	50.97	76.22	57.91
3a	24.30	39.43	32.16

Figure 12: minimum, maximum and the mean values for each experiment

### 4.2.1 Genetic Algorithm

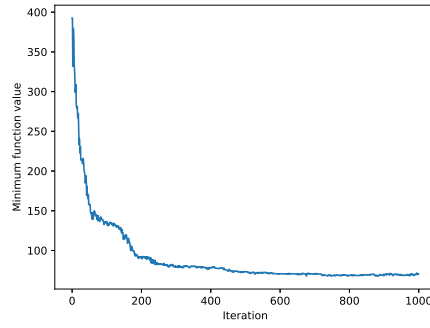


Figure 13: Function value

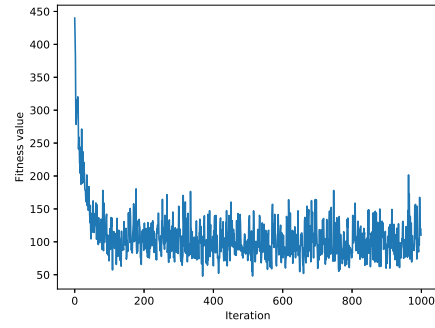


Figure 14: Fitness value

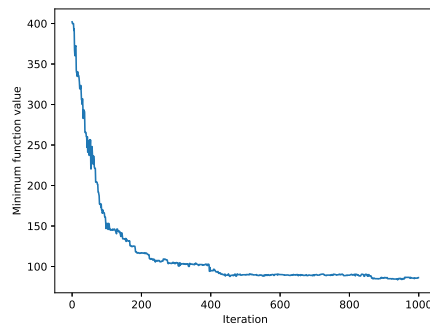


Figure 15: Function value

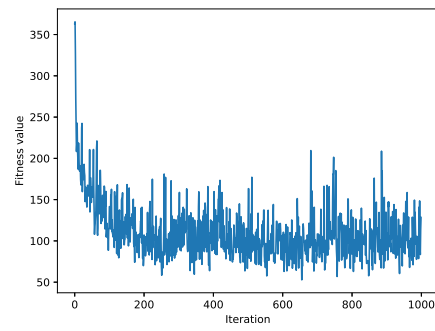


Figure 16: Fitness value

#### 4.2.2 Hill Climbing

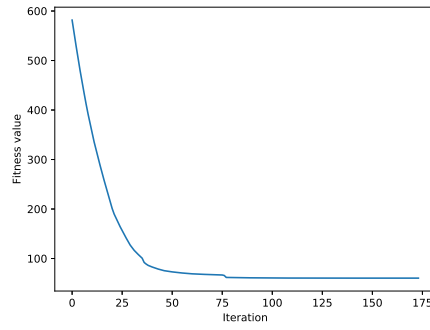


Figure 17: Best improvement

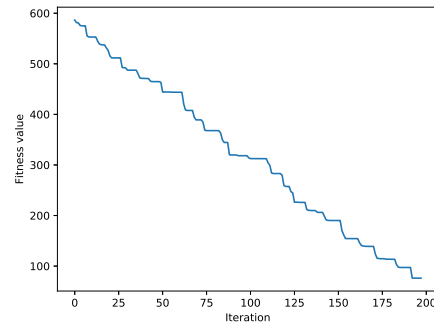


Figure 18: First improvement

