

# Exam

## 1 Accounting System

### Question 1.1

I have written the following test:

```
for (int i = 0; i < 20000; i++) {
    new Thread(() -> {
        accounts.deposit(n - 1, 1);
        int value = accounts.get(n - 1);
        accounts.transfer(n - 1, n - 2, value);
        assert (accounts.get(n - 1) == 0);
    });
    new Thread(() -> {
        accounts.deposit(n - 1, 1);
        int value = accounts.get(n - 1);
        accounts.transfer(n - 1, n - 2, value);
        assert (accounts.get(n - 1) == 0);
    });
}
assert (accounts.get(n - 1) == 0);
```

By transferring an amount to an account, checking that what the current value on the account is and then removing that amount 20000 across two Threads we see that the value on the account is not what we expect due to interleaved transfers.

### Question 1.2

I have written the following test:

```
accounts.deposit(n - 1, 99);
new Thread(() -> {
    while (accounts.get(n - 1) != 100) {
    }
    assert (true); // Never run.
});
new Thread(() -> {
    accounts.deposit(n - 1, 1); // Makes .get(n-1) == 100
    accounts.deposit(n - 1, 1);
    accounts.deposit(n - 1, 1);
});
```

This test never succeeds, which it should.

### Question 1.3

The full LockAccounts class is shown below:

```
import java.util.Arrays;

public class LockAccounts implements Accounts {
    private volatile Integer[] accounts;
```

```

public LockAccounts(int n) {
    accounts = new Integer[n];
    Arrays.fill(accounts, 0, accounts.length, 0);
}

public void init(int n) {
    synchronized (accounts) {
        accounts = new Integer[n];
        Arrays.fill(accounts, 0, accounts.length, 0);
    }
}

public int get(int account) {
    synchronized (accounts[account]) {
        return accounts[account];
    }
}

public int sumBalances() {
    synchronized (accounts) {
        int sum = 0;
        for (int i = 0; i < accounts.length; i++) {
            sum += accounts[i];
        }
        return sum;
    }
}

public void deposit(int to, int amount) {
    synchronized (accounts[to]) {
        accounts[to] += amount;
    }
}

public void transfer(int from, int to, int amount) {
    synchronized (accounts[from]) {
        synchronized (accounts[to]) {
            accounts[from] -= amount;
            accounts[to] += amount;
        }
    }
}

public void transferAccount(Accounts other) {
    synchronized (accounts) {
        synchronized (other) {
            for (int i = 0; i < accounts.length; i++) {
                accounts[i] += other.get(i);
            }
        }
    }
}

```

```

    public String toString() {
        String res = "";
        if (accounts.length > 0) {
            synchronized (accounts) {
                res = "" + accounts[0];
                for (int i = 1; i < accounts.length; i++) {
                    res = res + " " + accounts[i];
                }
            }
        }
        return res;
    }
}

```

The accounts field is made `volatile` to ensure visibility.

The `int` array has been turned into an `Integer` array in order to enable “striping” by locking just the accounts being modified.

`init`, `sumBalances`, `transferAccount` and `toString` lock the entire `accounts` array since the operations herein involve the entire array and would give inconsistent results otherwise.

`sumBalances` can show inconsistent results since a specific account can be modified while `sumBalances` iterates over the `accounts` array.

My solution **can** deadlock in both `transfer` and `transferAccount` since one thread can obtain (for example in `transfer`) a lock on one account while another thread has a lock on the other related account (and they are both waiting for each other). The same applies to `transferAccount` with two related `Account` objects.

Running `java -ea Runner` gives:

```

class UnsafeAccounts passed sequential tests
class UnsafeAccounts passed concurrent tests

```

## Question 1.4

Relevant snippets of `LockAccountsFast` (the rest of the class is identical to `LockAccounts`) below:

```

public class LockAccountsFast implements Accounts {
    private volatile Integer[] accounts;
    private volatile Integer[] sums;
    private static final int threads = 4;

    [...]

    public int sumBalances() {
        int sum = 0;
        for (int i = 0; i < sums.length; i++) {
            synchronized (sums[i]) {
                sum += sums[i];
            }
        }
        return sum;
    }

    public void deposit(int to, int amount) {

