Homework 2.1 10 points. End term: 8-th week (19-25 november 2020)

- 1. Devise an implementation (C, C++, C#, Java) for the Two Phase Algorithm (reusing the Simplex Algorithm code).
 - 2. Run the Two Phase implemented algorithm on the following problems:

(a)
$$\begin{cases} \min & z = -x_1 \\ \text{s. t.} & x_1 + x_2 \ge 6 \\ & 2x_1 + 3x_2 \le 4 \\ & x_1, x_2 \ge 0 \end{cases}$$
 (b)
$$\begin{cases} \min & z = x_1 + x_2 \\ \text{s. t.} & 2x_1 + x_2 + x_3 = 4 \\ & x_1 + x_2 + 2x_3 = 2 \\ & x_1, x_2, x_3 \ge 0 \end{cases}$$

(c)
$$\begin{cases} \min & z = -3x_1 + x_2 + 3x_3 - x_4 \\ \text{s. t.} & x_1 + 2x_2 - x_3 + x_4 = 0 \\ 2x_1 - 2x_2 + 3x_3 + 3x_4 = 9 \\ x_1 - x_2 + 2x_3 - x_4 = 6 \\ x_1, x_2, x_3, x_4 \geqslant 0 \end{cases}$$
4.
$$\begin{cases} \min & z = x_1 + 2x_2 \\ \text{s. t.} & x_1 + x_2 = 2 \\ 2x_1 + 2x_2 = 4 \\ x_1, x_2 \geqslant 0 \end{cases}$$

2 points bonus. Modify your Simplex algorithm in order to detect (if exists) at least an alternative optimal solutions (if any).