Due: Wednesday, 11 May

## Homework #6

1. Show that if S has a primitive recursive <u>acceptor</u> then S has a primitive recursive recognizer.

Show that if S has an exponential time <u>acceptor</u> then S has an exponential time recognizer.

Give an example of a class which has acceptors, but does not have recognizers.

2. Do Ex 8.1 from Hard Problem Notes.

Hamiltonian Circuit ≤ Hamiltonian Path.

3. Do Ex 8.2 from Hard Problem Notes.

Hamiltonian Path < Hamiltonian Circuit.

4. Do Ex 8.3 from Hard Problem Notes.

Find **TSP** tour.

5. Do Ex 8.4 from Hard Problem Notes.

YES/NO Towers of Hanoi.

6. Do Ex 8.5 from Hard Problem Notes.

Graph Isomorphism.

## 7. Star Free Regular Expression Non-Equivalence

**INPUT:** Two star-free regular expressions,  $E_1$  and  $E_2$ .

**QUESTION:** Are the languages represented by  $E_1$  and  $E_2$  different (not equal)?

A Star Free Regular Expression contains strings over a finite alphabet, the operators:  $\vee$  (OR),  $\wedge$  (Followed By),

and parentheses to indicate the order of operations.

The empty string represents the empty language.

E and (E) represent the same language.

The language consists of a single string, if the expression is E or (E) where E is a single string.

If the expression has the form  $R_1 \vee R_2$  then the corresponding language consists of the union of the languages corresponding to  $R_1$  and  $R_2$ .

If the expression has the form  $R_1 \wedge R_2$  then the corresponding language consists of all strings which can be written as a string from the language of  $R_1$  followed by a string from the language of  $R_2$ .

SHOW that Star Free Regular Expression Non-Equivalence is NP-complete.