### 4.2.3 Hybrid

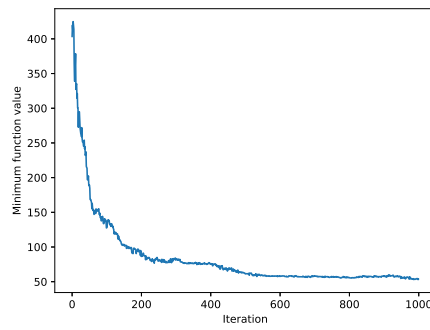


Figure 19: Genetic algorithm

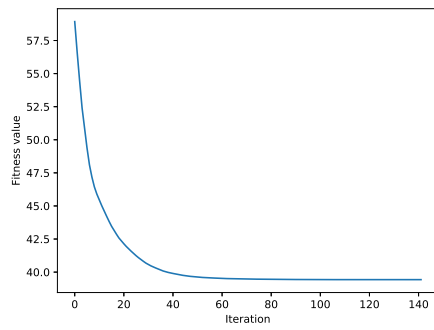


Figure 20: Hill Climbing

### 4.2.4 Interpretation

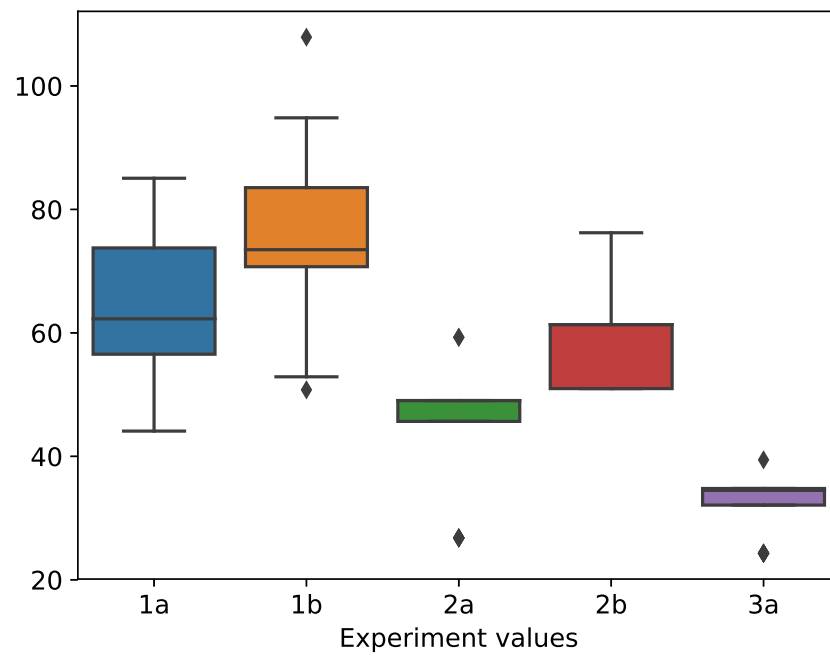


Figure 21: Rastrigin experiments boxplot



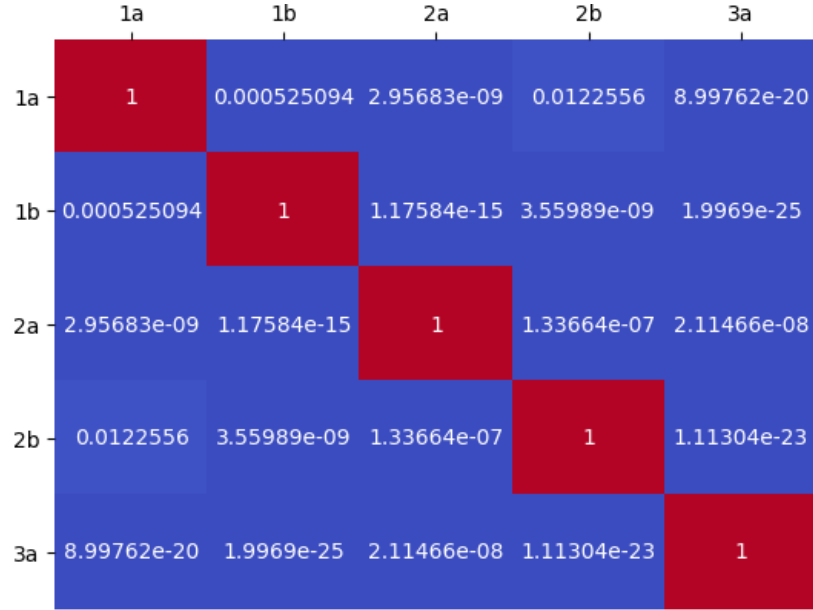


Figure 22: Rastrigin experiments t test matrix

**Observations** We can observe in Fig. 21 that the experiment 3a goes to the best minimum value. This conclusion is also verified using t test. We can see that in Fig. 22 which shows the p value between experiments.

