

Find the median using Selection (DAC) where $v = 2^{\text{nd}}$ element.

$A = [7, 8, 11, 3, 9, 1, 4, 10, 3, 8, 6, 12]$

select(array [7, 8, 11, 3, 9, 1, 4, 10, 3, 8, 6, 12], $K = 6$):

split_array([7, 8, 11, 3, 9, 1, 4, 10, 3, 8, 6, 12]):

$A_L = [7, 3, 1, 4, 3, 6]$; $N_L = 6$

$A_P = [8, 8]$; $N_P = 2$

$A_R = [11, 9, 10, 12]$; $N_R = 4$

Since $K \leq N_L \Rightarrow 6 = 6$, return select(A_L , K)

select([7, 3, 1, 4, 3, 6], $K = 6$):

split_array([7, 3, 1, 4, 3, 6]):

$A_L = [1]$; $N_L = 1$

$A_P = [3, 3]$; $N_P = 2$

$A_R = [7, 4, 6]$; $N_R = 3$

Since $K > (N_L + N_P) \Rightarrow 6 > (1 + 2)$, return select(A_R , $K = 6 - (1 + 2) = 3$)

select([7, 4, 6], $K = 3$):

split_array([7, 4, 6]):

$A_L = [0]$; $N_L = 0$

$A_P = [4]$; $N_P = 1$

$A_R = [7, 6]$; $N_R = 2$

Since $K > (N_L + N_P)$, return select(A_R , $K - (N_L + N_P) \Rightarrow K = 3 - 1 = 2$)

select([7, 6], $K = 2$):

split_array([7, 6]):

$A_L = [0]$; $N_L = 0$

$A_P = [6]$; $N_P = 1$

$A_R = [7]$; $N_R = 1$

Since $K > (N_L + N_P)$: return select(A_R , $K - (N_L + N_P) \Rightarrow K = 2 - 1 = 1$)

select([7], K = 1):

split_array([7]):

$A_L = []$; $N_L = 0$

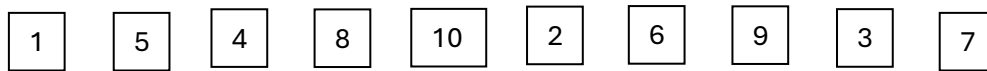
$A_P = [7]$; $N_P = 1$

$A_R = []$; $N_R = 0$

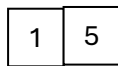
Since $N_L < K \leq (N_L + N_P) \Rightarrow 0 < 1 \leq 1$, return $A_P[0] = 7$

Count and list (in ascending order) the inversions in $A = [1, 5, 4, 8, 10, 2, 6, 9, 3, 7]$ using merge sort.

After merge sort (split array into halves until only one element is left):



Merge:



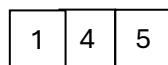
Inversions:

Inversions count = 0



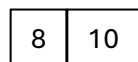
Inversion:

Inversions count = 0 + 0



Inversions: (5, 4)

Inversions count = 0 + 0 + 1



Inversions: (5, 4)

Inversions count = 0 + 0 + 1 + 0

1	4	5	8	10
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Inversions: (5, 4)

Inversions count = $0 + 0 + 1 + 0 + 0$

2	6
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Inversions: (5, 4)

Inversions count = $0 + 0 + 1 + 0 + 0 + 0$

2	6	9
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Inversions: (5, 4)

Inversions count = $0 + 0 + 1 + 0 + 0 + 0 + 0$

3	7
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Inversions: (5, 4)

Inversions count = $0 + 0 + 1 + 0 + 0 + 0 + 0 + 0$

2	3	6	7	9
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Inversions: (5, 4), (6, 3), (9, 3), (9, 7)

Inversions count = $0 + 0 + 1 + 0 + 0 + 0 + 0 + 0 + 3$

1	4	5	8	10
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2	3	6	7	9
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1	2	3	4	5	6	7	8	9	10
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Inversions: (5, 4), (6, 3), (9, 3), (9, 7), (4, 2), (5, 2), (8, 2), (10, 2), (4, 3), (5, 3), (8, 3), (10, 3), (8, 6), (10, 6), (8, 7), (10, 7), (10, 9)

Inversions count = $0 + 0 + 1 + 0 + 0 + 0 + 0 + 0 + 3 + 13 = 17$