

$S_1$  = How can I be a geologist?

$S_2$  = What should I do to be a geologist?

Word vector space: [HOW, CAN, I, BE, A, GEOLOGIST, WHAT, SHOULD, DO, TO]

To convert, we put a '1' every where the word occurs, and a '0' if the word does not occur.

Therefore, for  $S_1$

HOW	1
CAN	1
I	1
BE	1
A	1
GEOLOGIST	1
WHAT	0
SHOULD	0
DO	0
TO	0

$S_1$ : [1, 1, 1, 1, 1, 1, 0, 0, 0, 0]

For,  $S_2$

HOW	0
CAN	0
I	1
BE	1
A	1
GEOLOGIST	1
WHAT	1
SHOULD	1
DO	1
TO	1

$S_2$ : [0, 0, 1, 1, 1, 1, 1, 1, 1, 1]

$$S_1 \cdot S_2 = |S_1||S_2|\cos\theta$$

So,  $\cos\theta$  (which is our cosine similarity) =  $(S_1 \cdot S_2) / (|S_1||S_2|)$

$$S_1 \cdot S_2 = 4$$

$$|S_1| = \sqrt{(1^2 + 1^2 + 1^2 + 1^2 + 1^2 + 1^2 + 0^2 + 0^2 + 0^2 + 0^2)} \cong 2.44949$$

$$|S_2| = \sqrt{(0^2 + 0^2 + 1^2 + 1^2 + 1^2 + 1^2 + 1^2 + 1^2 + 1^2 + 1^2)} \cong 2.82843$$

$$\cos\theta = 4 / (2.44949 * 2.82843) \cong 0.5773496$$

So, our cosine similarity between these two sentence vectors is **0.5773496**.

(recall:

- if the cosine similarity is '0', it means they bear no similarity;
- if the cosine similarity is '1', it means they are exactly similar – or the same even)