```

```

        synchronized (accounts[to]) {
            int index = Thread.currentThread().hashCode()
                % sums.length;
            synchronized (sums[index]) {
                accounts[to] += amount;
                sums[index] += amount;
            }
        }
    }
    [...]
}

```

### Question 1.5

The full STMAccounts can seen below.

```

import java.util.Arrays;

public class STMAccounts implements Accounts {
    private volatile Integer[] accounts;

    public STMAccounts(int n) {
        accounts = new Integer[n];
        Arrays.fill(accounts, 0, accounts.length, 0);
    }

    public void init(int n) {
        atomic(() -> {
            this.accounts = new Integer[n];
            Arrays.fill(accounts, 0, accounts.length, 0);
        });
    }

    public int get(int account) {
        return atomic(() -> this.accounts[account]);
    }

    public int sumBalances() {
        return atomic(() -> {
            int sum = 0;
            for (int i = 0; i < this.accounts.length; i++) {
                sum += this.accounts[i];
            }
            return sum;
        });
    }

    public void deposit(int to, int amount) {
        atomic(() -> this.accounts[to] += amount);
    }

    public void transfer(int from, int to, int amount) {
        atomic(() -> {

```

```

        this.accounts[from] -= amount;
        this.accounts[to] += amount;
    });
}

public void transferAccount(Accounts other) {
    atomic(() -> {
        for (int i = 0; i < accounts.length; i++) {
            this.accounts[i] += other.get(i);
        }
    });
}

public String toString() {
    return atomic(() -> {
        String res = "";
        if (this.accounts.length > 0) {
            res = "" + this.accounts[0];
            for (int i = 1; i < this.accounts.length; i++) {
                res = res + " " + this.accounts[i];
            }
        }
        return res;
    });
}
}

```

I have been unable to run `Runner` with the `multiverse.jar` file. The code looks almost identical to the code I wrote in hand-in 9, though.

I have chosen to implement the `sumBalances` that risks competing with other method calls. The other implementation option would use transactions on a more granular level, but would then risk that the array could change while `toString`'ing.

## Question 1.6

My full implementation of `CASAccounts` can be seen below:

```

public class CASAccounts implements Accounts {
    private AtomicInteger[] accounts;
    private AtomicInteger sum = new AtomicInteger();

    public CASAccounts(int n) {
        accounts = new AtomicInteger[n];
        for (int i = 0; i < accounts.length; i++) {
            accounts[i] = new AtomicInteger(0);
        }
    }

    public void init(int n) {
        accounts = new AtomicInteger[n];
        for (int i = 0; i < accounts.length; i++) {
            accounts[i] = new AtomicInteger(0);
        }
    }
}

```

```

public int get(int account) {
    return accounts[account].get();
}

public int sumBalances() {
    return sum.get();
}

public void deposit(int to, int amount) {
    int previous, previousSum;
    do {
        previous = accounts[to].get();
        previousSum = sum.get();
    } while (!(accounts[to].compareAndSet(previous, previous + amount)
        && sum.compareAndSet(previousSum, previousSum + amount)));
}

public void transfer(int from, int to, int amount) {
    int previousTo, previousFrom;
    do {
        previousFrom = accounts[from].get();
        previousTo = accounts[to].get();
    } while (!(accounts[from].compareAndSet(previousFrom, previousFrom - amount)
        && accounts[to].compareAndSet(previousTo, previousTo + amount)));
}

public void transferAccount(Accounts other) {
    for (int i = 0; i < accounts.length; i++) {
        int previous, otherValue, sumPrevious;
        do {
            previous = accounts[i].get();
            otherValue = other.get(i);
            sumPrevious = sum.get();
        } while (otherValue == other.get(i)
            && !(accounts[i].compareAndSet(previous, otherValue + previous)
            && sum.compareAndSet(sumPrevious, sumPrevious + otherValue)));
    }
}

public String toString() {
    String res = "";
    if (accounts.length > 0) {
        res = "" + accounts[0].get();
        for (int i = 1; i < accounts.length; i++) {
            res = res + " " + accounts[i].get();
        }
    }
    return res;
}
}

```

I have added the `sum` field which maintains the current total sum of the accounts. `sum` is set using CAS in every method that has to update the sum. The update of `sum` is done in the same `while` loop as the other

CAS updates in order to ensure correctness of the values.

