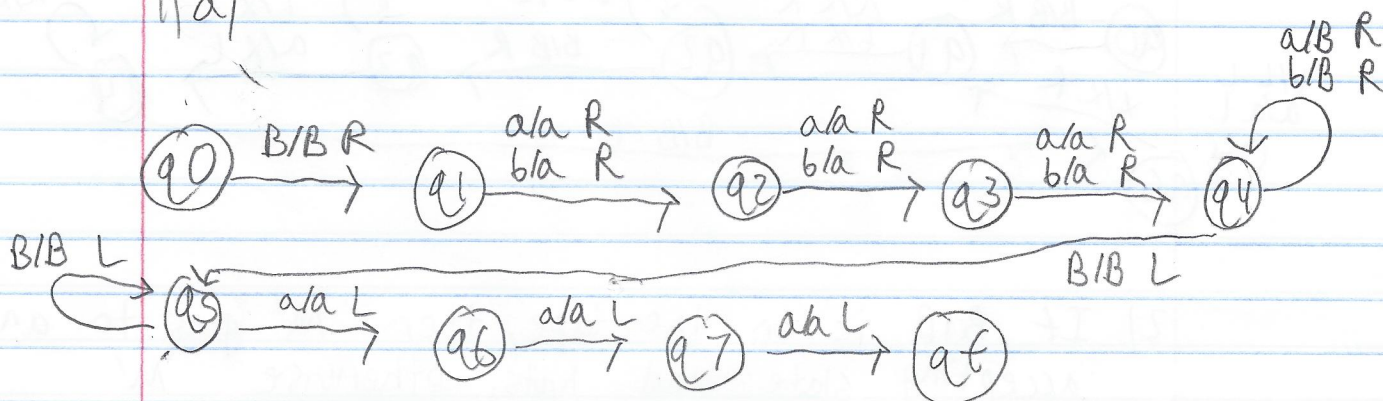
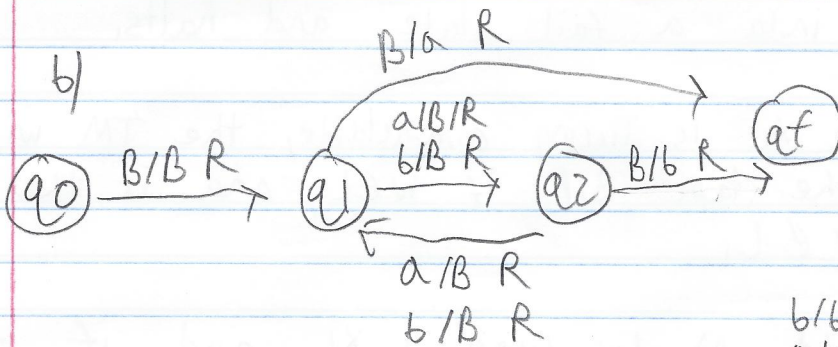


Chapter 9

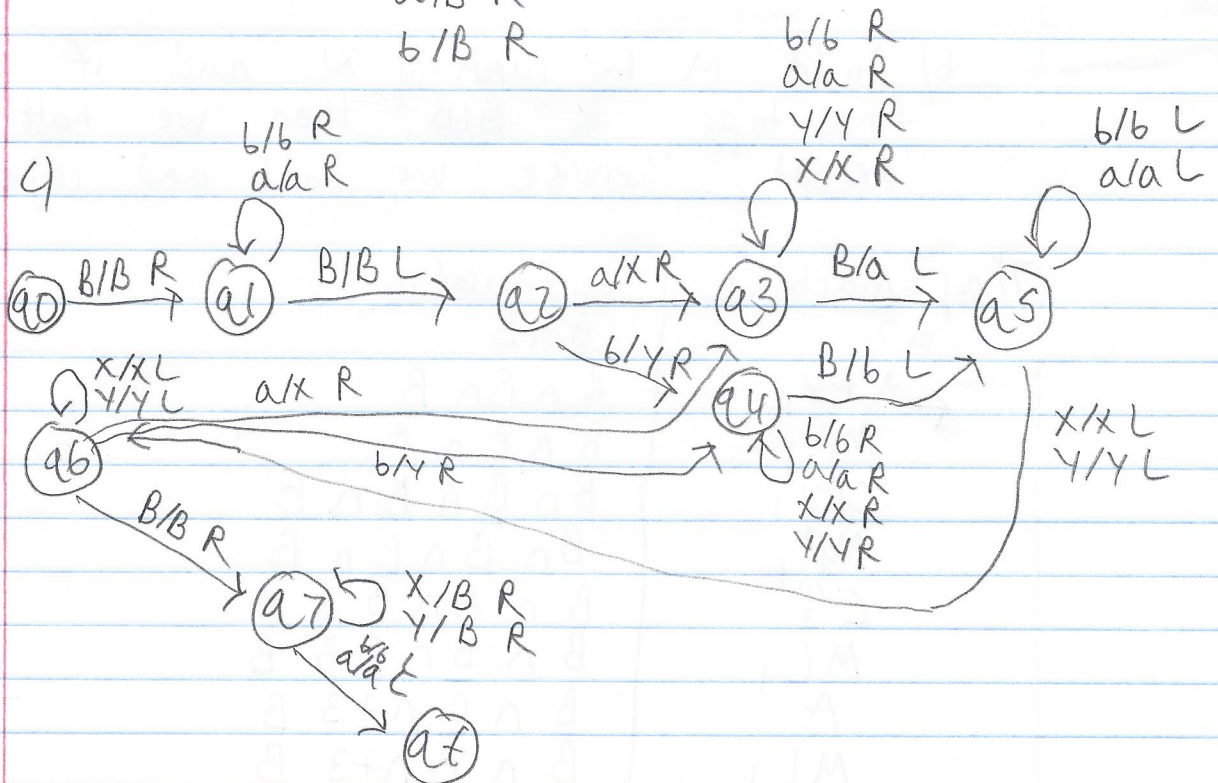
1/a)