### 4.3 Rosenbrock

Experiment	Min	Max	Mean
1a	154.07	398.18	253.27
1b	109.52	382.73	272.65
2a	28.13	122.93	37.68
2b	25.25	132.46	33.21
3a	23.09	136.88	26.88

Figure 23: minimum, maximum and the mean values for each experiment

#### 4.3.1 Genetic Algorithm

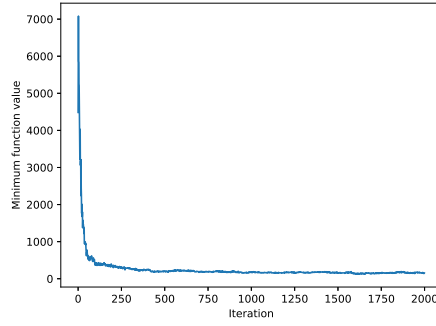


Figure 24: Function value

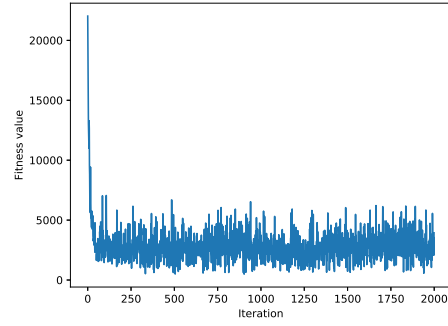


Figure 25: Fitness value

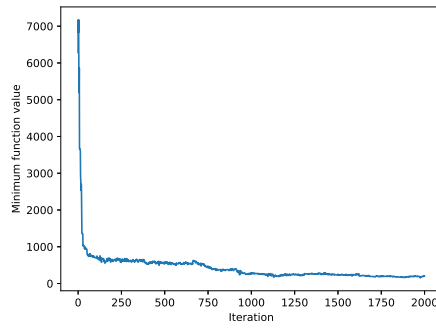


Figure 26: Function value

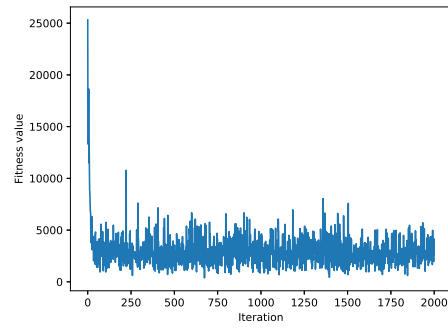


Figure 27: Fitness value

### 4.3.2 Hill Climbing

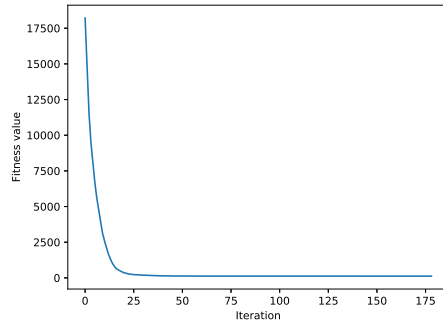


Figure 28: Best improvement

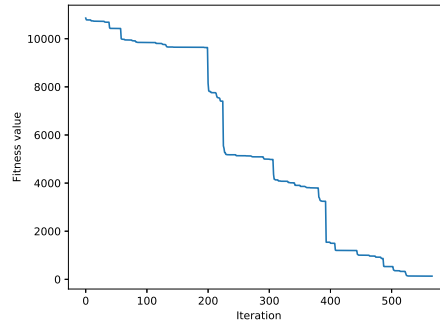


Figure 29: First improvement

### 4.3.3 Hybrid

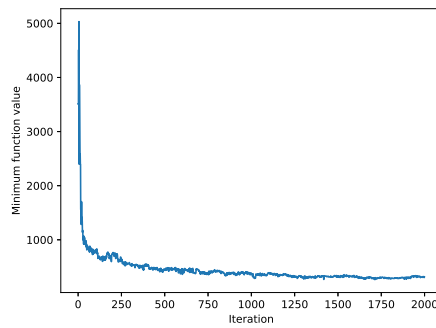


Figure 30: Genetic algorithm