No writes are lost in the tests I have performed, and `CASAccounts` passes both sequential and concurrent tests.

The operations cannot be guaranteed to happen in constant time since any given update/set of a value might have to be retried a number of times.

I cannot guarantee that the implementation does not livelock, since i.e. a `transfer` operation could go “back and forth” between values indefinitely.

### Question 1.7.1

My implementation of `applyTransactionsLoop` with a helper (`printAccounts`) for printing balances can be seen below:

```
private static void printAccounts(Accounts accounts, int numberOfAccounts) {
    System.out.println("sumBalances is: " + accounts.sumBalances());
    if (numberOfAccounts <= 100) {
        System.out.println("accounts contain: ");
        for (int i = 0; i < numberOfAccounts; i++) {
            System.out.println("Account " + i + " is: " + accounts.get(i));
        }
    }
}

// Question 1.7.1
private static void applyTransactionsLoop(int numberOfAccounts, int numberOfTransactions,
    Supplier<Accounts> generator) {
    final Accounts accounts = generator.get();
    Stream<Transaction> transaction = IntStream.range(0, numberOfTransactions).parallel()
        .mapToObj((i) -> new Transaction(numberOfAccounts, i));

    transaction.parallel().forEach(t -> {
        if (t.from == -1) {
            accounts.deposit(t.to, t.amount);
        } else {
            accounts.transfer(t.from, t.to, t.amount);
        }
    });
    printAccounts(accounts, numberOfAccounts);
}
```

The output of the above with `n = 10` can be seen below:

```
sumBalances is: 9811
accounts contain:
Account 0 is: 1632
Account 1 is: 40
Account 2 is: 1272
Account 3 is: 992
Account 4 is: 940
Account 5 is: 577
Account 6 is: 1841
Account 7 is: 1071
Account 8 is: 339
```

Account 9 is: 1107

### Question 1.7.2

I have not been able to get my code for this question to compile, but pseudocode and a description of my intended solution can be seen below:

```
// Question 1.7.2
private static void applyTransactionsCollect(int numberOfAccounts, int numberOfTransactions,
    Supplier<Accounts> generator) {
    Stream<Transaction> transactions = IntStream.range(0, numberOfTransactions).parallel()
        .mapToObj((i) -> new Transaction(numberOfAccounts, i));

    // (Failed) attempt using collect:
    //var collect = transactions
    //    .collect(Collectors.mapping(t -> generator.get(), Accounts::transferAccount));

    // Attempt using map:
    var mapping = transactions.parallel().map(t -> {
        var a = generator.get();
        if (t.from == -1) {
            a.deposit(t.to, t.amount);
        } else {
            a.transfer(t.from, t.to, t.amount);
        }
        return a;
    }).collect(Accounts::transferAccount);
}
```

My understanding is that we want to build an `Accounts` object that is the result of applying all transactions. Using `collect` I wanted to get an initial `Accounts` object using the generator, and then run through all `Transactions` generating `Accounts` that are the representation of applying a `Transaction`, on one `Accounts` object, and finally collecting/folding the `Accounts` into one `Accounts` object using `transferAccount`. Unfortunately, I did not succeed.

I then wanted to do it in a more simple way (in my opinion) using a `map`. I attempted to `map` over all transactions, then applying them to the aggregated `Accounts` object (again initially created using the generator). This results in an `Accounts` object `Stream` representing all applied `Transactions`. I would then be able to flatten all of these `Accounts` into one `Accounts` object using `transferAccount`.

I currently get cryptic type errors on `map`, but I hope that my attempt and explanation of my thought process is worth something.

### Question 1.7.3

I've used the `Timer` class from the course material to time the performance of the serial `UnsafeAccounts` and `applyTransactionsLoop` tests using `n = 1000`

Both methods use the `UnsafeAccounts` implementation.

- Running serially through all accounts takes 0.048224722 seconds.
- Running through all transactions takes only 0.018207435 seconds, which is about a 3x speed-up.