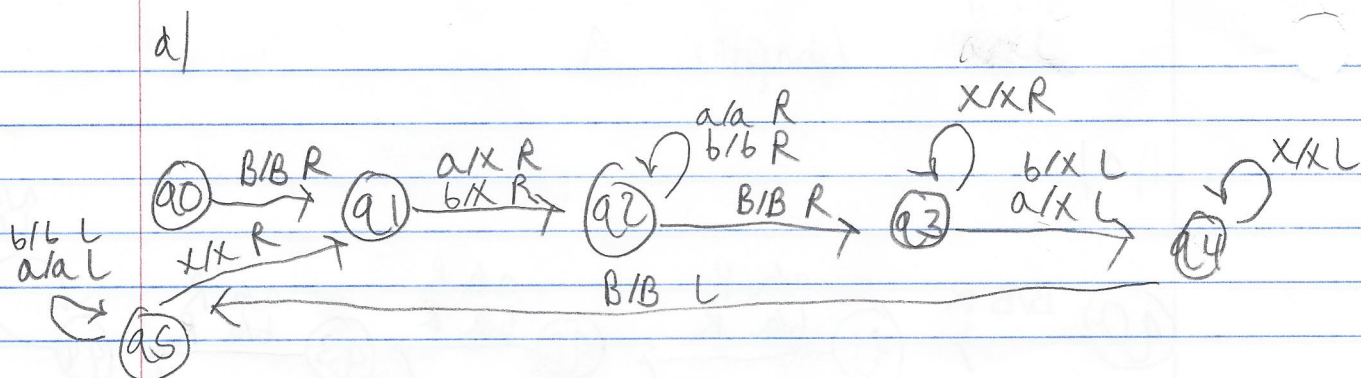


b)



c)





2) If B/B is on the tape, then M' goes to an accepting state and halts, otherwise M' goes into a fail state and halts.

4) a) Since X_L is Turing computable, the TM will halt with the tape B/B if $w \in L$, and if the tape is B/B $w \notin L$.

b) Build M by running X_L and if the final tape is B/B then we halt and accept, otherwise we halt and reject.

Machine	Configuration
	<u>B</u> n B
CPY ₁	B n B n B
MR ₁	B n <u>B</u> n B
CPY ₁	B n <u>B</u> n B n B
MR ₁	B n <u>B</u> n <u>B</u> n B
C ₃ ⁽¹⁾	B n B n <u>B</u> 3 B
ML ₁	B n <u>B</u> n B 3 B
A	B n <u>B</u> n+3 B
ML ₁	B n B n+3 B
A	<u>B</u> 2n+3 B



$$\begin{aligned}
 1b) \quad a) &= \text{add}(\text{mult}(\text{id}(n), \text{id}(n)), \text{add}(\text{id}(n), \text{id}(n))) \\
 &= \text{add}(\text{mult}(n, n), \text{add}(n, n)) \\
 &= \text{add}(n \cdot n, n + n) \\
 &= n^2 + 2n
 \end{aligned}$$

$$\begin{aligned}
 b) \quad & p_1^{(2)} \circ (\text{sop}_{p_1}^{(2)}, \text{eop}_2^{(2)}) (a, b) \\
 & p_1^{(2)} \circ (\text{sop}_{p_1}^{(2)}(a, b), \text{eop}_2^{(2)}(a, b)) \\
 & p_1^{(2)} \circ (\text{soa}, \text{eob}) \\
 & p_1^{(2)} \circ (a + 1, e(b)) \\
 & \quad \quad \quad a + 1
 \end{aligned}$$

$$\begin{aligned}
 c) \quad & \text{mult} \circ (c_2^{(3)}, \text{add} \circ (p_1^{(3)}, \text{sop}_2^{(3)})) (a, b, c) \\
 & \text{mult} \circ (c_2^{(3)}(a, b, c), \text{add} \circ (p_1^{(3)}, \text{sop}_2^{(3)})(a, b, c)) \\
 & \text{mult} \circ (2, \text{add} \circ (p_1^{(3)}(a, b, c), \text{sop}_2^{(3)}(a, b, c))) \\
 & \text{mult} \circ (2, \text{add} \circ (a, \text{so } b)) \\
 & \text{mult} \circ (2, \text{add} \circ (a, s(b))) \\
 & \text{mult} \circ (2, a + s(b)) \\
 & \quad \quad \quad 2 * (a + b + 1)
 \end{aligned}$$

$$\begin{aligned}
 d) \quad & \text{mult} \circ (\text{mult} \circ (p_1^{(1)}, p_1^{(1)}), p_1^{(1)}) (a) \\
 & \text{mult} \circ (\text{mult} \circ (p_1^{(1)}, p_1^{(1)})(a), p_1^{(1)}(a)) \\
 & \text{mult} \circ (\text{mult} \circ (p_1^{(1)}(a), p_1^{(1)}(a)), p_1^{(1)}(a)) \\
 & \text{mult} \circ (\text{mult} \circ (a, a), a) \\
 & \text{mult} \circ (a^2, a) \\
 & \quad \quad \quad a^3
 \end{aligned}$$