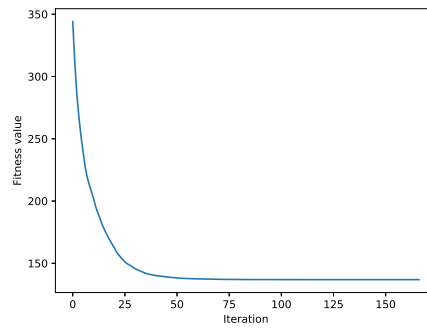


Figure 31: Hill Climbing

### 4.3.4 Interpretation

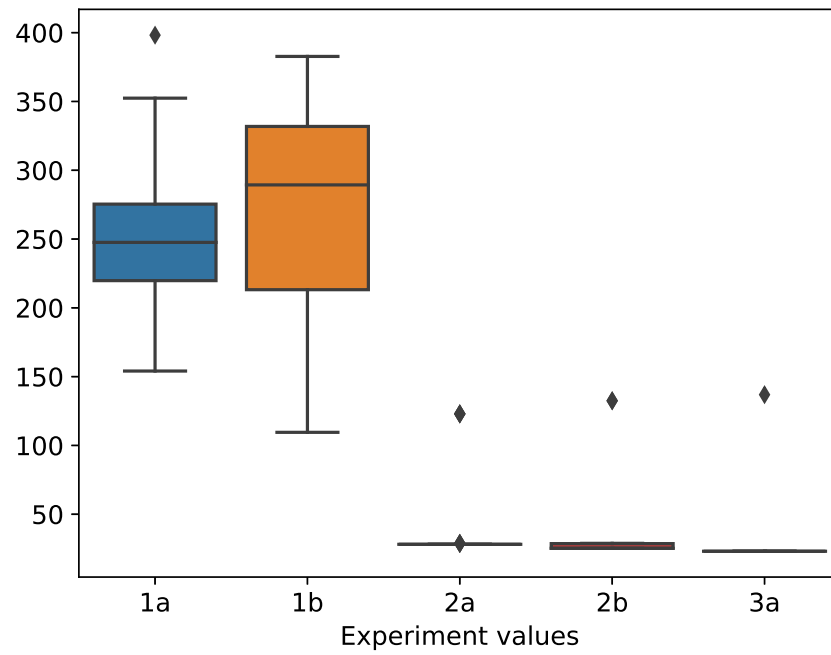


Figure 32: Rosenbrock experiments boxplot

	1a	1b	2a	2b	3a
1a	1	0.240323	3.8189e-27	6.45136e-28	1.59379e-29
1b	0.240323	1	1.05867e-23	2.77928e-24	2.17933e-25
2a	3.8189e-27	1.05867e-23	1	0.53855	0.101892
2b	6.45136e-28	2.77928e-24	0.53855	1	0.313074
3a	1.59379e-29	2.17933e-25	0.101892	0.313074	1

Figure 33: Rosenbrock experiments t test matrix

Observations //TODO:

## 5 Conclusions

## References

- [1] Wikipedia Commons  
Rastrigin's Function rendered image. [https://commons.wikimedia.org/wiki/Main\\_Page](https://commons.wikimedia.org/wiki/Main_Page)
- [2] Rastrigin, L. A. "Systems of extremal control." Mir, Moscow (1974).