The serial run will be slower due to the fact that we cannot execute work concurrently. Given more threads, more `Accounts` can be processed in a shorter amount of time. There does not seem to be an overhead in



having many `Transaction` objects in memory, nor does there seem to be a big overhead in using the `Stream` API, which is to be expected.

The amount of `numberOfTransactions` can be raised to 200000 before the execution time of the sequential and stream-based approaches begin to look alike. If `n` is raised, then the two approaches diverge again and the stream-based approach is much faster again.

## 2 Buffered Merging Priority Queue

### Question 2.1

Results of benchmarking the class can be seen below:

Default parameters:

```
n 10000000 s 45678, extract 2500000 bufLen 20 maxDepth 4 cutOff 4
# OS: Mac OS X; 10.14.2; x86_64
# JVM: Oracle Corporation; 11.0.1
# CPU: null; 4 "cores"
# Date: 2018-12-18T18:43:18+0100
-1073351325 One Serial Real time: 1.040 ( 1.022)
-1073351325 One Parallel Real time: 0.455 ( 0.445)
-1073351325 BufferedPQ Ser/Serial Real time: 0.911 ( 0.695)
```

One Parallel: ~50% speed-up  
BufferedPQ Ser/Serial: ~10% speed-up

Big bufLen:

```
n 10000000 s 45678, extract 2500000 bufLen 10000 maxDepth 4 cutOff 4
# OS: Mac OS X; 10.14.2; x86_64
# JVM: Oracle Corporation; 11.0.1
# CPU: null; 4 "cores"
# Date: 2018-12-18T18:49:17+0100
-1073351325 One Serial Real time: 1.023 ( 1.003)
-1073351325 One Parallel Real time: 0.456 ( 0.446)
-1073351325 BufferedPQ Ser/Serial Real time: 0.878 ( 0.712)
```

One Parallel: ~45% speed-up  
BufferedPQ Ser/Serial: ~15% speed-up

Small bufLen:

```
n 10000000 s 45678, extract 2500000 bufLen 10 maxDepth 4 cutOff 4
# OS: Mac OS X; 10.14.2; x86_64
# JVM: Oracle Corporation; 11.0.1
# CPU: null; 4 "cores"
# Date: 2018-12-18T18:50:18+0100
-1073351325 One Serial Real time: 1.067 ( 1.051)
-1073351325 One Parallel Real time: 0.457 ( 0.447)
-1073351325 BufferedPQ Ser/Serial Real time: 0.935 ( 0.703)
```

One Parallel: ~45% speed-up  
BufferedPQ Ser/Serial: ~10% speed-up

Big cutOff:

```
n 10000000 s 45678, extract 2500000 bufLen 20 maxDepth 4 cutOff 12
# OS: Mac OS X; 10.14.2; x86_64
# JVM: Oracle Corporation; 11.0.1
# CPU: null; 4 "cores"
# Date: 2018-12-18T18:51:03+0100
-1073351325 One Serial Real time: 1.019 ( 1.002)
-1073351325 One Parallel Real time: 0.459 ( 0.448)
-1073351325 BufferedPQ Ser/Serial Real time: 0.922 ( 0.704)
```

One Parallel: ~45% speed-up  
BufferedPQ Ser/Serial: ~10% speed-up

Small cutOff:

```
n 10000000 s 45678, extract 2500000 bufLen 20 maxDepth 4 cutOff 1
# OS: Mac OS X; 10.14.2; x86_64
# JVM: Oracle Corporation; 11.0.1
# CPU: null; 4 "cores"
# Date: 2018-12-18T18:51:33+0100
-1073351325 One Serial Real time: 1.023 ( 1.006)
-1073351325 One Parallel Real time: 0.465 ( 0.454)
-1073351325 BufferedPQ Ser/Serial Real time: 0.927 ( 0.706)
```

One Parallel: ~50% speed-up  
BufferedPQ Ser/Serial: ~10% speed-up

Huge n:

```
n 100000000 s 45678, extract 25000000 bufLen 20 maxDepth 4 cutOff 4
# OS: Mac OS X; 10.14.2; x86_64
# JVM: Oracle Corporation; 11.0.1
# CPU: null; 4 "cores"
# Date: 2018-12-18T18:52:18+0100
-1073571373 One Serial Real time: 11.857 ( 11.779)
-1073571373 One Parallel Real time: 5.573 ( 5.541)
-1073571373 BufferedPQ Ser/Serial Real time: 10.794 ( 9.342)
```

One Parallel: ~50% speed-up  
BufferedPQ Ser/Serial: ~10% speed-up

Tiny n:

```
n 1000000 s 45678, extract 250000 bufLen 20 maxDepth 4 cutOff 4
# OS: Mac OS X; 10.14.2; x86_64
# JVM: Oracle Corporation; 11.0.1
# CPU: null; 4 "cores"
# Date: 2018-12-18T18:53:17+0100
-1073155617 One Serial Real time: 0.125 ( 0.121)
-1073155617 One Parallel Real time: 0.212 ( 0.212)
-1073155617 BufferedPQ Ser/Serial Real time: 0.111 ( 0.065)
```

One Parallel: NO speed-up  
BufferedPQ Ser/Serial: ~10% speed-up

It is interesting to see that there is a slowdown on small  $n$ . The overhead of multithreading is simply too big to outweigh the single-core speed. Otherwise the results are quite consistent with the biggest speed-up seen using *One Parallel*.

## Question 2.2

Implementation can be seen below:

```
public void createPairParam(Parameters param, Function<Parameters, PQ> instanceCreator) {
    var executor = Executors.newWorkStealingPool();
    var tasks = new ArrayList<Callable<PQ>>();
    Future<PQ> leftTask = executor.submit(() -> instanceCreator.apply(param.left()));
    Future<PQ> rightTask = executor.submit(() -> instanceCreator.apply(param.right()));
    try {
        left = leftTask.get();
        right = leftTask.get();
    } catch (InterruptedException e) {
        throw e;
    } catch (ExecutionException e) {
        throw e;
    }
};
```

## Question 2.3

My initial implementation can be seen below. Parts of the code have been omitted since it is identical to BufferedPQ.

```
public class BufferedPQP implements PQ {
    // buffer containing the elements in order
    private int[] buffer;
    private int[] nextBuffer;
    private ExecutorService executorService;

    [...]

    BufferedPQP(Parameters pp) {
        executorService = Executors.newWorkStealingPool();
        [...]
    }

    [...]

    public int getMin() {
        int res = peek();
        current++;
        if (current >= buffer.length) { // the buffer is empty
            var f = executorService.submit(() -> getNewBuffer(bufLen));
            try {
                while (!f.isDone()) {
                    buffer = nextBuffer;
                }
            }
        }
    }
}
```

```

        }
        buffer = f.get();
    } catch (InterruptedException e) {
        throw e;
    } catch (ExecutionException e) {
        throw e;
    }
    current = 0;
}
return res;
}
[...]
}

```

### 3 Message Passing

I've implemented the Erlang reference implementation in *Java+Akka* according to “spec”, using Java 10 (which lets me use `var` type declarations).

My full implementation of the Erlang reference implementation can be seen below:

```

import java.io.Serializable;
import java.util.ArrayList;
import java.util.Arrays;
import java.util.List;
import java.util.stream.Collectors;

import akka.actor.*;

class MergeSort {
    public static void main(String[] args) {
        final var system = ActorSystem.create("MergeSortPipelineSystem");
        final var tester = system.actorOf(Props.create(TesterActor.class));
        final var sorter = system.actorOf(Props.create(SorterActor.class));
        tester.tell(new InitMessage(sorter), ActorRef.noSender());
    }
}

// -- Actors

class SorterActor extends UntypedActor {
    public void onReceive(Object o) throws Exception {
        if (o instanceof SortMessage) {
            var list = ((SortMessage) o).list;
            var x = ((SortMessage) o).receiver;

            if (list.size() > 1) {
                var m = getContext().actorOf(Props.create(MergerActor.class));
                m.tell(new ResultMessage(x), ActorRef.noSender());

                var l1 = list.subList(0, list.size() / 2);
                var l2 = list.subList(list.size() / 2, list.size());
            }
        }
    }
}

```

```

        var s1 = getContext().actorOf(Props.create(SorterActor.class));
        s1.tell(new SortMessage(l1, m), ActorRef.noSender());

        var s2 = getContext().actorOf(Props.create(SorterActor.class));
        s2.tell(new SortMessage(l2, m), ActorRef.noSender());
    }

    else {
        x.tell(new SortedMessage(list), ActorRef.noSender());
    }
}

}

}

class MergerActor extends UntypedActor {
    private ActorRef receiver;
    private List<Integer> l1;
    private List<Integer> l2;

    private List<Integer> merge(List<Integer> l1, List<Integer> l2) {
        var result = new ArrayList<Integer>();
        if (l1.stream().max(Integer::compare).get() < l2.stream().max(Integer::compare).get()) {
            result.addAll(l1);
            result.addAll(l2);
        } else {
            result.addAll(l2);
            result.addAll(l1);
        }
        return result;
    }

    public void onReceive(Object o) throws Exception {
        if (o instanceof ResultMessage) {
            this.receiver = ((ResultMessage) o).receiver;
        }

        else if (o instanceof SortedMessage) {
            // Since we can't do nested onReceive, we do stateful receiver and
            // list building on this actor.
            if (receiver == null)
                return;
            if (l1 == null) {
                l1 = ((SortedMessage) o).sorted;
            } else {
                l2 = ((SortedMessage) o).sorted;
                var sorted = merge(l1, l2);
                System.out.println("Merged: " + sorted);
                receiver.tell(new SortedMessage(sorted), ActorRef.noSender());
            }
        }
    }
}

}

class TesterActor extends UntypedActor {

```

```

    public void onReceive(Object o) throws Exception {
        if (o instanceof InitMessage) {
            var sorter = ((InitMessage) o).sorter;
            //Hardcoded list as in .erl example, changed in test runs.
            var list = Arrays.asList(new Integer[] { 8, 7, 6, 5, 4, 3, 2, 1 });
            sorter.tell(new SortMessage(list, getSelf()), ActorRef.noSender());
        } else if (o instanceof SortedMessage) {
            System.out.println("RESULT: " + ((SortedMessage) o).sorted);
        }
    }
}

// -- Messages

class InitMessage implements Serializable {
    private static final long serialVersionUID = 1L;
    public final ActorRef sorter;

    public InitMessage(ActorRef sorter) {
        this.sorter = sorter;
    }
}

class SortMessage implements Serializable {
    private static final long serialVersionUID = 2L;
    public final List<Integer> list;
    public final ActorRef receiver;

    public SortMessage(List<Integer> list, ActorRef receiver) {
        this.list = list;
        this.receiver = receiver;
    }
}

class ResultMessage implements Serializable {
    private static final long serialVersionUID = 3L;
    public final ActorRef receiver;

    public ResultMessage(ActorRef receiver) {
        this.receiver = receiver;
    }
}

class SortedMessage implements Serializable {
    private static final long serialVersionUID = 4L;
    public final List<Integer> sorted;

    public SortedMessage(List<Integer> sorted) {
        this.sorted = sorted;
    }
}

```

Test input and results can be seen below:

# Input:

```

[8, 7, 6, 5, 4, 3, 2, 1]

# Result:
Merged: [7, 8]
Merged: [3, 4]
Merged: [5, 6]
Merged: [1, 2]
Merged: [5, 6, 7, 8]
Merged: [1, 2, 3, 4]
Merged: [1, 2, 3, 4, 5, 6, 7, 8]
RESULT: [1, 2, 3, 4, 5, 6, 7, 8]

# Input:
[8, 8, 8, 8, 8, 8, 2, 1]

# Result:
Merged: [8, 8]
Merged: [8, 8]
Merged: [8, 8]
Merged: [8, 8, 8, 8]
Merged: [1, 2]
Merged: [1, 2, 8, 8]
Merged: [1, 2, 8, 8, 8, 8, 8, 8]
RESULT: [1, 2, 8, 8, 8, 8, 8, 8]

# Input:
[8, 8, 8, 8, 1, 1, 1, 1]

#Result:
Merged: [1, 1]
Merged: [8, 8]
Merged: [1, 1]
Merged: [8, 8]
Merged: [8, 8, 8, 8]
Merged: [1, 1, 1, 1]
Merged: [1, 1, 1, 1, 8, 8, 8, 8]
RESULT: [1, 1, 1, 1, 8, 8, 8, 8]

```